## Real-Time Systems

Lecture 16: The Universality Problem for TBA

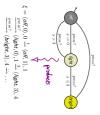
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... vs. Timed Automata

Timed Languages



New: Given a timed word  $(a, 1), (b, 2), (a, 3), (b, 4), (a, 5), (b, 6), \dots,$ does A accept it?

 $\xi$  is a computation path and run of  $\mathcal{A}$ .

New: acceptance criterion is visiting accepting state infinitely often.

Definition. A timed language over an alphabet  $\Sigma$  is a set of timed words over  $\Sigma.$ 

Definition. A timed word over an alphabet  $\Sigma$  is a pair  $(\sigma,\tau)$  where  $\sigma=\sigma_1,\sigma_2,\dots\in\Sigma^{\omega}$  is an <u>infinite</u> word over  $\Sigma$ , and  $\tau$  is a time sequence.

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(i) Monotonicity:  $\tau \text{ increases strictly monotonically, i.e. } \tau_i < \tau_{i+1} \text{ for all } i \geq 1.$  (ii) Progress: For every  $t \in \mathbb{R}^+_0$ , there is some  $i \geq 1$  such that  $\tau_i > t$ . Definition. A time sequence  $\tau=\tau_1,\tau_2,\dots$  is an infinite sequence of time values  $\tau_i\in\mathbb{R}^+_0$ , satisfying the following constraints:

## Contents & Goals

Last Lecture:

Using Uppaal to check whether a TA satisfies a DC requirement:
Testable DC properties

## This Lecture:

- Educational Objectives: Capabilities for following tasks/questions.
   What's a TBA and what's the difference to (extended) TA?
   What's undeclabel for finned (Bitch) automata?
   What's the idea of the proof?

- Timed Bichi Automata and timed regular languages [Alur and Dill, 1994].

  The University Problem is undecidable for TBA [Alur and Dill, 1994].

  Why this is infortunate.

  Timed regular languages are not everything.

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Timed Büchi Automata [Alur and Dill, 1994]

Example: Timed Language

Timed word over alphabet Σ: a pair (r, r) where

or = a\_1, a\_2,... is an infinite word over Σ, and

or is a time sequence (strictly (I) monotonic, non-Zeno).

$$\begin{split} L_{crt} = \{ & \{ ((ab)^\omega, \tau) \mid \exists \ i \ \forall j \geq i : (\tau_{2j} < \tau_{2j-1} + 2) \} \\ & \text{Thurstong that there } \\ & \text{of a be of the a before} \end{split}$$
a could be 'openor heaps' b would be 'openor Alather light'

A b a b a b ... a b a b a b ...

The to the

## Timed Büchi Automata

Definition. The set  $\Phi(X)$  of clock constraints over X is defined inductively by where  $x \in X$  and  $c \in \mathbb{Q}$  is a rational constant.  $\delta ::= x \leq c \mid c \leq x \mid -\delta \mid \delta_1 \wedge \delta_2$ 

Definition. A timed Büchi automaton (TBA)  $\mathcal A$  is a tuple  $(\Sigma,S,S_0,X,E,F)$ , where

 Σ is an alphabet, • S is a finite set of states,  $S_0 \subseteq S$  is a set of start states,

\* X is a finite set of clocks, and \*  $E \subseteq S \times S \times \Sigma \times 2^{N} \times \phi(X)$  gives the set of transitions. An edge  $(s,s',a,\lambda,h)$  represents transition from state s to state s' on input symbol. The set  $A \subseteq X$  gives the clocks to be reset with this transition, and  $\delta$  is a clock constraint over X.

•  $F \subseteq S$  is a set of accepting states.

Example: TBA

(Accepting) TBA Runs

 $A = (\Sigma, S, S_0, X, E, F)$   $(s, s', a, \lambda, \delta) \in E$ 

 $s_0 \xrightarrow{a} s_2 \xrightarrow{b, x < 2} s_3$  a, x := 0· E={ (50,51, 4. B, toue), (5, 53, 6, 8, 44), (5, 53, 6, 8, x<2), (3, 53, 9, 8x}, 44) (s,, so, 6, 0, sw.),

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# Example: (Accepting) Runs

(Accepting) TBA Runs

Definition. A run r, denoted by  $(\bar{s},\bar{\nu})$ , of a TBA  $(\Sigma,S,S_0,X,E,F)$  over a timed word  $(\sigma,\tau)$  is an infinite sequence of the form

with  $s_i \in S$  and  $\nu_i: X \to \mathbb{R}^+_0$ , satisfying the following requirements:

 $r: \langle s_0, \nu_0 \rangle \xrightarrow{\sigma_1} \langle s_1, \nu_1 \rangle \xrightarrow{\sigma_2} \langle s_2, \nu_2 \rangle \xrightarrow{\sigma_3} \dots$ 

• Initiation:  $s_0 \in S_0$  and  $\nu(x) = 0$  for all  $x \in X$ .

- Consecution: for all  $i \ge 1$ , there is an edge in E of the form  $(s_{i-1}, s_i, \sigma_i, \lambda_i, \delta_i)$  such that

 $\nu_{i-1} + (\tau_i - \tau_{i-1}))$  satisfies  $\delta_i$  and  $\nu_i = (\nu_{i-1} + (\tau_i - \tau_{i-1}))[\lambda_i := 0].$ 

 $\begin{array}{ll} r: \langle s_0, \iota_0 \rangle \xrightarrow{\sigma_1} \langle s_1, \iota_1 \rangle \xrightarrow{\sigma_2} \langle s_2, \iota_2 \rangle \xrightarrow{\sigma_3} \dots \text{ initial and } (s_{\ell-1}, s_\ell, \sigma_\ell, \lambda_\ell, \delta_\ell) \in E, \text{ s.t.} \\ (\iota_{\ell-1} + (\tau_\ell - \tau_{\ell-1})) \models \delta_i, \iota_\ell = (\iota_{\ell-1} + (\tau_\ell - \tau_{\ell-1}))[\lambda_i := 0]. \text{ Accepting iff } \inf(r) \cap F \neq \emptyset. \end{array}$ 

Timed word:  $(a, 1), (b, \$), (a, 3), (b, 4), (a, 5), (b, 6), \dots$  $\underbrace{s_1 \atop a} \underbrace{s_0 \atop x := 0} \underbrace{s_2 \atop s_2} \underbrace{b, x < 2}_{a, x := 0} \underbrace{s_3}_{s_3}$ 

• Can we construct any num'l sit accepting?

•  $\{x_{k_1,k_2}, x_{k_2}, x_{$ 

 Can we construct a (non-)accepting run?  $\int_{1}^{1} (-1)^{2} \left( -1 \right) \left( -1 \right)$ 

Definition. A run  $r=(\bar{s},\bar{\nu})$  of a TBA over timed word  $(\sigma,\tau)$  is called (an) accepting (run) if and only if  $inf(r)\cap F\neq\emptyset$ .

The set  $\inf(r)\subseteq S$  consists of those states  $s\in S$  such that  $s=s_i$  for infinitely many  $i\geq 0.$ 

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# The Language of a TBA

 $\{(\sigma,\tau)\mid \mathcal{A} \text{ has an accepting run over } (\sigma,\tau)\}.$  For short:  $L(\mathcal{A})$  is the language of  $\mathcal{A}.$ Definition. For a TBA  $\mathcal A$ , the language  $L(\mathcal A)$  of timed words it accepts is defined to be the set 00

Definition. A timed language L is a timed regular language if and only if  $L=L(\mathcal{A})$  for some TBA  $\mathcal{A}$ .

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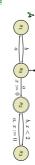
K • Consecution: for all  $i \ge 1$ , there is an edge in E of the form  $(s_{i-1}, s_i|\widehat{\mathcal{O}}_{j-k}, \delta_i)$  such that  $(s_{i-1}, s_i|\widehat{\mathcal{O}}_{j-k}, \delta_i)$  such that  $(s_{i-1}, s_i|\widehat{\mathcal{O}}_{j-k}, \delta_i)$  such that  $s_i = 0$ .

•  $s_i = (s_{i-1}, s_i|\widehat{\mathcal{O}}_{j-k}, \delta_i)$  is  $s_i = 0$ .

•  $s_i = (s_{i-1}, s_i|\widehat{\mathcal{O}}_{j-k}, \delta_i)$  is  $s_i = (s_i, s_{i-1})$ . Definition. A run r, denoted by  $(\bar{s},\bar{\nu})$ , of a TBA  $(\Sigma,S,S_0,X,E,F)$  over a timed word  $(\sigma,\tau)$  is an infinite sequence of the form with  $s_i \in S$  and  $\nu_i : X$ • Initiation:  $s_0 \in S_0$  and  $\nu(x) = 0$  for all  $x \in X$ .  $r: \langle s_0, \nu_0 \rangle \xrightarrow{\sigma_+} \langle s_1, \nu_1 \rangle \xrightarrow{\mathfrak{Q}_2} \langle s_2, \nu_2 \rangle \xrightarrow{\sigma_3} \cdots$  and  $\nu_i: \mathscr{X} \to \mathbf{R}_0^+$ , satisfying the following requirements:

# Example: Language of a TBA

# $L(\mathcal{A}) = \{(\sigma,\tau) \mid \mathcal{A} \text{ has an accepting run over } (\sigma,\tau)\}.$



. L(A)  $\leq$  L(E)<sup>-1</sup> Poids span<sup>2</sup> (5(2)  $\leq$  L(A), then there is an electrophian pair ( $\leq$  j0) spec (5(1)). · Lat ( L(A): " pile som" (517) 6 Lat. (softeet in accepting run in ot.  $L(\mathcal{A}) = L_{crt} \ (= \{ ((ab)^{\omega}, \tau) \mid \exists i \ \forall j \ge i : (\tau_{2j} < \tau_{2j-1} + 2) \})$ 

Question: Is  $L_{crt}$  timed regular or not?

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The Universality Problem is Undecidable for TBA [Alur and Dill, 1994]

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# The Universality Problem

- Given: A TBA A over alphabet Σ.

 $\begin{array}{l} \bullet \ \, \text{Question: Does} \ \, \mathcal{A} \ \, \text{accept all timed words over} \ \, \Sigma? \\ \text{In other words: Is} \ \, L(\mathcal{A}) = \{(\sigma,\tau) \ | \ \, \sigma \in \Sigma^\omega, \tau \ \, \text{time sequence}\}. \end{array}$ 

Theorem 5.2. The problem of deciding whether a timed automaton over alphabet  $\Sigma$  accepts all timed words over  $\Sigma$  is  $\Pi^1_1\text{-hard}.$ 

("The class  $\Pi_1^1$  consists of highly undecidable problems, including some nonarithmetical sets (for an exposition of the analytical hierarchy consult, for instance [Rogers, 1967].)

- B' such that  $L(B')=\overline{L(B)}$  is effectively computable. Language emptyness is decidable for Büchi Automata.

Recall: With classical Büchi Automata (untimed), this is different:

• Let B be a Büchi Automatan over  $\Sigma$ .

• B is universal if and only if  $\overline{L(B)} = \emptyset$ .

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## Proof Idea

Theorem 5.2. The problem of deciding whether a timed automaton over alphabet  $\Sigma$  accepts all timed words over  $\Sigma$  is  $\Pi^1_t\text{-hard}.$ 

- $\circ$  Consider a language  $L_{wandec}$  which consists of the recurring computations of a 2-counter machine M.
- Construct a TBA A from M which accepts the complement of  $L_{undec}$ , i.e. with

## $L(A) = L_{undec}$ .

- ullet Then  ${\mathcal A}$  is universal if and only if  $L_{undec}$  is empty...
- $\dots$  which is the case if and only if M doesn't have a recurring computation.

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# The Universality Problem

- Given: A TBA A over alphabet  $\Sigma$ .
   Question: Does A accept all timed words over  $\Sigma$ ?
  In other words: Is  $L(A) = \{(\sigma,\tau) \mid \sigma \in \Sigma^{\omega}, \tau \text{ time sequence}\}.$

D=fabc?

A: 309

COS6 ... is amirace!

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Once Again: Two Counter Machines (Different Flavour)

A two-counter machine M• has two counters C,D and 

- jumps, here even non-deterministically.
- A configuration of M is a triple (i, c, d):
- program counter  $i\in\{1,\ldots,n\}$ , values  $c,d\in\mathbb{N}_0$  of C and D.
- $\bullet\,$  A computation of M is an infinite consecutive sequence

 $\langle 1, 0, 0 \rangle = \langle i_0, c_0, d_0 \rangle, \langle i_1, c_1, d_1 \rangle, \langle i_2, c_2, d_2 \rangle, \dots$ 

that is,  $\langle i_{j+1}, c_{j+1}, d_{j+1} \rangle$  is a result executing instruction  $i_j$  at  $\langle i_j, c_j, d_j \rangle$ .

A computation of M is called **recurring** iff  $i_j=1$  for infinitely many  $j\in\mathbb{N}_0.$ 

# Step 1: The Language of Recurring Computations

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 $\langle i,c,d \rangle$  represented by  $b_1 a_1^c a_2^d$ 

Let  $L_{undec}$  be the set of the timed words  $(\sigma,\tau)$  with •  $\langle i_1,c_1,d_1 \rangle, \langle i_2,c_2,d_2 \rangle, \dots$  is a recurring computation of M. •  $\sigma$  is of the form  $b_{i_1}a_1^{c_1}a_2^{d_1}b_{i_2}a_1^{c_2}a_2^{d_2}...$ 

For all j ∈ N<sub>0</sub>,

the time of b<sub>ij</sub> is j.

 $\bullet$  Let M be a 2CM with n instructions.

**Wanted**: A timed language  $L_{undec}$  (over some alphabet) representing exactly the recurring computations of M. In particular such that  $L_{undec} = \emptyset$  if and only if M has no recurring computation.

- Choose  $\Sigma = \{b_1, \dots, b_n, a_1, a_2\}$  as alphabet.
- $\bullet$  We represent a configuration  $\langle i,c,d\rangle$  of M by the sequence

$$b_i \underbrace{a_1 \dots a_1}_{c \text{ times}} \underbrace{a_2 \dots a_2}_{d \text{ times}} = b_1 a_1^c a_2^d$$

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Let  $L_{undec}$  be the set of the timed words  $(\sigma, \tau)$  with  $\langle i,c,d \rangle$  represented by  $b_1 a_1^c a_2^d$ 

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• if  $c_{j+1}=c_j-1$  then for every  $a_1$  at time t in the interval [j,j+1] except for the last one, there is an  $a_1$  at time t+1.

And analogously for the  $a_2$ 's.

• if  $c_{j+1}=c_j$  then for every  $a_1$  at time t in the interval [j,j+1] there is an  $a_1$  at time t+1, • if  $c_{j+1}=c_j+1$  then for every  $a_1$  at time t in the interval [j+1,j+2] except for the last one, there is an  $a_1$  at time t-1.

# Step 2: Construct "Observer" for $L_{undec}$

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Wanted: A TBA A such that

 $L(A) = \overline{L_{undec}}$ 

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Wanted: A TBA  ${\cal A}$  such that

 $L(A) = \overline{L_{undec}}$ 

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What are the reasons for a timed word not to be in  $L_{undec}$ ?

- (i) The  $b_i$  at time  $j \in \mathbb{N}$  is missing, or there is a spurious  $b_i$  at time  $t \in ]j, j+1[$ .
- (ii) The prefix of the timed word with times  $0 \le t < 1$  doesn't encode (1,0,0).
- (iii) The timed word is not recurring, i.e. it has only finitely many  $b_i$ .
- (iv) The configuration encoded in [j+1,j+2] doesn't faithfully represent the effect of instruction  $b_i$  on the configuration encoded in [j,j+1].

(iv) The configuration encoded in [j+1,j+2[ doesn't faithfully represent the effect of instruction  $b_t$  on the configuration encoded in [j,j+1[. (iii) The timed word is not recurring, i.e. it has only finitely many  $b_i$ . (ii) The prefix of the timed word with times  $0 \le t < 1$  doesn't encode  $\langle 1, 0, 0 \rangle$ . (i) The  $b_i$  at time  $j \in \mathbb{N}$  is missing, or there is a spurious  $b_i$  at time  $t \in ]j, j+1[$ . What are the reasons for a timed word not to be in  $L_{undec}$ ?

Plan: Construct a TBA  $\mathcal{A}_0$  for case (i), a TBA  $\mathcal{A}_{nnt}$  for case (ii), a TBA  $\mathcal{A}_{recur}$  for case (iii), and one TBA  $\mathcal{A}_i$  for each instruction for case (iv).

 $A = A_0 \cup A_{init} \cup A_{recur} \cup \bigcup_{1 \leq i \leq n} A_i$ 

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# Step 2.(i): Construct $A_0$

(i) The  $b_i$  at time  $j\in\mathbb{N}$  is missing, or there is a spurious  $b_i$  at time  $t\in ]j,j+1[$ .

[Alur and Dill, 1994]: "It is easy to construct such a timed automaton."  $\,$ 

Step 2.(iv): Construct  $A_i$ **Example:** assume instruction 7 is: Increment counter D and jump non-deterministically to instruction 3 or 5. Once again: stepwise.  $\mathcal{A}_T$  is  $\mathcal{A}_T^1 \cup \cdots \cup \mathcal{A}_T^6$ . (iv) The configuration encoded in [j+1,j+2] doesn't faithfully represent the effect of instruction  $b_i$  on the configuration encoded in [j,j+1].

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Step 2.(ii): Construct A<sub>init</sub>

Step 2.(iii): Construct Arecur

(iii) The timed word is not recurring, i.e. it has only finitely many  $b_i$ .

•  $\mathcal{A}_{recur}$  accepts words with only finitely many  $b_i$ .

(ii) The prefix of the timed word with times  $0 \le t < 1$  doesn't encode  $\langle 1, 0, 0 \rangle$ .

 $\{(\sigma_j,\tau_j)_{j\in\mathbb{N}_0}\mid (\sigma_0\neq b_1)\vee (\tau_0\neq 0)\vee (\tau_1\neq 1)\}.$ 

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Step 2.(iv): Construct  $A_i$ 

Step 2.(iv): Construct  $A_i$ 

Increment counter D and jump non-deterministically to instruction 3 or 5. Once again: Stepwise.  $\mathcal{A}_7$  is  $\mathcal{A}_7^1\cup\cdots\cup\mathcal{A}_7^6$ .

.  $\mathcal{A}_7^1$  accepts words with  $b_7$  at time j but neither  $b_3$  nor  $b_5$  at time j+1. "Easy to construct."

Example: assume instruction 7 is:

(iv) The configuration encoded in [j+1,j+2] doesn't faithfully represent the effect of instruction  $b_i$  on the configuration encoded in [j,j+1].

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•  $A_7^1$  accepts words with  $b_7$  at time j but neither  $b_3$  nor  $b_6$  at time j+1. "Easy to construct."

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# Step 2.(iv): Construct $A_i$

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**Example:** assume instruction 7 is: Increment counter D and jump non-deterministically to instruction 3 or 5. Once again: stepwise.  $\mathcal{A}_{7}$  is  $\mathcal{A}_{7}^{1} \cup \cdots \cup \mathcal{A}_{7}^{6}$ .

•  $\mathcal{A}_7^1$  accepts words with  $b_7$  at time j but neither  $b_3$  nor  $b_5$  at time j+1. "Easy to construct."

A<sup>4</sup><sub>7</sub>,...,A<sup>6</sup><sub>7</sub> accept words with missing decrement of D.

Aha, And...?

Consequences: Language Inclusion

• Given: Two TBAs  $A_1$  and  $A_2$  over alphabet B.
• Question: Is  $\mathcal{L}(A_1) \subseteq \mathcal{L}(A_2)$ ?

Possible applications of a decision procedure:

Characterise the allowed behaviour as A<sub>2</sub> and model the design as A<sub>1</sub>.
 Automatically check whether the behaviour of the design is a subset of the allowed behaviour.

A<sup>2</sup><sub>7</sub> accepts words which encode unexpected increment of counter C.

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# Consequences: Complementation

Consequences: Language Inclusion

• Given: Two TBAs  $A_1$  and  $A_2$  over alphabet B.
• Question: Is  $\mathcal{L}(A_1) \subseteq \mathcal{L}(A_2)$ ?

Possible applications of a decision procedure:

 Automatically check whether the behaviour of the design is a subset of the allowed behaviour. ullet Characterise the allowed behaviour as  $\mathcal{A}_2$  and model the design as  $\mathcal{A}_1.$ 

 $\bullet$  If language inclusion was decidable, then we could use it to decide universality of  ${\cal A}$  by checking

where  $\mathcal{A}_{univ}$  is any universal TBA (which is easy to construct).  $\mathcal{L}(\mathcal{A}_{univ}) \subseteq \mathcal{L}(\mathcal{A})$ 

- Given: A timed regular language W over B (that is, there is a TBA A such that  $\mathcal{L}(A)=W$ ).
   Question: Is  $\overline{W}$  timed regular?

Possible applications of a decision procedure:

$$L(A_1) \cap L(A_3) = \emptyset$$
,

- that is, whether the design has any non-allowed behaviour.
- Characterise the allowed behaviour as  $\mathcal{A}_2$  and model the design as  $\mathcal{A}_1$ .
   Automatically construct  $\mathcal{A}_3$  with  $L(\mathcal{A}_3)=\overline{L(\mathcal{A}_2)}$  and check

$$L(A_1) \cap L(A_3) = 0$$

Taking for granted that:
 The interaction automator is effectively computable.
 The interaction automator is effectively computable.
 The emptyness problem for Bickli automata is decidable.
 (Proof by construction of region automaton [Alur and Dill, 1994].)

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Consequences: Complementation

- \* Given: A timed regular language W over B (that is, there is a TBA  $\mathcal A$  such that  $\mathcal L(\mathcal A)=W$ ). 
   Question: Is  $\overline W$  timed regular?

# Consequences: Complementation

- Given: A timed regular language W over B (that is, there is a TBA A such that L(A)=W). Question: Is  $\overline{W}$  timed regular?
- If the class of timed regular languages were closed under comple-mentation, "the complement of the inclusion problem is recursively enumerable. This contradicts the III<sub>1</sub>-hardness of the inclusion prob-lem." [Alur and Dili, 1994]

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## Beyond Timed Regular

With clock constraints of the form

$$x + y \le x' + y'$$

we can describe timed languages which are not timed regular.

In other words:

- There are strictly timed languages than timed regular languages.
- There exists timed languages L such that there exists no  $\mathcal A$  with  $L(\mathcal A)=L$ .



 $\{((abc)^\omega,\tau)\mid \forall j.(\tau_{3j}-\tau_{3j-1})=2(\tau_{3j-1}-\tau_{3j-2})\}$ 

here exists timed languages 
$$L$$
 such that there exists no  ${\cal A}$  with  $L({\cal A})=L$ 

# Consequences: Complementation

- Given: A timed regular language W over B (that is, there is a TBA A such that L(A) = W).
   Question: Is W timed regular?
- If the class of timed regular languages were closed under comple-mentation, "the complement of the inclusion problem is recursively enumerable. This contradicts the II]-hardness of the inclusion prob-lem." [Alur and Dill, 1994]

A non-complementable TBA A:

Complement language:  $\mathcal{L}(\mathcal{A}) = \{ (a^{\omega}, (t_i)_{i \in \mathbb{N}_0}) \mid \exists i \in \mathbb{N}_0 \ \exists j > i : (t_j = t_i + 1) \}$ 

 $\overline{\mathcal{L}(\mathcal{A})} = \{(a^\omega, (t_t)_{t \in \mathbb{N}_0}) \mid \text{no two } a \text{ are separated by distance 1}\}.$ 

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Beyond Timed Regular

References

[Alur and Dill, 1994] Alur, R. and Dill, D. L. (1994). A theory of timed automata. Theoretical Computer Science, 126(2):183–235. [Olderog and Diets, 2008] Olderog, E.R. and Diets, H. (2008). Real-Time Systems - Formal Specification and Automatic Verification. Cambridge University Press.

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