

## Contents & Goals

### Last Lecture:

- Undecidability Results for TBA

### This Lecture:

- Educational Objectives: Capabilities for following tasks/questions.
  - How can we refine TA and DC formulae? What's a bit tricky about that?
  - Can we use Uppaal to check whether a TA satisfies a DC formula?
- Content:
  - An evolution-of-observables semantics of TA
  - A satisfaction relation between TA and DC
  - Model-checking DC properties with Uppaal

## Lecture 17: Automatic Verification of DC Properties for TA

2013-07-09

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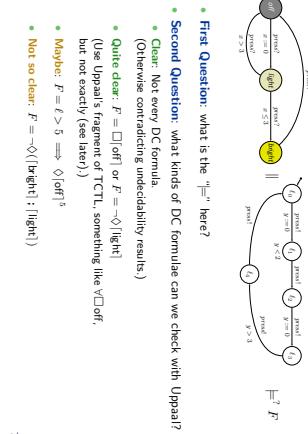
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## Model-Checking DC Properties with Uppaal



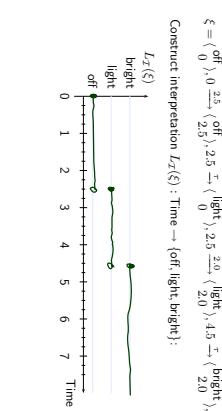
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- First Question: what is the “=?” here?
- Second Question: what kinds of DC formulae can we check with Uppaal?
- Clear: Not every DC formula. (Otherwise contradicting undecidability results.)
- Quite clear:  $F = \square[\text{off}]$  or  $F = \neg \square[\text{light}]$
- (Use Uppaal's fragment of CTL, something like  $\vee \square[\text{off}$ , but not exactly see later)
- Maybe:  $F = \ell \geq 3 \implies \diamond[\text{off}]^3$
- Not so clear:  $F = \neg \diamond[\text{bright}] \cdot [\text{light}]$

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## Example 2: Let's Start With Single Runs



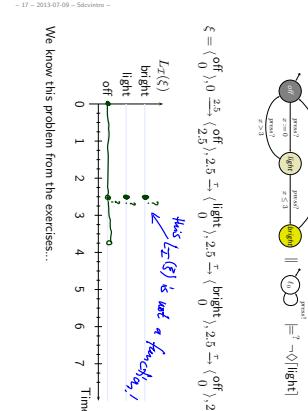
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## Example 2: Another Single Run



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## Observing Timed Automata

### DC Properties of Timed Automata

### Observables of TA Network

Let  $\mathcal{N}$  be a network of  $n$  extended timed automata  
 $\mathcal{A}_{i,i} = (L_i, C_i, B_i, U_i, X_i, V_i, I_i, E_i, \ell_{\min,i})$

**For simplicity:** assume that the  $L_i$  and  $X_i$  are pairwise disjoint and that each  $V_i$  is pairwise disjoint to every  $L_i$  and  $X_i$  (otherwise rename).

**Remarks**

- Definition: The observables  $\text{Obs}(\mathcal{N})$  of  $\mathcal{N}$  are

with  
•  $D(\ell_i) = L_i$   
•  $D(v)$  as given,  $v \in V_i$ .  
 $\{\text{would be less confusing}\}$   
 $\{\text{if we used } \{\mathbb{Q}_1, \dots, \mathbb{Q}_n\}\}$

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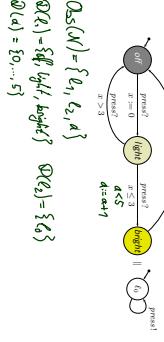
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### Observables of TA Network; Example

$\mathcal{A}_{\text{el}} = \langle L_i, C_i, B_i, U_i, X_i, V_i, I_i, E_i, \ell_{init} \rangle$ ,

The observables  $\text{Obs}(\mathcal{N})$  of  $\mathcal{N}$  are  $\{\ell_1, \dots, \ell_n\} \cup \bigcup_{1 \leq i \leq n} V_i$  with

- $D(\ell) = L_i$ ,
- $D(v)$  as given,  $v \in V_i$ .



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### References

- [Oldehoeft and Dierks, 2008] Oldehoeft, E.-R. and Dierks, H. (2008). *Real-Time Systems - Formal Specification and Automatic Verification*. Cambridge University Press.

### References

- [Oldehoeft and Dierks, 2008] Oldehoeft, E.-R. and Dierks, H. (2008). *Real-Time Systems - Formal Specification and Automatic Verification*. Cambridge University Press.

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