

Softwaretechnik / Software-Engineering

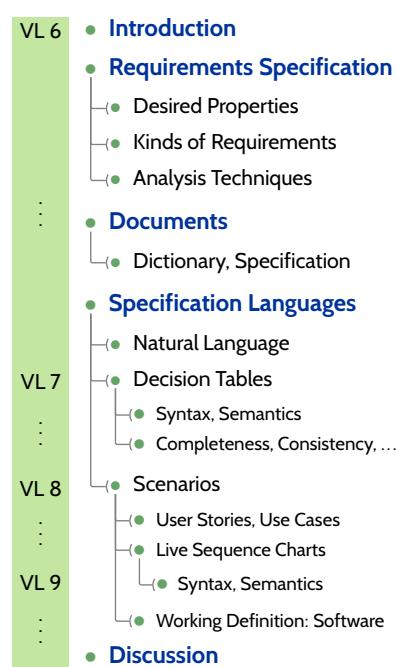
Lecture 9: Live Sequence Charts

2016-06-06

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Topic Area Requirements Engineering: Content



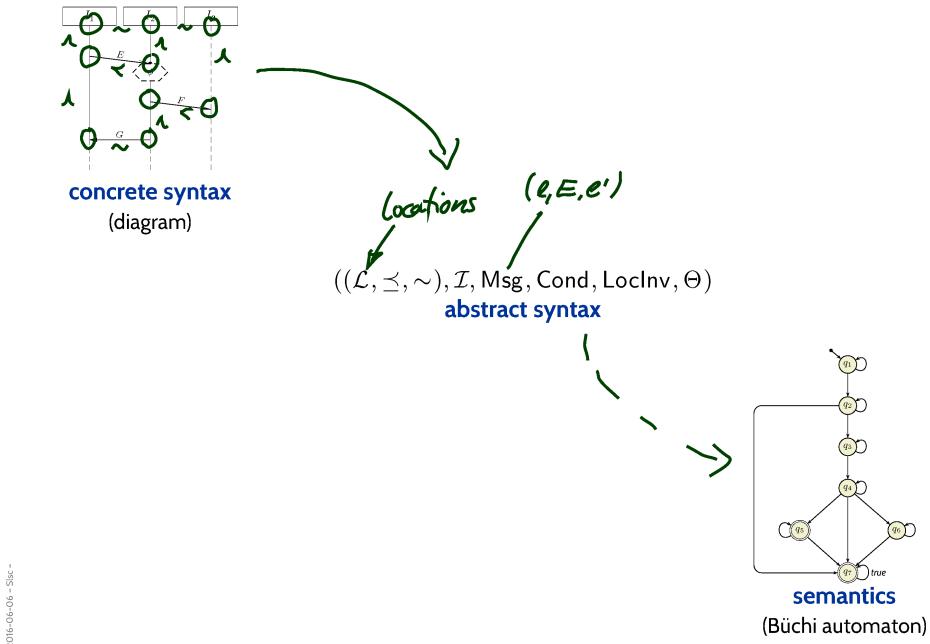
Content

- **Excursion: Symbolic Büchi Automata**
- **LSC Semantics:**
 - ↳ Cuts, Firedsets,
 - ↳ Automaton Construction
 - ↳ Full LSC (activation, chart mode)
- **Pre-Charts**
 - ↳ Requirements Engineering with scenarios
 - ↳ Strengthening scenarios into requirements
- **Software, formally**
 - ↳ Software specification
 - ↳ Requirements Engineering, formally
 - ↳ Software **implements** specification
- **LSCs vs. Software**
 - ↳ Software **implements** LSCs
 - ↳ Scenarios and tests
 - ↳ Play In/Play Out
- **Requirements Engineering Wrap-Up**

3/56

LSC Semantics

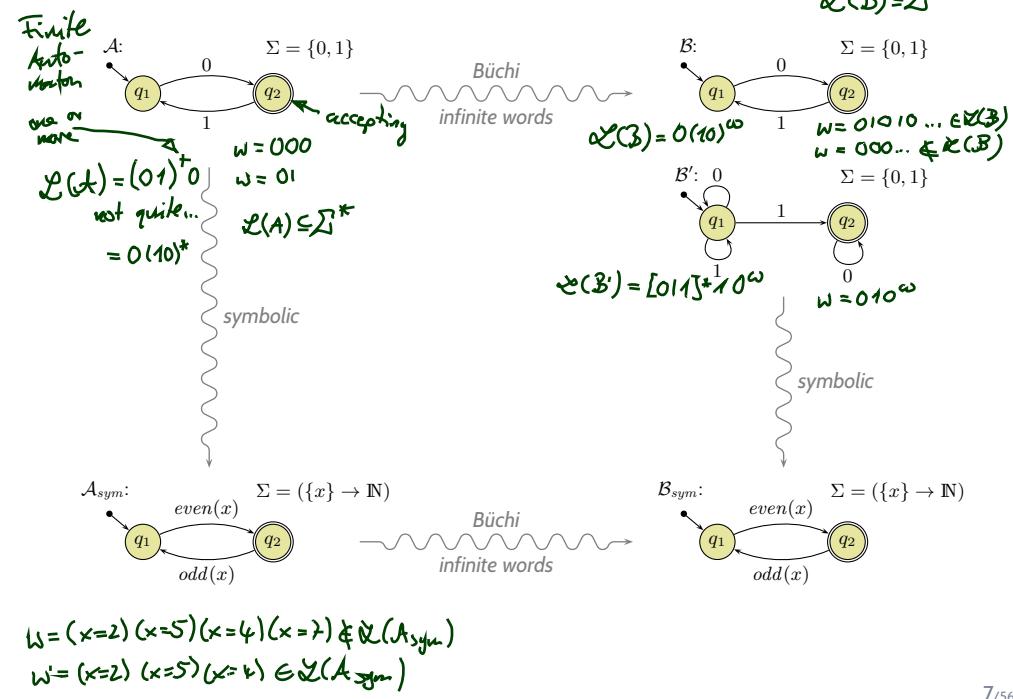
The Plan: A Formal Semantics for a Visual Formalism



Excursion: Symbolic Büchi Automata

From Finite Automata to Symbolic Büchi Automata

$$\mathcal{L}(\mathcal{B}) \subseteq \Sigma^\omega$$



Symbolic Büchi Automata

Definition. A **Symbolic Büchi Automaton** (TBA) is a tuple

$$\mathcal{B} = (\mathcal{C}_B, Q, q_{ini}, \rightarrow, Q_F)$$

where

- \mathcal{C}_B is a set of atomic propositions,
- Q is a finite set of **states**,
- $q_{ini} \in Q$ is the initial state,
- $\rightarrow \subseteq Q \times \Phi(\mathcal{C}_B) \times Q$ is the finite **transition relation**.
Each transitions $(q, \psi, q') \in \rightarrow$ from state q to state q' is labelled with a formula $\psi \in \Phi(\mathcal{C}_B)$.
- $Q_F \subseteq Q$ is the set of **fair** (or accepting) states.

Run of TBA

Definition. Let $\mathcal{B} = (\mathcal{C}_\mathcal{B}, Q, q_{ini}, \rightarrow, Q_F)$ be a TBA and

$$w = \sigma_1, \sigma_2, \sigma_3, \dots \in (\Phi(\mathcal{C}_\mathcal{B}) \rightarrow \mathbb{B})^\omega$$

an infinite word, each letter is a valuation of $\Phi(\mathcal{C}_\mathcal{B})$.

An infinite sequence

$$\varrho = q_0, q_1, q_2, \dots \in Q^\omega$$

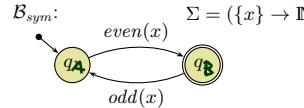
of states is called **run** of \mathcal{B} over w if and only if

- $q_0 = q_{ini}$,
- for each $i \in \mathbb{N}_0$ there is a transition $(q_i, \psi_i, q_{i+1}) \in \rightarrow$ s.t. $\sigma_i \models \psi_i$.

$$\Sigma = (x=2)(x=5)(x=4)^\omega$$

$$\varrho = q_A, q_B, q_A, q_B, \dots$$

Example:



9/56

The Language of a TBA

Definition.

We say TBA $\mathcal{B} = (\mathcal{C}_\mathcal{B}, Q, q_{ini}, \rightarrow, Q_F)$ **accepts** the word

$$w = (\sigma_i)_{i \in \mathbb{N}_0} \in (\Phi(\mathcal{C}_\mathcal{B}) \rightarrow \mathbb{B})^\omega$$

if and only if \mathcal{B} **has** a run

$$\varrho = (q_i)_{i \in \mathbb{N}_0}$$

over w such that

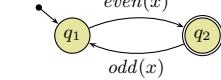
fair (or accepting) states are **visited infinitely often** by ϱ , i.e., such that

$$\forall i \in \mathbb{N}_0 \exists j > i : q_j \in Q_F.$$

We call the set $Lang(\mathcal{B}) \subseteq (\Phi(\mathcal{C}_\mathcal{B}) \rightarrow \mathbb{B})^\omega$ of words that are accepted by \mathcal{B} the **language of \mathcal{B}** .

$$\mathcal{B}_{sym}: \Sigma = (\{x\} \rightarrow \mathbb{N})$$

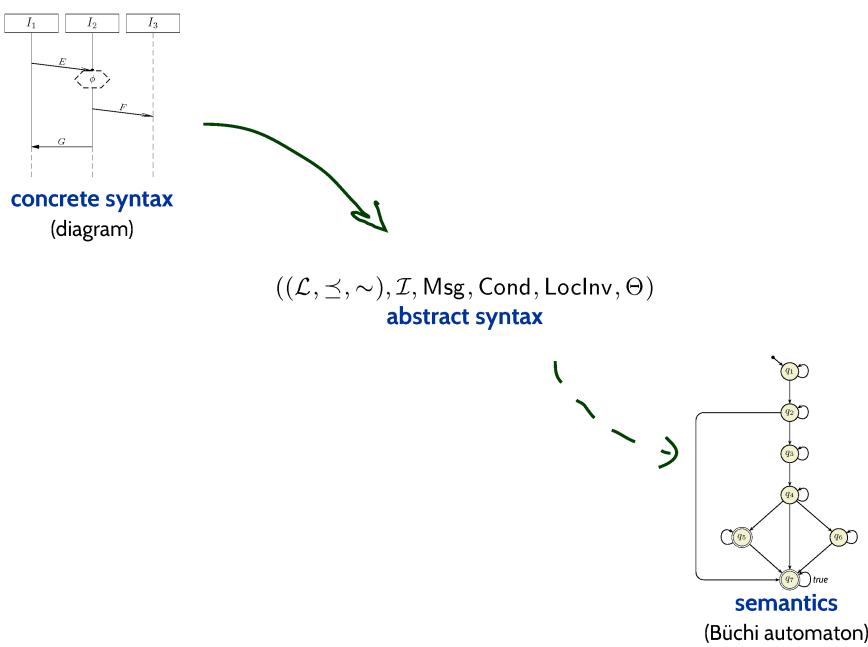
Example:



10/56

LSC Semantics: TBA Construction

The Plan: A Formal Semantics for a Visual Formalism



LSC Semantics: It's in the Cuts!

$\{I_1, \dots, I_n\}$

Definition. Let $((\mathcal{L}, \preceq, \sim), \mathcal{I}, \text{Msg}, \text{Cond}, \text{LocInv}, \Theta)$ be an LSC body.

A non-empty set $\emptyset \neq C \subseteq \mathcal{L}$ is called a **cut** of the LSC body iff C

- is **downward closed**, i.e.

$$\forall l, l' \in \mathcal{L} \bullet l' \in C \wedge l \preceq l' \implies l \in C,$$

- is **closed under simultaneity**, i.e.

$$\forall l, l' \in \mathcal{L} \bullet l' \in C \wedge l \sim l' \implies l \in C, \text{ and}$$

- comprises at least **one location per instance line**, i.e.

$$\forall I \in \mathcal{I} \bullet C \cap I \neq \emptyset.$$

The temperature function is extended to cuts as follows:

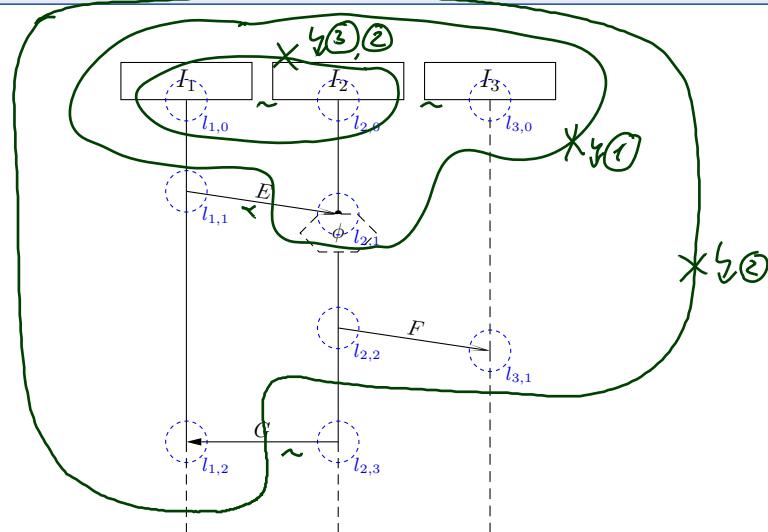
$$\Theta(C) = \begin{cases} \text{hot} & , \text{if } \exists l \in C \bullet (\nexists l' \in C \bullet l \prec l') \wedge \Theta(l) = \text{hot} \\ \text{cold} & , \text{otherwise} \end{cases}$$

that is, C is **hot** if and only if at least one of its maximal elements is hot.

Cut Examples

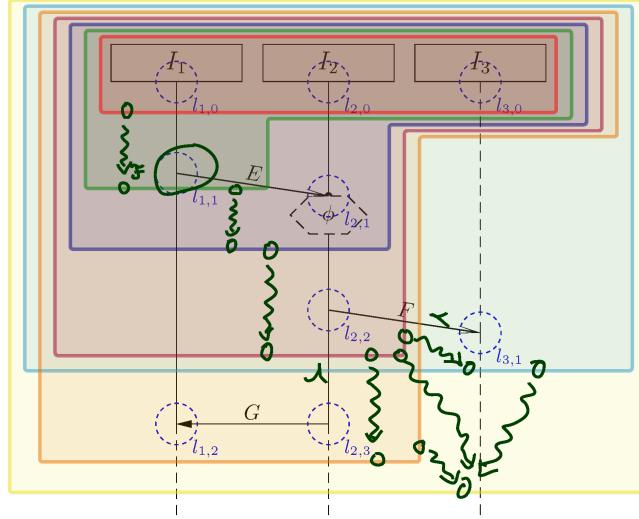
① ② ③

$\emptyset \neq C \subseteq \mathcal{L}$ – downward closed – simultaneity closed – at least one loc. per instance line



Cut Examples

$\emptyset \neq C \subseteq \mathcal{L}$ – downward closed – simultaneity closed – at least one loc. per instance line



A Successor Relation on Cuts

The partial order “ \preceq ” and the simultaneity relation “ \sim ” of locations induce a **direct successor relation** on cuts of an LSC body as follows:

Definition.

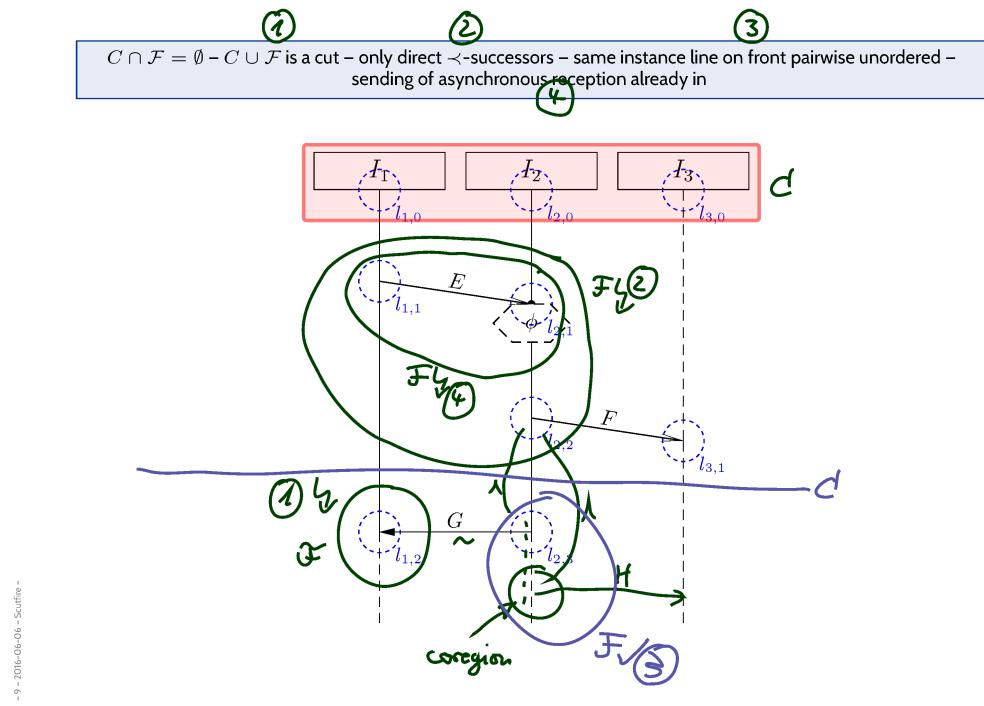
Let $C \subseteq \mathcal{L}$ be a cut of LSC body $((\mathcal{L}, \preceq, \sim), \mathcal{I}, \text{Msg}, \text{Cond}, \text{LocInv}, \Theta)$.

A set $\emptyset \neq \mathcal{F} \subseteq \mathcal{L}$ of locations is called fired-set \mathcal{F} of cut C if and only if

- $C \cap \mathcal{F} = \emptyset$ and $C \cup \mathcal{F}$ is a **cut**, i.e. \mathcal{F} is closed under simultaneity,
- all locations in \mathcal{F} are **direct \prec -successors** of the front of C , i.e.
 $\forall l \in \mathcal{F} \exists l' \in C \bullet l' \prec l \wedge (\nexists l'' \in C \bullet l' \prec l'')$,
- locations in \mathcal{F} , that lie on the same instance line, are **pairwise unordered**, i.e.
 $\forall l \neq l' \in \mathcal{F} \bullet (\exists I \in \mathcal{I} \bullet \{l, l'\} \subseteq I) \implies l \not\preceq l' \wedge l' \not\preceq l$,
- for each asynchronous message reception in \mathcal{F} ,
the corresponding sending is already in C ,
 $\forall (l, E, l') \in \text{Msg} \bullet l' \in \mathcal{F} \implies l \in C$.

The cut $C' = C \cup \mathcal{F}$ is called **direct successor of C via \mathcal{F}** , denoted by $C \rightsquigarrow_{\mathcal{F}} C'$.

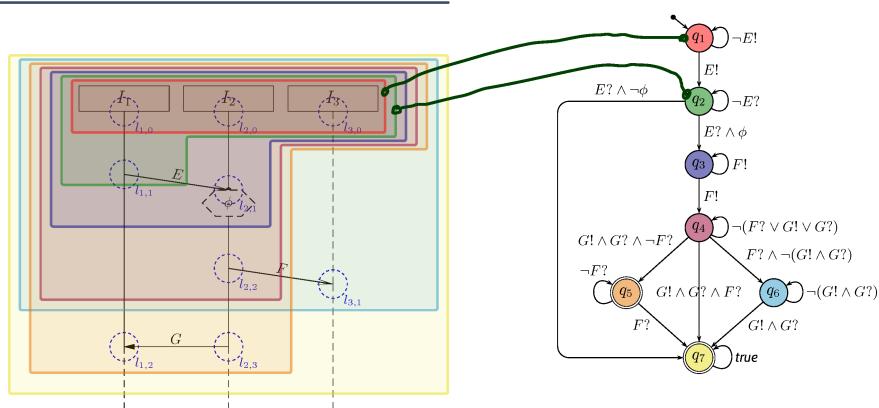
Successor Cut Example



- 9 - 2016-06-06 - Scattolon -

16/56

Language of LSC Body: Example



The TBA $\mathcal{B}(\mathcal{L})$ of LSC \mathcal{L} over \mathcal{C} and \mathcal{E} is $(\mathcal{C}_B, Q, q_{ini}, \rightarrow, Q_F)$ with

- $\mathcal{C}_B = \mathcal{C} \dot{\cup} \mathcal{E}_{!?}$, where $\mathcal{E}_{!?} = \{E!, E? \mid E \in \mathcal{E}\}$,
- Q is the set of cuts of \mathcal{L} , q_{ini} is the instance heads cut,
- \rightarrow consists of loops, progress transitions (from $\rightsquigarrow_{\mathcal{F}}$), and legal exits (cold cond./local inv.),
- $Q_F = \{C \in Q \mid \Theta(C) = \text{cold} \vee C = \mathcal{L}\}$ is the set of cold cuts and the maximal cut.

- 9 - 2016-06-06 - Scattolon -

17/56

TBA Construction Principle

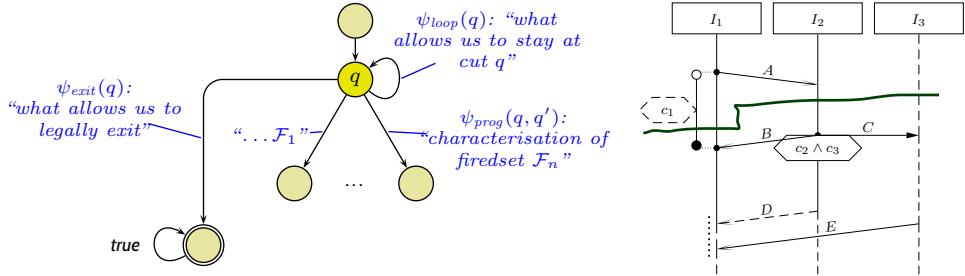
Recall: The TBA $\mathcal{B}(\mathcal{L})$ of LSC \mathcal{L} is $(\mathcal{C}, Q, q_{ini}, \rightarrow, Q_F)$ with

- Q is the set of cuts of \mathcal{L} , q_{ini} is the instance heads cut,
- $\mathcal{C}_{\mathcal{B}} = \mathcal{C} \cup \mathcal{E}_{!?}$,
- \rightarrow consists of loops, progress transitions (from $\rightsquigarrow_{\mathcal{F}}$), and legal exits (cold cond./local inv.),
- $\mathcal{F} = \{C \in Q \mid \Theta(C) = \text{cold} \vee C = \mathcal{L}\}$ is the set of cold cuts.

So in the following, we “only” need to construct the transitions’ labels:

$$\rightarrow = \{(q, \psi_{loop}(q), q) \mid q \in Q\} \cup \{(q, \psi_{prog}(q, q'), q') \mid q \rightsquigarrow_{\mathcal{F}} q'\} \cup \{(q, \psi_{exit}(q), \mathcal{L}) \mid q \in Q\}$$

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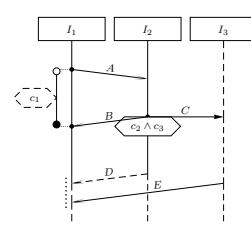
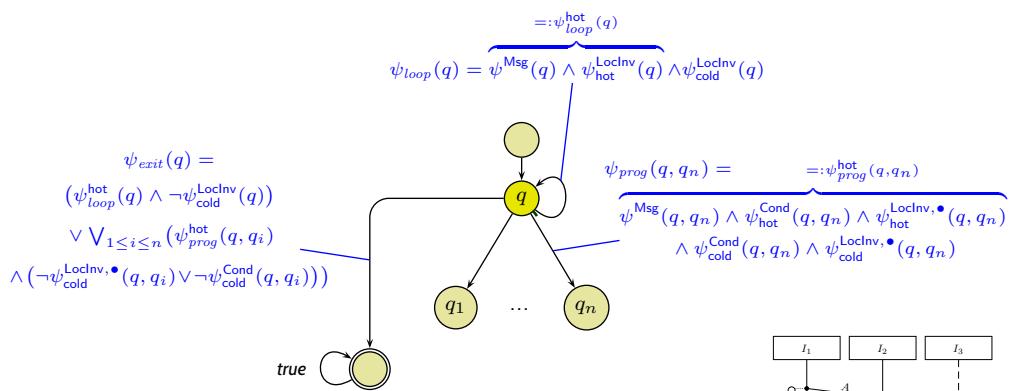
18/56

TBA Construction Principle

“Only” construct the transitions’ labels:

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- 9 - 2016-06-Scifire -



19/56

Loop Condition

$$\psi_{loop}(q) = \psi^{\text{Msg}}(q) \wedge \psi_{\text{hot}}^{\text{LocInv}}(q) \wedge \psi_{\text{cold}}^{\text{LocInv}}(q)$$

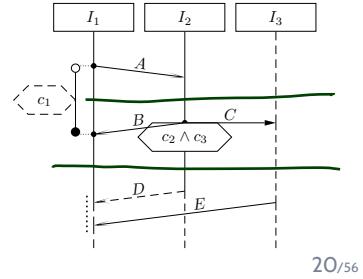
- $\psi^{\text{Msg}}(q) = \neg \bigvee_{1 \leq i \leq n} \psi^{\text{Msg}}(q, q_i) \wedge (\text{strict} \implies \underbrace{\bigwedge_{\psi \in \mathcal{E}_{!?} \cap \text{Msg}(\mathcal{L})} \neg \psi}_{=: \psi_{\text{strict}}(q)})$

- $\psi_{\theta}^{\text{LocInv}}(q) = \bigwedge_{\ell=(l, \iota, \phi, l', \iota') \in \text{LocInv}, \Theta(\ell)=\theta, \ell \text{ active at } q} \phi$

A location l is called **front location** of cut C if and only if $\nexists l' \in \mathcal{L} \bullet l \prec l'$.

Local invariant $(l_0, \iota_0, \phi, l_1, \iota_1)$ is **active** at cut $(!) q$ if and only if $l_0 \preceq l \prec l_1$ for some front location l of cut q or $l = l_1 \wedge \iota_1 = \bullet$.

- $\text{Msg}(\mathcal{F}) = \{E! \mid (l, E, l') \in \text{Msg}, l \in \mathcal{F}\} \cup \{E? \mid (l, E, l') \in \text{Msg}, l' \in \mathcal{F}\}$
- $\text{Msg}(\mathcal{F}_1, \dots, \mathcal{F}_n) = \bigcup_{1 \leq i \leq n} \text{Msg}(\mathcal{F}_i)$



20/56

Progress Condition

$$\psi_{\text{prog}}^{\text{hot}}(q, q_i) = \psi^{\text{Msg}}(q, q_n) \wedge \psi_{\text{hot}}^{\text{Cond}}(q, q_n) \wedge \psi_{\text{hot}}^{\text{LocInv}, \bullet}(q_n)$$

- $\psi^{\text{Msg}}(q, q_i) = \bigwedge_{\psi \in \text{Msg}(q_i \setminus q)} \psi \wedge \bigwedge_{j \neq i} \bigwedge_{\psi \in (\text{Msg}(q_j \setminus q) \setminus \text{Msg}(q_i \setminus q))} \neg \psi$
 $\wedge (\text{strict} \implies \underbrace{\bigwedge_{\psi \in (\mathcal{E}_{!?} \cap \text{Msg}(\mathcal{L})) \setminus \text{Msg}(\mathcal{F}_i)} \neg \psi}_{=: \psi_{\text{strict}}(q, q_i)})$

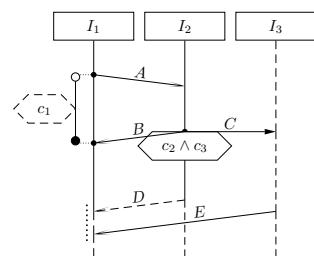
- $\psi_{\theta}^{\text{Cond}}(q, q_i) = \bigwedge_{\gamma=(L, \phi) \in \text{Cond}, \Theta(\gamma)=\theta, L \cap (q_i \setminus q) \neq \emptyset} \phi$

- $\psi_{\theta}^{\text{LocInv}, \bullet}(q, q_i) = \bigwedge_{\lambda=(l, \iota, \phi, l', \iota') \in \text{LocInv}, \Theta(\lambda)=\theta, \lambda \bullet\text{-active at } q_i} \phi$

Local invariant $(l_0, \iota_0, \phi, l_1, \iota_1)$ is **•-active** at q if and only if

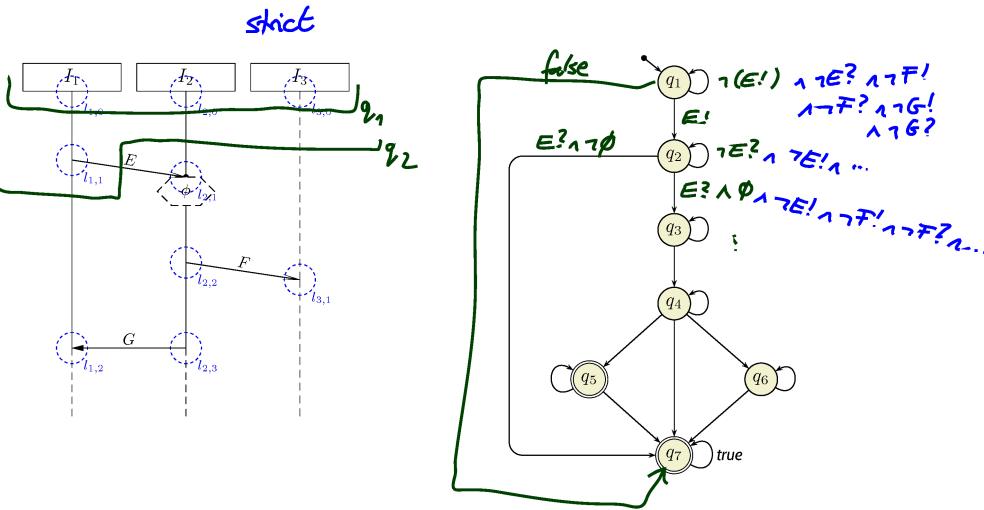
- $l_0 \prec l \prec l_1$, or
- $l = l_0 \wedge \iota_0 = \bullet$, or
- $l = l_1 \wedge \iota_1 = \bullet$

for some front location l of cut $(!) q$.



21/56

Example

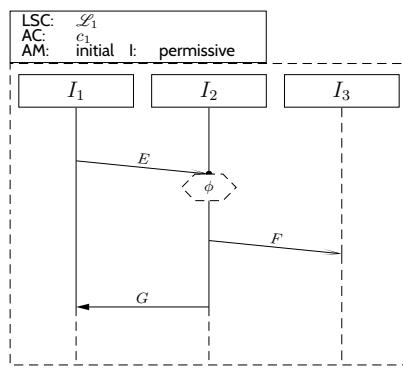


Full LSCs

A **full LSC** $\mathcal{L} = (((\mathcal{L}, \preceq, \sim), \mathcal{I}, \text{Msg}, \text{Cond}, \text{LocInv}, \Theta), ac_0, am, \Theta_{\mathcal{L}})$ consists of

- **body** $((\mathcal{L}, \preceq, \sim), \mathcal{I}, \text{Msg}, \text{Cond}, \text{LocInv}, \Theta)$,
- **activation condition** $ac_0 \in \Phi(\mathcal{C})$,
- **strictness flag** *strict* (if *false*, \mathcal{L} is **permissive**)
- **activation mode** $am \in \{\text{initial}, \text{invariant}\}$,
- **chart mode existential** ($\Theta_{\mathcal{L}} = \text{cold}$) or **universal** ($\Theta_{\mathcal{L}} = \text{hot}$).

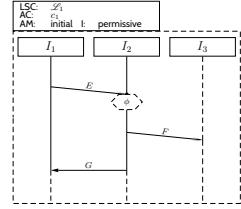
Concrete syntax:



Full LSCs

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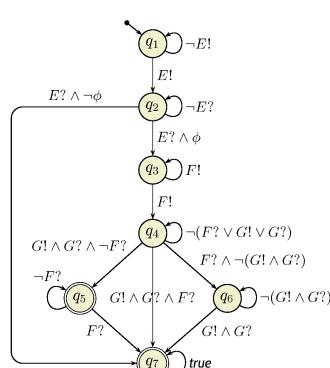
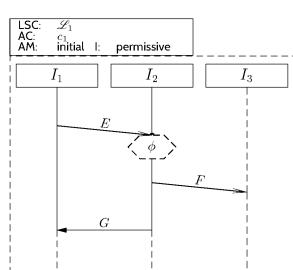


A set of words $W \subseteq (\mathcal{C} \rightarrow \mathbb{B})^\omega$ is **accepted** by \mathcal{L} if and only if

| $\Theta_{\mathcal{L}}$ | $am = \text{initial}$ | $am = \text{invariant}$ |
|------------------------|--|---|
| cold | $\exists w \in W \bullet w^0 \models ac \wedge w^0 \models \psi_{\text{hot}}^{\text{Cond}}(\emptyset, C_0) \wedge w/1 \in \text{Lang}(\mathcal{B}(\mathcal{L}))$ | $\exists w \in W \exists k \in \mathbb{N}_0 \bullet w^k \models ac \wedge w^k \models \psi_{\text{hot}}^{\text{Cond}}(\emptyset, C_0) \wedge w/k + 1 \in \text{Lang}(\mathcal{B}(\mathcal{L}))$ |
| hot | $\forall w \in W \bullet w^0 \models ac \implies w^0 \models \psi_{\text{hot}}^{\text{Cond}}(\emptyset, C_0) \wedge w/1 \in \text{Lang}(\mathcal{B}(\mathcal{L}))$ | $\forall w \in W \forall k \in \mathbb{N}_0 \bullet w^k \models ac \implies w^k \models \psi_{\text{hot}}^{\text{Cond}}(\emptyset, C_0) \wedge w/k + 1 \in \text{Lang}(\mathcal{B}(\mathcal{L}))$ |

where $ac = ac_0 \wedge \psi_{\text{cold}}^{\text{Cond}}(\emptyset, C_0) \wedge \psi^{\text{Msg}}(\emptyset, C_0)$; C_0 is the minimal (or **instance heads**) cut.

Full LSC Semantics: Example



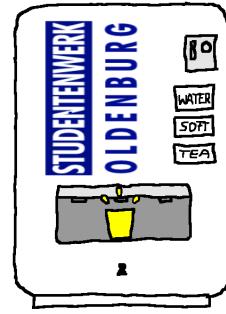
Example: Vending Machine

- **Positive scenario:** Buy a Softdrink

- Insert one 1 euro coin.
- Press the 'softdrink' button.
- Get a softdrink.

- **Positive scenario:** Get Change

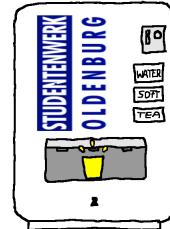
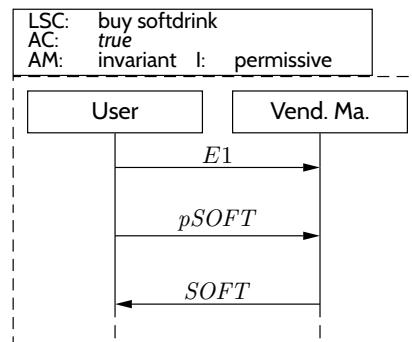
- Insert one 50 cent and one 1 euro coin.
- Press the 'softdrink' button.
- Get a softdrink.
- Get 50 cent change.



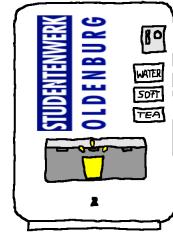
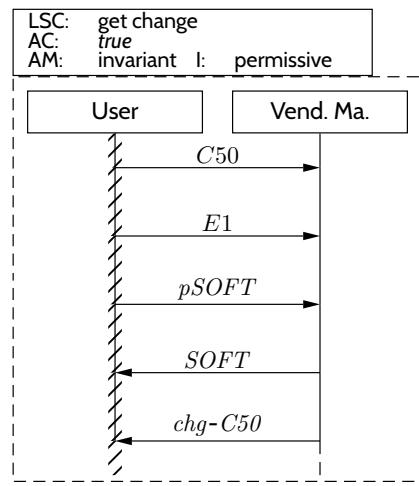
- **Negative scenario:** A Drink for Free

- Insert one 1 euro coin.
- Press the 'softdrink' button.
- Do not insert any more money.
- Get **two** softdrinks.

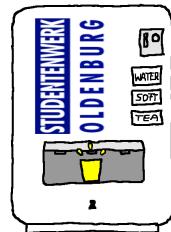
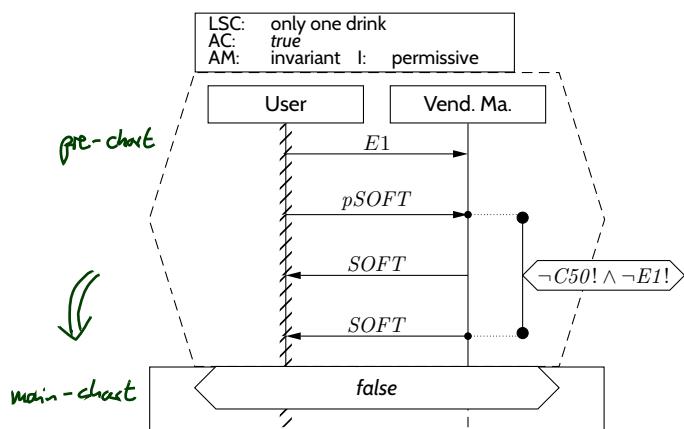
Example: Buy A Softdrink



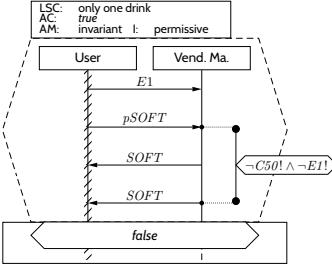
Example: Get Change



Anti-Scenarios: Don't Give Two Drinks



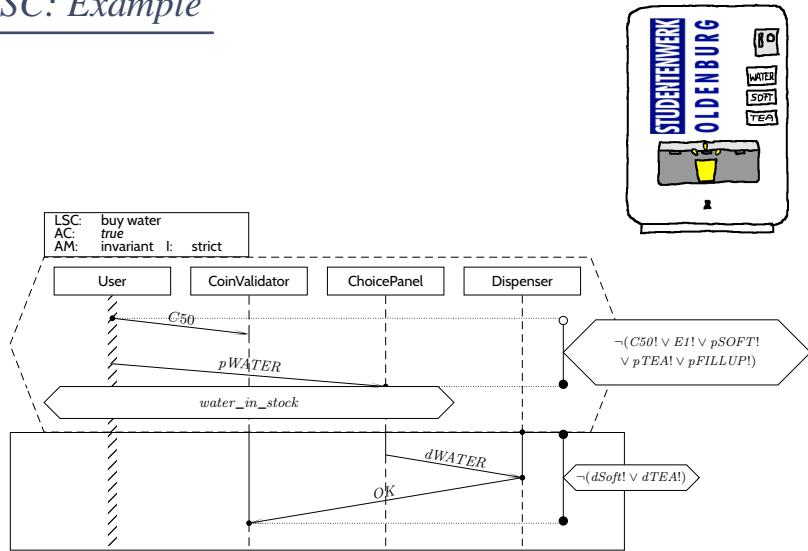
Pre-Charts



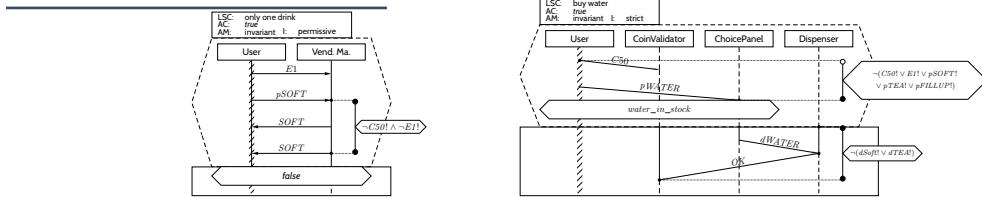
A full LSC $\mathcal{L} = (PC, MC, ac_0, am, \Theta_{\mathcal{L}})$ actually consist of

- **pre-chart** $PC = ((\mathcal{L}_P, \preceq_P, \sim_P), \mathcal{I}_P, \text{Msg}_P, \text{Cond}_P, \text{LocInv}_P, \Theta_P)$ (possibly empty).
- **main-chart** $MC = ((\mathcal{L}_M, \preceq_M, \sim_M), \mathcal{I}_M, \text{Msg}_M, \text{Cond}_M, \text{LocInv}_M, \Theta_M)$ (non-empty).
- **activation condition** $ac_0 \in \Phi(\mathcal{C})$.
- **strictness flag** *strict* (if *false*, \mathcal{L} is **permissive**)
- **activation mode** $am \in \{\text{initial}, \text{invariant}\}$,
- **chart mode existential** ($\Theta_{\mathcal{L}} = \text{cold}$) or **universal** ($\Theta_{\mathcal{L}} = \text{hot}$).

Universal LSC: Example

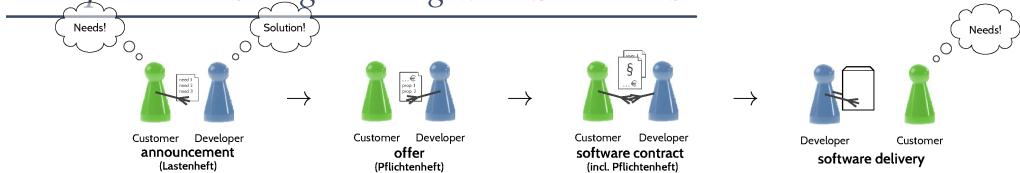


Pre-Charts Semantics



| $\Theta_{\mathcal{L}}$ | $am = \text{initial}$ | $am = \text{invariant}$ |
|------------------------|--|--|
| cold | $\exists w \in W \exists m \in \mathbb{N}_0 \bullet w^0 \models ac$ $\wedge w^0 \models \psi_{\text{hot}}^{\text{Cond}}(\emptyset, C_0^P)$ $\wedge w/1, \dots, w/m \in \text{Lang}(\mathcal{B}(PC))$ $\wedge w^{m+1} \models \psi_{\text{hot}}^{\text{Cond}}(\emptyset, C_0^M)$ $\wedge w/m + 1 \in \text{Lang}(\mathcal{B}(MC))$ | $\exists w \in W \exists k < m \in \mathbb{N}_0 \bullet w^k \models ac$ $\wedge w^k \models \psi_{\text{hot}}^{\text{Cond}}(\emptyset, C_0^P)$ $\wedge w/k + 1, \dots, w/m \in \text{Lang}(\mathcal{B}(PC))$ $\wedge w^{m+1} \models \psi_{\text{hot}}^{\text{Cond}}(\emptyset, C_0^M)$ $\wedge w/m + 1 \in \text{Lang}(\mathcal{B}(MC))$ |
| hot | $\forall w \in W \bullet w^0 \models ac$ $\wedge w^0 \models \psi_{\text{hot}}^{\text{Cond}}(\emptyset, C_0^P)$ $\wedge w/1, \dots, w/m \in \text{Lang}(\mathcal{B}(PC))$ $\wedge w^{m+1} \models \psi_{\text{cold}}^{\text{Cond}}(\emptyset, C_0^M)$ $\implies w^{m+1} \models \psi_{\text{cold}}^{\text{Cond}}(\emptyset, C_0^M)$ $\wedge w/m + 1 \in \text{Lang}(\mathcal{B}(MC))$ | $\forall w \in W \forall k \leq m \in \mathbb{N}_0 \bullet w^k \models ac$ $\wedge w^k \models \psi_{\text{hot}}^{\text{Cond}}(\emptyset, C_0^P)$ $\wedge w/k + 1, \dots, w/m \in \text{Lang}(\mathcal{B}(PC))$ $\wedge w^{m+1} \models \psi_{\text{cold}}^{\text{Cond}}(\emptyset, C_0^M)$ $\implies w^{m+1} \models \psi_{\text{cold}}^{\text{Cond}}(\emptyset, C_0^M)$ $\wedge w/m + 1 \in \text{Lang}(\mathcal{B}(MC))$ |

Requirements Engineering with Scenarios

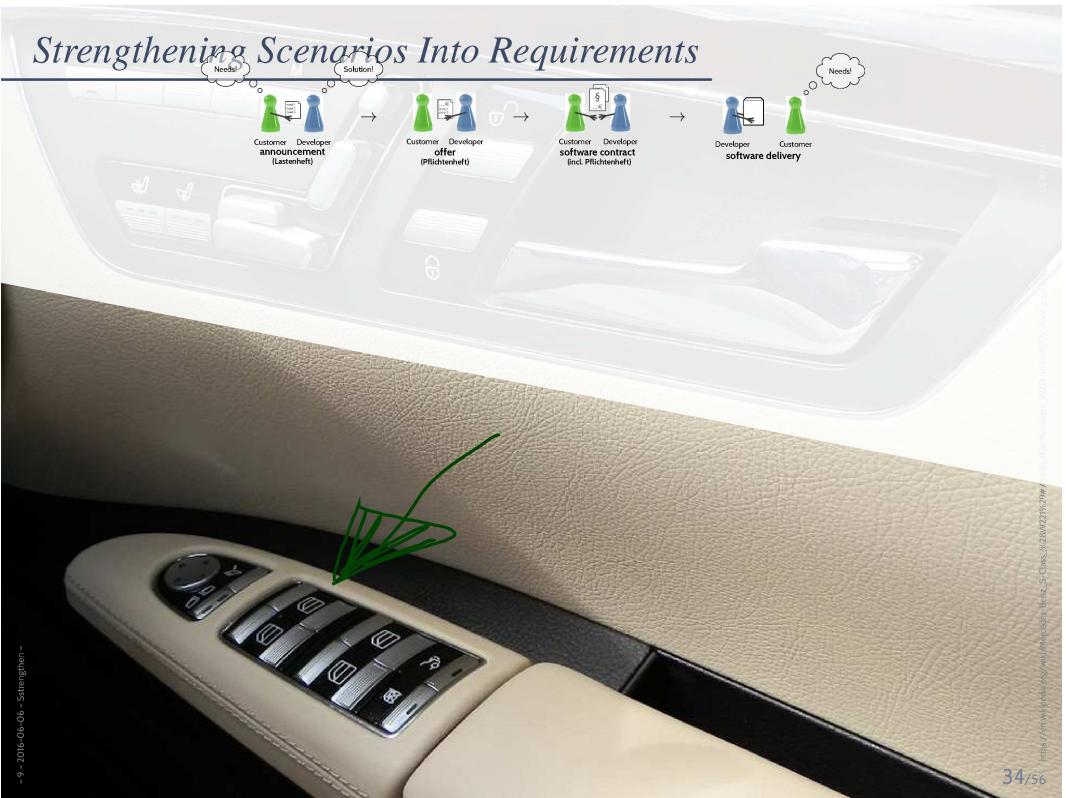


One quite effective approach:

- (i) **Approximate** the software requirements: ask for positive / negative **existential scenarios**.
- (ii) **Refine** result into **universal scenarios** (and validate them with customer).

That is:

- Ask the customer to describe **example usages** of the desired system.
In the sense of: "If the system is not at all able to do this, then it's not what I want."
(\rightarrow positive use-cases, existential LSC)
- Ask the customer to describe behaviour that **must not happen** in the desired system.
In the sense of: "If the system does this, then it's not what I want."
(\rightarrow negative use-cases, LSC with pre-chart and hot-false)
- Investigate preconditions, side-conditions, exceptional cases and corner-cases.
(\rightarrow extend use-cases, refine LSCs with conditions or local invariants)
- Generalise into universal requirements, e.g., **universal LSCs**.
- **Validate** with customer using new positive / negative scenarios.

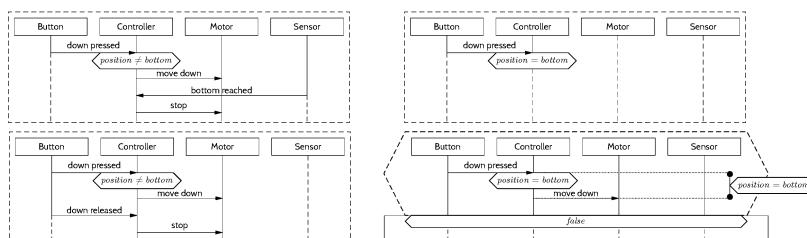


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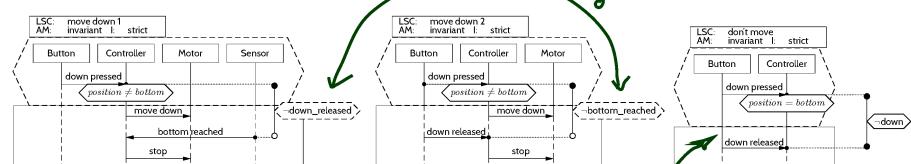
Strengthening Scenarios Into Requirements

Customer -> Developer announcement (Lastenheft) → Customer -> Developer offer (Pflichtenheft) → Customer -> Developer software contract (incl. Pflichtenheft) → Developer software delivery

- Ask customer for (pos./neg.) scenarios, note down as existential LSCs:



- Strengthen into requirements, note down as universal LSCs:



- Re-Discuss with customer using example words of the LSCs' language.

could be cold

Tell Them What You've Told Them...

- **Live Sequence Charts** (if well-formed)
 - have an abstract syntax.
- From an abstract syntax, mechanically construct its **TBA**.
- A **universal LSC** is **satisfied** by a software S if and only if
 - **all words** induced by the computation paths of S
 - are **accepted** by the LSC's TBA.
- An **existential LSC** is **satisfied** by a software S if and only if
 - **there is a word** induced by a computation path of S
 - which is **accepted** by the LSC's TBA.
- **Pre-charts** allow us to specify
 - anti-scenarios ("this must not happen"),
 - activation interactions.
- **Method:**
 - discuss (anti-)scenarios with customer,
 - generalise into universal LSCs and re-validate.

References

References

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