

Softwaretechnik / Software-Engineering

Lecture 13: Behavioural Software Modelling

2016-06-27

Prof. Dr. Andreas Podelski, Dr. Bernd Westphal

Albert-Ludwigs-Universität Freiburg, Germany

Topic Area Architecture & Design: Content

VL 11

- **Introduction and Vocabulary**

- **Principles of Design**

- (i) modularity
- (ii) separation of concerns
- (iii) information hiding and data encapsulation
- (iv) abstract data types, object orientation

⋮

- **Software Modelling**

- (i) views and viewpoints, the 4+1 view
- (ii) model-driven/-based software engineering
- (iii) Unified Modelling Language (UML)
- (iv) **modelling structure**

VL 12

⋮

- a) (simplified) class diagrams
- b) (simplified) object diagrams
- c) (simplified) object constraint logic (OCL)



VL 13

- (v) **modelling behaviour**

- a) communicating finite automata
- b) Uppaal query language

} Ex. 1/2

VL 14

⋮

- c) implementing CFA
- d) an outlook on **UML State Machines**

VL 15

- **Design Patterns**

⋮

- **Testing: Introduction**

} Ex. 3

- **Communicating Finite Automata (CFA)**

- concrete and abstract syntax,
- networks of CFA,
- operational semantics.

- **Transition Sequences**

- **Deadlock, Reachability**

- **Uppaal**

- tool demo (simulator),
- query language,
- CFA model-checking.

- **CFA at Work**

- drive to configuration,
- scenarios,
- invariants,
- tool demo (verifier).

- **CFA vs. Software**

Communicating Finite Automata
presentation follows (Olderog and Dierks, 2008)

Channel Names and Actions

To define communicating finite automata, we need the following sets of symbols:

- A set $(a, b \in) \text{Chan}$ of **channel names** or **channels**.
- For each channel $a \in \text{Chan}$, two **visible actions**:
 $a?$ and $a!$ denote **input** and **output** on the **channel** ($a?, a! \notin \text{Chan}$).
- $\tau \notin \text{Chan}$ represents an **internal action**, not visible from outside.
- $(\alpha, \beta \in) \text{Act} := \{a? \mid a \in \text{Chan}\} \cup \{a! \mid a \in \text{Chan}\} \cup \{\tau\}$ is the set of **actions**.
- An **alphabet** B is a set of **channels**, i.e. $B \subseteq \text{Chan}$.
- For each alphabet B , we define the corresponding **action set**

$$B_{?!} := \{a? \mid a \in B\} \cup \{a! \mid a \in B\} \cup \{\tau\}.$$

Note: $\text{Chan}_{?!} = \text{Act}$.

Integer Variables and Expressions, Resets

- Let $(v, w \in) V$ be a set of ((finite domain) integer) variables.

By $(\varphi \in) \Psi(V)$ we denote the set of **integer expressions** over V using function symbols $+, -, \dots, >, \leq, \dots$

- A **modification** on v is *(or update)*

$$v := \varphi, \quad v \in V, \quad \varphi \in \Psi(V).$$

example: $x := 1$
 $y := \underbrace{x+1}_{\in \Psi(V)}$
 $\in V$

By $R(V)$ we denote the set of all modifications.

- By \vec{r} we denote a finite list $\langle r_1, \dots, r_n \rangle, n \in \mathbb{N}_0$, of modifications $r_i \in R(V)$.

$\langle \rangle$ is the empty list ($n = 0$). *(reset vector) or (update vector)*

- By $R(V)^*$ we denote the set of all such finite lists of modifications.

Communicating Finite Automata

Definition. A **communicating finite automaton** is a structure

$$\mathcal{A} = (L, B, V, E, \ell_{ini})$$

where

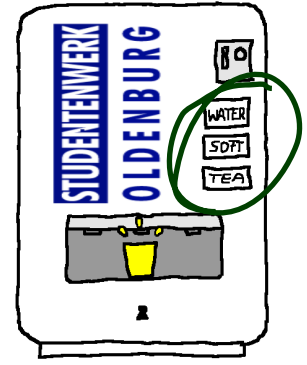
- $(\ell \in) L$ is a finite set of **locations** (or **control states**),
- $B \subseteq \text{Chan}$,
- V : a set of data variables,
- $E \subseteq L \times B_{!?} \times \Phi(V) \times R(V)^* \times L$: a finite set of **directed edges** such that

$$(\ell, \alpha, \varphi, \vec{r}, \ell') \in E \wedge \text{chan}(\alpha) \in U \implies \varphi = \text{true}.$$

Edges $(\ell, \alpha, \varphi, \vec{r}, \ell')$ from location ℓ to ℓ' are labelled with an **action** α , a **guard** φ , and a list \vec{r} of **modifications**.

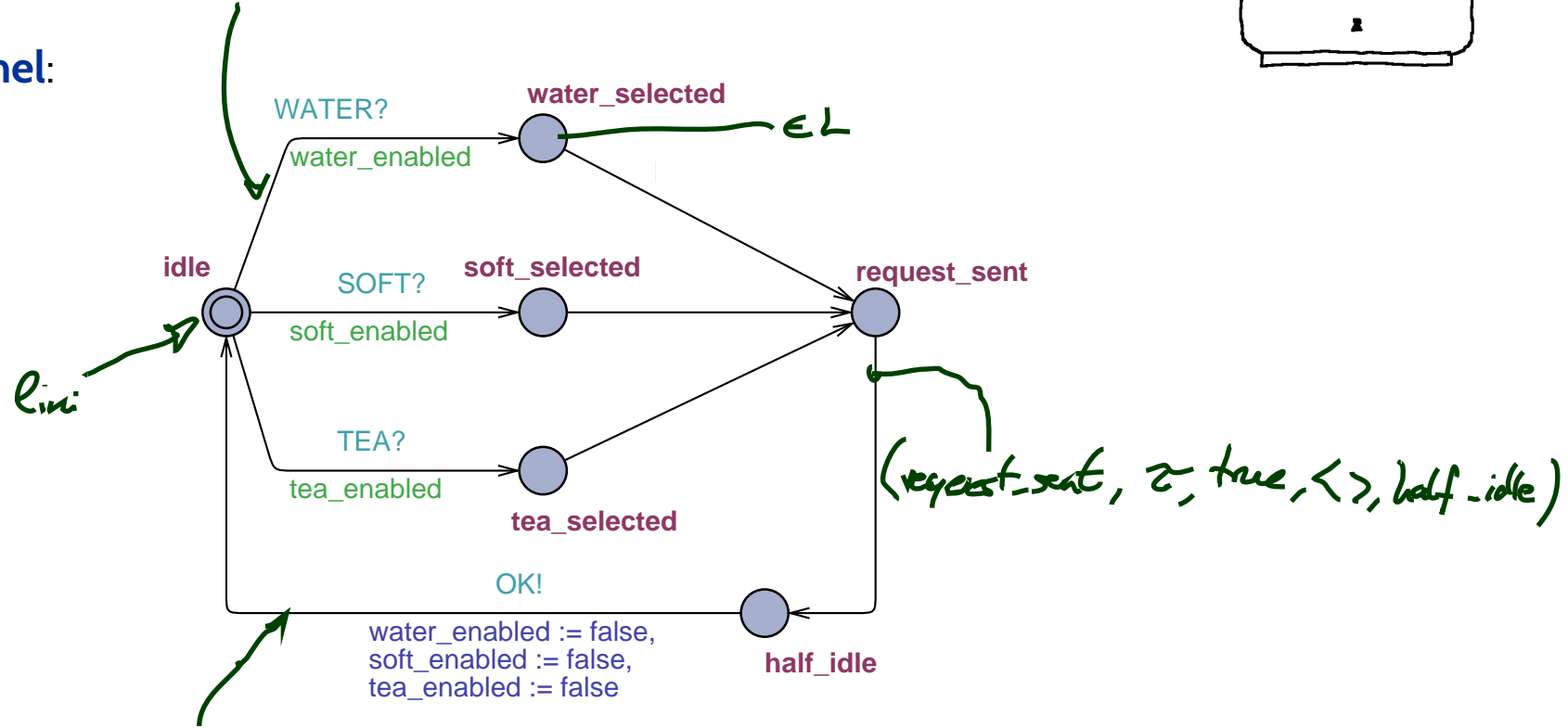
- ℓ_{ini} is the **initial location**.

Example



$(idle, WATER?, water_enabled, \langle \rangle, water_selected) \in E$

ChoicePanel:
(simplified)



$(half_idle, OK!, true, \langle water_enabled := false, \dots \rangle, idle)$

Operational Semantics of Networks of FCA

Definition.

Let $\mathcal{A}_i = (L_i, B_i, V_i, E_i, \ell_{ini,i}), 1 \leq i \leq n$, be communicating finite automata.

The **operational semantics** of the **network** of FCA $\mathcal{C}(\mathcal{A}_1, \dots, \mathcal{A}_n)$ is the labelled transition system

$$\mathcal{T}(\mathcal{C}(\mathcal{A}_1, \dots, \mathcal{A}_n)) = (\text{Conf}, \underbrace{\text{Chan} \cup \{\tau\}}_{\text{labels}}, \underbrace{\{\xrightarrow{\lambda} \mid \lambda \in \text{Chan} \cup \{\tau\}\}}_{\text{labelled transition relations}}, C_{ini})$$

where

- $V = \bigcup_{i=1}^n V_i$, *location vector valuation*
- $\text{Conf} = \{ \langle \vec{\ell}, \nu \rangle \mid \ell_i \in L_i, \nu : V \rightarrow \mathcal{D}(V) \}$, *$\vec{\ell} = (\ell_1, \dots, \ell_n)$*
- $C_{ini} = \langle \vec{\ell}_{ini}, \nu_{ini} \rangle$ with $\nu_{ini}(v) = 0$ for all $v \in V$.

The transition relation consists of transitions of the following two types.

Helpers: Extended Valuations and Effect of Resets

- $\nu : V \rightarrow \mathcal{D}(V)$ is a **valuation** of the variables,
- A valuation ν of the variables canonically assigns an integer value $\nu(\varphi)$ to each integer expression $\varphi \in \Phi(V)$.
- $\models \subseteq (V \rightarrow \mathcal{D}(V)) \times \Phi(V)$ is the canonical **satisfaction relation** between valuations and integer expressions from $\Phi(V)$. *e.g. $\nu \models x > 10$*
- **Effect of modification** $r \in R(V)$ **on** ν , denoted by $\nu[r]$:

$$\left(\begin{array}{l} \nu[v := \varphi] \\ : V \rightarrow \mathcal{D}(V) \end{array} \right)(a) := \begin{cases} \nu(\varphi), & \text{if } a = v, \\ \nu(a), & \text{otherwise} \end{cases}$$

- We set $\nu[\langle r_1, \dots, r_n \rangle] := \nu[r_1] \dots [r_n] = (((\nu[r_1])[r_2]) \dots)[r_n]$.

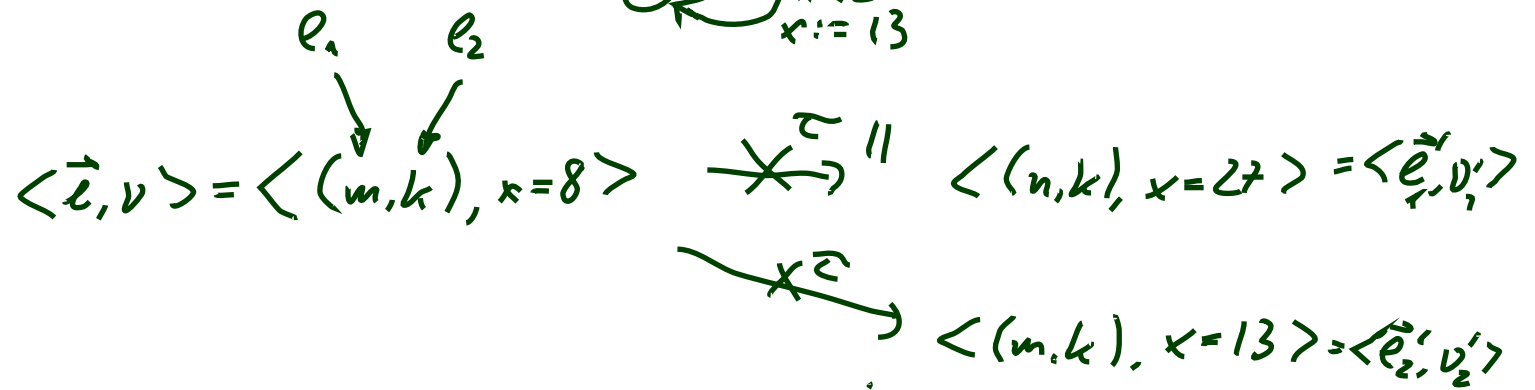
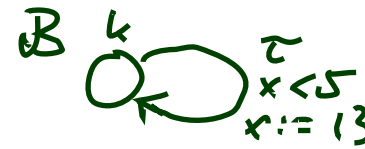
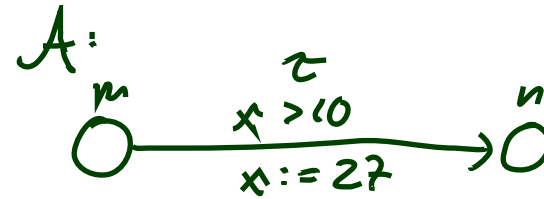
That is, modifications are executed sequentially from left to right.

Operational Semantics of Networks of FCA

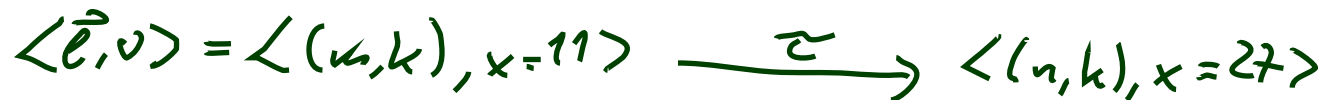
- An **internal transition** $\langle \vec{l}, \nu \rangle \xrightarrow{\tau} \langle \vec{l}', \nu' \rangle$ occurs if there is $i \in \{1, \dots, n\}$ and

- there is a τ -edge $(l_i, \tau, \varphi, \vec{r}, l'_i) \in E_i$ such that $\vec{e} = (e_1, \dots, e_i, \dots, e_n)$

- $\nu \models \varphi$,
- $\vec{l}' = \vec{l}[l_i := l'_i]$,
- $\nu' = \nu[\vec{r}]$,



NONE: ~~111~~ 1



Operational Semantics of Networks of FCA

- An **internal transition** $\langle \vec{l}, \nu \rangle \xrightarrow{\tau} \langle \vec{l}', \nu' \rangle$ occurs if there is $i \in \{1, \dots, n\}$ and
 - there is a τ -edge $(l_i, \tau, \varphi, \vec{r}, l'_i) \in E_i$ such that
 - $\nu \models \varphi$, “source valuation satisfies guard”
 - $\vec{l}' = \vec{l}[l_i := l'_i]$, “automaton i changes location”
 - $\nu' = \nu[\vec{r}]$, “ ν' is ν modified by \vec{r} ”
- A **synchronisation transition** $\langle \vec{l}, \nu \rangle \xrightarrow{b} \langle \vec{l}', \nu' \rangle$ occurs if there are $i, j \in \{1, \dots, n\}$ with $i \neq j$ and
 - there are edges $(l_i, \underline{b!}, \varphi_i, \vec{r}_i, l'_i) \in E_i$ and $(l_j, \underline{b?}, \varphi_j, \vec{r}_j, l'_j) \in E_j$ such that
 - $\nu \models \varphi_i \wedge \varphi_j$,
 - $\vec{l}' = \vec{l}[l_i := l'_i][l_j := l'_j]$,
 - $\nu' = (\nu[\vec{r}_i])[\vec{r}_j]$, “sends updates first”

This style of communication is known under the names “rendezvous”, “synchronous”, “blocking” communication (and possibly many others).

Transition Sequences

- A **transition sequence** of $\mathcal{C}(\mathcal{A}_1, \dots, \mathcal{A}_n)$ is any (in)finite sequence of the form

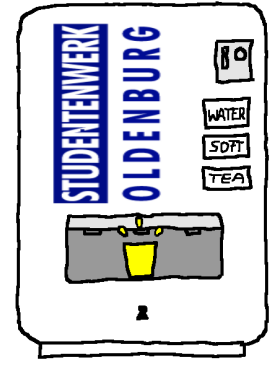
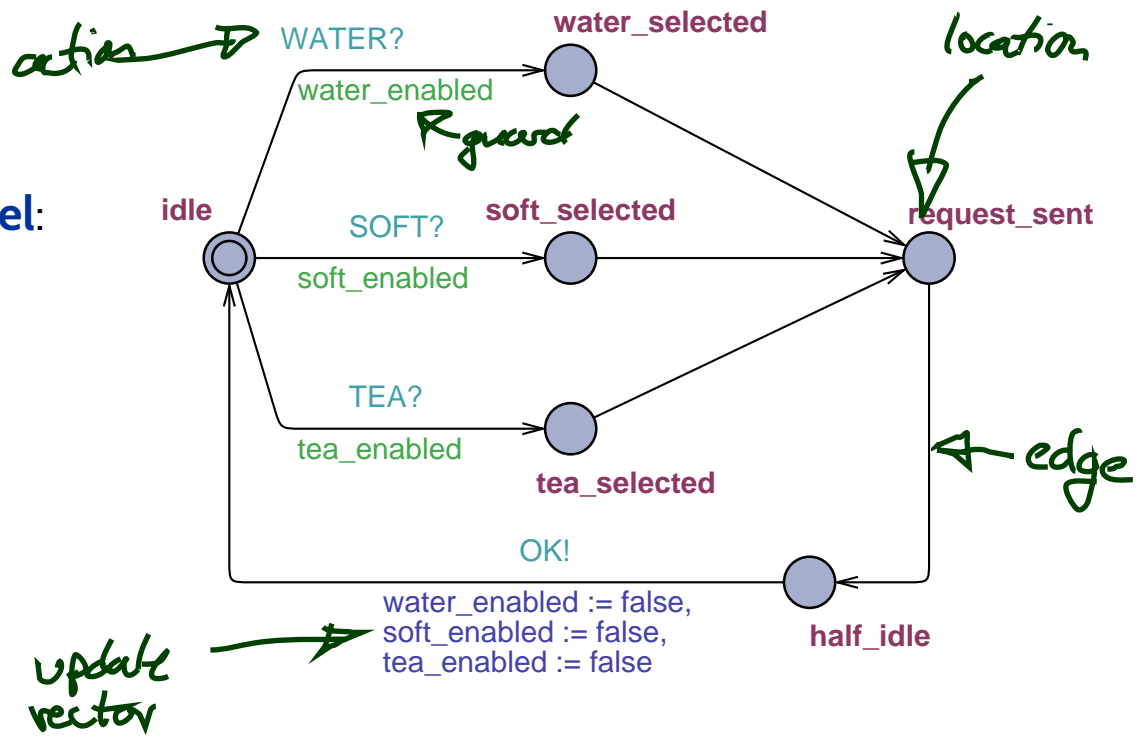
$$\langle \vec{\ell}_0, \nu_0 \rangle \xrightarrow{\lambda_1} \langle \vec{\ell}_1, \nu_1 \rangle \xrightarrow{\lambda_2} \langle \vec{\ell}_2, \nu_2 \rangle \xrightarrow{\lambda_3} \dots$$

with

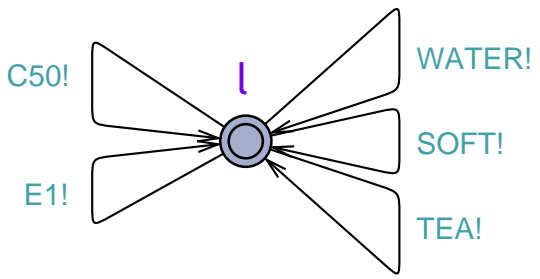
- $\langle \vec{\ell}_0, \nu_0 \rangle = C_{ini}$,
- for all $i \in \mathbb{N}$, there is $\xrightarrow{\lambda_{i+1}}$ in $\mathcal{T}(\mathcal{C}(\mathcal{A}_1, \dots, \mathcal{A}_n))$ with $\langle \vec{\ell}_i, \nu_i \rangle \xrightarrow{\lambda_{i+1}} \langle \vec{\ell}_{i+1}, \nu_{i+1} \rangle$.

Example

ChoicePanel:
(simplified)



User:



$$\langle (idle, l), \begin{matrix} w=1 \\ s=1 \\ t=0 \end{matrix} \rangle \xrightarrow{WATER} \langle (w_sel, e), \begin{matrix} w=1 \\ s=1 \\ t=0 \end{matrix} \rangle \xrightarrow{\tau} \langle (req_s, e), \begin{matrix} w=1 \\ s=1 \\ t=0 \end{matrix} \rangle \xrightarrow{\tau} \langle (half_id, e), \begin{matrix} w=1 \\ s=1 \\ t=0 \end{matrix} \rangle$$

*
C_{ini} \xrightarrow{SOFT} $\langle (s_sel, e), \begin{matrix} w=1 \\ s=1 \\ t=0 \end{matrix} \rangle \dots$

here nothing
else: guard tea-enabled not satisfied, and no comm. partners for C50 or E1

Deadlock, Reachability

- A **configuration** $\langle \ell, \nu \rangle$ of $\mathcal{C}(\mathcal{A}_1, \dots, \mathcal{A}_n)$ is called **deadlock** if and only if there are no transitions from $\langle \ell, \nu \rangle$, i.e. if

$$\neg(\exists \lambda \in \Lambda \exists \langle \ell', \nu' \rangle \in \text{Conf} \bullet \langle \ell, \nu \rangle \xrightarrow{\lambda} \langle \ell', \nu' \rangle).$$

The **network** $\mathcal{C}(\mathcal{A}_1, \dots, \mathcal{A}_n)$ is said to **have a deadlock** if and only if there is a configuration $\langle \ell, \nu \rangle$ which is a deadlock.

reachable

- A **configuration** $\langle \vec{\ell}, \nu \rangle$ is called **reachable** (in $\mathcal{C}(\mathcal{A}_1, \dots, \mathcal{A}_n)$) if and only if there is a transition sequence of the form

$$\langle \vec{\ell}_0, \nu_0 \rangle \xrightarrow{\lambda_1} \langle \vec{\ell}_1, \nu_1 \rangle \xrightarrow{\lambda_2} \langle \vec{\ell}_2, \nu_2 \rangle \xrightarrow{\lambda_3} \dots \xrightarrow{\lambda_n} \langle \vec{\ell}_n, \nu_n \rangle = \langle \vec{\ell}, \nu \rangle.$$

A **location** $\ell \in L_i$ is called **reachable** if and only if **any** configuration $\langle \vec{\ell}, \nu \rangle$ with $\underline{\ell_i = \ell}$ is reachable, i.e. there exist $\vec{\ell}$ and ν such that $\ell_i = \ell$ and $\langle \vec{\ell}, \nu \rangle$ is reachable.

Uppaal

(Larsen et al., 1997; Behrmann et al., 2004)

Tool Demo

The Uppaal Query Language

Consider $\mathcal{N} = \mathcal{C}(\mathcal{A}_1, \dots, \mathcal{A}_n)$ over data variables V .

- **basic formula:**

$$atom ::= \mathcal{A}_i.l \mid \varphi \mid \text{deadlock}$$

where $l \in L_i$ is a location and φ an expression over V .

- **configuration formulae:**

$$term ::= atom \mid \text{not } term \mid term_1 \text{ and } term_2$$

- **existential path formulae:**

$$\begin{aligned} e\text{-formula} ::= & \exists \diamond term && \text{(exists finally)} \\ & \mid \exists \square term && \text{(exists globally)} \end{aligned}$$

- **universal path formulae:**

$$\begin{aligned} a\text{-formula} ::= & \forall \diamond term && \text{(always finally)} \\ & \mid \forall \square term && \text{(always globally)} \\ & \mid term_1 \rightarrow term_2 && \text{(leads to)} \end{aligned}$$

- **formulae (or queries):**

$$F ::= e\text{-formula} \mid a\text{-formula}$$

Satisfaction of Uppaal Queries by Configurations

- The **satisfaction relation**

$$\langle \vec{l}, \nu \rangle \models F$$

between **configurations**

$$\langle \vec{l}, \nu \rangle = \langle (l_1, \dots, l_n), \nu \rangle$$

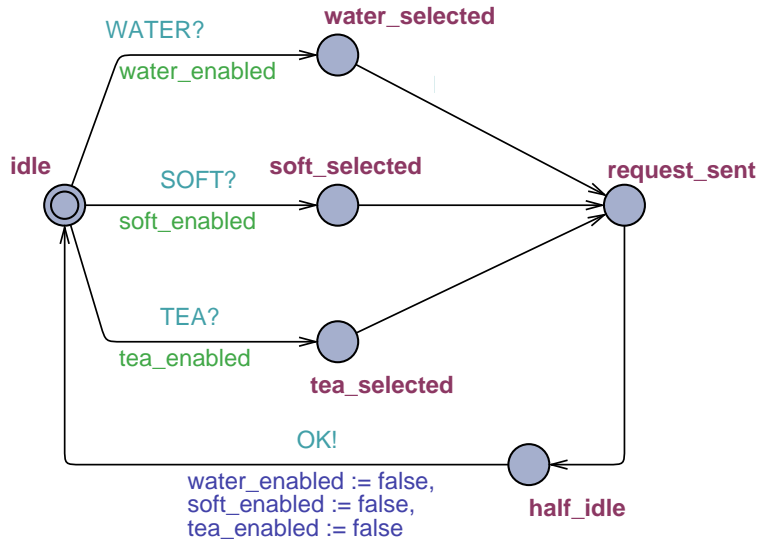
of a network $\mathcal{C}(\mathcal{A}_1, \dots, \mathcal{A}_n)$ and **formulae** F of the Uppaal logic is defined **inductively** as follows:

- $\langle \vec{l}, \nu \rangle \models \text{deadlock}$ iff $\langle \vec{e}, \nu \rangle$ is a deadlock configuration
- $\langle \vec{l}, \nu \rangle \models \mathcal{A}_i.l$ iff $l_i = l$
- $\langle \vec{l}, \nu \rangle \models \varphi$ iff $\nu \models \varphi$
- $\langle \vec{l}, \nu \rangle \models \text{not term}$ iff $\langle \vec{e}, \nu \rangle \neq \text{term}$
- $\langle \vec{l}, \nu \rangle \models \text{term}_1$ and term_2 iff $\langle \vec{e}, \nu \rangle \models \text{term}_1$ and $\langle \vec{e}, \nu \rangle \models \text{term}_2$

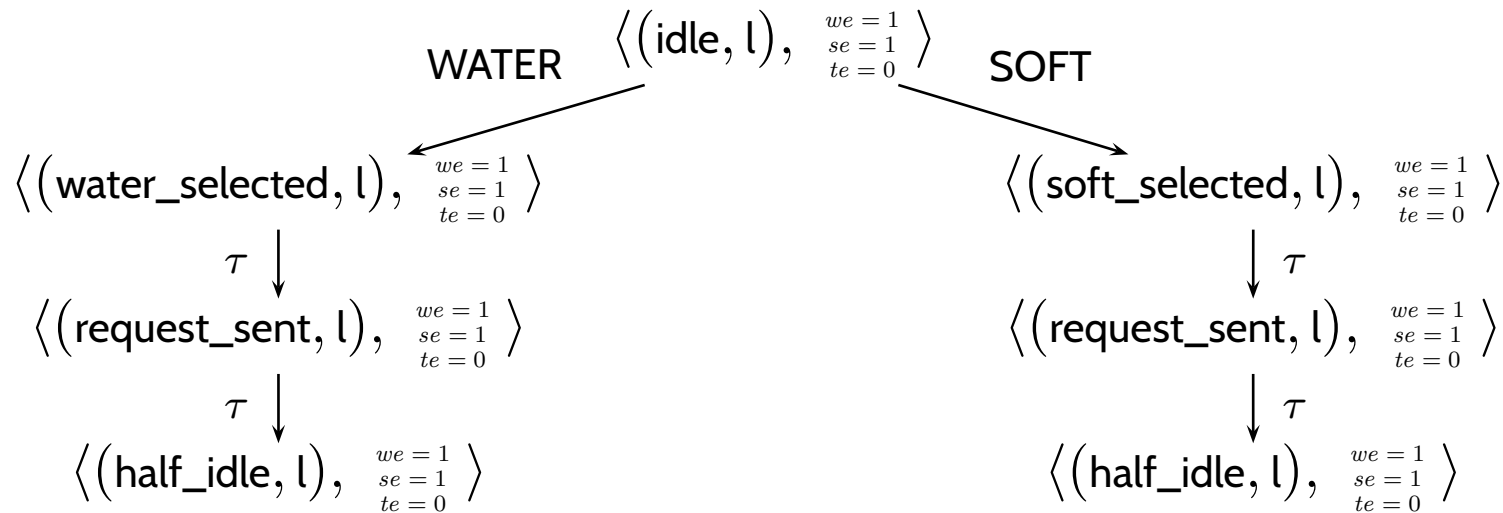
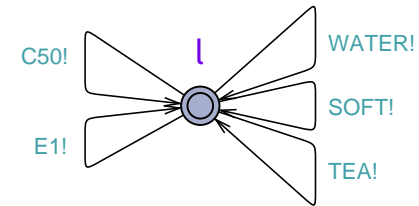
Example: Computation Paths vs. Computation Tree



ChoicePanel:



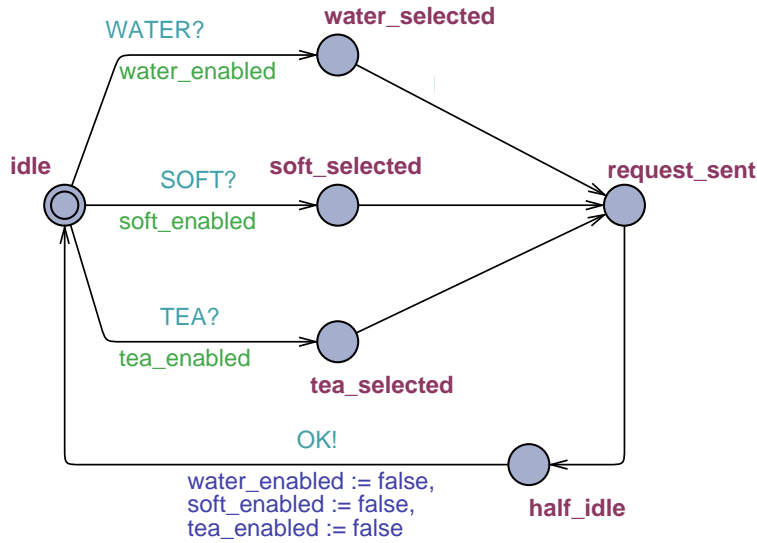
User:



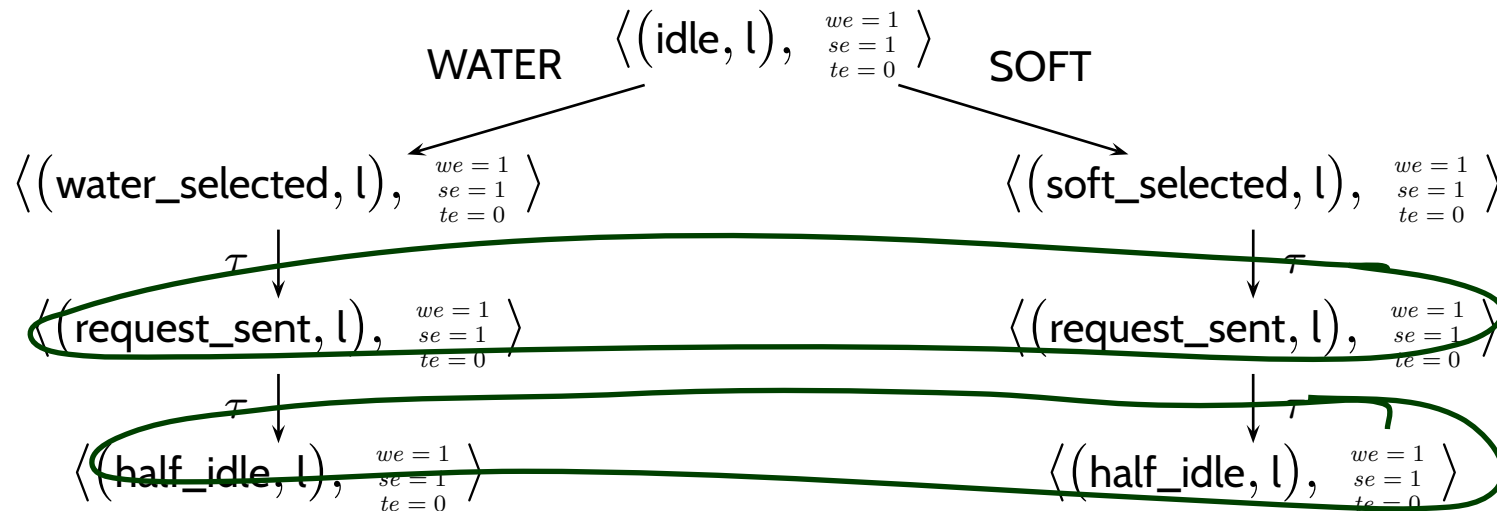
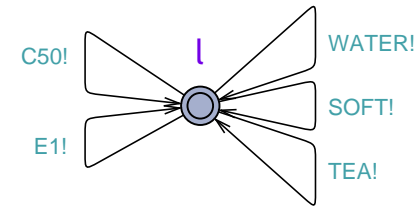
Example: Computation Paths vs. Computation Tree



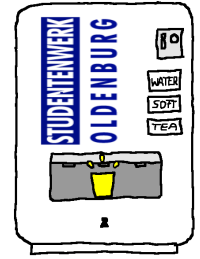
ChoicePanel:



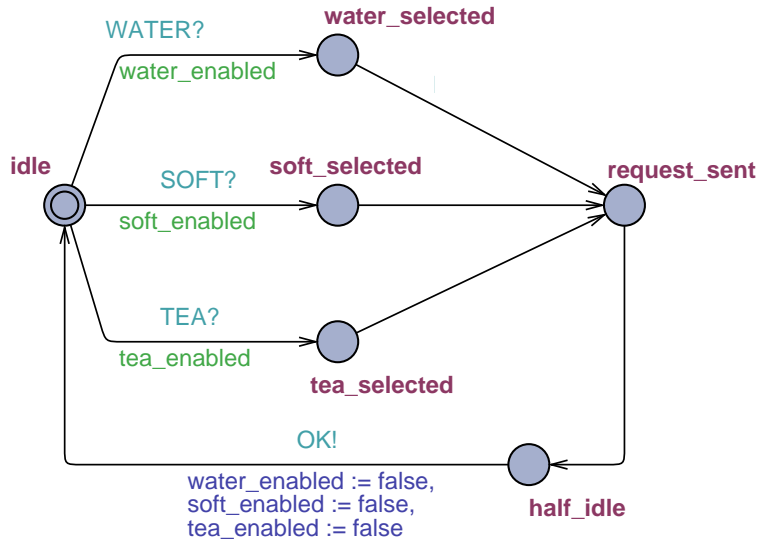
User:



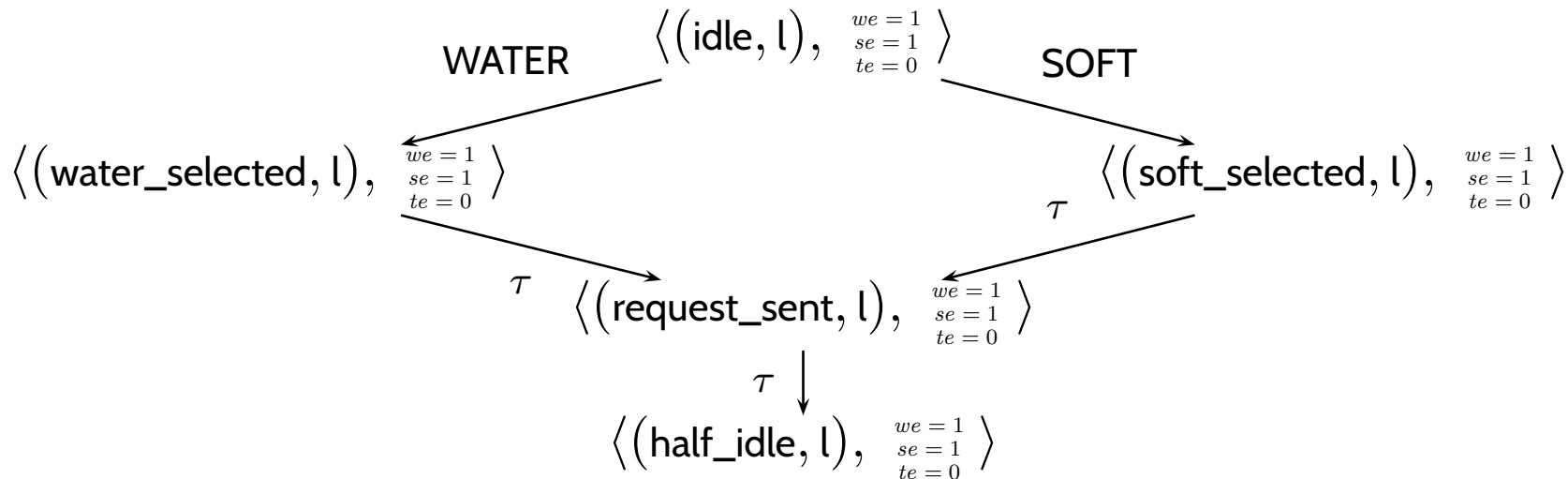
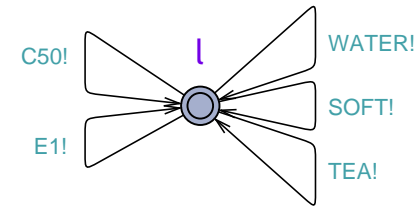
Example: Computation Paths vs. Computation Graph



ChoicePanel:



User:



Satisfaction of Uppaal Queries by Configurations

Exists finally:

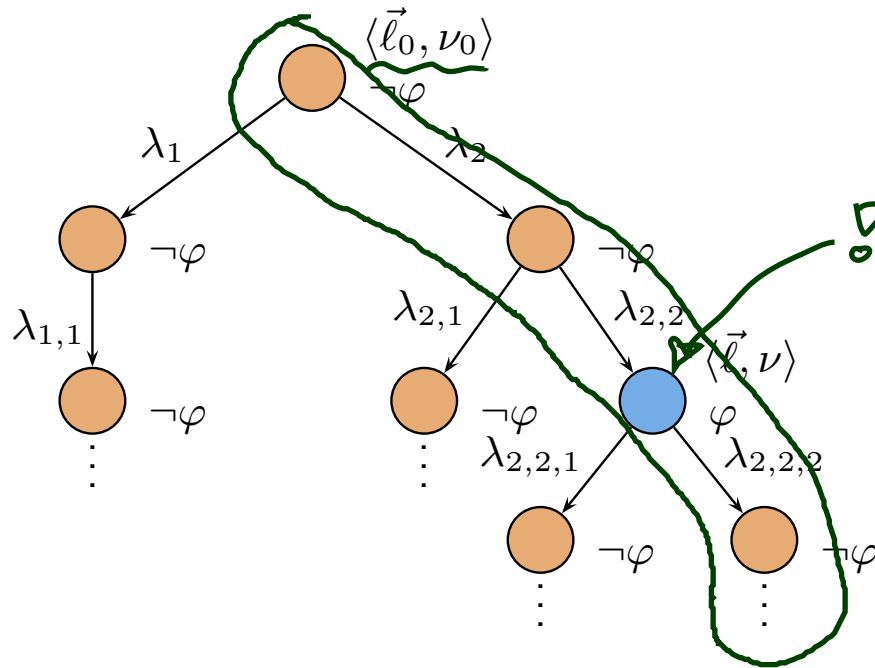
• $\langle \vec{\ell}_0, \nu_0 \rangle \models \exists \diamond term$

iff \exists path ξ of \mathcal{C} starting in $\langle \vec{\ell}_0, \nu_0 \rangle$
 $\exists i \in \mathbb{N}_0 \bullet \xi^i \models term$

i-th configuration in ξ

“some configuration satisfying *term* is reachable”

Example: $\langle \vec{\ell}_0, \nu_0 \rangle \models \exists \diamond \varphi$



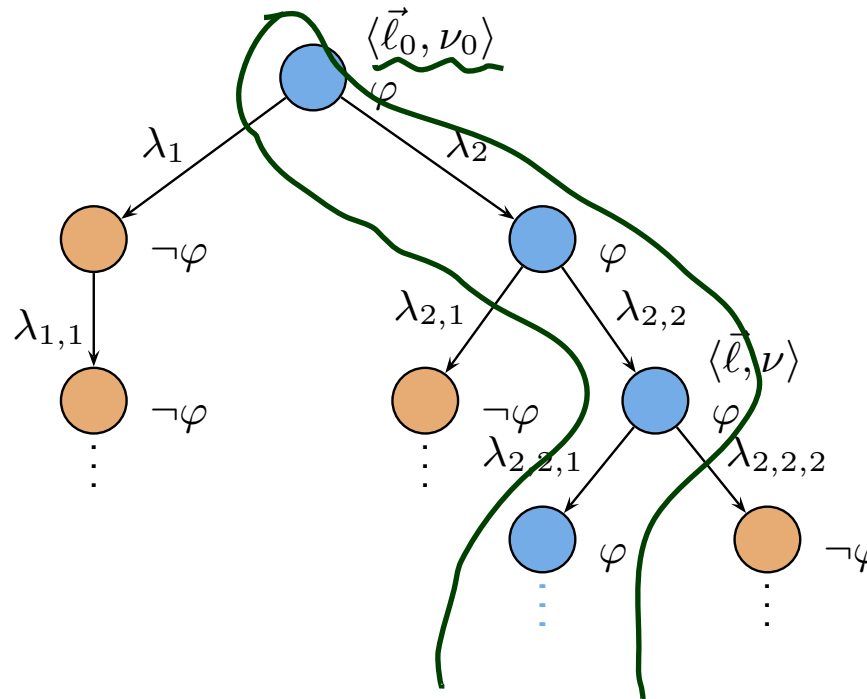
Satisfaction of Uppaal Queries by Configurations

Exists globally:

- $\langle \vec{\ell}_0, \nu_0 \rangle \models \exists \square \textit{term}$
iff \exists path ξ of \mathcal{C} starting in $\langle \vec{\ell}_0, \nu_0 \rangle$
 $\forall i \in \mathbb{N}_0 \bullet \xi^i \models \textit{term}$

“on some computation path, all configurations satisfy *term*”

Example: $\langle \vec{\ell}_0, \nu_0 \rangle \models \exists \square \varphi$



Satisfaction of Uppaal Queries by Configurations

- **Always globally:**

- $\langle \vec{\ell}_0, \nu_0 \rangle \models \forall \square term$ iff $\langle \vec{\ell}_0, \nu_0 \rangle \not\models \exists \diamond \neg term$

“not (some configuration satisfying $\neg term$ is reachable)”

or: “all reachable configurations satisfy $term$ ”

- **Always finally:**

- $\langle \vec{\ell}_0, \nu_0 \rangle \models \forall \diamond term$ iff $\langle \vec{\ell}_0, \nu_0 \rangle \not\models \exists \square \neg term$

“not (on some computation path, all configurations satisfy $\neg term$)”

or: “on all computation paths, there is a configuration satisfying $term$ ”

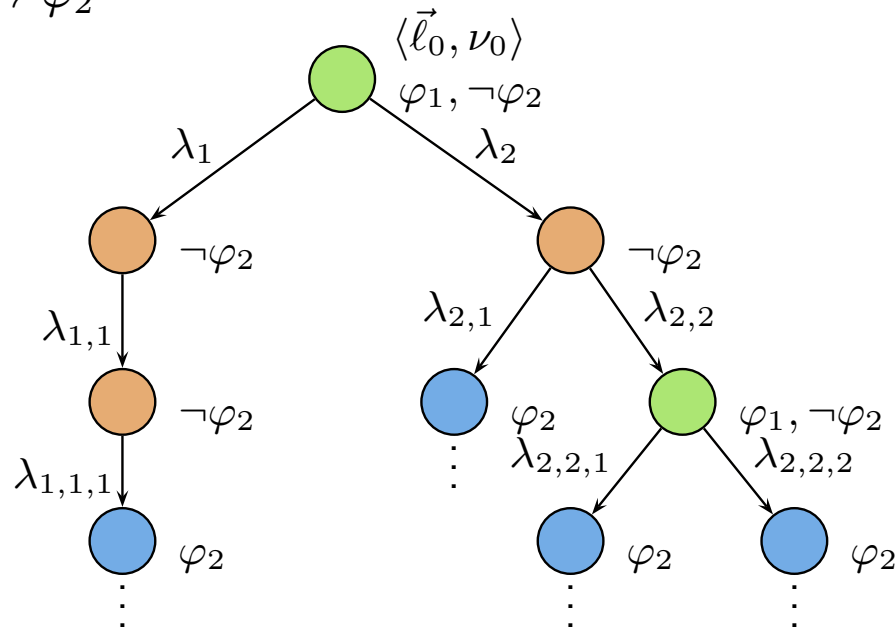
Satisfaction of Uppaal Queries by Configurations

Leads to:

- $\langle \vec{\ell}_0, \nu_0 \rangle \models term_1 \longrightarrow term_2$
iff
 $\forall \text{ path } \xi \text{ of } \mathcal{N} \text{ starting in } \langle \vec{\ell}_0, \nu_0 \rangle \forall i \in \mathbb{N}_0 \bullet$
 $\xi^i \models term_1 \implies \xi^i \models \forall \Diamond term_2$

“on all paths, from each configuration satisfying $term_1$, a configuration satisfying $term_2$ is reachable” (**response pattern**)

Example: $\langle \vec{\ell}_0, \nu_0 \rangle \models \varphi_1 \longrightarrow \varphi_2$



Definition. Let $\mathcal{N} = \mathcal{C}(\mathcal{A}_1, \dots, \mathcal{A}_n)$ be a network and F a query.

- (i) We say \mathcal{N} **satisfies** F , denoted by $\mathcal{N} \models F$, if and only if $C_{ini} \models F$.
- (ii) The **model-checking problem** for \mathcal{N} and F is to decide whether $(\mathcal{N}, F) \in \models$.

Proposition.

The model-checking problem for communicating finite automata is **decidable**.

- **Communicating Finite Automata (CFA)**

- concrete and abstract syntax,
- networks of CFA,
- operational semantics.

- **Transition Sequences**

- **Deadlock, Reachability**

- **Uppaal**

- tool demo (simulator),
- query language,
- CFA model-checking.



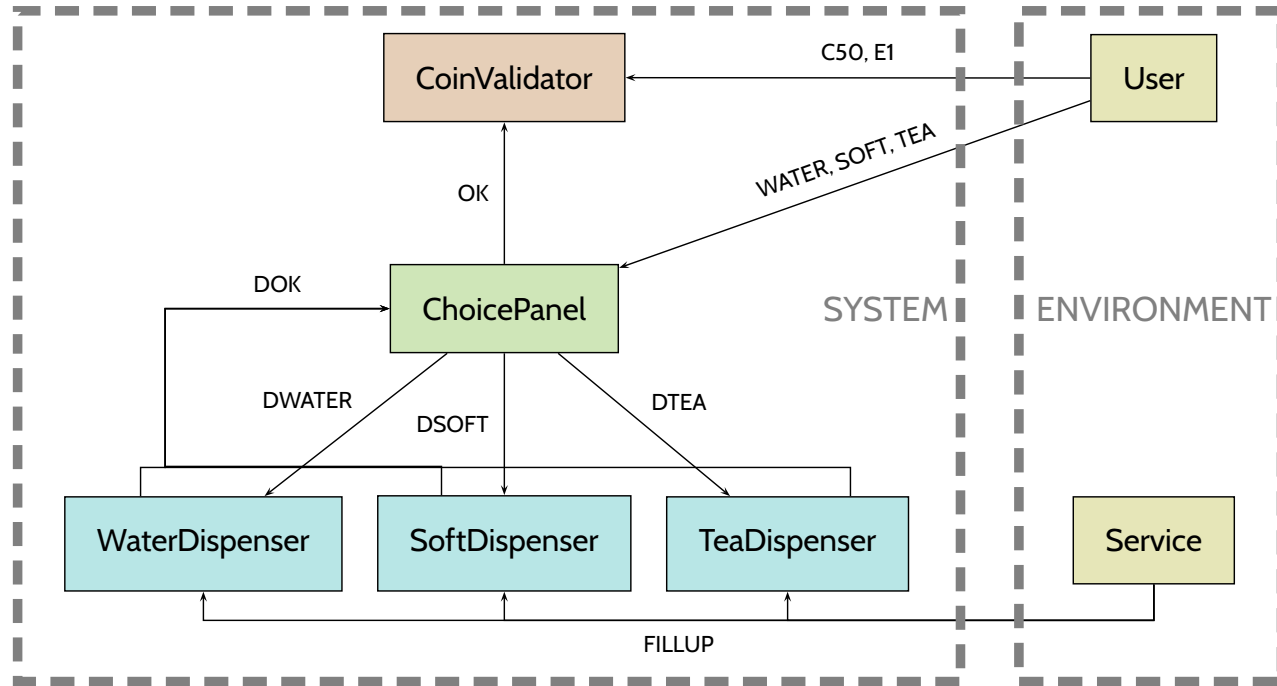
- **CFA at Work**

- drive to configuration,
- scenarios,
- invariants,
- tool demo (verifier).

- **CFA vs. Software**

CFA and Queries at Work

Model Architecture — Who Talks What to Whom

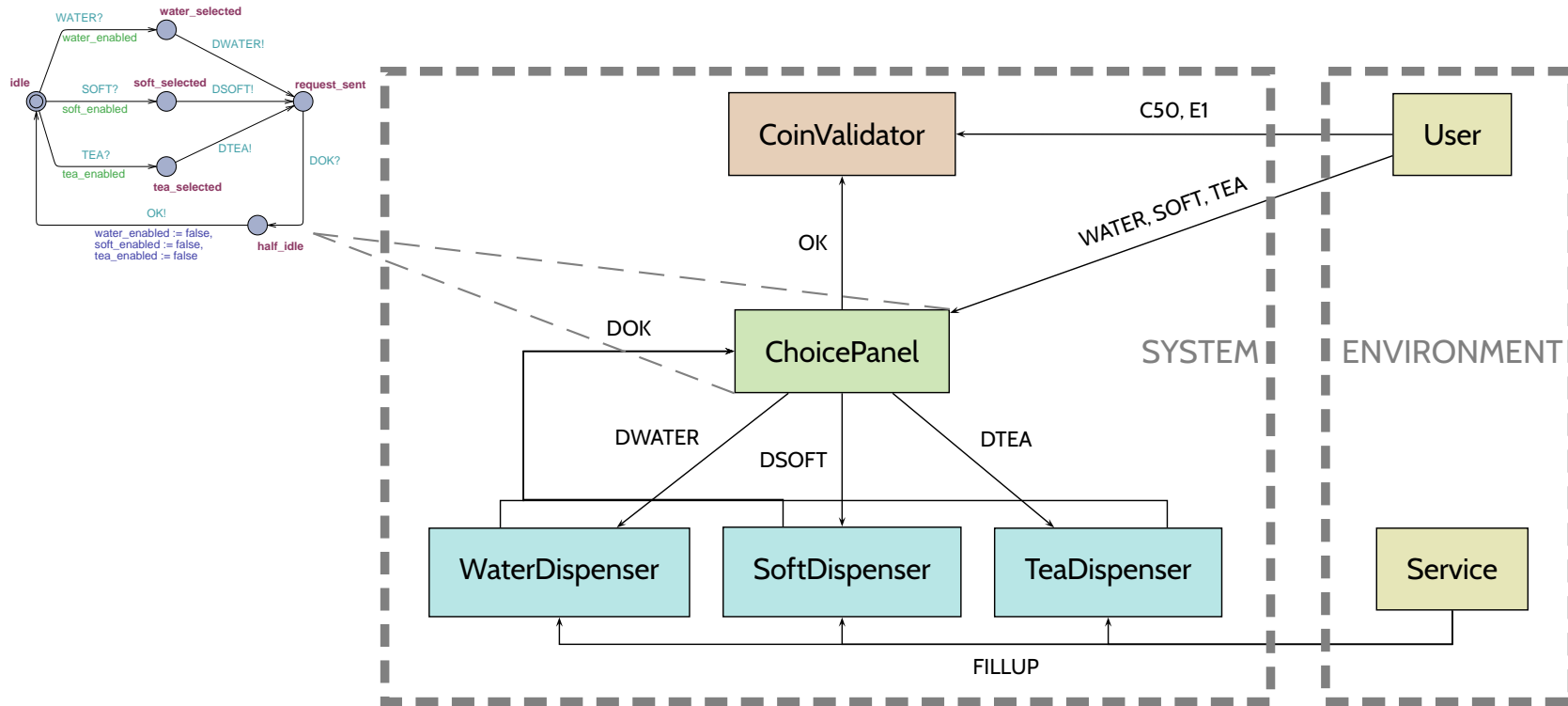


- **Shared variables:**

- `bool water_enabled, soft_enabled, tea_enabled;`
- `int w = 3, s = 3, t = 3;`

- **Note:** Our model does not use scopes (“information hiding”) for channels. That is, ‘Service’ could send ‘WATER’ if the modeler wanted to.

Model Architecture — Who Talks What to Whom

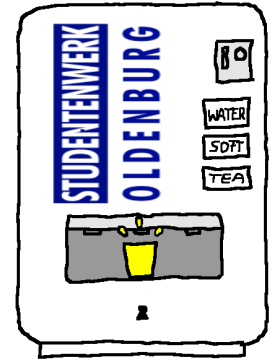


- **Shared variables:**

- `bool water_enabled, soft_enabled, tea_enabled;`
- `int w = 3, s = 3, t = 3;`

- **Note:** Our model does not use scopes (“information hiding”) for channels. That is, ‘Service’ could send ‘WATER’ if the modeler wanted to.

Design Sanity Check: Drive to Configuration



- **Question:** Is it (at all) possible to have no water in the vending machine model? (Otherwise, the design is definitely broken.)
- **Approach:** Check whether a configuration satisfying

$$w = 0$$

is reachable, i.e. check

$$\mathcal{N}_{VM} \models \exists \diamond w = 0.$$

for the vending machine model \mathcal{N}_{VM} .

References

References

Behrmann, G., David, A., and Larsen, K. G. (2004). A tutorial on uppaal 2004-11-17. Technical report, Aalborg University, Denmark.

Larsen, K. G., Pettersson, P., and Yi, W. (1997). UPPAAL in a nutshell. *International Journal on Software Tools for Technology Transfer*, 1(1):134–152.

Ludewig, J. and Lichter, H. (2013). *Software Engineering*. dpunkt.verlag, 3. edition.

Olderog, E.-R. and Dierks, H. (2008). *Real-Time Systems - Formal Specification and Automatic Verification*. Cambridge University Press.