

Softwaretechnik / Software-Engineering

Lecture 17: Software Verification

2016-07-14

Prof. Dr. Andreas Podelski, Dr. Bernd Westphal

Albert-Ludwigs-Universität Freiburg, Germany

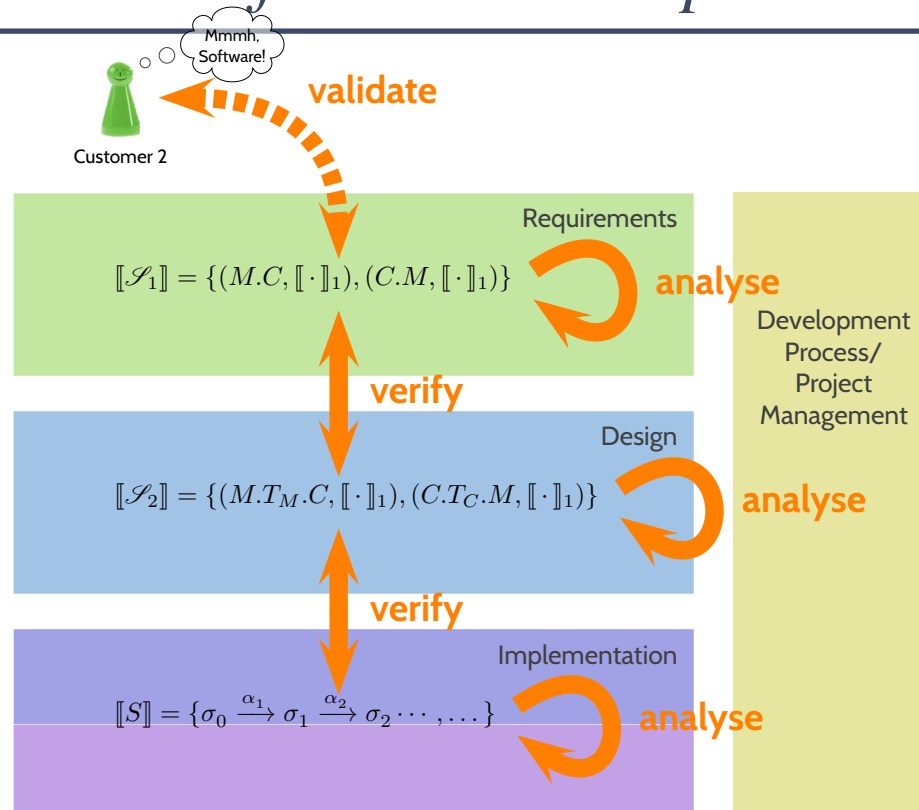
Topic Area Code Quality Assurance: Content

- VL 15 ● **Introduction and Vocabulary**
- VL 16 ● **Limits of Software Testing**
- **Glass-Box Testing**
 - Statement-, branch-, term-coverage.
- ⋮
- **Other Approaches**
 - Model-based testing,
 - Runtime verification.
- VL 17 ● **Software quality assurance**
in a larger scope.
- ⋮
- **Program Verification**
 - partial and total correctness,
 - Proof System PD.
- VL 18 ● **Review**
- ⋮

- Software quality assurance in a **larger scope**:
 - vocabulary,
 - fault, error, failure,
 - concepts of software quality assurance (next to testing)
- **Formal Program Verification**
 - **Deterministic Programs**
 - **Syntax**
 - **Semantics**
 - Termination, Divergence
 - **Correctness** of deterministic programs
 - **partial** correctness,
 - **total** correctness.
 - **Proof System PD**
- **The Verifier for Concurrent C**

Software Quality Assurance

Formal Methods in the Software Development Process



validation–

The process of evaluating a system or component during or at the end of the development process to determine whether it satisfies specified requirements.

Contrast with: **verification**.

IEEE 610.12 (1990)

verification–

- (1) The process of evaluating a system or component to determine whether the products of a given development phase satisfy the conditions imposed at the start of that phase. Contrast with: **validation**.

- (2) Formal proof of program correctness.

IEEE 610.12 (1990)

software quality assurance – See: quality assurance.

IEEE 610.12 (1990)

quality assurance –

- (1) A planned and systematic pattern of all actions necessary to provide adequate confidence that an item or product conforms to established technical requirements.
- (2) A set of activities designed to evaluate the process by which products are developed or manufactured.

IEEE 610.12 (1990)

Note: in order to trust a product, it can be **built well**,
or **proven to be good** (at best: both) – both is QA in the sense of (1).

Fault, Error, Failure

fault – abnormal condition that can cause an element or an item to fail.

Note: Permanent, intermittent and transient **faults** (especially soft-errors) are considered.

Note: An **intermittent fault** occurs time and time again, then disappears. This type of fault can occur when a component is on the verge of breaking down or, for example, due to a glitch in a switch. Some **systematic faults** (e.g. timing marginalities) could lead to intermittent faults.

ISO 26262 (2011)

error – discrepancy between a computed, observed or measured value or condition, and the true, specified, or theoretically correct value or condition.

Note: An error can arise as a result of unforeseen operating conditions or due to a **fault** within the system, subsystem or, component being considered.

Note: A **fault** can manifest itself as an error within the considered element and the error can ultimately cause a **failure**.

ISO 26262 (2011)

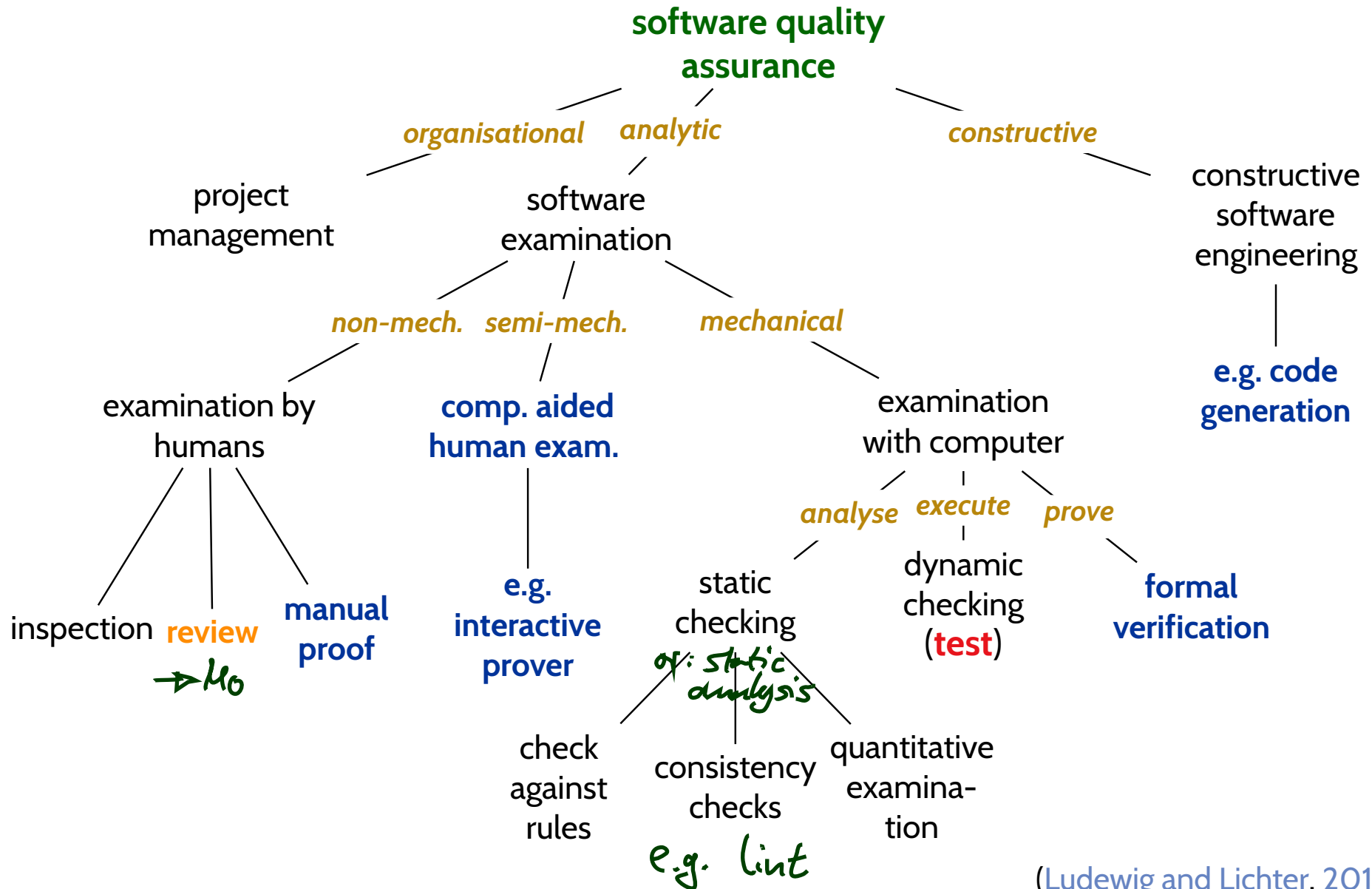
failure – termination of the ability of an element, to perform a function as required.

Note: Incorrect specification is a source of failure.

ISO 26262 (2011)

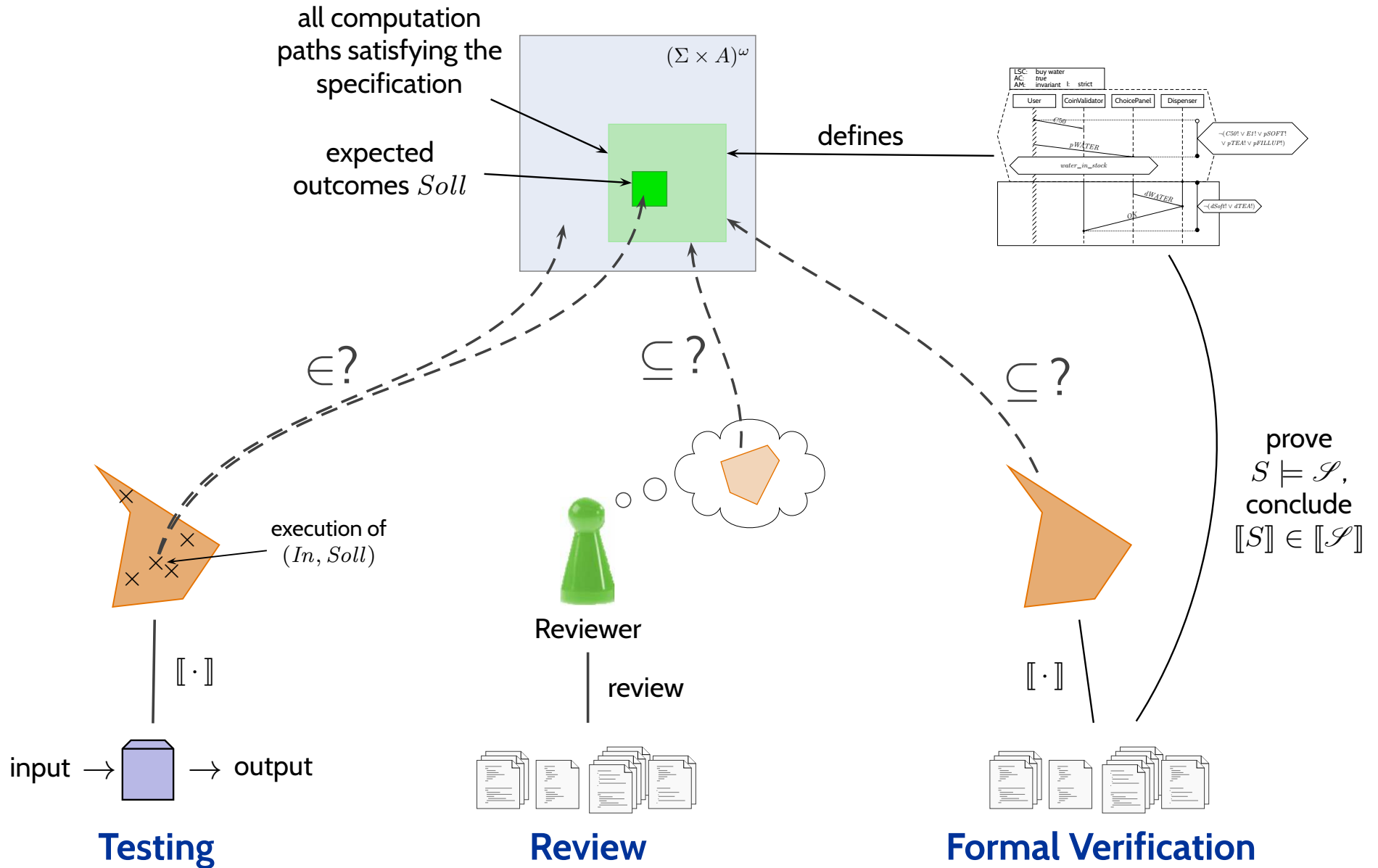
We want to avoid **failures**, thus we try to detect **faults** and **errors**.

Concepts of Software Quality Assurance



(Ludewig and Lichter, 2013)

Three Basic Approaches



Sequential, Deterministic While-Programs

Deterministic Programs

Syntax:

$$S ::= \text{skip} \mid u := t \mid S_1; S_2 \mid \text{if } B \text{ then } S_1 \text{ else } S_2 \text{ fi} \mid \text{while } B \text{ do } S_1 \text{ od}$$

where $u \in V$ is a **variable**, t is a type-compatible **expression**, B is a Boolean **expression**.

Semantics: (is induced by the following transition relation) – $\sigma : V \rightarrow \mathcal{D}(V)$

- (i) $\langle \text{skip}, \sigma \rangle \rightarrow \langle E, \sigma \rangle$ *empty program*
- (ii) $\langle u := t, \sigma \rangle \rightarrow \langle E, \sigma[u := \sigma(t)] \rangle$
- (iii)
$$\frac{\langle S_1, \sigma \rangle \rightarrow \langle S_2, \tau \rangle}{\langle S_1; S, \sigma \rangle \rightarrow \langle S_2; S, \tau \rangle}$$
- (iv) $\langle \text{if } B \text{ then } S_1 \text{ else } S_2 \text{ fi}, \sigma \rangle \rightarrow \langle S_1, \sigma \rangle$, if $\sigma \models B$,
- (v) $\langle \text{if } B \text{ then } S_1 \text{ else } S_2 \text{ fi}, \sigma \rangle \rightarrow \langle S_2, \sigma \rangle$, if $\sigma \not\models B$,
- (vi) $\langle \text{while } B \text{ do } S \text{ od}, \sigma \rangle \rightarrow \langle S; \text{while } B \text{ do } S \text{ od}, \sigma \rangle$, if $\sigma \models B$,
- (vii) $\langle \text{while } B \text{ do } S \text{ od}, \sigma \rangle \rightarrow \langle E, \sigma \rangle$, if $\sigma \not\models B$,

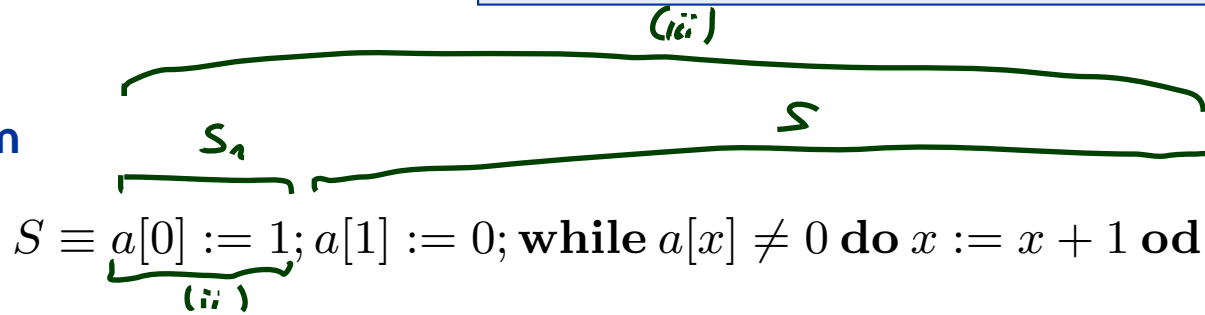
E denotes the **empty program**; define $\underline{E}; S \equiv S$; $\underline{E} \equiv S$.

Note: the first component of $\langle S, \sigma \rangle$ is a program (**structural operational semantics (SOS)**).

Example

- (i) $\langle skip, \sigma \rangle \rightarrow \langle E, \sigma \rangle$ $E; S \equiv S; E \equiv S$
- (ii) $\langle u := t, \sigma \rangle \rightarrow \langle E, \sigma[u := \sigma(t)] \rangle$
- (iii) $\frac{\langle S_1, \sigma \rangle \rightarrow \langle S_2, \tau \rangle}{\langle S_1; S, \sigma \rangle \rightarrow \langle S_2; S, \tau \rangle}$
- (iv) $\langle \text{if } B \text{ then } S_1 \text{ else } S_2 \text{ fi}, \sigma \rangle \rightarrow \langle S_1, \sigma \rangle, \text{ if } \sigma \models B,$
- (v) $\langle \text{if } B \text{ then } S_1 \text{ else } S_2 \text{ fi}, \sigma \rangle \rightarrow \langle S_2, \sigma \rangle, \text{ if } \sigma \not\models B,$
- (vi) $\langle \text{while } B \text{ do } S \text{ od}, \sigma \rangle \rightarrow \langle S; \text{while } B \text{ do } S \text{ od}, \sigma \rangle, \text{ if } \sigma \models B,$
- (vii) $\langle \text{while } B \text{ do } S \text{ od}, \sigma \rangle \rightarrow \langle E, \sigma \rangle, \text{ if } \sigma \not\models B,$

Consider program



and a state σ with $\sigma \models x = 0$.

$$\begin{aligned}
 \langle S, \sigma \rangle &\xrightarrow{(ii), (iii)} \langle a[1] := 0; \text{while } a[x] \neq 0 \text{ do } x := x + 1 \text{ od}, \sigma[a[0] := 1] \rangle \\
 &\xrightarrow{(ii), (iii)} \langle \text{while } a[x] \neq 0 \text{ do } x := x + 1 \text{ od}, \sigma' \rangle \\
 &\xrightarrow{(vi)} \langle x := x + 1; \text{while } a[x] \neq 0 \text{ do } x := x + 1 \text{ od}, \sigma' \rangle \\
 &\xrightarrow{(ii), (iii)} \langle \text{while } a[x] \neq 0 \text{ do } x := x + 1 \text{ od}, \sigma'[x := 1] \rangle \\
 &\xrightarrow{(vii)} \langle E, \sigma'[x := 1] \rangle
 \end{aligned}$$

where $\sigma' = \sigma[a[0] := 1][a[1] := 0]$.

Another Example

(i)	$\langle skip, \sigma \rangle \rightarrow \langle E, \sigma \rangle$	$E; S \equiv S; E \equiv S$
(ii)	$\langle u := t, \sigma \rangle \rightarrow \langle E, \sigma[u := \sigma(t)] \rangle$	
(iii)	$\frac{\langle S_1, \sigma \rangle \rightarrow \langle S_2, \tau \rangle}{\langle S_1; S, \sigma \rangle \rightarrow \langle S_2; S, \tau \rangle}$	
(iv)	$\langle \text{if } B \text{ then } S_1 \text{ else } S_2 \text{ fi}, \sigma \rangle \rightarrow \langle S_1, \sigma \rangle, \text{ if } \sigma \models B,$	
(v)	$\langle \text{if } B \text{ then } S_1 \text{ else } S_2 \text{ fi}, \sigma \rangle \rightarrow \langle S_2, \sigma \rangle, \text{ if } \sigma \not\models B,$	
(vi)	$\langle \text{while } B \text{ do } S \text{ od}, \sigma \rangle \rightarrow \langle S; \text{while } B \text{ do } S \text{ od}, \sigma \rangle, \text{ if } \sigma \models B,$	
(vii)	$\langle \text{while } B \text{ do } S \text{ od}, \sigma \rangle \rightarrow \langle E, \sigma \rangle, \text{ if } \sigma \not\models B,$	

Consider **program**

$$S_1 \equiv y := x; y := (x - 1) \cdot x + y$$

and a **state** σ with $\sigma \models x = 3$.

$$\begin{aligned} \langle S_1, \sigma \rangle &\xrightarrow{(ii),(iii)} \langle y := (x - 1) \cdot x + y, \{x \mapsto 3, y \mapsto 3\} \rangle \\ &\xrightarrow{(ii)} \langle E, \{x \mapsto 3, y \mapsto 9\} \rangle \end{aligned}$$

Consider **program** $S_3 \equiv y := x; y := (x - 1) \cdot x + y; \text{ while } 1 \text{ do } skip \text{ od}.$

$$\begin{aligned} \langle S_3, \sigma \rangle &\xrightarrow{(ii),(iii)} \langle y := (x - 1) \cdot x + y; \text{ while } 1 \text{ do } skip \text{ od}, \{x \mapsto 3, y \mapsto 3\} \rangle \\ &\xrightarrow{(ii),(iii)} \langle \text{while } 1 \text{ do } skip \text{ od}, \{x \mapsto 3, y \mapsto 9\} \rangle \\ &\xrightarrow{(vi)} \langle skip; \text{ while } 1 \text{ do } skip \text{ od}, \{x \mapsto 3, y \mapsto 9\} \rangle \\ &\xrightarrow{(i),(iii)} \langle \text{while } 1 \text{ do } skip \text{ od}, \{x \mapsto 3, y \mapsto 9\} \rangle \\ &\xrightarrow{(vi)} \dots \end{aligned}$$

Computations of Deterministic Programs

Definition. Let S be a deterministic program.

(i) A **transition sequence** of S (starting in σ) is a finite or infinite sequence

$$\langle S, \sigma \rangle = \langle S_0, \sigma_0 \rangle \rightarrow \langle S_1, \sigma_1 \rangle \rightarrow \dots$$

(that is, $\langle S_i, \sigma_i \rangle$ and $\langle S_{i+1}, \sigma_{i+1} \rangle$ are in transition relation for all i).

(ii) A **computation (path)** of S (starting in σ) is a **maximal** transition sequence of S (starting in σ), i.e. infinite or not extendible.

(iii) A computation of S is said to

a) **terminate** in τ if and only if it is finite and ends with $\langle E, \tau \rangle$,

b) **diverge** if and only if it is infinite.

S **can diverge from** σ if and only if a diverging computation starts in σ .

(iv) We use \rightarrow^* to denote the transitive, reflexive closure of \rightarrow .

Lemma. For each deterministic program S and each state σ , there is exactly one computation of S which starts in σ .

Input/Output Semantics of Deterministic Programs

Definition.

Let S be a deterministic program.

- (i) The semantics of partial correctness is the function

$$\mathcal{M}[[S]] : \Sigma \rightarrow 2^\Sigma$$

with $\mathcal{M}[[S]](\sigma) = \{\tau \mid \langle S, \sigma \rangle \rightarrow^* \langle E, \tau \rangle\}$.

- (ii) The semantics of total correctness is the function

$$\mathcal{M}_{tot}[[S]] : \Sigma \rightarrow 2^\Sigma \dot{\cup} \{\infty\}$$

with $\mathcal{M}_{tot}[[S]](\sigma) = \mathcal{M}[[S]](\sigma) \cup \{\infty \mid S \text{ can diverge from } \sigma\}$.

∞ is an error state representing **divergence**.

Note: $\mathcal{M}_{tot}[[S]](\sigma)$ has exactly one element, $\mathcal{M}[[S]](\sigma)$ at most one.

Example: $\mathcal{M}[[S_1]](\sigma) = \mathcal{M}_{tot}[[S_1]](\sigma) = \{\tau \mid \tau(x) = \sigma(x) \wedge \tau(y) = \sigma(x)^2\}$, $\sigma \in \Sigma$.

(Recall: $S_1 \equiv y := x; y := (x - 1) \cdot x + y$)

Correctness of While-Programs

Correctness of Deterministic Programs

Definition.

Let S be a program over variables V , and p and q Boolean expressions over V .

(i) The **correctness formula**

$$\{p\} S \{q\} \quad \text{("Hoare triple")}$$

holds in the sense of **partial correctness**,

denoted by $\models \{p\} S \{q\}$, if and only if

$$\mathcal{M}[S](\llbracket p \rrbracket) \subseteq \llbracket q \rrbracket.$$

We say S is **partially correct** wrt. p and q .

$$\llbracket q \rrbracket := \{\sigma \mid \sigma \models q\}$$

$$\{\tau \mid \exists \sigma \in \llbracket p \rrbracket \cdot \mathcal{M}[S](\sigma) = \{\tau\}\}$$

(ii) A **correctness formula**

$$\{p\} S \{q\}$$

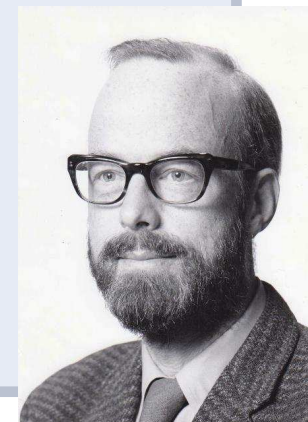
holds in the sense of **total correctness**,

denoted by $\models_{tot} \{p\} S \{q\}$, if and only if

$$\mathcal{M}_{tot}[S](\llbracket p \rrbracket) \subseteq \llbracket q \rrbracket.$$

We say S is **totally correct** wrt. p and q .

∞ is never in here!



Example: Computing squares (of numbers $0, \dots, 27$)

- **Pre-condition:** $p \equiv 0 \leq x \leq 27$,
- **Post-condition:** $q \equiv y = x^2$.

Program S_1 :

```
1 int y = x;  
2 y = (x - 1) * x + y;
```

$\models^? \{p\} S_1 \{q\}$ ✓
 $\models_{tot}^? \{p\} S_1 \{q\}$ ✓

Program S_3 :

```
1 int y = x;  
2 y = (x - 1) * x + y;  
3 while (1);
```

$\models^? \{p\} S_3 \{q\}$ ✓
 $\models_{tot}^? \{p\} S_3 \{q\}$ ✗

Program S_2 :

```
1 int y = x;  
2 int z; // uninitialised  
3 y = ((x - 1) * x + y) + z;
```

$\models^? \{p\} S_2 \{q\}$ ✗
 $\models_{tot}^? \{p\} S_2 \{q\}$ ✗

Program S_4 :

```
1 int x = read_input();  
2 int y = x + (x-1) * x;
```

$\models^? \{p\} S_4 \{q\}$ ✗
 $\models_{tot}^? \{p\} S_4 \{q\}$ ✗

Example: Correctness

- By the example, we have shown

$$\models \{x = 0\} S \{x = 1\}$$

and

$$\models_{tot} \{x = 0\} S \{x = 1\}.$$

(because we only assumed $\sigma \models x = 0$ for the example, which is exactly the precondition.)

- We have also shown (= **proved (!)**):

$$\models \{x = 0\} S \{x = 1 \wedge a[x] = 0\}.$$

- The correctness formula $\{x = 2\} S \{true\}$ **does not hold** for S . (For example, if $\sigma \models a[i] \neq 0$ for all $i > 2$.)
- In the sense of **partial correctness**, $\{x = 2 \wedge \forall i \geq 2 \bullet a[i] = 1\} S \{false\}$ also holds.

Example

(i) $\langle skip, \sigma \rangle \rightarrow \langle E, \sigma \rangle$	$E; S \equiv S; E \equiv S$
(ii) $\langle u := t, \sigma \rangle \rightarrow \langle E, \sigma[u := \sigma(t)] \rangle$	
(iii) $\frac{\langle S_1, \sigma \rangle \rightarrow \langle S_2, \tau \rangle}{\langle S_1; S, \sigma \rangle \rightarrow \langle S_2; S, \tau \rangle}$	
(iv) $\langle \text{if } B \text{ then } S_1 \text{ else } S_2 \text{ fi}, \sigma \rangle \rightarrow \langle S_1, \sigma \rangle, \text{ if } \sigma \models B,$	
(v) $\langle \text{if } B \text{ then } S_1 \text{ else } S_2 \text{ fi}, \sigma \rangle \rightarrow \langle S_2, \sigma \rangle, \text{ if } \sigma \not\models B,$	
(vi) $\langle \text{while } B \text{ do } S \text{ od}, \sigma \rangle \rightarrow \langle S; \text{while } B \text{ do } S \text{ od}, \sigma \rangle, \text{ if } \sigma \models B,$	
(vii) $\langle \text{while } B \text{ do } S \text{ od}, \sigma \rangle \rightarrow \langle E, \sigma \rangle, \text{ if } \sigma \not\models B,$	

Consider **program**

$S \equiv a[0] := 1; a[1] := 0; \text{while } a[x] \neq 0 \text{ do } x := x + 1 \text{ od}$

and a **state** σ with $\sigma \models x = 0$.

$$\begin{array}{l} \langle S, \sigma \rangle \xrightarrow{(ii),(iii)} \langle a[1] := 0; \text{while } a[x] \neq 0 \text{ do } x := x + 1 \text{ od}, \sigma[a[0] := 1] \rangle \\ \xrightarrow{(ii),(iii)} \langle \text{while } a[x] \neq 0 \text{ do } x := x + 1 \text{ od}, \sigma' \rangle \\ \xrightarrow{(vi)} \langle x := x + 1; \text{while } a[x] \neq 0 \text{ do } x := x + 1 \text{ od}, \sigma' \rangle \\ \xrightarrow{(ii),(iii)} \langle \text{while } a[x] \neq 0 \text{ do } x := x + 1 \text{ od}, \sigma'[x := 1] \rangle \\ \xrightarrow{(vii)} \langle E, \sigma'[x := 1] \rangle \end{array}$$

where $\sigma' = \sigma[a[0] := 1][a[1] := 0]$.

-17-2016-07-14 - while -

5/18

Proof-System PD

Proof-System PD (for sequential, deterministic programs)

Axiom 1: Skip-Statement

$$\{p\} \text{ skip } \{p\}$$

Axiom 2: Assignment

$$\{p[u := t]\} u := t \{p\}$$

Rule 3: Sequential Composition

$$\frac{\{p\} S_1 \{r\}, \{r\} S_2 \{q\}}{\{p\} S_1; S_2 \{q\}}$$

Rule 4: Conditional Statement

$$\frac{\{p \wedge B\} S_1 \{q\}, \{p \wedge \neg B\} S_2 \{q\}}{\{p\} \text{ if } B \text{ then } S_1 \text{ else } S_2 \text{ fi } \{q\}}$$

Rule 5: While-Loop

$$\frac{\{p \wedge B\} S \{p\}}{\{p\} \text{ while } B \text{ do } S \text{ od } \{p \wedge \neg B\}}$$

Rule 6: Consequence

$$\frac{p \rightarrow p_1, \{p_1\} S \{q_1\}, q_1 \rightarrow q}{\{p\} S \{q\}}$$

Theorem. PD is correct (“sound”) and (relative) complete for partial correctness of deterministic programs, i.e. $\vdash_{PD} \{p\} S \{q\}$ if and only if $\models \{p\} S \{q\}$.

Example Proof

$$DIV \equiv \overbrace{a := 0; b := x}^{=:S_0^D}; \text{ while } \overbrace{b \geq y}^{=:B^D} \text{ do } \overbrace{b := b - y; a := a + 1}^{=:S_1^D} \text{ od}$$

(The first (textually represented) program that has been formally verified (Hoare, 1969).

We can prove $\models \{x \geq 0 \wedge y \geq 0\} DIV \{a \cdot y + b = x \wedge b < y\}$

by showing $\vdash_{PD} \underbrace{\{x \geq 0 \wedge y \geq 0\}}_{=:p^D} DIV \underbrace{\{a \cdot y + b = x \wedge b < y\}}_{=:q^D}$, i.e., derivability in PD:

$$\begin{array}{c}
 \text{(1)} \quad \frac{}{\{p^D\} S_0^D \{P\},} \quad \frac{\checkmark}{P \rightarrow P,} \quad \frac{\text{(2)} \quad \frac{}{\{P \wedge (B^D)\} S_1^D \{P\}}}{\{P\} \text{ while } B^D \text{ do } S_1^D \text{ od } \{P \wedge \neg(B^D)\}}, \quad \frac{\text{(3)} \quad \frac{}{P \wedge \neg(B^D) \rightarrow q^D}}{} \\
 \hline
 \frac{\{p^D\} S_0^D \{P\}, \quad \{P\} \text{ while } B^D \text{ do } S_1^D \text{ od } \{q^D\}}{\{p^D\} S_0^D; \text{ while } B^D \text{ do } S_1^D \text{ od } \{q^D\}} \text{(R3)}
 \end{array}$$

(A1) $\{p\} \text{ skip } \{p\}$

(A2) $\{p[u := t]\} u := t \{p\}$

(R3) $\frac{\{p\} S_1 \{r\}, \{r\} S_2 \{q\}}{\{p\} S_1; S_2 \{q\}}$

(R4) $\frac{\{p \wedge B\} S_1 \{q\}, \{p \wedge \neg B\} S_2 \{q\}}{\{p\} \text{ if } B \text{ then } S_1 \text{ else } S_2 \text{ fi } \{q\}}$

(R5) $\frac{\{p \wedge B\} S \{p\}}{\{p\} \text{ while } B \text{ do } S \text{ od } \{p \wedge \neg B\}}$

(R6) $\frac{p \rightarrow p_1, \{p_1\} S \{q_1\}, q_1 \rightarrow q}{\{p\} S \{q\}}$

Example Proof

$$DIV \equiv \underbrace{a := 0; b := x}_{=: S_0^D}; \mathbf{while} \underbrace{b \geq y}_{=: B^D} \mathbf{do} \underbrace{b := b - y; a := a + 1}_{=: S_1^D} \mathbf{od}$$

(The first (textually represented) program that has been formally verified (Hoare, 1969).

We can prove $\models \{x \geq 0 \wedge y \geq 0\} DIV \{a \cdot y + b = x \wedge b < y\}$

by showing $\vdash_{PD} \underbrace{\{x \geq 0 \wedge y \geq 0\}}_{=: p^D} DIV \underbrace{\{a \cdot y + b = x \wedge b < y\}}_{=: q^D}$, i.e., derivability in PD:

$$\frac{\frac{(1) \quad \frac{\{x \geq 0 \wedge y \geq 0\} a := 0; b := x \{P\},}{P \rightarrow P,} \quad \frac{(2) \quad \frac{\{P \wedge (b \geq y)\} b := b - y; a := a + 1 \{P\}}{\{P\} \mathbf{while} b \geq y \mathbf{do} b := b - y; a := a + 1 \mathbf{od} \{P \wedge \neg(b \geq y)\}}, \quad (R5)}{\{P\} \mathbf{while} b \geq y \mathbf{do} b := b - y; a := a + 1 \mathbf{od} \{a \cdot y + b = x \wedge b < y\}} \quad (R6)}{\{x \geq 0 \wedge y \geq 0\} a := 0; b := x; \mathbf{while} b \geq y \mathbf{do} b := b - y; a := a + 1 \mathbf{od} \{a \cdot y + b = x \wedge b < y\}} \quad (R3)$$

(A1) $\{p\} \text{ skip } \{p\}$

(A2) $\{p[u := t]\} u := t \{p\}$

(R3) $\frac{\{p\} S_1 \{r\}, \{r\} S_2 \{q\}}{\{p\} S_1; S_2 \{q\}}$

(R4) $\frac{\{p \wedge B\} S_1 \{q\}, \{p \wedge \neg B\} S_2 \{q\}}{\{p\} \mathbf{if} B \mathbf{then} S_1 \mathbf{else} S_2 \mathbf{fi} \{q\}}$

(R5) $\frac{\{p \wedge B\} S \{p\}}{\{p\} \mathbf{while} B \mathbf{do} S \mathbf{od} \{p \wedge \neg B\}}$

(R6) $\frac{p \rightarrow p_1, \{p_1\} S \{q_1\}, q_1 \rightarrow q}{\{p\} S \{q\}}$

Example Proof Cont'd

$$\begin{array}{c}
 \text{(1)} \quad \frac{}{\{x \geq 0 \wedge y \geq 0\} a := 0; b := x \{P\},} \\
 \text{(2)} \quad \frac{}{\{P \wedge (b \geq y)\} b := b - y; a := a + 1 \{P\}} \\
 \text{(3)} \quad \frac{}{P \wedge \neg(b \geq y) \rightarrow a \cdot y + b = x \wedge b < y} \\
 \text{(R5)} \quad \frac{\{P \wedge (b \geq y)\} b := b - y; a := a + 1 \{P\}}{P \rightarrow P, \{P\} \text{ while } b \geq y \text{ do } b := b - y; a := a + 1 \text{ od } \{P \wedge \neg(b \geq y)\},} \\
 \text{(R6)} \quad \frac{P \wedge \neg(b \geq y) \rightarrow a \cdot y + b = x \wedge b < y}{\{P\} \text{ while } b \geq y \text{ do } b := b - y; a := a + 1 \text{ od } \{a \cdot y + b = x \wedge b < y\}} \\
 \text{(R3)} \quad \frac{\{x \geq 0 \wedge y \geq 0\} a := 0; b := x \{P\}, \quad \{P\} \text{ while } b \geq y \text{ do } b := b - y; a := a + 1 \text{ od } \{a \cdot y + b = x \wedge b < y\}}{\{x \geq 0 \wedge y \geq 0\} a := 0; b := x; \text{ while } b \geq y \text{ do } b := b - y; a := a + 1 \text{ od } \{a \cdot y + b = x \wedge b < y\}}
 \end{array}$$

In the following, we show

- (1) $\vdash_{PD} \{x \geq 0 \wedge y \geq 0\} a := 0; b := x \{P\},$
- (2) $\vdash_{PD} \{P \wedge b \geq y\} b := b - y; a := a + 1 \{P\},$
- (3) $\models P \wedge \neg(b \geq y) \rightarrow a \cdot y + b = x \wedge b < y.$

As **loop invariant**, we choose (**creative act!**):

$$P \equiv a \cdot y + b = x \wedge b \geq 0$$

Proof of (1)

<p>(A1) $\{p\} \text{ skip } \{p\}$</p> <p>(A2) $\{p[u := t]\} u := t \{p\}$</p> <p>(R3) $\frac{\{p\} S_1 \{r\}, \{r\} S_2 \{q\}}{\{p\} S_1; S_2 \{q\}}$</p>	<p>(R4) $\frac{\{p \wedge B\} S_1 \{q\}, \{p \wedge \neg B\} S_2 \{q\}}{\{p\} \text{ if } B \text{ then } S_1 \text{ else } S_2 \text{ fi } \{q\}}$</p> <p>(R5) $\frac{\{p \wedge B\} S \{p\}}{\{p\} \text{ while } B \text{ do } S \text{ od } \{p \wedge \neg B\}}$</p> <p>(R6) $\frac{p \rightarrow p_1, \{p_1\} S \{q_1\}, q_1 \rightarrow q}{\{p\} S \{q\}}$</p>
---	--

- (1) claims:

$$\vdash_{PD} \{x \geq 0 \wedge y \geq 0\} a := 0; b := x \{P\}$$

where $P \equiv a \cdot y + b = x \wedge b \geq 0$.

- $\vdash_{PD} \underbrace{\{0 \cdot y + x = x \wedge x \geq 0\}}_{\substack{p[u := t] \\ p[a := 0]}} a := 0 \{a \cdot y + x = x \wedge x \geq 0\} \quad \text{by (A2),}$
-

Proof of (1)

<p>(A1) $\{p\} \text{ skip } \{p\}$</p> <p>(A2) $\{p[u := t]\} u := t \{p\}$</p> <p>(R3) $\frac{\{p\} S_1 \{r\}, \{r\} S_2 \{q\}}{\{p\} S_1; S_2 \{q\}}$</p>	<p>(R4) $\frac{\{p \wedge B\} S_1 \{q\}, \{p \wedge \neg B\} S_2 \{q\}}{\{p\} \text{ if } B \text{ then } S_1 \text{ else } S_2 \text{ fi } \{q\}}$</p> <p>(R5) $\frac{\{p \wedge B\} S \{p\}}{\{p\} \text{ while } B \text{ do } S \text{ od } \{p \wedge \neg B\}}$</p> <p>(R6) $\frac{p \rightarrow p_1, \{p_1\} S \{q_1\}, q_1 \rightarrow q}{\{p\} S \{q\}}$</p>
---	--

- (1) claims:

$$\vdash_{PD} \{x \geq 0 \wedge y \geq 0\} a := 0; b := x \{P\}$$

where $P \equiv a \cdot y + b = x \wedge b \geq 0$.

- $\vdash_{PD} \{0 \cdot y + x = x \wedge x \geq 0\} a := 0 \{a \cdot y + x = x \wedge x \geq 0\}$ by (A2),
- $\vdash_{PD} \{a \cdot y + x = \underbrace{x}_{P[b:=x]} \wedge \underbrace{x}_{P} \geq 0\} b := x \{a \cdot y + \underbrace{b}_{P} = x \wedge \underbrace{b}_{P} \geq 0\}$ by (A2),

$P[b:=x]$

$P \equiv P$

Proof of (1)

$$\begin{array}{ll}
 \text{(A1)} \{p\} \text{ skip } \{p\} & \text{(R4)} \frac{\{p \wedge B\} S_1 \{q\}, \{p \wedge \neg B\} S_2 \{q\}}{\{p\} \text{ if } B \text{ then } S_1 \text{ else } S_2 \text{ fi } \{q\}} \\
 \text{(A2)} \{p[u := t]\} u := t \{p\} & \text{(R5)} \frac{\{p \wedge B\} S \{p\}}{\{p\} \text{ while } B \text{ do } S \text{ od } \{p \wedge \neg B\}} \\
 \text{(R3)} \frac{\{p\} S_1 \{r\}, \{r\} S_2 \{q\}}{\{p\} S_1; S_2 \{q\}} & \text{(R6)} \frac{p \rightarrow p_1, \{p_1\} S \{q_1\}, q_1 \rightarrow q}{\{p\} S \{q\}}
 \end{array}$$

- **(1)** claims:

$$\vdash_{PD} \{x \geq 0 \wedge y \geq 0\} a := 0; b := x \{P\}$$

where $P \equiv a \cdot y + b = x \wedge b \geq 0$.

- $\vdash_{PD} \{0 \cdot y + x = x \wedge x \geq 0\} a := 0 \{a \cdot y + x = x \wedge x \geq 0\}$ by (A2),

- $\vdash_{PD} \{a \cdot y + x = x \wedge x \geq 0\} b := x \underbrace{\{a \cdot y + b = x \wedge b \geq 0\}}_{\equiv P}$ by (A2),

- thus, $\vdash_{PD} \{0 \cdot y + x = x \wedge x \geq 0\} a := 0; b := x \{P\}$ by (R3),

- using $x \geq 0 \wedge y \geq 0 \rightarrow 0 \cdot y + x = x \wedge x \geq 0$ and $P \rightarrow P$, we obtain

$$\vdash_{PD} \{x \geq 0 \wedge y \geq 0\} a := 0; b := x \{P\}$$

by (R6). □

Substitution

The rule '**Assignment**' uses (syntactical) **substitution**: $\{p[u := t]\} u := t \{p\}$

(In formula p , replace all (free) occurrences of (program or logical) variable u by term t .)

Defined as usual, only **indexed** and **bound** variables need to be treated specially:

Expressions:

- plain variable x : $x[u := t] \equiv \begin{cases} t & , \text{ if } x = u \\ x & , \text{ otherwise} \end{cases}$

- constant c :

$$c[u := t] \equiv c.$$

- constant op , terms s_i :

$$\begin{aligned} op(s_1, \dots, s_n)[u := t] \\ \equiv op(s_1[u := t], \dots, s_n[u := t]). \end{aligned}$$

- conditional expression:

$$\begin{aligned} (B ? s_1 : s_2)[u := t] \\ \equiv (B[u := t] ? s_1[u := t] : s_2[u := t]) \end{aligned}$$

- **indexed variable**, u plain or $u \equiv b[t_1, \dots, t_m]$ and $a \neq b$:

$$(a[s_1, \dots, s_n])[u := t] \equiv a[s_1[u := t], \dots, s_n[u := t]]$$

- **indexed variable**, $u \equiv a[t_1, \dots, t_m]$:

$$(a[s_1, \dots, s_n])[u := t] \equiv (\bigwedge_{i=1}^n s_i[u := t] = t_i ? t : a[s_1[u := t], \dots, s_n[u := t]])$$

Formulae:

- boolean expression $p \equiv s$:

$$p[u := t] \equiv s[u := t]$$

- negation:

$$(\neg q)[u := t] \equiv \neg(q[u := t])$$

- conjunction etc.:

$$\begin{aligned} (q \wedge r)[u := t] \\ \equiv q[u := t] \wedge r[u := t] \end{aligned}$$

- **quantifier**:

$$(\forall x : q)[u := t] \equiv \forall y : q[x := y][u := t]$$

y fresh (not in q, t, u), same type as x .

Proof of (2)

(A1) $\{p\} \text{ skip } \{p\}$	(R4) $\frac{\{p \wedge B\} S_1 \{q\}, \{p \wedge \neg B\} S_2 \{q\}}{\{p\} \text{ if } B \text{ then } S_1 \text{ else } S_2 \text{ fi } \{q\}}$
(A2) $\{p[u := t]\} u := t \{p\}$	(R5) $\frac{\{p \wedge B\} S \{p\}}{\{p\} \text{ while } B \text{ do } S \text{ od } \{p \wedge \neg B\}}$
(R3) $\frac{\{p\} S_1 \{r\}, \{r\} S_2 \{q\}}{\{p\} S_1; S_2 \{q\}}$	(R6) $\frac{p \rightarrow p_1, \{p_1\} S \{q_1\}, q_1 \rightarrow q}{\{p\} S \{q\}}$

- (2) claims:

$$\vdash_{PD} \{P \wedge b \geq y\} b := b - y; a := a + 1 \{P\}$$

where $P \equiv a \cdot y + b = x \wedge b \geq 0$.

- $\vdash_{PD} \{(a + 1) \cdot y + \underbrace{(b - y)} = x \wedge \underbrace{(b - y)} \geq 0\} b := b - y \{(a + 1) \cdot y + \underbrace{b} = x \wedge \underbrace{b} \geq 0\}$
by (A2), ✓

Proof of (2)

<p>(A1) $\{p\} \text{ skip } \{p\}$</p> <p>(A2) $\{p[u := t]\} u := t \{p\}$</p> <p>(R3) $\frac{\{p\} S_1 \{r\}, \{r\} S_2 \{q\}}{\{p\} S_1; S_2 \{q\}}$</p>	<p>(R4) $\frac{\{p \wedge B\} S_1 \{q\}, \{p \wedge \neg B\} S_2 \{q\}}{\{p\} \text{ if } B \text{ then } S_1 \text{ else } S_2 \text{ fi } \{q\}}$</p> <p>(R5) $\frac{\{p \wedge B\} S \{p\}}{\{p\} \text{ while } B \text{ do } S \text{ od } \{p \wedge \neg B\}}$</p> <p>(R6) $\frac{p \rightarrow p_1, \{p_1\} S \{q_1\}, q_1 \rightarrow q}{\{p\} S \{q\}}$</p>
---	--

- (2) claims:

$$\vdash_{PD} \{P \wedge b \geq y\} b := b - y; a := a + 1 \{P\}$$

where $P \equiv a \cdot y + b = x \wedge b \geq 0$.

- $\vdash_{PD} \{(a + 1) \cdot y + (b - y) = x \wedge (b - y) \geq 0\} b := b - y \{(a + 1) \cdot y + b = x \wedge b \geq 0\}$
by (A2),
- $\vdash_{PD} \{(a + 1) \cdot y + b = x \wedge b \geq 0\} a := a + 1 \underbrace{\{a \cdot y + b = x \wedge b \geq 0\}}_{\equiv P} \text{ by (A2), } \checkmark$

Proof of (2)

$$\begin{array}{ll}
 \text{(A1)} \{p\} \text{ skip } \{p\} & \text{(R4)} \frac{\{p \wedge B\} S_1 \{q\}, \{p \wedge \neg B\} S_2 \{q\}}{\{p\} \text{ if } B \text{ then } S_1 \text{ else } S_2 \text{ fi } \{q\}} \\
 \text{(A2)} \{p[u := t]\} u := t \{p\} & \text{(R5)} \frac{\{p \wedge B\} S \{p\}}{\{p\} \text{ while } B \text{ do } S \text{ od } \{p \wedge \neg B\}} \\
 \text{(R3)} \frac{\{p\} S_1 \{r\}, \{r\} S_2 \{q\}}{\{p\} S_1; S_2 \{q\}} & \text{(R6)} \frac{p \rightarrow p_1, \{p_1\} S \{q_1\}, q_1 \rightarrow q}{\{p\} S \{q\}}
 \end{array}$$

- **(2)** claims:

$$\vdash_{PD} \{P \wedge b \geq y\} b := b - y; a := a + 1 \{P\}$$

where $P \equiv a \cdot y + b = x \wedge b \geq 0$.

- $\vdash_{PD} \{(a + 1) \cdot y + (b - y) = x \wedge (b - y) \geq 0\} b := b - y \{(a + 1) \cdot y + b = x \wedge b \geq 0\}$
by (A2),

- $\vdash_{PD} \{(a + 1) \cdot y + b = x \wedge b \geq 0\} a := a + 1 \underbrace{\{a \cdot y + b = x \wedge b \geq 0\}}_{\equiv P}$ by (A2),

- $\vdash_{PD} \{(a + 1) \cdot y + (b - y) = x \wedge (b - y) \geq 0\} b := b - y; a := a + 1 \{P\}$ by (R3),

- using $(P \wedge b \geq y) \rightarrow ((a + 1) \cdot y + (b - y) = x \wedge (b - y) \geq 0)$ and $P \rightarrow P$ we obtain,

$$\vdash_{PD} \{P \wedge b \geq y\} b := b - y; a := a + 1 \{P\}$$

by (R6).

Proof of (3)

(3) claims

$$\models (P \wedge \neg(b \geq y)) \rightarrow (a \cdot y + b = x \wedge b < y.)$$

where $P \equiv a \cdot y + b = x \wedge b \geq 0$.

Proof: easy.

Back to the Example Proof

We have shown:

$$(1) \vdash_{PD} \{x \geq 0 \wedge y \geq 0\} a := 0; b := x \{P\},$$

$$(2) \vdash_{PD} \{P \wedge b \geq y\} b := b - y; a := a + 1 \{P\},$$

$$(3) \models P \wedge \neg(b \geq y) \rightarrow a \cdot y + b = x \wedge b < y.$$

and

$$\frac{\frac{\frac{(1)}{\{x \geq 0 \wedge y \geq 0\} a := 0; b := x \{P\}}, \frac{(2)}{\frac{P \rightarrow P, \{P\} \text{ while } b \geq y \text{ do } b := b - y; a := a + 1 \text{ od } \{P \wedge \neg(b \geq y)\}, \text{ (R5)}}{\{P \wedge \neg(b \geq y)\} b := b - y; a := a + 1 \{P\}}}{} \text{ (R6)}}{\frac{P \wedge \neg(b \geq y) \rightarrow a \cdot y + b = x \wedge b < y}{\{P\} \text{ while } b \geq y \text{ do } b := b - y; a := a + 1 \text{ od } \{a \cdot y + b = x \wedge b < y\}} \text{ (R3)}}{\{x \geq 0 \wedge y \geq 0\} a := 0; b := x; \text{ while } b \geq y \text{ do } b := b - y; a := a + 1 \text{ od } \{a \cdot y + b = x \wedge b < y\}} \text{ (R3)}$$

thus

$$\vdash_{PD} \{x \geq 0 \wedge y \geq 0\} \underbrace{a := 0; b := x; \text{ while } b \geq y \text{ do } b := b - y; a := a + 1 \text{ od } \{a \cdot y + b = x \wedge b < y\}}_{\equiv DIV}$$

and thus (since PD is sound) *DIV* is **partially correct** wrt.

- **pre-condition:** $x \geq 0 \wedge y \geq 0$,
- **post-condition:** $a \cdot y + b = x \wedge b < y$.

IOW: whenever *DIV* is called with x and y such that $x \geq 0 \wedge y \geq 0$, then (if *DIV* terminates) $a \cdot y + b = x \wedge b < y$ will hold.

Once Again

- $P \equiv a \cdot y + b = x \wedge b \geq 0$

$\{x \geq 0 \wedge y \geq 0\}$

$\{0 \cdot y + x = x \wedge x \geq 0\}$

- $a := 0;$

$\{a \cdot y + x = x \wedge x \geq 0\}$

- $b := x;$

$\{a \cdot y + b = x \wedge b \geq 0\}$

$\{P\}$

- **while** $b \geq y$ **do**

$\{P \wedge b \geq y\}$

$\{(a + 1) \cdot y + (b - y) = x \wedge (b - y) \geq 0\}$

- $b := b - y;$

$\{(a + 1) \cdot y + b = x \wedge b \geq 0\}$

- $a := a + 1$

$\{a \cdot y + b = x \wedge b \geq 0\}$

$\{P\}$

- **od**

$\{P \wedge \neg(b \geq y)\}$

$\{a \cdot y + b = x \wedge b < y\}$

A2

A2

R3

R6

A2

A2

R3

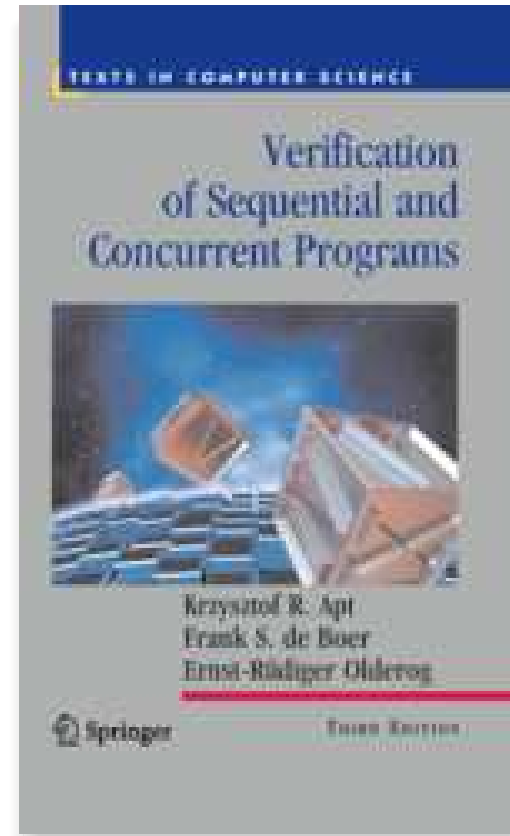
R6

R5

R6

- (A1) $\{p\} \text{ skip } \{p\}$
- (A2) $\{p[u := t]\} u := t \{p\}$
- (R3) $\frac{\{p\} S_1 \{r\}, \{r\} S_2 \{q\}}{\{p\} S_1; S_2 \{q\}}$
- (R4) $\frac{\{p \wedge B\} S_1 \{q\}, \{p \wedge \neg B\} S_2 \{q\}}{\{p\} \text{ if } B \text{ then } S_1 \text{ else } S_2 \text{ fi } \{q\}}$
- (R5) $\frac{\{p \wedge B\} S \{p\}}{\{p\} \text{ while } B \text{ do } S \text{ od } \{p \wedge \neg B\}}$
- (R6) $\frac{p \rightarrow p_1, \{p_1\} S \{q_1\}, q_1 \rightarrow q}{\{p\} S \{q\}}$

Literature Recommendation



Assertions

Assertions

- Extend the **syntax** of **deterministic programs** by

$$S ::= \dots \mid \text{assert}(B)$$

- and the **semantics** by rule

$$\langle \text{assert}(B), \sigma \rangle \rightarrow \langle E, \sigma \rangle \text{ if } \sigma \models B.$$

(If the asserted boolean expression B does not hold in state σ , the empty program is not reached; otherwise the assertion remains in the first component: **abnormal** program termination).

Extend PD by axiom:

$$(A7) \{p\} \text{assert}(p) \{p\}$$

- That is, if p holds **before** the assertion, then we can **continue** with the derivation in PD. If p does not hold, we **“get stuck”** (and cannot complete the derivation).
- So we **cannot** derive $\{true\} x := 0; \text{assert}(x = 27) \{true\}$ in PD.

Modular Reasoning

Modular Reasoning

We can add another rule for calls of functions $f : F$ (simplest case: only global variables):

$$(R7) \frac{\{p\} F \{q\}}{\{p\} f() \{q\}}$$

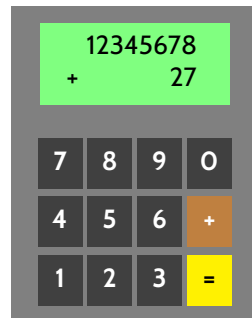
“If we have $\vdash \{p\} F \{q\}$ for the **implementation** of function f , then if f is **called** in a state satisfying p , the state after return of f will satisfy q .”

p is called **pre-condition** and q is called **post-condition** of f .

Example: if we have

- $\{true\} \text{read_number} \{0 \leq result < 10^8\}$
- $\{0 \leq x \wedge 0 \leq y\} \text{add} \{(old(x) + old(y) < 10^8 \wedge result = old(x) + old(y)) \vee result < 0\}$
- $\{true\} \text{display} \{(0 \leq old(x) < 10^8 \implies \text{”old(x)”}) \wedge (old(x) < 0 \implies \text{”-E-”})\}$

we may be able to prove our pocket calculator correct.



```
1 int main() {
2
3   while (true) {
4     int x = read_number();
5     int y = read_number();
6
7     int sum = add( x, y );
8
9     display(sum);
10  }
11 }
```

Return Values and Old Values

- For **modular reasoning**, it's often useful to refer in the post-condition
 - to the **return value** as *result*,
 - the **values** of variable *x* **at calling time** as *old(x)*.

- Can be defined using **auxiliary variables**:

- Transform function

$$T f() \{ \dots; \mathbf{return} \textit{expr}; \}$$

(over variables $V = \{v_1, \dots, v_n\}$, \textit{result} , $v_i^{old} \notin V$) to

$$T f() \{ \\ v_1^{old} := v_1; \dots; v_n^{old} := v_n; \\ \dots; \\ \textit{result} := \textit{expr}; \\ \mathbf{return} \textit{result}; \\ \}$$

over $V' = V \cup \{v^{old} \mid v \in V\} \cup \{\textit{result}\}$.

- Then *old(x)* is just an abbreviation for x^{old} .

The Verifier for Concurrent C

- The **Verifier for Concurrent C** (VCC) basically implements Hoare-style reasoning.
- **Special syntax:**
 - `#include <vcc.h>`
 - `_(requires p)` – **pre-condition**, *p* is (basically) a C expression
 - `_(ensures q)` – **post-condition**, *q* is (basically) a C expression
 - `_(invariant expr)` – **loop invariant**, *expr* is (basically) a C expression
 - `_(assert p)` – **intermediate invariant**, *p* is (basically) a C expression
 - `_(writes &v)` – VCC considers **concurrent** C programs; we need to declare for each procedure which global variables it is allowed to write to (also checked by VCC)
- **Special expressions:**
 - `\thread_local(&v)` – no other thread writes to variable *v* (in pre-conditions)
 - `\old(v)` – the value of *v* when procedure was called (useful for post-conditions)
 - `\result` – return value of procedure (useful for post-conditions)

VCC Syntax Example

```
1 #include <vcc.h>
2
3 int a, b;
4
5 void div( int x, int y )
6     _(requires x >= 0 && y >= 0)
7     _(ensures a * y + b == x && b < y)
8     _(writes &a)
9     _(writes &b)
10 {
11     a = 0;
12     b = x;
13     while (b >= y)
14         _(invariant a * y + b == x && b >= 0)
15         {
16             b = b - y;
17             a = a + 1;
18         }
19 }
```

pre-cond. P

post-cond. Q

loop invariant P

$DIV \equiv a := 0; b := x; \mathbf{while} \ b \geq y \ \mathbf{do} \ b := b - y; a := a + 1 \ \mathbf{od}$

$\{x \geq 0 \wedge y \geq 0\} DIV \{x \geq 0 \wedge y \geq 0\}$

VCC Web-Interface



Vcc @ rise4fun from Micr... x

rise4fun.com/Vcc/4Kqe

VCC

Does this C program always work?

```
1 #include <vcc.h>
2
3 int a, b;
4
5 void div( int x, int y )
6   _(requires x >= 0 && y >= 0)
7   _(ensures a * y + b == x && b < y)
8   _(writes &a)
9   _(writes &b)
10  {
11    a = 0;
12    b = x;
13    while (b >= y)
14      _(invariant a * y + b == x && b >= 0)
15      {
16        b = b - y;
17        a = a + 1;
18      }
19 }
```

[home](#) [video](#) [permalink](#)
⌘ shortcut: Alt+B

[samples](#)
[hello](#)
[lsearch](#)
[safestring](#)
[bozosort](#)
[spinlock](#)

[about Vcc - A Verifier for Concurrent C](#)
VCC is a tool that proves correctness of annotated concurrent C programs or finds problems in them. VCC extends C with design by contract features, like pre- and postcondition as well as type invariants. Annotated programs are translated to logical formulas using the Boogie tool, which passes them to an automated SMT solver Z3 to check their validity.

[tools](#) [developer](#) [about](#)

rise4fun © 2016 Microsoft Corporation - [terms of use](#) - [privacy & cookies](#) - [code of conduct](#)

Example program *DIV*: <http://rise4fun.com/Vcc/4Kqe>

Interpretation of Results

- VCC says: “**verification succeeded**”

We can **only** conclude that the tool

– under its interpretation of the C-standard, under its platform assumptions (32-bit), etc. – “thinks” that it can prove $\models \{p\} DIV \{q\}$.

Can be due to an error in the tool! (That’s a **false negative** then.)

Yet we can ask **for a printout of the proof** and check it manually (hardly possible in practice) or with other tools like interactive theorem provers.

Note: $\models \{false\} f \{q\}$ **always** holds.

That is, a **mistake** in writing down the pre-condition can make errors in the program go undetected.

- VCC says: “**verification failed**”

- May be a **false positive**.

The tool **does not provide counter-examples** in the form of a computation path, it (only) gives **hints on input values** satisfying p and causing a violation of q .

→ try to construct a (true) counter-example from the hints.

or: → make pre-condition p or loop-invariant(s) stronger, and try again.

- Other case: “**timeout**” etc. – completely **inconclusive** outcome.

VCC Features

- For the exercises, we use VCC only for **sequential, single-thread programs**.
- VCC checks a number of **implicit assertions**:
 - no arithmetic overflow in expressions (according to C-standard),
 - **array-out-of-bounds access**,
 - **NULL-pointer dereference**,
 - and many more.
- VCC also supports:
 - **concurrency**:
different threads may write to shared global variables; VCC can check whether concurrent access to shared variables is properly managed;
 - **data structure invariants**:
we may declare invariants that have to hold for, e.g., records (e.g. the length field l is always equal to the length of the string field str); those invariants may **temporarily** be violated when updating the data structure.
 - and much more.
- Verification **does not always succeed**:
 - The backend SMT-solver may not be able to discharge proof-obligations (in particular non-linear multiplication and division are challenging);
 - In many cases, we need to provide **loop invariants** manually.

Tell Them What You've Told Them. . .

- There are **more approaches** to software quality assurance than just **testing**.
- For example, **program verification**.
- **Proof System PD** can be used
 - to **prove**
 - that a given program is
 - **correct** wrt. its specification.

This approach considers **all inputs** inside the specification!

- Tools like **VCC** implement this approach.

References

References

Hoare, C. A. R. (1969). An axiomatic basis for computer programming. *Commun. ACM*, 12(10):576–580.

IEEE (1990). *IEEE Standard Glossary of Software Engineering Terminology*. Std 610.12-1990.

ISO (2011). *Road vehicles – Functional safety – Part 1: Vocabulary*. 26262-1:2011.

Ludewig, J. and Lichter, H. (2013). *Software Engineering*. dpunkt.verlag, 3. edition.