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Tutorial for Cyber-Physical Systems - Hybrid Models
Exercise Sheet 8

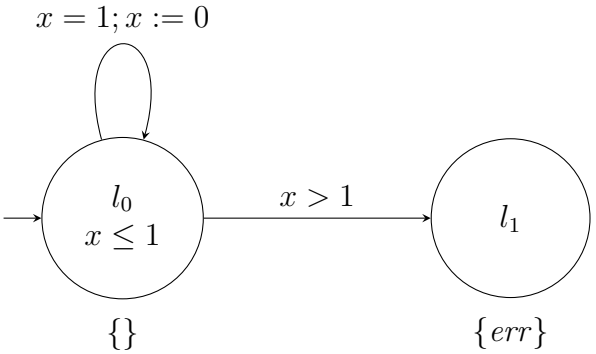

Figure 1: A timed automaton.

Exercise 1: Timed automata and programs 1
Consider the timed automaton $\mathcal{T}_1$ from Figure 1 with clock variable x, i.e., $\mathcal{C} = \{x\}$.

(a) Translate $\mathcal{T}_1$ to an equivalent program $\mathcal{P}_1$, i.e., with the same executions/paths.

(b) Compute the reachable states φ_{reach} of $\mathcal{P}_1$ by iteration of *post*.

Exercise 2: Timed automata and programs 2

Consider the timed automaton $\mathcal{T}_2$ which is obtained from $\mathcal{T}_1$ (see Figure 1) by adding another clock variable y, i.e., $\mathcal{C} = \{x, y\}$. Note that y is never read in any guard or invariant. Still, the state space changes (recall that a state is a pair (ℓ, ν) with $\nu : \mathcal{C} \to \mathbb{R}$).

You may wonder why adding an unused clock should affect the reachability of a state. In fact, it does not (in some sense). However, the algorithms behave differently.

(a) Translate $\mathcal{T}_2$ to an equivalent program $\mathcal{P}_2$.

(b) What are the reachable states φ_{reach} of $\mathcal{P}_2$?
Solve this exercise intuitively, i.e., do not apply a formal algorithm. Alternatively, you may reason about the reachable states *Reach* of $\mathcal{T}_2$.

(c) What happens when you try to compute the reachable states φ_{reach} of $\mathcal{P}_2$ by iteration of *post*?

(d) Find a suitable set of predicates *Preds* such that the predicate abstraction (iteration of $post^{\#}$) can prove safety (specified by the TCTL formula $\mathbf{A}\mathcal{G}\neg err$) of $\mathcal{P}_2$.
Provide the abstract reachability graph that you obtain.

Hint: Consider *some* of the predicates which are used to define the regions for the region transition system (*RTS*) construction.