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- **Class Diagrams**
 - semantics: system states
- **Object Diagrams**
 - concrete syntax
 - dangling references
 - partial vs. complete
 - object diagrams at work
- **Proto-OCL**
 - syntax semantics
 - Proto-OCL vs. OCL
 - Putting it All Together
 - Proto-OCL vs. Software

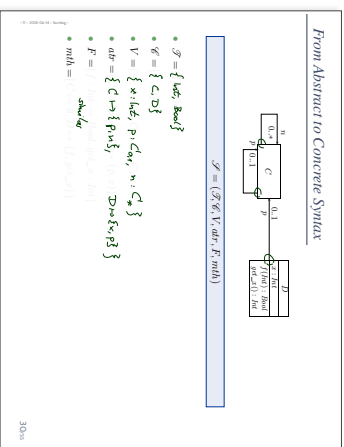
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Topic Area Architecture & Design: Content

- VL11
 - Introduction and Vocabulary
 - Software Modelling
 - model view / viewpoints: 4+1 view
 - Modelling structure
 - identified class object diagrams
 - identified object container figs: (OCL)
- VL12
 - Principles of Design
 - identifying required functions
 - information modelling and data encapsulation
 - abstract data types, object orientation
 - Design Patterns
 - modelling behaviour
 - communicating finite automata (CFA)
 - Uppaal query language
- VL13
 - Modelling behaviour
 - communicating finite automata (CFA)
 - Uppaal query language
- VL14
 - Object Modelling Language (OML)
 - OPL vs. Software
 - Object Modelling Language (OML)
 - an outlook on formalised state-machines
 - Model-driven-based Software Engineering

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From Abstract to Concrete Syntax



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Content

A More Abstract Class Diagram Semantics



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Object System Structure

Definition. An Object System Structure of signature

$$\mathcal{S} = (\mathcal{S}, \mathcal{V}, \text{dir}, F, \text{mth})$$

is a domain function \mathcal{S} which assigns to each type a domain, i.e.

- $T \in \mathcal{S}$ is mapped to $\mathcal{S}(T)$.
- $C \in \mathcal{C}$ is mapped to an **infinite set** $\mathcal{S}(C)$ of **abstract identities**.
- object identities of different classes are disjoint, i.e. $\forall C, D \in \mathcal{C}: C \neq D \rightarrow \mathcal{S}(C) \cap \mathcal{S}(D) = \emptyset$.
- on object identities, (only) comparison for equality "=" is defined.
- C_1 and $C_{0,1}$ for $C \in \mathcal{C}$ are mapped to $2^{\mathcal{S}(C)}$.

We use $\mathcal{S}(F)$ to denote $\bigcup_{C \in \mathcal{C}} \mathcal{S}(C)$, analogously $\mathcal{S}(F')$.

Note: We identify objects and object identities, because both uniquely determine each other (cf. OCL 2.0 standard)

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Basic Object System Structure Example

Wanted: a structure for signature

$$\mathcal{S}_0 = (\text{Int, Bool}), \{C, D\}, \{x: \text{Int}, p: \text{Co}, n: C, \}, \{C \rightarrow \text{Int}, D \rightarrow \text{Int}, x\}, \\ \{f: \text{Int} \rightarrow \text{Bool}, \text{get}_x: \text{Int}, \{C \rightarrow \text{Int}, D \rightarrow \{f, \text{get}_x\}\}\}$$

A structure \mathcal{S} maps

- $\tau \in \mathcal{S}$ to some $\mathcal{D}(\tau), C \in \mathcal{S}$ to some identities $\mathcal{D}(C)$ (infinite, pairwise disjoint).
- C_1 and C_2 , for $C \in \mathcal{S}$ to $\mathcal{D}(C_1) = \mathcal{D}(C_2) = \mathcal{D}(C)$.

$$\begin{aligned} \mathcal{D}(\text{Int}) &= \{ \text{int, zero} \} \\ \mathcal{D}(\text{Bool}) &= \{ \text{true, false} \} \\ \mathcal{D}(C) &= \{ \text{Int} \times \mathbb{Z}, \text{Int} \times \mathbb{Z}, \dots \} \\ \mathcal{D}(D) &= \{ \text{Int} \times \text{Bool}, \text{Int} \times \text{Bool}, \dots \} \\ \mathcal{D}(C_1) &= \mathcal{D}(C_2) = \mathbb{Z} \\ \mathcal{D}(D_1) &= \mathcal{D}(D_2) = \mathbb{Z} \times \text{Bool} \end{aligned}$$

System State

Definition: Let \mathcal{S} be a structure, $\sigma = (\mathcal{D}, \tau, \text{arr}, p, \text{init})$.
A system state of \mathcal{S} w.r.t. \mathcal{S} is a **pre-consistent mapping**

$$\sigma: \mathcal{D}(C) \rightarrow V \cup \{\emptyset\} \cup \mathcal{D}(C)$$

That is, for each $u \in \mathcal{D}(C), C \in \mathcal{S}$, if $u \in \text{dom}(\sigma)$

- $\text{dom}(\sigma|u) = \text{arr}(C)$
- $(\tau(u)|v) \in \mathcal{D}(v)$ if $v: \tau \in \mathcal{S}$
- $(\tau(u)|v) \in \mathcal{D}(D)$ if $v: D_1, \sigma|v: D$, with $D \in \mathcal{S}$

We call $u \in \mathcal{D}(C)$ **live** in σ if and only if $u \in \text{dom}(\sigma)$.

We use \mathcal{S}^σ to denote the set of all system states of \mathcal{S} w.r.t. \mathcal{S} .

Handwritten notes: object identifiers, operations of basic object identifiers, partial function

System State Examples

$$\mathcal{S}_0 = (\text{Int, Bool}), \{C, D\}, \{x: \text{Int}, p: \text{Co}, n: C, \}, \{C \rightarrow \text{Int}, D \rightarrow \text{Int}, x\}, \\ \{f: \text{Int} \rightarrow \text{Bool}, \text{get}_x: \text{Int}, \{C \rightarrow \text{Int}, D \rightarrow \{f, \text{get}_x\}\}\}$$

$\mathcal{D}(\text{Int}) = \{ \text{int} \}$

$$\mathcal{D}(\text{Bool}) = \{ \text{true}, \text{false} \}$$

$$\mathcal{D}(C) = \{ \text{Int} \times \mathbb{Z}, \text{Int} \times \mathbb{Z}, \dots \}$$

$$\mathcal{D}(D) = \{ \text{Int} \times \text{Bool}, \text{Int} \times \text{Bool}, \dots \}$$

A system state is a partial function $\sigma: \mathcal{D}(C) \rightarrow V \cup \{\emptyset\} \cup \mathcal{D}(C)$ such that

- $\text{dom}(\sigma|u) = \text{arr}(C)$
- $(\tau(u)|v) \in \mathcal{D}(v)$ if $v: \tau \in \mathcal{S}$
- $(\tau(u)|v) \in \mathcal{D}(D)$ if $v: D_1, \sigma|v: D$, with $D \in \mathcal{S}$.

$$\sigma_1 = \{ \text{int} \times \mathbb{Z} \rightarrow \text{Int}, \text{int} \times \mathbb{Z} \rightarrow \text{Int} \}$$

$$\sigma_2 = \emptyset$$

$$\sigma_3 = \{ \text{Int} \times \mathbb{Z} \rightarrow \text{Int}, \text{Int} \times \mathbb{Z} \rightarrow \text{Int} \}$$

Content

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- Object Diagrams
 - concrete syntax
 - diagram references
 - partial vs. complete
 - object diagrams at work
- Proto-OCL
 - approx semantics
 - Proto-OCL vs. OCL
 - Putting it All Together
 - Proto-OCL vs. Software

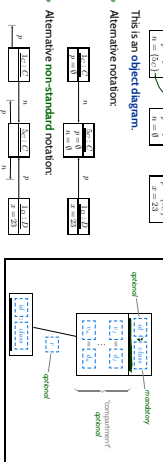
Object Diagrams

Object Diagrams

$$\mathcal{S}_0 = (\text{Int, Bool}), \{C, D\}, \{x: \text{Int}, p: \text{Co}, n: C, \}, \{C \rightarrow \text{Int}, D \rightarrow \text{Int}, x\}, \\ \{f: \text{Int} \rightarrow \text{Bool}, \text{get}_x: \text{Int}, \{C \rightarrow \text{Int}, D \rightarrow \{f, \text{get}_x\}\}\}$$

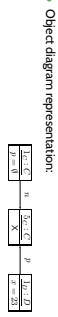
$\sigma = \{ \text{int} \times \mathbb{Z} \rightarrow \text{Int}, \text{int} \times \mathbb{Z} \rightarrow \text{Int}, \text{Int} \times \text{Bool} \rightarrow \text{Int}, \text{Int} \times \text{Bool} \rightarrow \text{Int} \}$

We may represent σ graphically as follows:



Definition.
 Let $\sigma \in \Sigma_{\mathcal{C}}^{\mathcal{D}}$ be a system state and $n \in \text{dom}(\sigma)$ an alive object of class C in σ .
 We say $r \in \text{arr}(C)$ is a **dangling reference** in σ if and only if
 $r \in C_{\text{in}}$ or $r \in C_{\text{out}}$ and it refers to a non-alive object via σ , i.e.
 $(\sigma(n))_r \notin \text{dom}(\sigma)$

Example:
 $\sigma = \{1_C \mapsto \{p \mapsto \emptyset, n \mapsto \{x_C\}\}, 1_D \mapsto \{p \mapsto \{x_C\}, x \mapsto 2D\}\}$



By now we discussed "object diagram represents system state".
 $\{1_C \mapsto \{p \mapsto \emptyset, n \mapsto \{x_C\}\}, 1_D \mapsto \{p \mapsto \{x_C\}, x \mapsto 2D\}\}$

What about the other way round...?



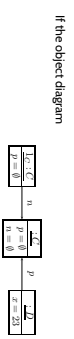
we may omit information.

Is the following object diagram **partial** or **complete**?

If an object diagram
 • has values for all attributes of all objects in the diagram, and
 • if we say that it's meant to be complete
 then we can uniquely reconstruct a system state σ .

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Object Diagrams at Work

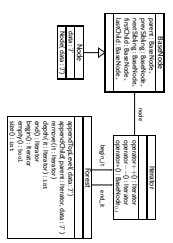


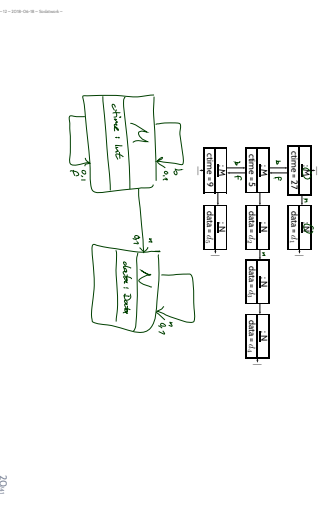
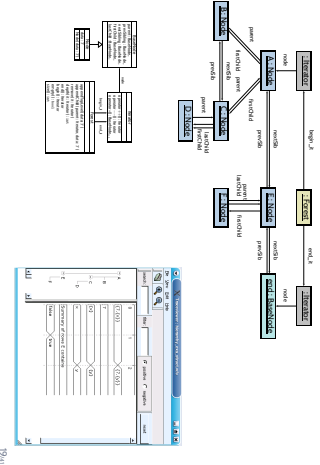
is considered as **complete**, then it denotes the set of all system states

$$\{1_C \mapsto \{p \mapsto \emptyset, n \mapsto \{c\}\}, c \mapsto \{p \mapsto \emptyset, n \mapsto \emptyset\}, d \mapsto \{p \mapsto \{c\}, x \mapsto 2D\}\}$$

where $c \in \mathcal{D}(C)$, $d \in \mathcal{D}(D)$, $c \neq 1_C$.

Intuition: different boxes represent different objects.

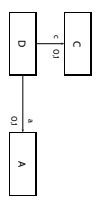




- Class Diagrams
 - semantics: system states.
- Object Diagrams
 - concrete syntax.
 - diagram references.
 - partial vs. complete.
 - object diagrams framework.
- Proto-OCL
 - syntax, semantics.
 - Proto-OCL vs OCL.
 - Putting it all together.
 - Proto-OCL vs. SMT solver.

Towards Object Constraint Logic (OCL) — "Proto-OCL" —

Motivation



- How do I precisely, formally tell my developers that **every** **instance** has a link to the same C object?
 - That is, the following system state is **forbidden** in the software.
- Note formally, it is a proper system state
- Use (Proto-)OCL: "Dear developers, please only use system states which satisfy"
 - $\forall A, E \in \text{instances}(O) \bullet \forall A_2, E \in \text{instances}(O) \bullet c(A_1) = c(A_2) \implies a(A_1) = a(A_2)$

Constraints on System States

- Example for all C-Instances, x should never have the value 27: $\forall (C, 27)$
- Proto-OCL Syntax wrt signature $(\mathcal{F}, \mathcal{F}_1, \text{dir}, \mathcal{F}, \text{init}, \mathcal{F}, \text{init}), c, r$ is a logical variable, $C \in \mathcal{C}$:
 - $F ::= c$
 - $\text{instances}(C) : \mathcal{F}^C$
 - $c(C) : \mathcal{F}_1$
 - $r(C) : \mathcal{F}$
 - $f(F_1, \dots, F_n) : \mathcal{F}_1 \times \dots \times \mathcal{F}_n \rightarrow \mathcal{F}$
 - $\forall A, E \in \mathcal{F}_1 \bullet f(A, E) : \mathcal{F} \times \mathcal{F}^C \times \mathcal{B}_1 \rightarrow \mathcal{B}_2$
- The formula above in prefix normal form: $\forall C \in \text{instances}(C) \bullet \forall (c(C), 27)$



Semantics

- **Prop-OCL type**: $\{ \perp, \top \}$, $\neg \perp = \top$, $\neg \top = \perp$, $\perp \vee \perp = \perp$, $\perp \vee \top = \top$, $\top \vee \perp = \top$, $\top \vee \top = \top$
- $\neg \perp = \top$, $\neg \top = \perp$, $\perp \wedge \perp = \perp$, $\perp \wedge \top = \perp$, $\top \wedge \perp = \perp$, $\top \wedge \top = \top$
- **Functions**:
 - We assume f is given for each function symbol f (\rightarrow is a binary)
- **Prop-OCL Semantics (interpretation function)**:
 - $\mathcal{I}[\perp](\alpha, \beta) = \beta \wedge \alpha$, assuming β is a type-consistent value of the logical variable.
 - $\mathcal{I}[\text{and}](\alpha, \beta) = \beta \wedge \alpha$
 - $\mathcal{I}[\text{or}](\alpha, \beta) = \beta \vee \alpha$
 - $\mathcal{I}[\text{not}](\alpha, \beta) = \neg \beta$
 - $\mathcal{I}[\text{if}](\alpha, \beta) = \begin{cases} \beta & \text{if } \alpha = \top \\ \perp & \text{otherwise} \end{cases}$
 - $\mathcal{I}[\text{if not}](\alpha, \beta) = \begin{cases} \perp & \text{if } \alpha = \top \\ \beta & \text{otherwise} \end{cases}$
 - $\mathcal{I}[\text{if } \perp](\alpha, \beta) = \begin{cases} \beta & \text{if } \alpha = \perp \\ \perp & \text{otherwise} \end{cases}$
 - $\mathcal{I}[\text{if } \top](\alpha, \beta) = \begin{cases} \beta & \text{if } \alpha = \top \\ \perp & \text{otherwise} \end{cases}$

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Semantics Cont'd

- **Prop-OCL is a three-valued logic**: a formula evaluates to true, false, or \perp .
- **Example**: $\neg(\perp \vee \top) = (\text{true}, \text{false}, \perp) \times (\text{true}, \text{false}, \perp) = (\text{true}, \text{false}, \perp)$ defined as follows:

\perp	\perp	\top
\perp	\perp	\perp
\top	\perp	\perp
\top	\perp	\perp
- We assume common logical connectives $\neg, \wedge, \vee, \dots$ with canonical 3-valued interpretation.
 - **Example**: $\neg(\perp \vee \top) = (\text{true}, \text{false}, \perp) \times (\text{true}, \text{false}, \perp) = (\text{true}, \text{false}, \perp)$

\perp	\perp	\top
\perp	\perp	\perp
\top	\perp	\perp
\top	\perp	\perp
- We assume common arithmetic operators $+, \dots$
 - and relation symbols $>, <, \leq, \dots$ with monoidal 3-valued interpretation.
 - And we assume the special unary function symbol isUndefined :
 - $\text{isUndefined}(x) = \begin{cases} \text{true} & \text{if } x = \perp \\ \text{false} & \text{otherwise} \end{cases}$
 - isUndefined is definite in new yields \perp .

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Example: Evaluate Formula for System State

- **Recall prefix notation**: $\forall \alpha \in \text{addressSpace} \bullet \#f(\alpha)(\alpha, \beta)$
- **Note**: β is a binary function symbol, β is a 0-ary function symbol.

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Example: Evaluate Formula for System State

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- **Example**:
 - $\mathcal{I}[\forall \alpha \in \text{addressSpace} \bullet \#f(\alpha)(\alpha, \beta)](\alpha, \beta) = \text{true}$, because...
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Example: Evaluate Formula for System State



$\forall c \in \text{address}(c) \bullet \alpha(c) \neq 2^7$

- Recall predicate notation $\forall c \in \text{address}(c) \bullet \alpha(c) \in \{0, 1\}$

Note: β is a binary function symbol, 2^7 is a 32-bit function symbol.

Example:

$\exists \gamma \in \text{address}(c) \bullet \alpha(\gamma) \in \{0, 2^7\} \wedge \beta(\gamma) = \text{true}$, because...

$$\begin{aligned} & \exists \gamma \in \text{address}(c) \bullet \alpha(\gamma) \in \{0, 2^7\} \wedge \beta(\gamma) = \text{true} \\ & \iff \exists \gamma \in \{0, 2^7\} \bullet \alpha(\gamma) \in \{0, 2^7\} \wedge \beta(\gamma) = \text{true} \\ & \iff \exists \gamma \in \{0, 2^7\} \bullet \alpha(\gamma) \in \{0, 2^7\} \wedge \beta(\gamma) = \text{true} \\ & \iff \exists \gamma \in \{0, 2^7\} \bullet \alpha(\gamma) \in \{0, 2^7\} \wedge \beta(\gamma) = \text{true} \\ & \iff \exists \gamma \in \{0, 2^7\} \bullet \alpha(\gamma) \in \{0, 2^7\} \wedge \beta(\gamma) = \text{true} \end{aligned}$$

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More Interesting Example



$\forall c \in \text{address}(c) \bullet \alpha(c) \neq 2^7$

- Similar to the previous slide, we need the value of $Z[\alpha(c)]$ for $\beta = \{c \mapsto 1, c\}$

$Z[\alpha(c)] = \beta(c) = 1$

- $Z[\alpha(c)] = \beta(c) = 1$ since $\alpha(c) \in \{0, 2^7\} \wedge \beta(c) = 1$ by rule

$$Z[\alpha(c)] = \begin{cases} 1 & \text{if } \alpha(c) \in \{0, 2^7\} \wedge \beta(c) = 1 \\ 0 & \text{otherwise} \end{cases}$$

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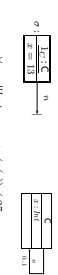
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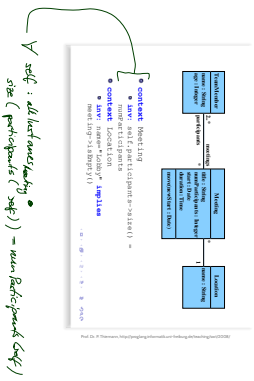


$\forall c \in \text{address}(c) \bullet \alpha(c) \neq 2^7$

- OCL is the same — just with less readable (?) syntax.

Literature (DMG, 2006; Warner and Kopp, 1999).

Object Constraint Language (OCL)



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Putting It All Together

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- Note: A UML note is a diagram element of the form
- *Text* can partially be **everything**, in particular comments and constraints.
- Sometimes, content is explicitly classified for clarity.
- Conventions



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Definition: Software is a finite description S of a possibly infinite set $\{S\}$ of finite or infinite sets $S_1, S_2, \dots \in \mathcal{R}$, the cardinalities for elements s_i being and $n_i \in \mathbb{N}$. $A, A_i \in \mathcal{R}$, is called **union** for event. The (possibly partial) function $[\] : S \rightarrow \{S\}$ is called the **representation** of S .

- The set of states S could be the set of system states as defined by a class diagram, e.g.
- A corresponding **computation path** of a software S could be
- If a requirement is formalised by the Proto-OCL constraint $F = \forall e \in \text{allInstances}(C) \bullet \#(e) < 4$ then S **does not** satisfy the requirement.

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- Let \mathcal{S} be an object system signature and \mathcal{P} a structure
- Let S be a software with
 - states $S \subseteq S_{\mathcal{S}}^{\mathcal{P}}$ and
 - computation paths $[S]$
- Let F be a Proto-OCL constraint over \mathcal{S} .
- We say $[S]$ **satisfies** F , denoted by $[S] \models F$, if and only if for all $\alpha_0 \xrightarrow{\alpha_1} \alpha_1 \xrightarrow{\alpha_2} \alpha_2 \dots \alpha_n \in [S]$ and all $i \in \mathbb{N}_0$,

$$\mathcal{I}[F](\alpha_i, \theta) = \text{true}$$
- We say $[S]$ **does not satisfy** F , denoted by $[S] \not\models F$, if and only if there exists $\alpha_0 \xrightarrow{\alpha_1} \alpha_1 \xrightarrow{\alpha_2} \alpha_2 \dots \alpha_n \in [S]$ and $i \in \mathbb{N}_0$ such that $\mathcal{I}[F](\alpha_i, \theta) = \text{false}$.
- Note $\neg([S] \models F)$ does not imply $[S] \models \neg F$.

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- Class Diagram can be used to **graphically**
 - visualize code.
 - define an object system structure \mathcal{S} .
- An Object System Structure \mathcal{S} (together with a structure \mathcal{P})
 - defines a set of system states $S_{\mathcal{S}}^{\mathcal{P}}$.
 - can be **visualized** by an object diagram.
- A System State $\sigma \in S_{\mathcal{S}}^{\mathcal{P}}$
 - can be **visualized** by an object diagram.
- Proto-OCL constraints can be evaluated on system states.
- A software over $S_{\mathcal{S}}^{\mathcal{P}}$ satisfies a Proto-OCL constraint F if and only if F evaluates to **true** on every system state of all the software computation paths.

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References

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