

# Software Design, Modelling and Analysis in UML

## Lecture 02: Semantical Model

2012-10-24

Prof. Dr. Andreas Poddick, Dr. Bernd Westphal  
Albert-Ludwigs-Universität Freiburg, Germany

### Contents & Goals

#### Last Lecture:

- Motivation: model-based development of things (houses, software) to cope with complexity, detect errors early
- Model-based (or -driven) Software Engineering
- UML Mode of the Lecture: Blueprint.

#### This Lecture:

- **Educational Objectives:** Capabilities for these tasks/questions:
  - Why is UML of the form it is?
  - Shall one feel bad if not using all diagrams during software development?
  - What is a signature, an object, a system state, etc.?
  - What is the purpose of signature, object, etc. in the course?
  - How do Basic Object System Signatures relate to UML class diagrams?
- **Content:**
  - Brief history of UML
  - Course map revisited
  - Basic Object System Signature, Structure, and System State

2/12

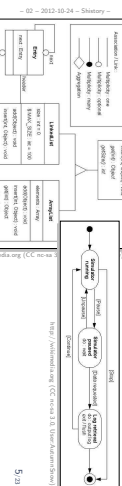
### Why (of all things) UML?

- Note: being a **modelling** languages doesn't mean being graphical (or: being a visual formalism [Harel])
- For instance, [Kastens and Blinng, 2008] also name:
  - Sets, Relations, Functions
  - Terms and Algebras
  - Propositional and Predicate Logic
  - Graphs
  - XML Schema, Entity Relation Diagrams, UML Class Diagrams
  - Finite Automata, Petri Nets, UML State Machines
- **Pro:** visual formalisms are found appealing and easier to **grasp**. Yet they are not necessarily easier to **write!**
- **Beware:** you may meet people who dislike visual formalisms just for being graphical — maybe because it is easier to “trick” people with a meaningless picture than with a meaningless formula. More serious: it's maybe easier to misunderstand a picture than a formula.

4/12

### A Brief History of UML

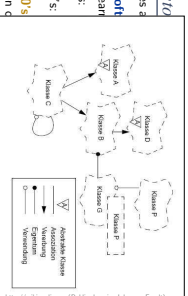
- Boxes/lines and finite automata are used to visualise software for **rges**.
- **1970's, Software Crisis**™
  - Idea: learn from engineering disciplines to handle growing complexity.
  - Languages: Flowcharts, Nassi-Shneiderman, Entity-Relation Diagrams
- Mid **1980's, Statecharts** [Harel, 1987], **StateMare**™ [Harel et al., 1990]
  - Inflation of notations and methods, most prominent:
    - **Early 1990's, advent of Object-Oriented-Analysis/Design/Programming**
      - Inflation of notations and methods, most prominent:
        - **Object-Modeling Technique (OMT)** [Rumbaugh et al., 1990]



5/12

### Why (of all things) UML?

- Boxes/lines and finite automata are used to visualise software for **rges**.
- **1970's, Software Crisis**™
  - Idea: learn from engineering disciplines to handle growing complexity.
  - Languages: Flowcharts, Nassi-Shneiderman, Entity-Relation Diagrams
- Mid **1980's, Statecharts** [Harel, 1987], **StateMare**™ [Harel et al., 1990]
  - Inflation of notations and methods, most prominent:
    - **Early 1990's, advent of Object-Oriented-Analysis/Design/Programming**
      - Inflation of notations and methods, most prominent:
        - **Object-Modeling Technique (OMT)** [Rumbaugh et al., 1990]
        - **Booch Method and Notation** [Booch, 1993]



5/12

- Boxes/lines and finite automata are used to visualise software for ages.
- **1970's, Software Crisis**™
  - Idea: learn from engineering disciplines to handle growing complexity
  - Languages: Flowcharts, Nassi-Shneiderman, Entity-Relation Diagrams
- **Mid 1980's, Statecharts** [Harel, 1987], **StateMate**™ [Harel et al., 1990]
- **Early 1990's, advent of Object-Oriented-Analysis/Design/Programming**
  - Inflation of notations and methods, most prominent:
    - **Object-Modeling Technique (OMT)** [Rumbaugh et al., 1990]
    - **Booch Method and Notation** [Booch, 1993]
    - **Object-Oriented Software Engineering (OOSE)** [Jacobson et al., 1992]
- Each "persuasion" selling books, tools, seminars...
- **Late 1990's**: joint effort **UML 0.x, 1.x**
- Standards published by **Object Management Group (OMG)**, "international, open membership, not-for-profit computer industry consortium" .
- Since **2005: UML 2.x**

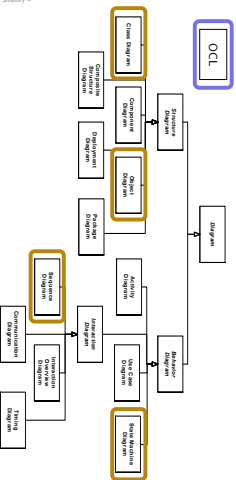


Figure A.5 - The taxonomy of structure and behavior diagrams

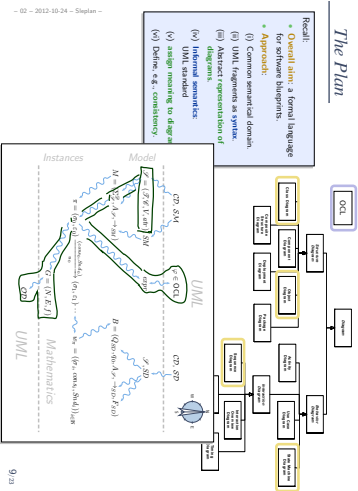
[Doherty and Parsons, 2006]

- Easily writable, readable even by customers
- Powerful enough to bridge the gap between idea and implementation
- Means to tame complexity by separation of concerns ("views")
- Unambiguous
- Standardised, exchangeable between modelling tools
- UML standard says how to develop software
- Using UML leads to better software
- ...

## We will see...

Seriously: After the course, you should have an own opinion on each of these claims. In how far/in what sense does it hold? Why? Why not? How can it be achieved? Which ones are really only hopes and expectations? ... ?

## Course Map Revisited



## UML: Semantic Areas

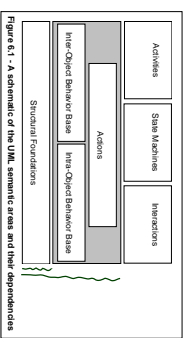


Figure 6.1 - A schematic of the UML semantic areas and their dependencies [OMG, 2007b, 11]

## Common Semantical Domain

## Basic Object System Signature

Definition: A (Basic) Object System Signature is a quadruple  $\mathcal{S} = (\mathcal{T}, \mathcal{C}, V, attr)$  where

- $\mathcal{T}$  is a set of (basic) types,
- $\mathcal{C}$  is a finite set of classes,
- $V$  is a finite set of typed attributes: i.e. each  $v \in V$  has type  $\tau \in \mathcal{T}$  or  $C_{0,1}$  or  $C_n$ , where  $C \in \mathcal{C}$ .
- $attr : \mathcal{C} \rightarrow 2^V$  maps each class to its set of attributes.

*Handwritten notes:*  $\mathcal{T} \subseteq \mathcal{C}$  (types are also classes),  $\mathcal{C} \subseteq \mathcal{C}$  (classes are also classes),  $\mathcal{C}_{0,1}$  is a type,  $\mathcal{C}_n$  is a type,  $\mathcal{C}_{0,1}$  is a class,  $\mathcal{C}_n$  is a class,  $\mathcal{C}_{0,1}$  is a class,  $\mathcal{C}_n$  is a class,  $\mathcal{C}_{0,1}$  is a class,  $\mathcal{C}_n$  is a class.

Note: Inspired by OCL 2.0 standard [OMG, 2006], Annex A.

## Basic Object System Signature Another Example

$\mathcal{S} = (\mathcal{T}, \mathcal{C}, V, attr)$  where

- (basic) types  $\mathcal{T}$  and classes  $\mathcal{C}$ , (both finite),
- typed attributes  $V$ ,  $\tau$  from  $\mathcal{T}$  or  $C_{0,1}$  or  $C_n$ ,  $C \in \mathcal{C}$ ,
- $attr : \mathcal{C} \rightarrow 2^V$  mapping classes to attributes.

## Basic Object System Structure

Definition: A Basic Object System Structure of  $\mathcal{S} = (\mathcal{T}, \mathcal{C}, V, attr)$  is a domain function  $\mathcal{D}$  which assigns to each type a domain, i.e.

- $\tau \in \mathcal{T}$  is mapped to  $\mathcal{D}(\tau)$ ,
- $C \in \mathcal{C}$  is mapped to an infinite set  $\mathcal{D}(C)$  of (object) identities.

Note: Object identities only have the "=" operation; object identities of different classes are disjoint, i.e.  $V, C, D \in \mathcal{C} : C \neq D \rightarrow \mathcal{D}(C) \cap \mathcal{D}(D) = \emptyset$ .

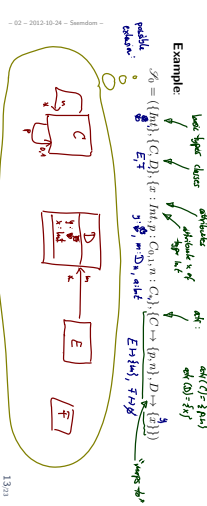
We use  $\mathcal{D}(\mathcal{C})$  to denote  $\bigcup_{C \in \mathcal{C}} \mathcal{D}(C)$ ; analogously  $\mathcal{D}(\mathcal{C}_n)$ .

Note: We identify objects and object identities, because both uniquely determine each other (cf. OCL 2.0 standard).

## Basic Object System Signature Example

$\mathcal{S} = (\mathcal{T}, \mathcal{C}, V, attr)$  where

- (basic) types  $\mathcal{T}$  and classes  $\mathcal{C}$ , (both finite),
- typed attributes  $V$ ,  $\tau$  from  $\mathcal{T}$  or  $C_{0,1}$  or  $C_n$ ,  $C \in \mathcal{C}$ ,
- $attr : \mathcal{C} \rightarrow 2^V$  mapping classes to attributes.

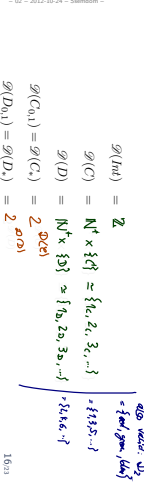


## Basic Object System Signature Example

Wanted: a structure for signature  $\mathcal{S} = (\{Int\}, \{C, D\}, \{a : Int, p : C_{0,1}, m : C_2\}, \{C \mapsto \{p, m\}, D \mapsto \{a\}\})$

Recall: by definition, seek a  $\mathcal{D}$  which maps

- $\tau \in \mathcal{T}$  to some  $\mathcal{D}(\tau)$ ,
- $C \in \mathcal{C}$  to some identities  $\mathcal{D}(C)$  (infinite, disjoint for different classes),
- $C_n$  and  $C_{0,1}$  for  $C \in \mathcal{C}$  to  $\mathcal{D}(C_n) = \mathcal{D}(C)$ .



System State

$\sigma : \mathcal{D}(\mathcal{F}) \rightarrow (V \rightarrow (\mathcal{D}(\mathcal{F}) \cup \mathcal{D}(\mathcal{G}_2)))$   
 $\sigma : \mathcal{D}(\mathcal{F}) \rightarrow (V \rightarrow (\mathcal{D}(\mathcal{F}) \cup \mathcal{D}(\mathcal{G}_2)))$   
 $\sigma : \mathcal{D}(\mathcal{F}) \rightarrow (V \rightarrow (\mathcal{D}(\mathcal{F}) \cup \mathcal{D}(\mathcal{G}_2)))$

Definition. Let  $\mathcal{D}$  be a structure of  $\mathcal{F} = \langle \mathcal{D}, \mathcal{F}, \text{dnt} \rangle$ .  
 A system state of  $\mathcal{F}$  wrt.  $\mathcal{D}$  is a **type-consistent** mapping  
 $\sigma : \mathcal{D}(\mathcal{F}) \rightarrow (V \rightarrow (\mathcal{D}(\mathcal{F}) \cup \mathcal{D}(\mathcal{G}_2)))$ .  
 That is, for each  $u \in \mathcal{D}(C)$ ,  $C \in \mathcal{F}$ , if  $u \in \text{dom}(\sigma)$

We call  $u \in \mathcal{D}(C)$  alive in  $\sigma$  if and only if  $u \in \text{dom}(\sigma)$ .  
 We use  $\mathcal{S}_{\mathcal{D}}$  to denote the set of all system states of  $\mathcal{F}$  wrt.  $\mathcal{D}$ .

System State Example

**Signature, Structure:**  
 $\mathcal{F} = (\{lm\}, \{C, D\}, \{e : \text{int}, p : \text{char}, n : C, l : C \rightarrow \{0, n\}, D \rightarrow \{x\}\})$   
 $\mathcal{D}(lm) = \mathbb{Z}$ ,  $\mathcal{D}(C) = \{1, c, 2a, 3b, \dots\}$ ,  $\mathcal{D}(D) = \{1b, 2b, 3b, \dots\}$

**Wanted:**  $\sigma : \mathcal{D}(\mathcal{F}) \rightarrow (V \rightarrow (\mathcal{D}(\mathcal{F}) \cup \mathcal{D}(\mathcal{G}_2)))$  such that  
 $\bullet \text{dom}(\sigma(u)) = \text{dnt}(C)$   
 $\bullet \sigma(u)(v) \in \mathcal{D}(C)$  if  $v : D$ , with  $D \in \mathcal{F}$ .

$\sigma_1 = \{ (c \mapsto \{1, 1, 1\}, n \mapsto \{5, 6, 6\}), 0, 0 \}$   
 $\sigma_2 = \{ (c \mapsto \{1, 1, -1\}, n \mapsto \{5, 6, 6\}), 0, 0 \}$   
 $\sigma_3 = \{ (c \mapsto \{1, 1, 1\}, n \mapsto \{5, 6, 6\}), 0, 0 \}$   
 $\sigma_4 = \{ (c \mapsto \{1, 1, 1\}, n \mapsto \{5, 6, 6\}), 0, 0 \}$   
 $\sigma_5 = \{ (c \mapsto \{1, 1, 1\}, n \mapsto \{5, 6, 6\}), 0, 0 \}$

Alternative: symbolic system state  
 $\sigma = \{ c_1 \mapsto \{p \mapsto 0, n \mapsto \{c_2\}, c_2 \mapsto \{p \mapsto 0, n \mapsto \theta\}, d \mapsto \{x \mapsto 23\}\}$   
 assuming  $c_1, c_2 \in \mathcal{D}(C)$ ,  $d \in \mathcal{D}(D)$ ,  $c_1 \neq c_2$

System State Example

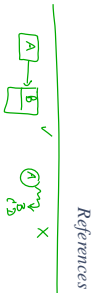
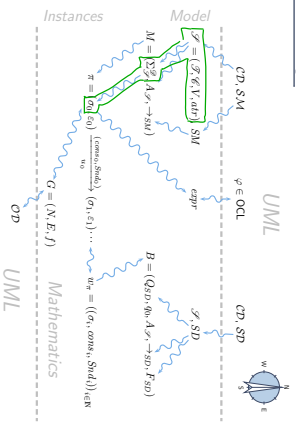
**Signature, Structure:**  
 $\mathcal{F} = (\{lm\}, \{C, D\}, \{e : \text{int}, p : \text{char}, n : C, l : C \rightarrow \{0, n\}, D \rightarrow \{x\}\})$   
 $\mathcal{D}(lm) = \mathbb{Z}$ ,  $\mathcal{D}(C) = \{1c, 2c, 3c, \dots\}$ ,  $\mathcal{D}(D) = \{1b, 2b, 3b, \dots\}$

**Wanted:**  $\sigma : \mathcal{D}(\mathcal{F}) \rightarrow (V \rightarrow (\mathcal{D}(\mathcal{F}) \cup \mathcal{D}(\mathcal{G}_2)))$  such that  
 $\bullet \text{dom}(\sigma(u)) = \text{dnt}(C)$   
 $\bullet \sigma(u)(v) \in \mathcal{D}(C)$  if  $v : \tau, \tau \in \mathcal{F}$ .

**Concrete, explicit:**  
 $\sigma = \{1c \mapsto \{p \mapsto 0, n \mapsto \{3c\}, 3c \mapsto \{p \mapsto 0, n \mapsto \theta\}, 1b \mapsto \{x \mapsto 23\}\}$   
**Alternative: symbolic system state**  
 $\sigma = \{c_1 \mapsto \{p \mapsto 0, n \mapsto \{c_2\}, c_2 \mapsto \{p \mapsto 0, n \mapsto \theta\}, d \mapsto \{x \mapsto 23\}\}$   
 assuming  $c_1, c_2 \in \mathcal{D}(C)$ ,  $d \in \mathcal{D}(D)$ ,  $c_1 \neq c_2$

You Are Here

Course Map



## References

- [Booch, 1993] Booch, G. (1993). *Object-oriented Analysis and Design with Applications*. Prentice-Hall.
- [Dohring and Parsons, 2006] Dohring, B. and Parsons, J. (2006). How UML is used. *Communications of the ACM*, 49(3):109–116.
- [Harel, 1987] Harel, D. (1987). Statecharts: A visual formalism for complex systems. *Science of Computer Programming*, 3(3):231–264.
- [Harel et al., 1999] Harel, D., Leshper, H. et al. (1999). Statecharts: A working environment for the development of complex reactive systems. *IEEE Transactions on Software Engineering*, 16(4):403–414.
- [Jacobson et al., 1992] Jacobson, I., Christerson, M., and Jonsson, P. (1992). *Object-Oriented Software Engineering - A Use Case Driven Approach*. Addison-Wesley.
- [Kastens and Bittling, 2008] Kastens, U. and Bittling, H. K. (2008). *Modellierung, Grundlagen und Formale Methoden*. Carl Hanser Verlag München, 2nd edition.
- [OMG, 2006] OMG (2006). *Object Constraint Language*, version 2.0. Technical Report formal/06-06-01.
- [OMG, 2007a] OMG (2007a). *Unified modeling language Infrastructure*, version 2.1.2. Technical Report formal/07.11.04.
- [OMG, 2007b] OMG (2007b). *Unified modeling Language: Superstructure*, version 2.1.2. Technical Report formal/07.11.01.
- [Rumbaugh et al., 1990] Rumbaugh, J., Blaha, M., Premerlani, W., Eddy, F., and Lomson, W. (1990). *Object-Oriented Modeling and Design*. Prentice Hall.