Software Design, Modelling and Analysis in UML

Lecture 16: Hierarchical State Machines II

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Composite States

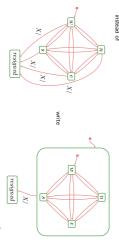
In a sense, composite states are about abbreviation, structuring, and avoiding redundancy.

and instead of F/\sqrt{fastN} Composite States

fE

write

Idea: in Tron, for the Player's Statemachine, instead of



fS

F/ F/ F/

Contents & Goals

- Last Lecture:

 Hierarchical State Machines Syntax
 Initial and Final State

- This Lecture:
- Educational Objectives: Capabilities for following tasks/questions.
 What does this State Machine mean? What happens if I inject this event?
 Can you please model the following behaviour.
 What does this literarchical State Machine mean? What may happen if I inject this event?
 What is: AND-State, OR-State, pseudo-state, entry/evit/do, final state, ...
- Composite State Semantics
 The Rest

2/44

3/44

Composite States (formalisation follows [Damm et al., 2003])

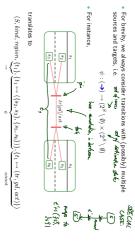
Recall: Syntax translates to 8,

 $\{top \mapsto \{\{s\}\}, s \mapsto \{\{s_1, s_1'\}, \{s_2, s_2'\}, \{s_3, s_3'\}\}, s_1 \mapsto \emptyset, s_1' \mapsto \emptyset, \ldots\},$ region $(\{(top, \mathsf{st}), (s, \mathsf{st}), (s_1, \mathsf{st})(s_1', \mathsf{st})(s_2, \mathsf{st})(s_2', \mathsf{st})(s_3, \mathsf{st})(s_3', \mathsf{st})\},$ \rightarrow , ψ , annot)



Composite States: Blessing or Curse?

Composite States: Blessing or Curse?



• Naming convention: $\psi(t) = (\underline{source}(t), \underline{target}(t))$.

7/44

SS F/ \$7 E what may happen on E?
what may happen on E, F?
can E, G kill the object? E/45 E. 9 Q E/ 50

what are legal transitions?when is a transition enabled?

what effects do transi-tions have?

Transitions:

[true]/

3

what may happen on E?
what may happen on E, F?
can E, G kill the object?

what are legal state configurations?
what is the type of the implicit & attribute?

', s₃ F/

\$6 E/

State Configuration

1-18-1-1-1

et= {se; s; op} =

- \bullet The type of st is from now on a set of states, i.e. $st:2^S$
- * A set $S_1\subseteq S$ is called (legal) state configurations if and only if * $top\in S_1$, and * for each state $s\in S_1$, for each non-empty region $\emptyset\neq R\in region(s)$, exactly one (non pseudo-state) child of s (from R) is in S_1 , i.e.
- $|\{s_0 \in R \mid kind(s_0) \in \{st, fin\}\} \cap S_1| = 1.$

S,= {s} NOT LEGAL, top missing

2

1s

(2) 1 mg

st={sqs2} No!

ste [34, 51, 2, ..., top] 4

of = {so, m, so}

Sy = { top, s, s, } LEGAL bz= Etop. s. s. n. s.s) NOT LECAL, too many diller of s 52 = { he, o} NOT LEGAL, missing will of s

9/44

State Configuration

- $\bullet\,$ The type of st is from now on a set of states, i.e. $st:2^S$
- A set $S_1 \subseteq S$ is called (legal) state configurations if and only if s $top \in S_1$, and s for each state $s \in S_1$, for each non-empty region $\emptyset \neq R \in region(s)$, exactly one (non pseudo-state) child of s (from R) is in S_1 , i.e.
- $|\{s_0 \in R \mid kind(s_0) \in \{\text{st}, \textit{fin}\}\} \cap S_1| = 1.$



53 = { 49,5,5,5,5,5} Sz={ top, s, s,, s,} NOT CEELAN, child of s for Rs Sn= {top, sn, so, so} NOT LEBAL, with of to is using

A Partial Order on States

The substate- (or child-) relation induces a partial order on states:

- $s \le s'$, for all $s' \in child(s)$, • $top \le s$, for all $s \in S$,

10/44

A Partial Order on States

The substate (or child-) relation induces a partial order on states:

• The least common ancestor is the function $lca: 2^S \setminus \{\emptyset\} \to S$ such that • The states in S_1 are (transitive) children of $lca(S_1)$, i.e. Least Common Ancestor and Ting insunot country pages

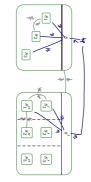
• Note: $lca(S_1)$ exists for all $S_1 \subseteq S$ (last candidate: top).

• $lca(S_1)$ is minimal, i.e. if $\hat{s} \leq s$ for all $s \in S_1$, then $\hat{s} \leq lca(S_1)$

 $lca(S_1) \le s$, for all $s \in S_1 \subseteq S$,

- $top \le s$, for all $s \in S$,
- $s \le s'$, for all $s' \in child(s)$,

 $\label{eq:state_state} \begin{tabular}{ll} \bullet & transitive, & reflexive, & antisymmetric, \\ \bullet & s' \leq s & and & s'' \leq s & implies & s' \leq s'' & or & s'' \leq s'. \\ \end{tabular}$



10/44

Least Common Ancestor and Ting

* A set of states $S_1\subseteq S$ is called consistent, denoted by $1:S_1$.

* $s\leq s'$, or

* $s'\leq s'$, or

* $s'\leq s$, or

• Two states $s_1, s_2 \in S$ are called **orthogonal**, denoted $s_1 \perp s_2$, if and only if • they are unordered, i.e. $s_1 \not \leq s_2$ and $s_2 \not \leq s_1$, and • they "live" in different regions of an AND-state, i.e.

 $\exists s, region(s) = \{S_1, \dots, S_n\} \ \exists \ 1 \leq i \neq j \leq n : s_1 \in child^*(S_i) \land s_2 \in child^*(S_j),$

S1 82 S2

12/44

\$3 \

Least Common Ancestor and Ting

(S2 /)

13/44

S₂'' S₂'.

S₃'' S₃'

11/44

Legal Transitions

A hierchical state-machine $(S,kind,region,\rightarrow,\psi,amnot)$ is called well-formed if and only if for all transitions $t\in\rightarrow$,

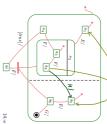
(ii) source and destination are consistent, i.e. \downarrow source(t) and \downarrow target(t). (ii) source (and destination) states are pairwise orthogonal, i.e. forall s‡s' ∈ source(t) (∈ target(t)), s ⊥ s'.

(iii) the top state is neither source nor destination, i.e.
 top ∉ source(t) ∪ source(t).

Recall: final states are not sources of transitions.

Legal Transitions

- A hiearchical state-machine $(S,kind,region,\rightarrow,\psi,annot)$ is called well-formed if and only if for all transitions $t\in\rightarrow$, (i) source and destination are consistent, i.e. ↓ source(t) and ↓ target(t),
- (ii) source (and destination) states are pairwise orthogonal, i.e.
- (iii) the top state is neither source nor destination, i.e. • forall $s \not= s' \in source(t)$ ($\in target(t)$), $s \perp s'$,
- Recall: final states are not sources of transitions. top ∉ source(t) ∪ source(t).



S₁ F/ 3 88 (g) de.

Transitions in Hierarchical State-Machines

- Let T be a set of transitions enabled in u.
- Then $(\sigma, \varepsilon) \xrightarrow{(cons, Snd)} (\sigma', \varepsilon')$ if
- $\sigma'(u)(st)$ consists of the target states of ${\it T}$,
- i.e. for simple states the simple states themselves, for composite states the initial states,
- $\sigma',\, \varepsilon', [\cos ns]$ and Snd are the effect of firing each transition $t\in T$ one by one, in any order, i.e. for each $t\in T$,
- the exit transformer of all affected states, highest depth first,
 the transformer of t,
 the entry transformer of all affected states, lowest depth first.
- \rightsquigarrow adjust (2.), (3.), (5.) accordingly.

17/44

The Depth of States

Enabledness in Hierarchical State-Machines

 \bullet The scope ("set of possibly affected states") of a transition t is the least common region of

 $source(t) \cup target(t)$.

Two transitions t₁, t₂ are called consistent if and only if their scopes are orthogonal (i.e. states in scopes pairwise orthogonal).
 The priority of transition t is the depth of its innermost source state, i.e.

 $prio(t) := \max\{depth(s) \mid s \in source(t)\}$

• A set of transitions $T \subseteq \Longrightarrow$ is enabled in an object u if and only if

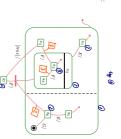
 \bullet T is maximal wrt. priority, \bullet all transitions in T share the same trigger, • all guards are satisfied by $\sigma(u)$, and • for all $t\in T$, the source states are active, i.e.

 $source(t) \subseteq \sigma(u)(st) \ (\subseteq S).$

16/44

T is consistent,

 $\label{eq:depth} \begin{array}{l} \bullet \ depth(top) = 0, \\ \\ \bullet \ depth(s') = depth(s) + 1, \ \text{for all} \ s' \in child(s) \end{array}$



15/44

Entry/Do/Exit Actions, Internal Transitions

Entry/Do/Exit Actions

• In general, with each state $s \in S$ there is associated

entry/ act_1^{entry} do/act_1^{ob} $exit/act_1^{exit}$ E_1/act_{E_1}

tr[gd]/act entry/act2016
do/act20
exit/act2017

- an entry, a do, and an exit action (default: skip)

- a possibly empty set of trigger/action pairs called internal transitions,

 E_n/act_{E_n}



- ullet Recall: each action's supposed to have a transformer. Here: $t_{act_1^{out}}, t_{act_1^{out}}, \ldots$
- Taking the transition above then amounts to applying

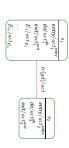
$$t_{acts_2}$$
 o t_{act} o t_{acts_1}

instead of only

18/44

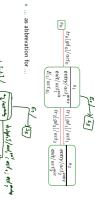
 \rightsquigarrow adjust (2.), (3.) accordingly.

Internal Transitions



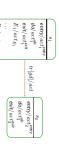
- ullet For internal transitions, taking the one for E_1 , for instance, still amounts to taking only $t_{act_{E_1}}$
- Intuition: The state is neither left nor entered, so: no exit, no entry.
- → adjust (2.) accordingly.
- Note: internal transitions also start a run-to-completion step.
- Note: the standard seems not to clarify whether internal transitions have priority over regular transitions with the same trigger at the same state. Some code generators assume that internal transitions have priority!

Alternative View: Entry/Exit/Internal as Abbreviations



21/44

Do Actions



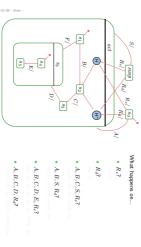
The Concept of History, and Other Pseudo-States

- Intuition: after entering a state, start its do-action
- If the do-action terminates,
- then the state is considered completed,
- otherwise,
- if the state is left before termination, the do-action is stopped.

22/44

Recall the overall UML State Machine philosophy:
 "An object is either idle or doing a run-to-completion step."
 Now, what is it exactly while the do action is executing...?

History and Deep History: By Example



23/44

Alternative View: Entry/Exit/Internal as Abbreviations



- ... as abbrevation for ...
- s_1

 s_2

 s_0

- That is: Entry/Internal/Exit don't add expressive power to Core State Machines.
 If internal actions should have priority, s₁ can be embedded into an OR-state (see later).
- Abbreviation may avoid confusion in context of hierarchical states (see later).

Junction and Choice

- Junction ("static conditional branch"):
- good: abbreviation
 unfolds to so many similar transitions with different guards, the unfolded transitions are then checked for enabledness.
- at best, start with trigger, branch into conditions, then apply actions
- Choice: ("dynamic conditional branch")

×

- enters the transition without knowing whether there's an enabled path
 at best, use "else" and convince yourself that it cannot get stuck
 maybe even better: avoid evil: may get stuck

Note: not so sure about naming and symbols, e.g., I'd guessed it was just the other way round...

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44/4

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References

25/44

Entry and Exit Point, Submachine State, Terminate

- Hierarchical states can be "folded" for readability.
 (but: this can also hinder readability.)
- $\, \bullet \,$ Can even be taken from a different state-machine for re-use. $\, \boxed{ S:s \, } \,$
- Entry/exit points
- ⊗ Provide connection points for finer integration into the current level, than just via initial state.
- Semantically a bit tricky: First the exit action of the exiting state,
- then the actions of the transition,
 then the entry actions of the entered state,

- then action of the transition from the entry point to an internal state,
 and then that internal state's entry action.

Terminate Pseudo-State
 When a terminate pseudo-state is reached, the object taking the transition is immediately killed.

26/44

References