Software Design, Modelling and Analysis in UML

Lecture 02: Semantical Model

2013-10-23

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Contents & Goals

Last Lecture:

- Motivation: model-based development of things (houses, software) to cope with complexity, detect errors early
- Model-based (or -driven) Software Engineering
- UML Mode of the Lecture: Blueprint.

This Lecture:

- Educational Objectives: Capabilities for these tasks/questions:
 - Why is UML of the form it is?
 - Shall one feel bad if not using all diagrams during software development?
 - What is a signature, an object, a system state, etc.? What's the purpose of signature, object, etc. in the course?
 - How do Basic Object System Signatures relate to UML class diagrams?

• Content:

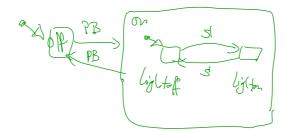
- Brief history of UML
- Course map revisited
- Basic Object System Signature, Structure, and System State

Why (of all things) UML?

- Note: being a **modelling** languages doesn't mean being graphical (or: being a visual formalism [Harel]).
- For instance, [Kastens and Büning, 2008] also name:
 - Sets, Relations, Functions
 - Terms and Algebras
 - Propositional and Predicate Logic
 - Graphs
 - XML Schema, Entity Relation Diagrams, UML Class Diagrams
 - Finite Automata, Petri Nets, UML State Machines
- **Pro**: visual formalisms are found appealing and easier to **grasp**. Yet they are not necessarily easier to **write**!
- Beware: you may meet people who dislike visual formalisms just for being graphical maybe because it is easier to "trick" people with a meaningless picture than with a meaningless formula.
 - More serious: it's maybe easier to misunderstand a picture than a formula.

A Brief History of UML

- Boxes/lines and finite automata are used to visualise software for ages.
- 1970's, Software CrisisTM
 - Idea: learn from engineering disciplines to handle growing complexity. Languages: Flowcharts, Nassi-Shneiderman, Entity-Relation Diagrams
- Mid 1980's: Statecharts [Harel, 1987], StateMateTM [Harel et al., 1990]

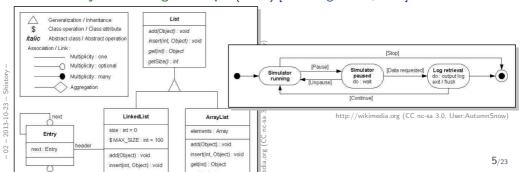


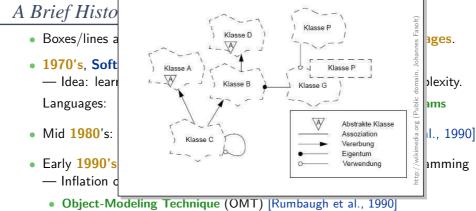
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- Early 1990's, advent of Object-Oriented-Analysis/Design/Programming
 Inflation of notations and methods, most prominent:
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- Booch Method and Notation [Booch, 1993]

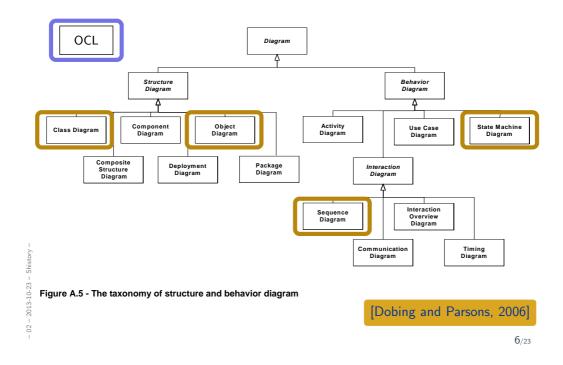
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 - Booch Method and Notation [Booch, 1993]
 - Object-Oriented Software Engineering (OOSE) [Jacobson et al., 1992]

Each "persuasion" selling books, tools, seminars...

- Late 1990's: joint effort UML 0.x, 1.x Standards published by Object Management Group (OMG), "international, open membership, not-for-profit computer industry consortium".
- Since 2005: UML 2.x

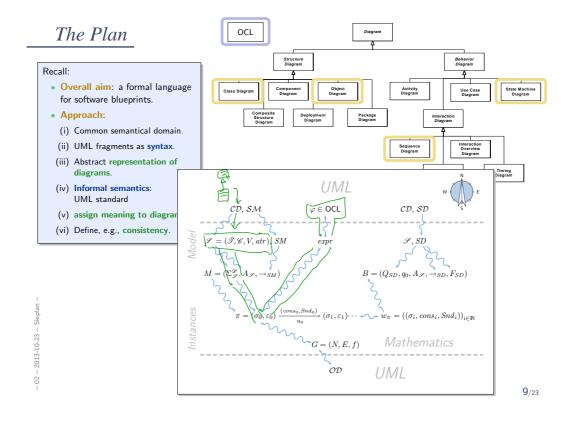


Common Expectations on UML

- Easily writeable, readable even by customers
- Powerful enough to bridge the gap between idea and implementation
- Means to tame complexity by separation of concerns ("views")
- Unambiguous
- Standardised, exchangeable between modelling tools
- UML standard says how to develop software
- Using UML leads to better software
- •

We will see...

Seriously: After the course, you should have an own opinion on each of these claims. In how far/in what sense does it hold? Why? Why not? How can it be achieved? Which ones are really only hopes and expectations? ...?

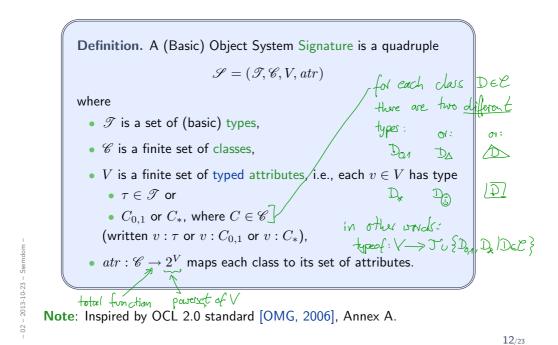


[OMG, 2007b, 11]

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Common Semantical Domain

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Basic Object System Signature Example

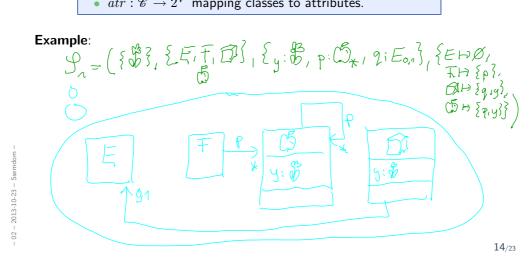
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\mathcal{S} = (\mathcal{T}, \mathcal{C}, V, atr) \text{ where}
• (basic) types \mathcal{T} and classes \mathcal{C}, (both finite),
• typed attributes V, \tau from \mathcal{T} or C_{0,1} or C_*, C \in \mathcal{C},
• atr: \mathcal{C} \to 2^V mapping classes to attributes.

\text{Example:} \quad \text{Attributes} \quad \text{Attributes}
```

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$\mathscr{S} = (\mathscr{T}, \mathscr{C}, V, atr)$ where

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- $atr: \mathscr{C} \to 2^V$ mapping classes to attributes.



Basic Object System Structure

Definition. A Basic Object System Structure of

$$\mathscr{S} = (\mathscr{T}, \mathscr{C}, V, atr)$$

is a domain function 2 which assigns to each type a domain, i.e.

- $\tau \in \mathscr{T}$ is mapped to $\mathscr{D}(\tau)$,
- $C \in \mathscr{C}$ is mapped to an infinite set $\mathscr{D}(C)$ of (object) identities. Note: Object identities only have the "=" operation; object identities of different classes are disjoint, i.e. $\forall C, D \in \mathscr{C} : C \neq D \to \mathscr{D}(C) \cap \mathscr{D}(D) = \emptyset.$
- C_* and $C_{0,1}$ for $C \in \mathscr{C}$ are mapped to $2^{\mathscr{D}(C)}$.

We use $\mathscr{D}(\mathscr{C})$ to denote $\bigcup_{C\in\mathscr{C}}\mathscr{D}(C)$; analogously $\mathscr{D}(\mathscr{C}_*).$

Note: We identify objects and object identities, because both uniquely determine each other (cf. OCL 2.0 standard).

Wanted: a structure for signature

$$\mathscr{S}_0 = (\{Int\}, \{C, D\}, \{x : Int, p : C_{0,1}, n : C_*\}, \{C \mapsto \{p, n\}, D \mapsto \{x\}\})$$

Recall: by definition, seek a \mathcal{D} which maps

- $\tau \in \mathscr{T}$ to some $\mathscr{D}(\tau)$,
- $c \in \mathscr{C}$ to some identities $\mathscr{D}(C)$ (infinite, disjoint for different classes),
- C_* and $C_{0,1}$ for $C\in\mathscr{C}$ to $\mathscr{D}(C_{0,1})=\mathscr{D}(C_*)=2^{\mathscr{D}(C)}.$

 $\mathcal{D}(Int) = \mathbb{Z}$ $\mathcal{D}(C) = \mathbb{N}^{\frac{1}{2}} \times \{C\} = \{A_{0}, A_{0}, A_{0}, A_{0}\}$ $\mathcal{D}(D) = \mathbb{N}^{\frac{1}{2}} \times \{D\} = \{A_{0}, A_{0}, A_{0}, A_{0}\}$ $\mathcal{D}(C_{0,1}) = \mathcal{D}(C_{*}) = 2^{\mathbb{N}^{\frac{1}{2}}} \times \{C\}$ $\mathcal{D}(D_{0,1}) = \mathcal{D}(D_{*}) = 2^{\mathbb{N}^{\frac{1}{2}}} \times \{C\}$

System State

all object identities partial function from

partial function V to types domains

Definition. Let \mathscr{D} be a structure of $\mathscr{S}=(\mathscr{T}\mathscr{K},V,atr).$ A system state of \mathscr{S} wrt. \mathscr{D} is a **type-consistent** mapping

$$\sigma: \widetilde{\mathscr{D}(\mathscr{C})} \not \to \underbrace{(V \nrightarrow (\mathscr{D}(\mathscr{T}) \cup \mathscr{D}(\mathscr{C}_*)))}.$$

That is, for each $u \in \mathcal{Q}(C)$, $C \in \mathcal{C}$, if $u \in \text{dom}(\sigma)$

•
$$\operatorname{dom}(\sigma(u)) = \operatorname{atr}(C)$$

$$\bullet \overline{\left(\sigma(u)\right)}\!\!\left(v\right) \in \mathscr{D}(\tau) \text{ if } v:\tau,\tau \in \mathscr{T}$$

We call $u \in \mathcal{D}(\mathscr{C})$ alive in σ if and only if $u \in \text{dom}(\sigma)$.

We use $\Sigma_{\mathscr{S}}^{\mathscr{D}}$ to denote the set of all system states of \mathscr{S} wrt. \mathscr{D} .

System State Example

Signature, Structure:

$$\mathcal{S}_0 = (\{Int\}, \{C, D\}, \{x : Int, p : C_{0,1}, n : C_*\}, \{C \mapsto \{p, n\}, D \mapsto \{x\}\})$$

$$\mathcal{D}(Int) = \mathbb{Z}, \quad \mathcal{D}(C) = \{1_C, 2_C, 3_C, \dots\}, \quad \mathcal{D}(D) = \{1_D, 2_D, 3_D, \dots\}$$

Wanted:
$$\sigma: \mathcal{D}(\mathscr{C}) \rightarrow (V \rightarrow (\mathcal{D}(\mathscr{T}) \cup \mathcal{D}(\mathscr{C}_*)))$$
 such that

• $dom(\sigma(u)) = atr(C)$,

• $\sigma(u)(v) \in \mathcal{D}(\tau)$ if $v: \tau, \tau \in \mathscr{T}$, • $\sigma(u)(v) \in \mathcal{D}(C_*)$ if $v: D_*$ with $D \in \mathscr{C}$.

• $\sigma_1 = \emptyset$ for such that

• $\sigma_2 = \{ 1_C \mapsto \{ p \mapsto \{ 1_C \}, n \mapsto \{ 5_{C_1} 6_C \} \} \}$

• $\sigma_2 = \{ 1_C \mapsto \{ p \mapsto \{ 1_C \}, n \mapsto \{ 5_{C_1} 6_C \} \} \}$

• $\sigma_3 = \{ 5 \mapsto \{ p \mapsto \{ 1_R \}, n \mapsto \emptyset \}$

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System State Example

Signature, Structure:

$$\mathcal{S}_0 = (\{Int\}, \{C, D\}, \{x : Int, p : C_{0,1}, n : C_*\}, \{C \mapsto \{p, n\}, D \mapsto \{x\}\})$$

$$\mathcal{D}(Int) = \mathbb{Z}, \quad \mathcal{D}(C) = \{1_C, 2_C, 3_C, \dots\}, \quad \mathcal{D}(D) = \{1_D, 2_D, 3_D, \dots\}$$

Wanted: $\sigma: \mathscr{D}(\mathscr{C}) \nrightarrow (V \nrightarrow (\mathscr{D}(\mathscr{T}) \cup \mathscr{D}(\mathscr{C}_*)))$ such that

- $dom(\sigma(u)) = atr(C)$,
- $\sigma(u)(v) \in \mathcal{D}(\tau)$ if $v : \tau, \tau \in \mathcal{T}$,
- $\sigma(u)(v) \in \mathscr{D}(C_*)$ if $v: D_*$ with $D \in \mathscr{C}$.
- Concrete, explicit:

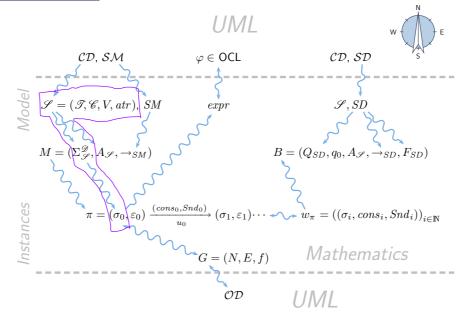
$$\sigma = \{\widehat{1_C} \mapsto \{p \mapsto \emptyset, n \mapsto \{5_C\}\}, 5_C \mapsto \{p \mapsto \emptyset, n \mapsto \emptyset\}, 1_D \mapsto \{x \mapsto 23\}\}.$$

• Alternative: symbolic system state

$$\sigma = \{ \overbrace{c_1} \mapsto \{p \mapsto \emptyset, n \mapsto \{c_2\}\}, \underbrace{c_2} \mapsto \{p \mapsto \emptyset, n \mapsto \emptyset\}, d \mapsto \{x \mapsto 23\} \}$$
 assuming $c_1, c_2 \in \mathscr{D}(C), d \in \mathscr{D}(D), c_1 \neq c_2.$

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Course Map



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