

# Software Design, Modelling and Analysis in UML

## Lecture 02: Semantical Model

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### Contents & Goals

#### Last Lecture:

- Motivation: model-based development of things (houses, software) to cope with complexity; detect errors early
- Model-based (or -driven) Software Engineering
- UML Mode of the Lecture: Blueprint.

#### This Lecture:

- **Educational Objectives:** Capabilities for these tasks/questions:
  - Why is UML of the form it is?
  - Shall one feel bad if not using all diagrams during software development?
  - What is a signature, an object, a system state, etc.?
  - What's the purpose of a signature, object, etc. in the course?
  - How do Basic Object System Signatures relate to UML class diagrams?
- **Content:**
  - Brief history of UML
  - Course map revisited
  - Basic Object System Signature, Structure, and System State

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### Why (of all things) UML?

- Note: being a **modelling** languages doesn't mean being graphical (or: being a visual formalism [Harel])
- For instance, [Kastens and Blinng, 2008] also name:
  - Sets, Relations, Functions
  - Terms and Algebras
  - Propositional and Predicate Logic
  - Graphs
  - XML Schema, Entity Relation Diagrams, UML Class Diagrams
  - Finite Automata, Petri Nets, UML State Machines
- **Pro:** visual formalisms are found appealing and easier to **grasp**. Yet they are not necessarily easier to **write!**
- **Beware:** you may meet people who dislike visual formalisms just for being graphical — maybe because it is easier to “trick” people with a meaningless picture than with a meaningless formula. More serious: it's maybe easier to misunderstand a picture than a formula.

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### A Brief History of UML

- Boxes/lines and finite automata are used to visualise software for **rges**.
- **1970's, Software Crisis**™
  - Idea: learn from engineering disciplines to handle growing complexity.
  - Languages: Flowcharts, Nassi-Shneiderman, Entity-Relation Diagrams
- Mid **1980's, Statecharts** [Harel, 1987], StateMate™ [Harel et al., 1990]

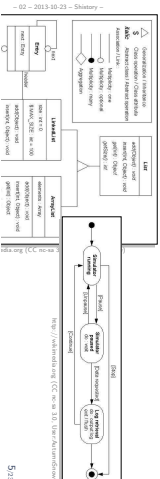


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### A Brief History of UML

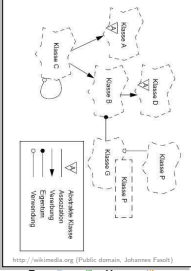
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- Early **1990's**, advent of **Object-Oriented Analysis/Design/Programming**
  - Inflation of notations and methods, most prominent:
    - Object-Modeling Technique (OMT) [Rumbaugh et al., 1990]



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## A Brief History

- Boxes/lines & arrows
- **1970's, SD**
  - Idea: learn Languages:
- **Mid 1980's**
  - Inflation & Object-Modeling Technique (OMT) [Rumbaugh et al., 1990]
  - **Booch Method and Notation** [Booch, 1993]



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  - Inflation of notations and methods, most prominent:
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    - **Booch Method and Notation** [Booch, 1993]
    - **Object-Oriented Software Engineering (OOSE)** [Jacobson et al., 1992]
- Each "persuasion" selling books, tools, seminars, ...
- **Late 1990's**: joint effort: **UML 0.x, 1.x**

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Standards published by **Object Management Group (OMG)**, "International open membership, not-for-profit computer industry consortium".

- Since **2005: UML 2.x**

## UML Overview (OMG 2003, 2004)

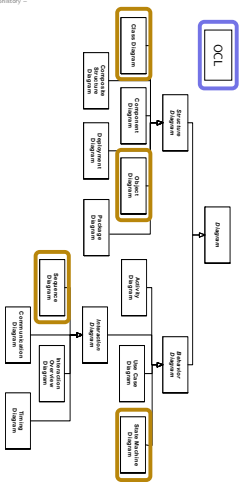


Figure A.5: The taxonomy of structure and behavior diagram

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## Common Expectations on UML

- Easily writable, readable even by customers
- Powerful enough to bridge the gap between idea and implementation
- Means to tame complexity by separation of concerns ("Views")
- Unambiguous
- Standardised, exchangeable between modelling tools
- UML standard says how to develop software
- Using UML leads to better software
- ...

## We will see...

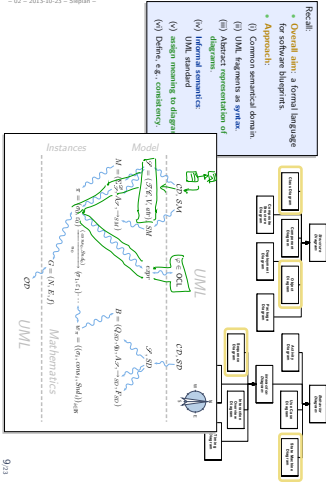
Seriously: After the course, you should have an own opinion on each of these claims. In how far/in what sense does it hold? Why? Why not? How can it be achieved? Which ones are really only hopes and expectations? ...?

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## Course Map Revisited

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## The Plan



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### Basic Object System Structure Example

**Wanted:** a structure for signature

$$\mathcal{S}_0 = (\{InI\}, \{C, D\}, \{x : InI, p : C_{0,1}, n : C_1, \{C\} \mapsto \{n, n\}, D \mapsto \{x\}\})$$

Recall: by definition, seek a  $\mathcal{D}$  which maps

- $\tau \in \mathcal{D}$  to some  $\mathcal{D}(C)$
- $c \in \mathcal{C}$  to some identities  $\mathcal{D}(C)$  (infinite, disjoint for different classes)
- $C_1$  and  $C_{0,1}$  for  $C \in \mathcal{C}$  to  $\mathcal{D}(C_{0,1}) = \mathcal{D}(C_1) = \mathcal{D}(C)$

$$\begin{aligned} \mathcal{D}(InI) &= \mathbb{Z} \\ \mathcal{D}(C) &= \mathbb{N}^+ \times \mathbb{Z} \times \mathbb{Z} = \{1, 2, 3, \dots\} \\ \mathcal{D}(D) &= \mathbb{N}^+ \times \mathbb{Z} \times \mathbb{Z} = \{1, 2, 3, \dots\} \\ \mathcal{D}(C_{0,1}) &= \mathcal{D}(C_1) = \mathcal{D}(C) = \mathbb{N}^+ \times \mathbb{Z} \\ \mathcal{D}(D_{0,1}) &= \mathcal{D}(D_1) = \mathcal{D}(D) = \mathbb{N}^+ \times \mathbb{Z} \end{aligned}$$

### System State

**Definition:** Let  $\mathcal{D}$  be a structure of  $\mathcal{S} = (\mathcal{S}, \mathcal{C}, V, \text{attr})$ . A system state of  $\mathcal{S}$  wrt.  $\mathcal{D}$  is a type-consistent mapping

$$\sigma : \mathcal{D}(\mathcal{S}) \mapsto (V \mapsto (\mathcal{D}(\mathcal{S}) \cup \mathcal{D}(\mathcal{C})))$$

That is, for each  $u \in \mathcal{D}(C)$ ,  $C \in \mathcal{C}$ , if  $u \in \text{dom}(\sigma)$

$$\text{dom}(\sigma(u)) = \text{attr}(C)$$

$$\sigma(u)(v) \in \mathcal{D}(v) \text{ if } v : \tau \in \mathcal{S}$$

$$\sigma(u)(v) \in \mathcal{D}(D_1) \text{ if } v : D_{0,1} \text{ or } v : D, \text{ with } D \in \mathcal{C}$$

We call  $u \in \mathcal{D}(\mathcal{C})$  *alive* in  $\sigma$  if and only if  $u \in \text{dom}(\sigma)$ .

We use  $\Sigma_{\mathcal{D}}^{\mathcal{S}}$  to denote the set of all system states of  $\mathcal{S}$  wrt.  $\mathcal{D}$ .

### System State Example

**Signature Structure:**

$$\begin{aligned} \mathcal{S}_0 &= (\{InI\}, \{C, D\}, \{x : InI, p : C_{0,1}, n : C_1, \{C\} \mapsto \{n, n\}, D \mapsto \{x\}\}) \\ \mathcal{D}(InI) &= \mathbb{Z}, \quad \mathcal{D}(C) = \{1, 2, 3, \dots\}, \quad \mathcal{D}(D) = \{1, 2, 3, 3n, \dots\} \end{aligned}$$

**Wanted:**  $\sigma : \mathcal{D}(\mathcal{S}) \mapsto (V \mapsto (\mathcal{D}(\mathcal{S}) \cup \mathcal{D}(\mathcal{C})))$  such that

- $\text{dom}(\sigma(u)) = \text{attr}(C)$
- $\sigma(u)(v) \in \mathcal{D}(v)$  if  $v : \tau \in \mathcal{S}$
- $\sigma(u)(v) \in \mathcal{D}(C_1)$  if  $v : D$ , with  $D \in \mathcal{C}$

**Concrete, explicit:**

$$\sigma = \{ \{1\} \mapsto \{p \mapsto 0, n \mapsto \{3\}\}, \{5\} \mapsto \{p \mapsto 0, n \mapsto \{1, 1, 1\}\} \mapsto \{x \mapsto 23\} \}$$

**Alternative: symbolic system state**

$$\sigma = \{ \{1\} \mapsto \{p \mapsto 0, n \mapsto \{c_1\}\}, \{5\} \mapsto \{p \mapsto 0, n \mapsto \{1\}, d \mapsto \{x \mapsto 23\} \} \}$$

assuming  $\{1\} \in \mathcal{D}(C)$ ,  $d \in \mathcal{D}(D)$ ,  $c_1 \neq c_2$

### System State Example

**Signature Structure:**

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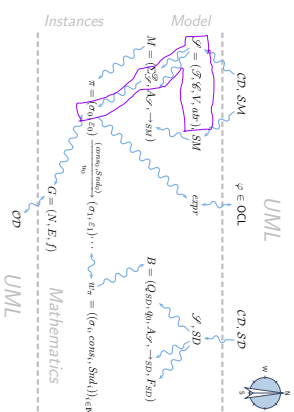
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$$\begin{aligned} \sigma_1 &= \emptyset \\ \sigma_2 &= \{1, 1, 1\} \mapsto \{p \mapsto \{1, 2, 3\}, n \mapsto \{5, 6, 3\}\} \\ &\quad \mapsto \{x \mapsto 23\} \\ \sigma_3 &= \{5\} \mapsto \{p \mapsto \{1, 1, 1\}, n \mapsto \emptyset\} \end{aligned}$$

Int. D1:   
 = object 1c refers to object 5c, 1c no state n

You Are Here.

### Course Map



## References

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