

Software Design, Modelling and Analysis in UML

Lecture 07: A Type System for Visibility

2013-11-18

Prof. Dr. Andreas Podolski, Dr. Bernd Westphal
 Albert-Ludwigs-Universität Freiburg, Germany

Contents & Goals

- Last Lecture:**
- Representing class diagrams as (extended) signatures — for the moment
 - without associations. (see Lecture 03)
 - And: in Lecture 03, implicit assumption of well-typedness of OCL expressions.

This Lecture:

- Educational Objectives: Capabilities for following tasks/questions:
 - Is this OCL expression well typed or not? Why?
 - How/in what form did we define well-typedness?
 - What is visibility good for?
- Content:
 - Recall: type theory/static type systems,
 - Well-typedness for OCL expression,
 - Visibility as a matter of well-typedness.

Recall: From Class Boxes to Extended Signatures

Extended Classes

- From now on, we assume that each class $C \in \mathcal{C}$ has:
- a finite (possibly empty) set S_C of **stereotypes**,
 - a boolean flag $a \in \{B\}$ indicating whether C is **abstract**,
 - a boolean flag $t \in \{B\}$ indicating whether C is **active**.
- We use S_C to denote the set $\bigcup_{C \in \mathcal{C}} S_C$ of stereotypes in \mathcal{C} .
 (Alternatively, we could add a set S as 5th component to \mathcal{C} to provide the stereotypes (names of stereotypes) to choose from. But: too unimportant to care.)
- Convention:**
- We write $\langle C, S_C, a, t \rangle \in \mathcal{C}$ when we want to refer to all aspects of C .
 - If the new aspects are irrelevant (for a given context), we simply write $C \in \mathcal{C}$; i.e. old definitions are still valid.

Extended Attributes

- From now on, we assume that each attribute $v \in Y$ has (in addition to the type):
- a **visibility** $\xi \in \{\text{public, private, protected, package}\}$
 - an **initial value expr.** given as a word from **language for initial values**, e.g. OCL expressions. (If using Java as **action language** (later) Java expressions would be fine.)
 - a finite (possibly empty) set of **properties** P_v . We define \mathcal{P} analogously to stereotypes.
- Convention:**
- We write $(v : \tau, \xi, \text{expr}, a, P_v) \in Y$ when we want to refer to all aspects of v .
 - Write only $v : \tau$ or v if details are irrelevant.

From Class Boxes to Extended Signatures

A class box n induces an (extended) signature class as follows:

where

- “abstract” is determined by the box: $a(n) = \begin{cases} \text{true} & \text{if } n = \boxed{C} \\ \text{false} & \text{otherwise} \end{cases}$
- “active” is determined by the frame: $t(n) = \begin{cases} \text{true} & \text{if } n = \boxed{C} \text{ or } n = \boxed{C} \\ \text{false} & \text{otherwise} \end{cases}$

A Type System for OCL

We will give a finite set of type rules (a type system) of the form

(“name”) $\frac{\text{“premises”}}{\text{“conclusion”}}$ “side condition”

These rules will establish well-typedness statements (type sentences) of three different “qualities”:

- (i) Universal well-typedness:

$$\frac{}{\vdash \text{expr} : \tau}$$

$$\vdash 1 + 2 : Int$$
- (ii) Well-typedness in a type environment A: (for logical variables)

$$\frac{A \vdash \text{expr} : \tau}{\text{self} : \tau C \vdash \text{self}.v : Int}$$
- (iii) Well-typedness in type environment A and context B: (for visibility)

$$\frac{A, B \vdash \text{expr} : \tau}{\text{self} : \tau C, C' \vdash \text{self}.r.v : Int}$$

Type Theory

Recall: In lecture 03, we introduced OCL expressions with types, for instance

```

expr ::= w | τ
       | true | false : Bool
       | 0 | -1 | 1 | ... : Int
       | expr1 + expr2 : Int × Int → Int ... operation
       | size(expr1) : Set(τ) → Int
       | not expr1 : Bool → Bool
       | size(expr1) > expr2 : Set(τ) → Bool
       | not w
       from not well-typed, such as,
       size(w)
    
```

Approach: Derivation System, that is, a finite set of derivation rules. We then say expr is well-typed if and only if we can derive

$A, C \vdash \text{expr} : \tau$ (read: “expression expr has type τ”)

for some OCL type τ, i.e. $\tau \in T_D \cup T_E \cup \{Set(\tau_0) \mid \tau_0 \in T_D \cup T_E\}, C \in \mathcal{C}$.

Constants and Operations

- If expr is a **boolean constant**, then expr is of type Bool:

$$(BOOL) \quad \frac{}{\vdash B : Bool} \quad B \in \{true, false\}$$
- If expr is an **integer constant**, then expr is of type Int:

$$(INT) \quad \frac{}{\vdash N : Int} \quad N \in \{0, 1, -1, \dots\}$$

• If expr is the application of operation $\omega : \tau_1 \times \dots \times \tau_n \rightarrow \tau$ to expressions $\text{expr}_1, \dots, \text{expr}_n$ which are of type τ_1, \dots, τ_n , then expr is of type τ:

(FunOp) $\frac{\vdash \text{expr}_1 : \tau_1 \dots \vdash \text{expr}_n : \tau_n \quad \omega : \tau_1 \times \dots \times \tau_n \rightarrow \tau}{\vdash \omega(\text{expr}_1, \dots, \text{expr}_n) : \tau} \quad n \geq 1, \omega \notin \text{def}(\mathcal{E})$

(Note: this rule also covers “=”, “≠”, “IsEmpty”, and “size”.)

A Type System for OCL

Constants and Operations Example

(BOOL)	$\frac{}{\vdash B : Bool}$	$B \in \{true, false\}$
(INT)	$\frac{}{\vdash N : Int}$	$N \in \{0, 1, -1, \dots\}$
(FunOp)	$\frac{\vdash \text{expr}_1 : \tau_1 \dots \vdash \text{expr}_n : \tau_n \quad \omega : \tau_1 \times \dots \times \tau_n \rightarrow \tau}{\vdash \omega(\text{expr}_1, \dots, \text{expr}_n) : \tau}$	$n \geq 1, \omega \notin \text{def}(\mathcal{E})$

Example:

- not true

$$(BOOL) \quad \frac{\text{true} : Bool}{\vdash \text{not true} : Bool}$$
 - true + 3

$$(FunOp) \quad \frac{\text{true} : Bool \quad 3 : Int \quad \omega : Bool \times Int \rightarrow Int}{\vdash \text{true} + 3 : Int}$$

get result - use correct type this from the rules
 - true < 3

$$(FunOp) \quad \frac{\text{true} : Bool \quad 3 : Int \quad \omega : Bool \times Int \rightarrow Bool}{\vdash \text{true} < 3 : Bool}$$

+ Int < Int < Bool
- ⊙ Can true + 3 is well-typed

Type Environment

- **Problem:** Whether $w + 3$ is well-typed or not depends on the type of logical variable $w \in W$.
- **Approach: Type Environments**

Definition. A **type environment** is a (possibly empty) finite sequence of type declarations for a given set W of logical variables and types T is defined by the grammar

$$A ::= \emptyset \mid A, w : \tau$$

where $w \in W, \tau \in T$.

Clear: We use this definition for the set of OCL logical variables W and the types $T = T_D \cup T_C \cup \{Set(\tau_0) \mid \tau_0 \in T_D \cup T_C\}$.

Environment Introduction and Logical Variables

- If $expr$ is of type τ , then it is of type τ in any type environment

$$(EnvIntro) \frac{}{A \vdash expr : \tau}$$

- Care for logical variables in sub-expressions of operator application:

$$(FuncA) \frac{A \vdash expr_1 : \tau_1, \dots, A \vdash expr_n : \tau_n, \quad w : \tau_1 \times \dots \times \tau_n \rightarrow \tau, \quad n \geq 1, w \notin \text{dom}(\theta)}{A \vdash w(expr_1, \dots, expr_n) : \tau}$$

- If $expr$ is a logical variable such that $w : \tau$ occurs in A , then we say w is of type τ .

$$(Var) \frac{w : \tau \in A}{A \vdash w : \tau}$$

Type Environment Example

$$(EnvIntro) \frac{}{A \vdash expr : \tau}$$

$$(FuncA) \frac{A \vdash expr_1 : \tau_1, \dots, A \vdash expr_n : \tau_n, \quad w : \tau_1 \times \dots \times \tau_n \rightarrow \tau, \quad n \geq 1, w \notin \text{dom}(\theta)}{A \vdash w(expr_1, \dots, expr_n) : \tau}$$

$$(Var) \frac{w : \tau \in A}{A \vdash w : \tau}$$

- **Example:** $w + 3, A = w : Int$



All Instances and Attributes in Type Environment

- If $expr$ refers to all instances of class C , then it is of type $Set(C)$.

$$(AllInst) \frac{}{\text{allinstances}_C : Set(C)}$$

- If $expr$ is an attribute access of an attribute of type τ for an object of C as denoted by $expr_1$, then the premise is that $expr_1$ is of type τ_C :

$$(Attr\tau) \frac{A \vdash expr_1 : \tau_C, \quad \tau_C \in \text{attr}(C), \quad \tau \in \mathcal{D}}{A \vdash expr_1.\tau : \tau}$$

$$(Attr\tau_1) \frac{A \vdash expr_1 : \tau_C, \quad \tau_1 : D_{\text{Attr}} \in \text{attr}(C)}{A \vdash \tau_1(expr_1) : \tau_D}$$

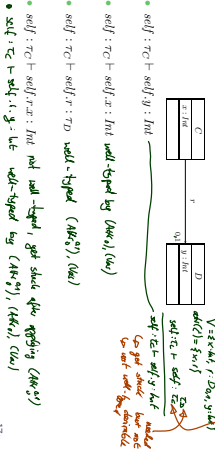
$$(Attr\tau_0) \frac{A \vdash expr_1 : \tau_C, \quad \tau_2 : D_s \in \text{attr}(C)}{A \vdash \tau_2(expr_1) : Set(\tau_D)}$$

Attributes in Type Environment Example

$$(Attr\tau) \frac{A \vdash expr_1 : \tau_C, \quad \tau_C \in \text{attr}(C), \quad \tau \in \mathcal{D}}{A \vdash expr_1.\tau : \tau}$$

$$(Attr\tau_1) \frac{A \vdash expr_1 : \tau_C, \quad \tau_1 : D_{\text{Attr}} \in \text{attr}(C)}{A \vdash \tau_1(expr_1) : \tau_D}$$

$$(Attr\tau_0) \frac{A \vdash expr_1 : \tau_C, \quad \tau_2 : D_s \in \text{attr}(C)}{A \vdash \tau_2(expr_1) : Set(\tau_D)}$$



Iterate

- If $expr$ is an iterate expression, then
- the iterator variable has to be type consistent with the base set, and
- initial and update expressions have to be consistent with the result variable.

$$(Iter) \frac{A \vdash expr_1 : Set(\tau), \quad A \vdash expr_2 : \tau, \quad A \vdash expr_3 : \tau}{A \vdash expr_1 \rightarrow \text{iterate}(var : \Delta : \tau_0 : \tau_D = expr_2 | expr_3) : \tau_2}$$

where $A' = A \oplus (var : \tau_0) \oplus (var : \tau_2)$.

variable typing of the code up in A'

initial step: $var : \tau_0$

update step: $var : \tau_2$

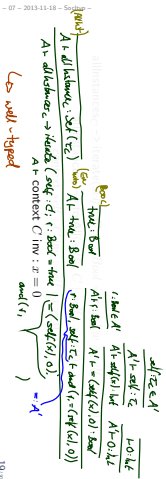
final step: $var : \tau_2$

Henke Example

(AllEnv)	$\frac{}{F \text{ allEnvEncr} : \text{Set}(\alpha)}$	(All)	$\frac{A \vdash \text{expr}_1 : \tau_1}{A \vdash \text{encr}_1 : \tau}$
(Let)	$\frac{A \vdash \text{expr}_1 : \tau_1 \quad \text{Set}(C) \vdash A \vdash \text{expr}_2 : \tau_2 \quad A \vdash \text{expr}_3 : \tau_2}{A \vdash \text{encr} \rightarrow \text{SetEnv}(\text{env} : \tau_1 \oplus \text{env}_2 : \tau_2)}$		

where $A' = A \oplus (\text{env} : \tau_1) \oplus (\text{env}_2 : \tau_2)$

Example: $\mathcal{C} = (\text{hd}), \{C; \text{hd}\}, \{C \mapsto (x)\}$



19¹¹

One Possible Extension: Implicit Casts

- We may wish to have

$$\vdash \text{! and false} : \text{Bool} \quad (*)$$
- In other words: We may wish that the type system allows to use `! 1`, `! hd` instead of `true` and `false` without breaking well-typedness.
- Then just have a rule:

$$\text{(Cast)} \quad \frac{A \vdash \text{expr} : \text{Int}}{A \vdash \text{expr} : \text{Bool}}$$
- With (Cast) (and (Int), and (Bool), and (Fun)), we can derive the sentence $(*)$, thus conclude well-typedness.
- But: that's only half of the story — the definition of the interpretation function I that we have is not prepared, it doesn't tell us what $(*)$ means...

22¹¹

First Recapitulation

- I only defined for well-typed expressions.
- What can hinder something, which looks like a well-typed OCL expression, from being a well-typed OCL expression...?

$$\mathcal{C} = (\text{hd}), \{C; D\}, \{x : \text{hd}, n : D_n\}, \{C \mapsto (n), D \mapsto (x)\}$$
- Raw syntax error: context C ; false
- Subtle syntax error (depends on signature) not in \mathcal{C}

$$\text{context } C \vdash \text{inv} : \beta = 0$$
- Type error: context $\text{self} : C \vdash \text{inv} : \text{self} \cdot n = \text{self} \cdot n \cdot x$

20¹¹

Implicit Casts Cont'd

- So, why isn't there an interpretation for `! and false`?
 - First of all, we have (syntax)

$$\text{expr}_1 \text{ and } \text{expr}_2 : \text{Bool} \times \text{Bool} \rightarrow \text{Bool}$$
 - Thus,

$$I(\text{and}) : I(\text{Bool}) \times I(\text{Bool}) \rightarrow I(\text{Bool})$$
 where $I(\text{Bool}) = \{\text{true}, \text{false}\} \cup \{\perp_{\text{Bool}}\}$.
- By definition,

$$I[\![\text{and}]\!] (\alpha, \beta) = I(\text{and}) (I[\![\alpha]\!] (\alpha, \beta), I[\![\beta]\!] (\alpha, \beta)),$$
 and there we're stuck.

23¹¹

Casting in the Type System

- Explicitly define

$$I[\![\text{and}]\!] (\text{expr}_1, \text{expr}_2) (\alpha, \beta) = \begin{cases} b_1 \wedge b_2 & , \text{ if } b_1 \neq \perp_{\text{Bool}} \wedge b_2 \\ \perp_{\text{Bool}} & , \text{ otherwise} \end{cases}$$
- where
 - $b_1 := I(\text{bool})(I[\![\text{expr}_1]\!] (\alpha, \beta))$,
 - $b_2 := I(\text{bool})(I[\![\text{expr}_2]\!] (\alpha, \beta))$,
 and where

$$\text{toBool} : I(\text{Int}) \cup I(\text{Bool}) \rightarrow I(\text{Bool})$$

$$x \mapsto \begin{cases} \text{true} & , \text{ if } x \in \{\text{true}\} \cup I(\text{Int}) \setminus \{0, \perp_{\text{Int}}\} \\ \text{false} & , \text{ if } x \in \{\text{false}\} \cup I(\text{Int}) \setminus \{0, \perp_{\text{Int}}\} \\ \perp_{\text{Bool}} & , \text{ otherwise} \end{cases}$$

24¹¹

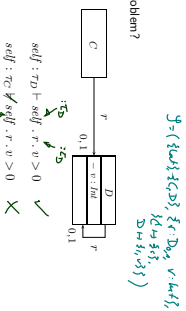
Bottomline

- There are **wishes** for the type-system which require changes in both the definition of τ and the type system. In most cases not difficult, but tedious.
- **Note:** the extension is still a basic type system.
- **Note:** OCL has a far more elaborate type system which in particular addresses the relation between Dom and Int (cf. [OCL'S 2009]).

Visibility in the Type System

Context

- **Example:** A problem?



- That is, whether an expression involving attributes with visibility is well-typed **depends** on the class of objects for which it is evaluated.
- **Therefore:** well-typedness in type environment \mathcal{A} and context $B \in \mathcal{C}$:
 $A, B \vdash expr : \tau$
- In particular: prepare to treat "protected" later (when doing inheritance).

Attribute Access in Context

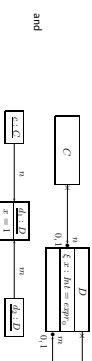
- If $expr$ is of type τ in a type environment, then it is in **any context**:
 $(Context \text{ Base}) \quad A, B \vdash expr : \tau$
- **Accessing attribute** v of a C -object via logical variable w is well-typed if
 - ~~$A, B \vdash w : \tau$~~
 - ~~$A, B \vdash w : \tau$~~

- $(Attr_1) \quad \frac{A, B \vdash w : \tau \quad (v : \tau, \xi, expr_0, R_0) \in attr(B)}{A, B \vdash (w.v) : \tau}$
- **Accessing attribute** v of a C -object of via expression $expr_1$ is well-typed in context B if
 - v is public, or $expr_1$ denotes an object of class B :
- $(Attr_2) \quad \frac{A, B \vdash expr_1 : \tau \quad (v : \tau, \xi, expr_0, R_0) \in attr(C) \quad \xi = +_v \text{ or } C = B}{A, B \vdash (expr_1.v) : \tau}$
- Accessing $C_{(v)}$ - or C_v -typed attributes: similar.

Visibility — The Intuition

$$\mathcal{C} = \{(w) \in \{C, D\} \mid \forall v \in \mathcal{D}_{w,v} \exists m : \mathcal{D}_{w,v} \{x : int, \xi : expr_0, \theta\}, (C \rightarrow (v) \mid D \rightarrow (x, m))\}$$

Let's study an Example:



Assume w_1, r_0 and w_2, r_0 are logical variables. Which of the following syntactically correct (?) OCL expressions shall we consider to be well-typed?

ξ of x :	public	private	protected	package
$w_1.r, x = 0$	✓	✗	✗	✗
$w_2.m, x = 0$	✗	✗	✗	✗
$x.(w_1.v) > 0$	✓	✗	✗	✗
?	?	?	?	?

Handwritten notes: 'v is not visible in C', 'm is not visible in B', 'v is visible in D', 'm is visible in D'.

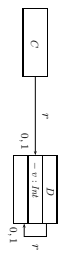
Context in Operator Application

- Operator Application:
 $(Func) \quad \frac{A, B \vdash expr_1 : \tau_1 \dots A, B \vdash expr_n : \tau_n \quad w : \tau_1 \times \dots \times \tau_n \rightarrow \tau \quad n \geq 1, w \notin attr(\mathcal{C})}{A, B \vdash w(expr_1, \dots, expr_n) : \tau}$
- Iterate:
 $(Iter_1) \quad \frac{A, B \vdash expr_1 : Set(C) \quad A', B \vdash expr_2 : \tau_2 \quad A', B \vdash expr_3 : \tau_3}{A, B \vdash expr_1 \rightarrow Iterate(w : \tau_1 \times \tau_2 : \tau_2 = expr_2 \mid expr_3) : \tau_3}$

where $A' = A \oplus (w_1 : \tau_1) \oplus (w_2 : \tau_2)$.

Attribute Access in Context Example

(Context **Exp**)
 $\lambda A.B \rightarrow expr : \tau$
 (Attr)
 $\lambda A.B \rightarrow expr_1 : \tau_C$ ($\forall \tau : \tau \in \text{expr}_0, P_0 \in \text{Attr}(C)$)
 $\lambda A.B \rightarrow v(\text{expr}_1) : \tau$ ($\forall \tau : \tau \in \text{expr}_0, P_0 \in \text{Attr}(C)$,
 $\xi = \tau_0, \text{and } \xi = \text{and } C = B$)



Example:

$\text{self} : \tau_C \quad \vdash \text{self} . r . v > 0$

34.17

Recapitulation

34.17

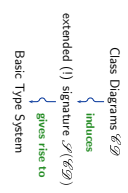
The Semantics of Visibility

- **Observation:**
- Whether an expression **does** or **does not** respect visibility is a matter of well-typedness **only**.
- We only evaluate (= apply I to) **well-typed** expressions.
- We need **not** adjust the interpretation function I to support visibility.

07 - 2013-11-18 - Savelop

32.17

Recapitulation



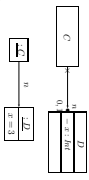
- We extended the type system for
 - casts (requires change of I) and **new** *object* *statics*
 - **visibility** (no change of I).
 - **Later:** **navigability** of associations.
- Good: well-typedness is decidable for these type-systems. That is, we can have automatic tools that check, whether OCL expressions in a model are well-typed.

07 - 2013-11-18 - Savelop

35.17

What is Visibility Good For?

- Visibility is a property of attributes — is it useful to consider it in OCL?
- In other words: given the picture above, is it useful to state the following invariant (even though x is private in D)
 $\text{context } C \text{ inv: } n.x > 0 ?$
- **It depends:**
- **Constraints and pre/post conditions:**
- Visibility is **sometimes** not taken into account. To state "global" requirements, it may be adequate to have a "global view", be able to look into all objects.
- But: visibility supports "narrow interfaces", "information hiding", and similar good design practices. To be more robust against changes, try to state requirements only in the terms which are visible to a class.
- **Rule-of-thumb:** if attributes are important to state requirements on design models, leave them public or provide get-methods (later).
- **Guards and operation bodies:**
- If in doubt, **yes** (= do take visibility into account).
- Any so-called **action language** typically takes visibility into account.



07 - 2013-11-18 - Savelop

33.17

References

36.17

References

- [OMG, 2006] OMG (2006). Object Constraint Language, version 2.0. Technical Report formal/06-05-01.
- [OMG, 2007a] OMG (2007a). Unified modeling language: Infrastructure, version 2.1.2. Technical Report formal/07-11-04.
- [OMG, 2007b] OMG (2007b). Unified modeling language: Superstructure, version 2.1.2. Technical Report formal/07-11-02.