

Software Design, Modelling and Analysis in UML

Lecture 09: Class Diagrams III

2013-11-25

Prof. Dr. Andreas Podelski, **Dr. Bernd Westphal**

Albert-Ludwigs-Universität Freiburg, Germany

Contents & Goals

Last Lectures:

- Studied syntax and semantics of associations in the general case.

This Lecture:

- **Educational Objectives:** Capabilities for following tasks/questions.
 - Cont'd: Please explain this class diagram with associations.
 - When is a class diagram a good class diagram?
 - What are purposes of modelling guidelines? (Example?)
 - Discuss the style of this class diagram.
- **Content:**
 - Effect of association semantics on OCL.
 - Treat “the rest” .
 - Where do we put OCL constraints?
 - Modelling guidelines, in particular for class diagrams (following [[Ambler, 2005](#)])
 - Examples: modelling games (made-up and real-world examples)

Links in System States

$$\langle r : \langle role_1 : C_1, -, P_1, -, -, - \rangle, \dots, \langle role_n : C_n, -, P_n, -, -, - \rangle \rangle$$

Only for the course of lectures 08/08 we change the definition of system states:

Definition. Let \mathcal{D} be a structure of the (extended) signature $\mathcal{S} = (\mathcal{I}, \mathcal{C}, V, atr)$.

A **system state** of \mathcal{S} wrt. \mathcal{D} is a pair (σ, λ) consisting of

- a type-consistent mapping

$$\sigma : \mathcal{D}(\mathcal{C}) \rightarrow (atr(\mathcal{C}) \rightarrow \mathcal{D}(\mathcal{I})),$$

- a mapping λ which assigns each association $\langle r : \langle role_1 : C_1 \rangle, \dots, \langle role_n : C_n \rangle \rangle \in V$ a relation

$$\lambda(r) \subseteq \mathcal{D}(C_1) \times \dots \times \mathcal{D}(C_n)$$

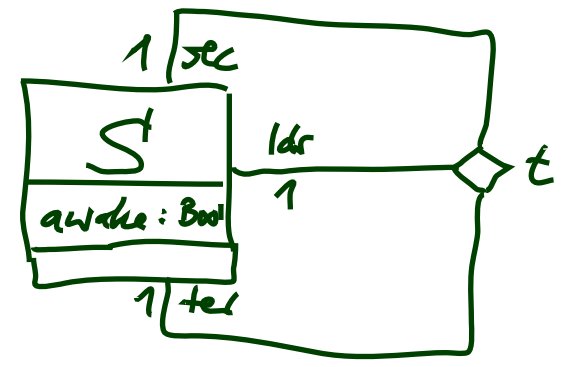
(i.e. a set of type-consistent n -tuples of identities).

for associations

values for basic type attributes only

Example

$\langle t: \langle ldr: S \rangle \rangle$
 $\langle sec: S \rangle$
 $\langle ter: S \rangle$

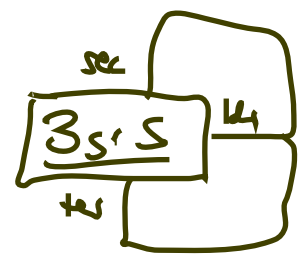
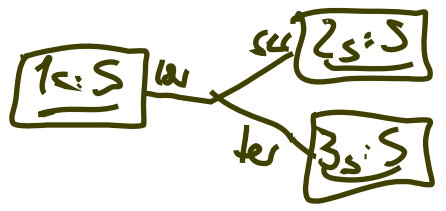


$\sigma = \{ 1_s \mapsto \{aw \mapsto 1\}, 2_s \mapsto \{aw \mapsto 0\}, 3_s \mapsto \{aw \mapsto 1\}, 27_s \mapsto \{aw \mapsto 0\} \}$

$\lambda = \{ t \mapsto \left\{ \begin{array}{l} \overset{ldr}{(1_s, 2_s, 3_s)}, \\ \overset{sec}{(1_s, 27_s, 3_s)}, \\ \overset{ter}{(2_s, 5_s, 6_s)}, \\ (3_s, 3_s, 3_s) \end{array} \right\} \}$

$\overset{D(S)}{D(S)}$ } students may join multiple groups
 $\overset{D(S)}{D(S)}$ } links may also have dangling references
 $\overset{D(S)}{D(S)}$ } one student may assume all roles
 (add a constraint if this is not desired)

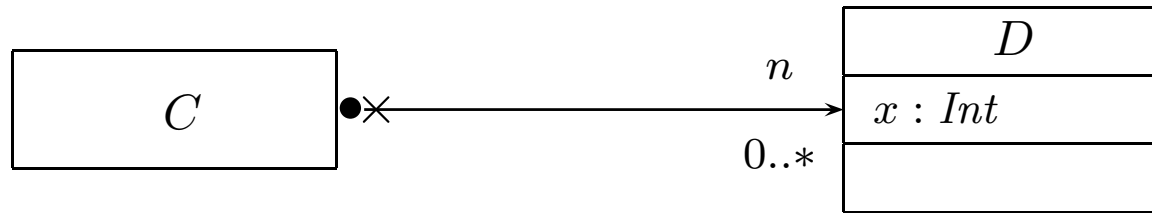
OBJECT DIAGRAMS:



\hookrightarrow we need hyperedges in general

WE WILL NOT FORMALLY DEFINE THAT

Association/Link Example



Signature:

$$\begin{aligned}
 \mathcal{S} = (& \{Int\}, \{C, D\}, \{x : Int, \\
 & \langle A_C_D : \langle c : C, 0..*, +, \{unique\}, \times, 1 \rangle, \\
 & \langle n : D, 0..*, +, \{unique\}, >, 0 \rangle \rangle), \\
 & \{C \mapsto \emptyset, D \mapsto \{x\}\})
 \end{aligned}$$

by convention (pointing to the '1' and 'x : Int')
by default (pointing to the '0..*' and '>' symbols)

A **system state** of \mathcal{S} (some reasonable \mathcal{D}) is (σ, λ) with:

$$\sigma = \{1_C \mapsto \emptyset, 3_D \mapsto \{x \mapsto 1\}, 7_D \mapsto \{x \mapsto 2\}\}$$

$$\lambda = \{A_C_D \mapsto \{(1_C, 3_D), (1_C, 7_D)\}\}$$

object 1_C is related to 3_D and 7_D by A-C-N

Associations and OCL

OCL and Associations: Syntax

Recall: OCL syntax as introduced in Lecture 03, interesting part:

$$\begin{array}{l}
 \text{expr} ::= \dots \quad | \quad r_1(\text{expr}_1) : \tau_C \rightarrow \tau_D \quad r_1 : D_{0,1} \in \text{atr}(C) \\
 \quad \quad \quad | \quad r_2(\text{expr}_1) : \tau_C \rightarrow \text{Set}(\tau_D) \quad r_2 : D_* \in \text{atr}(C)
 \end{array}$$

Now becomes

$$\begin{array}{l}
 \text{expr} ::= \dots \quad | \quad \text{role}(\text{expr}_1) : \tau_C \rightarrow \tau_D \quad \mu = 0..1 \text{ or } \mu = 1 \\
 \quad \quad \quad | \quad \text{role}(\text{expr}_1) : \tau_C \rightarrow \text{Set}(\tau_D) \quad \text{otherwise}
 \end{array}$$

if there is

$$\left\{ \begin{array}{l}
 \langle r : \dots, \langle \text{role} : D, \mu, -, -, -, - \rangle, \dots, \langle \text{role}' : C, -, -, -, -, - \rangle, \dots \rangle \in V \text{ or} \\
 \langle r : \dots, \langle \text{role}' : C, -, -, -, -, - \rangle, \dots, \langle \text{role} : D, \mu, -, -, -, - \rangle, \dots \rangle \in V, \text{role} \neq \text{role}' \quad \text{!}
 \end{array} \right.$$

two rows for tech. reasons: order matters

C participates in assoc. r

$$\boxed{C} \xrightarrow{n} \boxed{D} : \text{never } h(\text{set}_D)$$

$$\boxed{C} \xrightarrow[n]{p} \boxed{} : n(\text{self}_C) \text{ is ok}$$

OCL and Associations: Syntax

Recall: OCL syntax as introduced in Lecture 03, interesting part:

$$\begin{array}{l|l|l} \text{expr} ::= \dots & r_1(\text{expr}_1) : \tau_C \rightarrow \tau_D & r_1 : D_{0,1} \in \text{atr}(C) \\ & r_2(\text{expr}_1) : \tau_C \rightarrow \text{Set}(\tau_D) & r_2 : D_* \in \text{atr}(C) \end{array}$$

Now becomes

$$\begin{array}{l|l|l} \text{expr} ::= \dots & \text{role}(\text{expr}_1) : \tau_C \rightarrow \tau_D & \mu = 0..1 \text{ or } \mu = 1 \\ & \text{role}(\text{expr}_1) : \tau_C \rightarrow \text{Set}(\tau_D) & \text{otherwise} \end{array}$$

if

$$\langle r : \dots, \langle \text{role} : D, \mu, -, -, -, - \rangle, \dots, \langle \text{role}' : C, -, -, -, -, - \rangle, \dots \rangle \in V \text{ or} \\ \langle r : \dots, \langle \text{role}' : C, -, -, -, -, - \rangle, \dots, \langle \text{role} : D, \mu, -, -, -, - \rangle, \dots \rangle \in V, \text{role} \neq \text{role}'.$$

Note:

- Association name as such doesn't occur in OCL syntax, role names do.
- expr_1 has to denote an object of a class which “participates” in the association.

OCL and Associations Syntax: Example

$expr ::= \dots \mid role(expr_1) : \tau_C \rightarrow \tau_D \quad \mu = 0..1 \text{ or } \mu = 1$
 $\mid role(expr_1) : \tau_C \rightarrow Set(\tau_D) \quad \text{otherwise}$

if
 $\langle r : \dots, \langle role : D, \mu, -, -, -, - \rangle, \dots, \langle role' : C, -, -, -, -, - \rangle, \dots \rangle \in V$ or
 $\langle r : \dots, \langle role' : C, -, -, -, -, - \rangle, \dots, \langle role : D, \mu, -, -, -, - \rangle, \dots \rangle \in V, role \neq role'$.

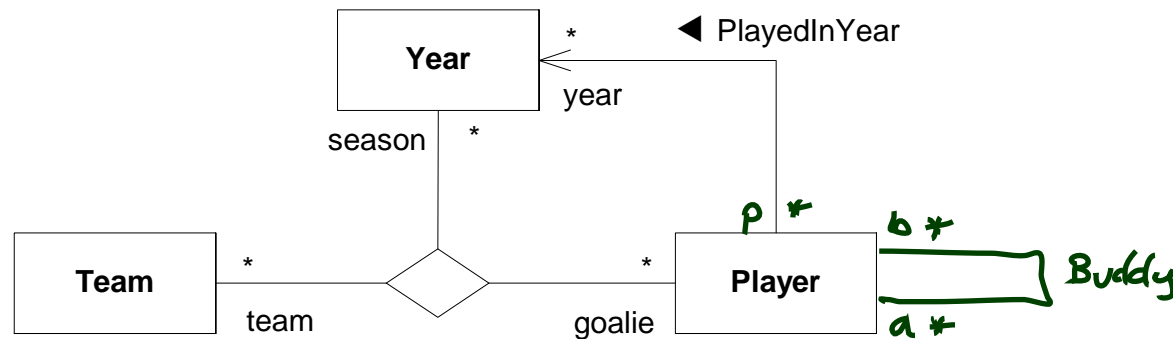


Figure 7.21 - Binary and ternary associations [OMG, 2007b, 44].

- context Player inv: size(year(self)) > 0 OK
- context Player inv: self.p → size > 0 NOT OK
- context Player inv: self.season → size > 0 OK
- context Player inv: self.b → size > 0 OK

OCL and Associations: Semantics

Recall: (Lecture 03)

Assume $expr_1 : \tau_C$ for some $C \in \mathcal{C}$. Set $u_1 := I[expr_1](\sigma, \beta) \in \mathcal{D}(\tau_C)$.

- $I[r_1(expr_1)](\sigma, \beta) := \begin{cases} u & , \text{ if } u_1 \in \text{dom}(\sigma) \text{ and } \sigma(u_1)(r_1) = \{u\} \\ \perp & , \text{ otherwise} \end{cases}$

- $I[r_2(expr_1)](\sigma, \beta) := \begin{cases} \sigma(u_1)(r_2) & , \text{ if } u_1 \in \text{dom}(\sigma) \\ \perp & , \text{ otherwise} \end{cases}$

$\subseteq \mathcal{D}(D)$

Now needed:

$$I[role(expr_1)](\underline{(\sigma, \lambda)}, \beta)$$

- We cannot simply write $\sigma(u)(role)$.
Recall: *role* is (**for the moment**) not an attribute of object u (not in $atr(C)$).
- What we have is $\lambda(r)$ (with r , not with *role*!) — but it yields a set of n -tuples, of which **some** relate u and other some instances of D .
- *role* denotes the position of the D 's in the tuples constituting the value of r .

OCL and Associations: Semantics Cont'd

Assume $expr_1 : \tau_C$ for some $C \in \mathcal{C}$. Set $u_1 := I[expr_1]((\sigma, \lambda), \beta) \in \mathcal{D}(\tau_C)$.

- $I[role(expr_1)]((\sigma, \lambda), \beta) := \begin{cases} u & , \text{ if } u_1 \in \text{dom}(\sigma) \text{ and } L(role)(u_1, \lambda) = \{u\} \\ \perp & , \text{ otherwise} \end{cases}$ $\mu=1 \text{ or } \mu=0..1$
- $I[role(expr_1)]((\sigma, \lambda), \beta) := \begin{cases} L(role)(u_1, \lambda) & , \text{ if } u_1 \in \text{dom}(\sigma) \\ \perp & , \text{ otherwise} \end{cases}$

where

$$L(\underline{role})(u, \lambda) = \left(\{(u_1, \dots, u_n) \in \lambda(r) \mid u \in \{u_1, \dots, u_n\}\} \downarrow i \right) \subseteq \mathcal{D}(C)$$

Handwritten annotations: "role name" points to $L(\underline{role})$; "object identities" points to $\lambda(r)$; "links" points to $\{(u_1, \dots, u_n) \in \lambda(r) \mid u \in \{u_1, \dots, u_n\}\}$; "projection on the i-th component" points to $\downarrow i$.

if

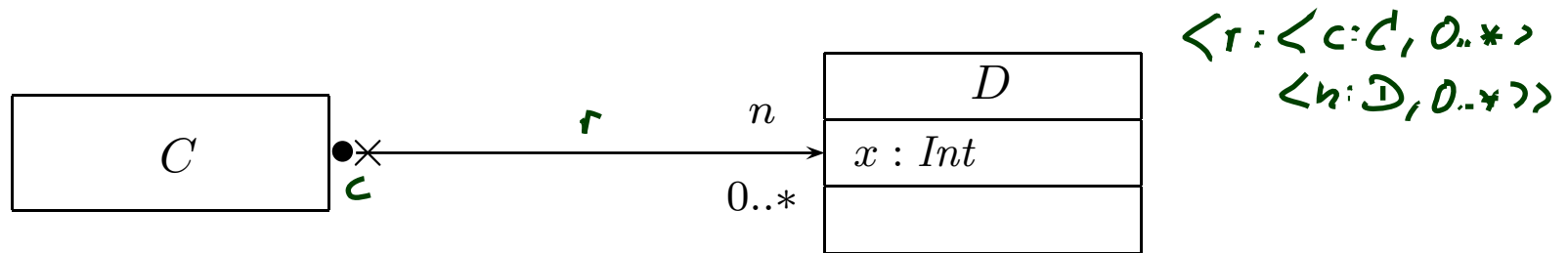
$$\langle r : \dots \langle role_1 : -, -, -, -, -, - \rangle, \dots \langle role_n : -, -, -, -, -, - \rangle, \dots \rangle, \underline{role = role_i}$$

Given a set of n -tuples A , $A \downarrow i$ denotes the element-wise projection onto the i -th component.

OCL and Associations Example

$$I[\text{role}(\text{expr}_1)]((\sigma, \lambda), \beta) := \begin{cases} L(\text{role})(u_1, \lambda) & , \text{ if } u_1 \in \text{dom}(\sigma) \\ \perp & , \text{ otherwise} \end{cases}$$

$$L(\text{role})(u, \lambda) = \{(u_1, \dots, u_n) \in \lambda(r) \mid u \in \{u_1, \dots, u_n\}\} \downarrow i$$



$$\sigma = \{1_C \mapsto \emptyset, 3_D \mapsto \{x \mapsto 1\}, 7_D \mapsto \{x \mapsto 2\}\} \cup \{2_C \mapsto \emptyset\}$$

$$\lambda = \{ \cancel{1_C, 3_D} \mapsto \{(1_C, 3_D), (1_C, 7_D)\} \cup \{(2_C, 7_D)\} \}$$

$$I[\text{self} . n]((\sigma, \lambda), \{\text{self} \mapsto 1_C\}) = \{3_D, 7_D\}$$

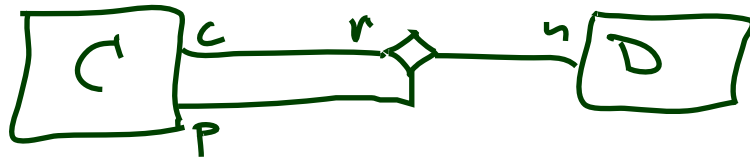
all tuples where 1c occurs

$$= L(n)(1_C, \lambda)$$

position of role n in r

$$= \{(1_C, 3_D), (1_C, 7_D)\} \downarrow 2$$

$$= \{3_D, 7_D\}$$



$\langle r: \langle c: c' \rangle,$
 $\langle n: D \rangle,$
 $\langle p: c' \rangle \rangle$

$$\lambda = \{ r \mapsto \{ (1_c, 3_D, 1_c), (6_c, 7_D, 2_c), (1_c, 8_D, 2_c), (5_c, 9_D, 6_c) \} \}$$

$$L(n)(1_c, \lambda) = \{ (1_c, 3_D, 1_c), (1_c, 8_D, 2_c) \} \downarrow 2 = \{ 3_D, 8_D \}$$

$$L(n)(2_c, \lambda) = \{ 7_D, 8_D \}$$

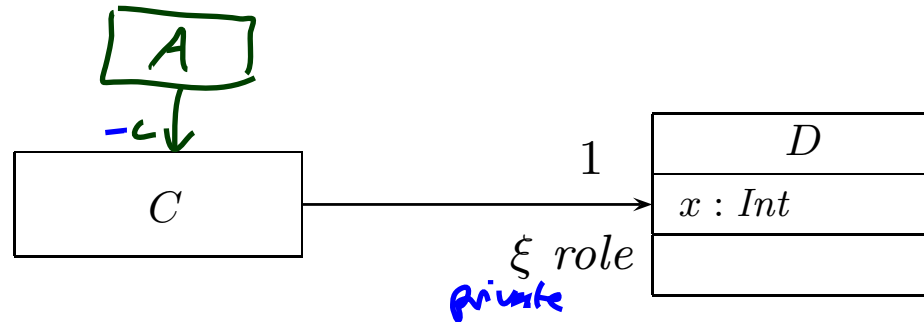
$$L(n)(5_c, \lambda) = \{ 9_D \}$$

Associations: The Rest

Visibility

Not so surprising: Visibility of role-names is treated completely similar to visibility of attributes, namely by **typing rules**.

Question: given



self_A.c OK
self_A.c.role NOT OK
self_C.role OK

is the following OCL expression well-typed or not (wrt. visibility):

context *C* inv : *self.role.x* > 0

Basically same rule as before: (analogously for other multiplicities)

$$(\text{Assoc}_1) \quad \frac{A, B \vdash \text{expr}_1 : \tau_C}{A, B \vdash \text{role}(\text{expr}_1) : \tau_D}, \quad \begin{array}{l} \mu = 0..1 \text{ or } \mu = 1, \\ \xi = +, \text{ or } \xi = - \text{ and } C = B \end{array}$$

$$\langle r : \dots \langle \text{role} : D, \mu, -, \xi, -, - \rangle, \dots \langle \text{role}' : C, -, -, -, -, - \rangle, \dots \rangle \in V$$

Navigability

Navigability is similar to visibility: expressions over non-navigable association ends ($\nu = \times$) are **basically** type-correct, but **forbidden**.

Question: given



is the following OCL expression well-typed or not (wrt. navigability):

context D inv : $self.role.x > 0$ *NOT well-typed*

The standard says:

- '—': navigation is possible
- '>': navigation is efficient
- '×': navigation is not possible

depends

on context,

e.g. slow vs. fast database, needs to be communicated to developers

So: In general, UML associations are different from pointers/references!

But: Pointers/references can faithfully be modelled by UML associations.

Recapitulation: Consider the following association:

$$\langle r : \langle role_1 : C_1, \mu_1, P_1, \xi_1, \nu_1, o_1 \rangle, \dots, \langle role_n : C_n, \mu_n, P_n, \xi_n, \nu_n, o_n \rangle \rangle$$

- Association name r and role names/types $role_i/C_i$ induce extended system states λ .
- Multiplicity μ is considered in OCL syntax.
- Visibility ξ and navigability ν give rise to well-typedness rules.

Now the rest:

- Multiplicity μ : we propose to view them as constraints.
- Properties P_i : even more typing.
- Ownership o : getting closer to pointers/references.
- Diamonds: exercise.

Multiplicities as Constraints

Recall: The multiplicity of an association end is a term of the form:

$$\mu ::= * \mid N \mid N..M \mid N..* \mid \mu, \mu \quad (N, M \in \mathbb{N})$$

Proposal: View multiplicities (except 0..1, 1) as additional invariants/constraints.

Recall: we can normalize each multiplicity to the form

$$\mu = N_1..N_2, \dots, N_{2k-1}..N_{2k}$$

where $N_i \leq N_{i+1}$ for $1 \leq i \leq 2k$, $N_1, \dots, N_{2k} \in \mathbb{N}$, $N_{2k} \in \mathbb{N} \cup \{*\}$.

Define

$\mu_{\text{OCL}} = \text{context } C \text{ inv :}$

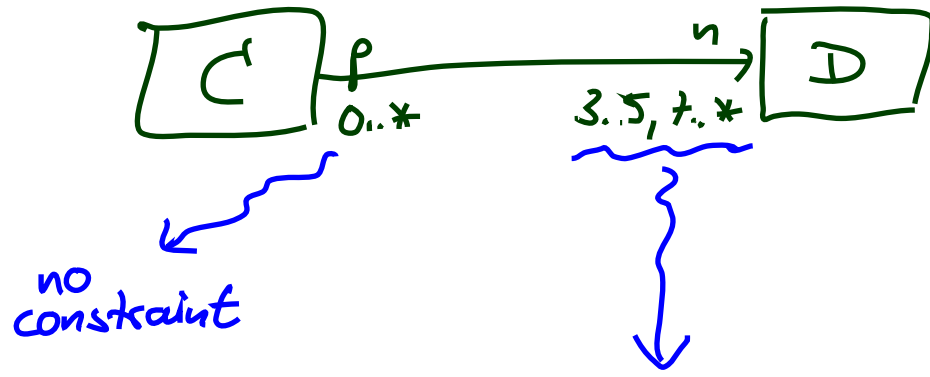
$$(N_1 \leq \text{role} \rightarrow \text{size}() \leq N_2) \overset{\text{or}}{\text{and}} \dots \overset{\text{or}}{\text{and}} (N_{2k-1} \leq \text{role} \rightarrow \text{size}() \leq N_{2k})$$

for each

$$\langle r : \dots, \langle \text{role} : D, \mu, -, -, -, - \rangle, \dots, \langle \text{role}' : C, -, -, -, -, - \rangle, \dots \rangle \in V \text{ or}$$

$$\langle r : \dots, \langle \text{role}' : C, -, -, -, -, - \rangle, \dots, \langle \text{role} : D, \mu, -, -, -, - \rangle, \dots \rangle \in V, \text{role} \neq \text{role}'.$$

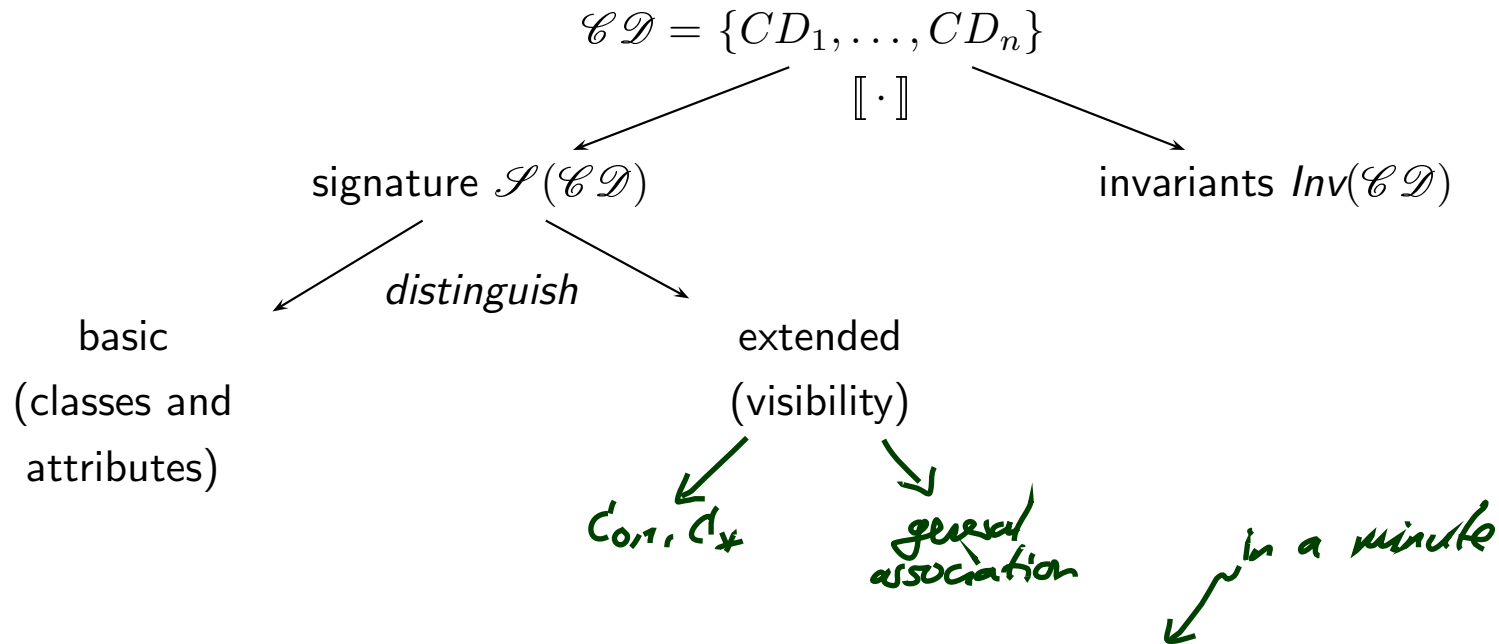
Note: in n -ary associations with $n > 2$, there is redundancy.



context C in U :
($n \rightarrow \text{size} \geq 3$
and $n \rightarrow \text{size} \leq 5$)
or
($n \rightarrow \text{size} \geq 7$)

Multiplicities as Constraints of Class Diagram

Recall:



From now on: $Inv(\mathcal{CD}) = \{\text{constraints occurring in notes}\} \cup \{\mu_{OCL} \mid$

$\langle r : \dots, \langle \text{role} : D, \mu, -, -, -, - \rangle, \dots, \langle \text{role}' : C, -, -, -, - \rangle, \dots \rangle \in V$ or

$\langle r : \dots, \langle \text{role}' : C, -, -, -, - \rangle, \dots, \langle \text{role} : D, \mu, -, -, -, - \rangle, \dots \rangle \in V,$

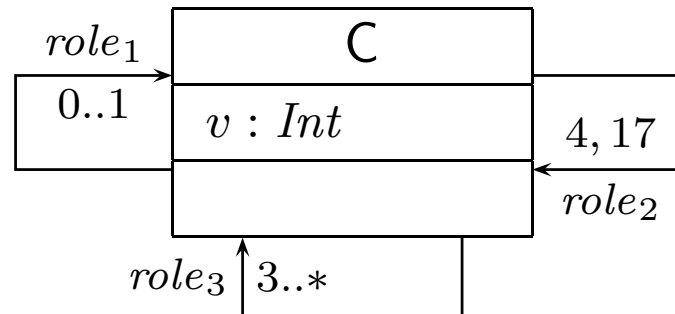
$\text{role} \neq \text{role}', \mu \notin \{0..1, 1\}\}.$

Multiplicities as Constraints Example

$\mu_{\text{OCL}} = \text{context } C \text{ inv :}$

$(N_1 \leq \text{role} \rightarrow \text{size}() \leq N_2)$ and ... and $(N_{2k-1} \leq \text{role} \rightarrow \text{size}() \leq N_{2k})$

$CD :$



$Inv(CD) =$

- $\{\text{context } C \text{ inv : } 4 \leq \text{role}_2 \rightarrow \text{size}() \leq 4 \text{ or } 17 \leq \text{role}_2 \rightarrow \text{size}() \leq 17\}$
 $= \{\text{context } C \text{ inv : } \text{role}_2 \rightarrow \text{size}() = 4 \text{ or } \text{role}_2 \rightarrow \text{size}() = 17\}$
- $\cup \{\text{context } C \text{ inv : } 3 \leq \text{role}_3 \rightarrow \text{size}()\}$

Why Multiplicities as Constraints?

More precise, can't we just use **types**? (cf. Slide 29)

- $\mu = 0..1$, $\mu = 1$:
many programming language have direct correspondences (the first corresponds to type pointer, the second to type reference) — this is why we excluded them.
- $\mu = *$:
could be represented by a set data-structure type without fixed bounds — no problem with our approach, we have $\mu_{\text{OCL}} = \text{true}$ anyway.
- $\mu = 0..4$:
use array of size 4 — if model behaviour (or the implementation) adds 5th identity, we'll get a runtime error, and thereby see that the constraint is violated. **Principally acceptable**, but: checks for array bounds everywhere...?
- $\mu = 5..7$:
could be represented by an array of size 7 — but: few programming languages/data structure libraries allow lower bounds for arrays (other than 0). If we have 5 identities and the model behaviour removes one, this should be a violation of the constraints imposed by the **model**.
The implementation which does this removal is **wrong**. How do we see this...?

Multiplicities Never as Types...?

Well, if the **target platform** is known and fixed, and the target platform has, for instance,

- reference types,
- range-checked arrays with positions $0, \dots, N$,
- set types,

then we could simply **restrict** the syntax of multiplicities to

$$\mu ::= 1 \mid 0..N \mid *$$

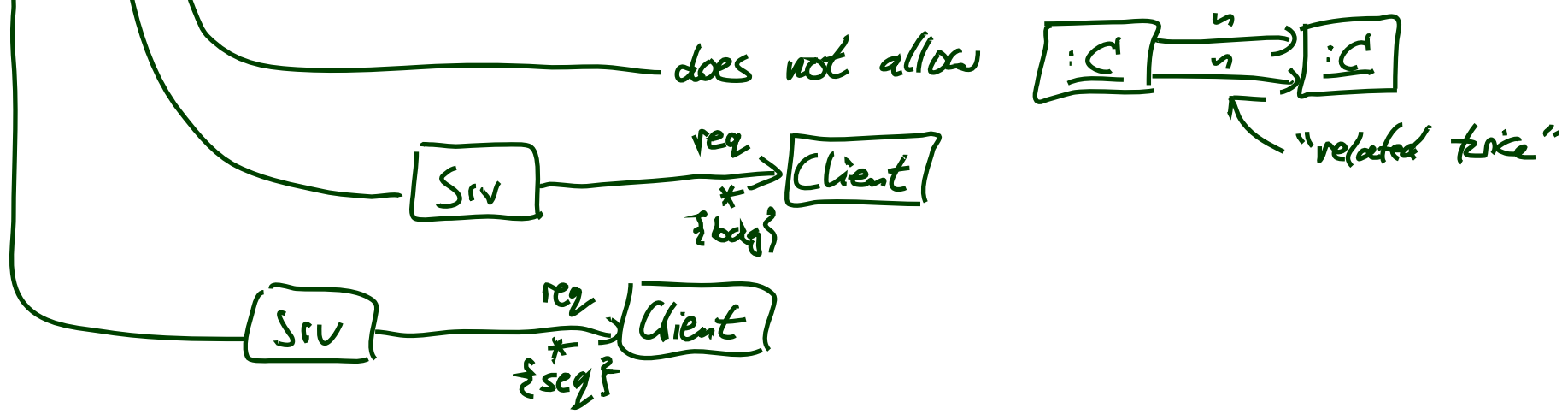
and don't think about constraints
(but use the obvious 1-to-1 mapping to types)...

In general, **unfortunately**, we don't know.

Properties

We don't want to cover association **properties** in detail, only some observations (assume binary associations):

| Property | Intuition | Semantical Effect |
|--------------------------|--|------------------------------------|
| unique | one object has at most one r -link to a single other object | current setting |
| bag | one object may have multiple r -links to a single other object | have $\lambda(r)$ yield multi-sets |
| ordered, sequence | an r -link is a sequence of object identities (possibly including duplicates) | have $\lambda(r)$ yield sequences |



Properties

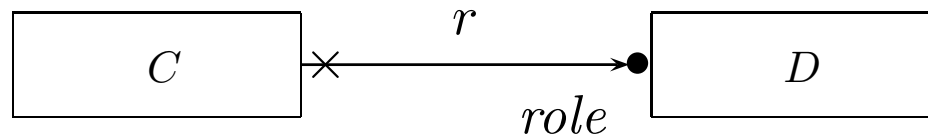
We don't want to cover association **properties** in detail, only some observations (assume binary associations):

| Property | Intuition | Semantical Effect |
|--------------------------|--|------------------------------------|
| unique | one object has at most one r -link to a single other object | current setting |
| bag | one object may have multiple r -links to a single other object | have $\lambda(r)$ yield multi-sets |
| ordered, sequence | an r -link is a sequence of object identities (possibly including duplicates) | have $\lambda(r)$ yield sequences |

| Property | OCL Typing of expression $role(expr)$ |
|--------------------------|---------------------------------------|
| unique | $\tau_D \rightarrow Set(\tau_C)$ |
| bag | $\tau_D \rightarrow Bag(\tau_C)$ |
| ordered, sequence | $\tau_D \rightarrow Seq(\tau_C)$ |

For **subsets**, **redefines**, **union**, etc. see [OMG, 2007a, 127].

Ownership



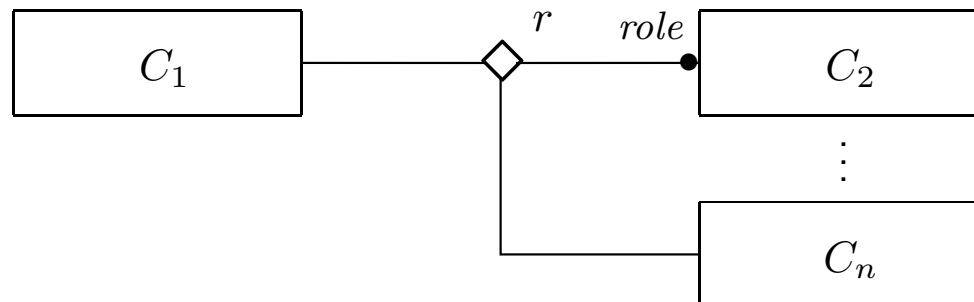
Intuitively it says:

Association r is **not a “thing on its own”** (i.e. provided by λ), but association end ‘ $role$ ’ is **owned** by C (!). (That is, it’s stored inside C object and provided by σ).

So: if multiplicity of $role$ is 0..1 or 1, then the picture above is very close to concepts of pointers/references.

Actually, ownership is seldom seen in UML diagrams. Again: if target platform is clear, one may well live without (cf. [OMG, 2007b, 42] for more details).

Not clear to me:



Back to the Main Track

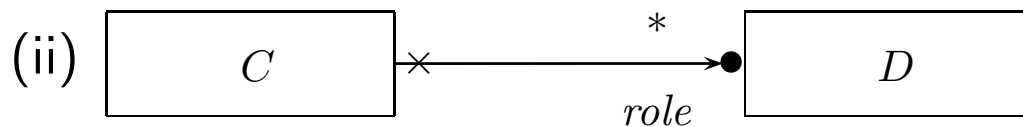
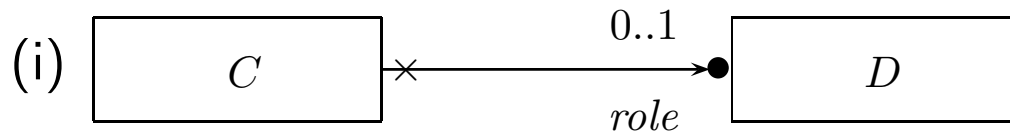
Back to the main track:

Recall: on some earlier slides we said, the extension of the signature is **only** to study associations in “full beauty”.

For the remainder of the course, we should look for something simpler...

Proposal:

- **from now on**, we only use associations of the form



(And we may omit the non-navigability and ownership symbols.)

- Form (i) introduces $role : C_{0,1}$, and form (ii) introduces $role : C_*$ in V .
- In both cases, $role \in atr(C)$.
- We drop λ and go back to our nice σ with $\sigma(u)(role) \subseteq \mathcal{D}(D)$.

OCL Constraints in (Class) Diagrams

Where Shall We Put OCL Constraints?

Two options:

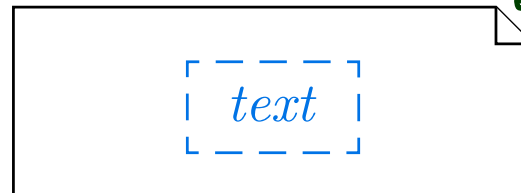
(0) *additional documents*

(i) Notes.

(ii) Particular dedicated places.

(i) **Notes:**

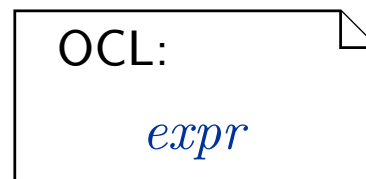
A UML **note** is a picture of the form



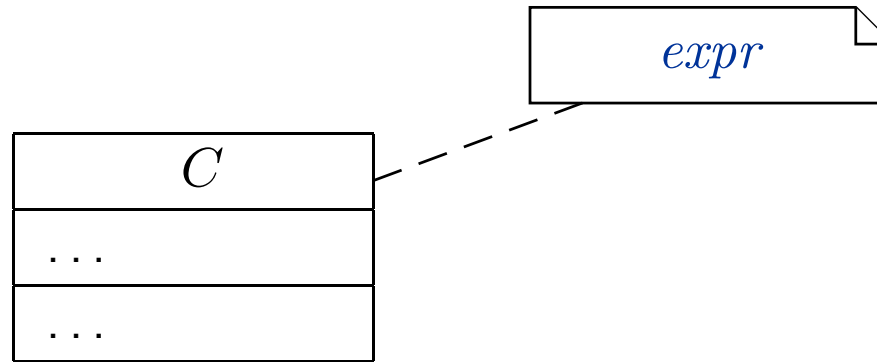
*Eselsohr
(dog's ear)*

text can principally be **everything**, in particular **comments** and **constraints**.

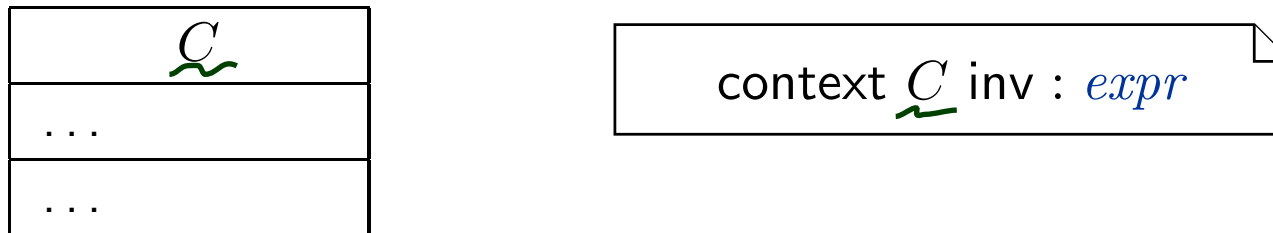
Sometimes, content is **explicitly classified** for clarity:



OCL in Notes: Conventions

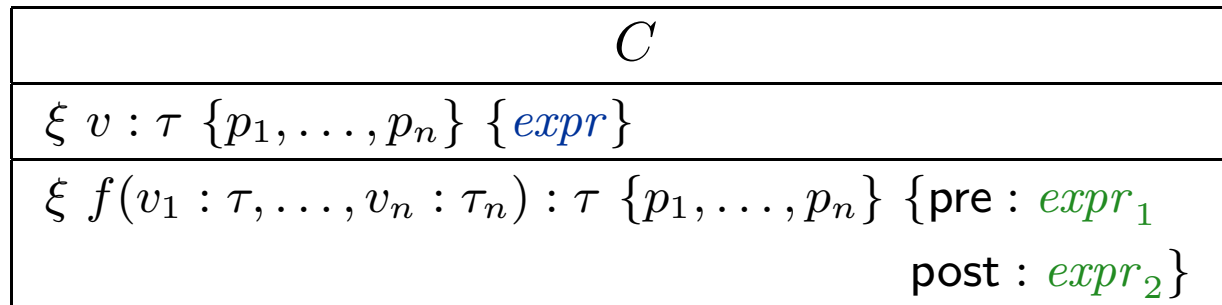


stands for

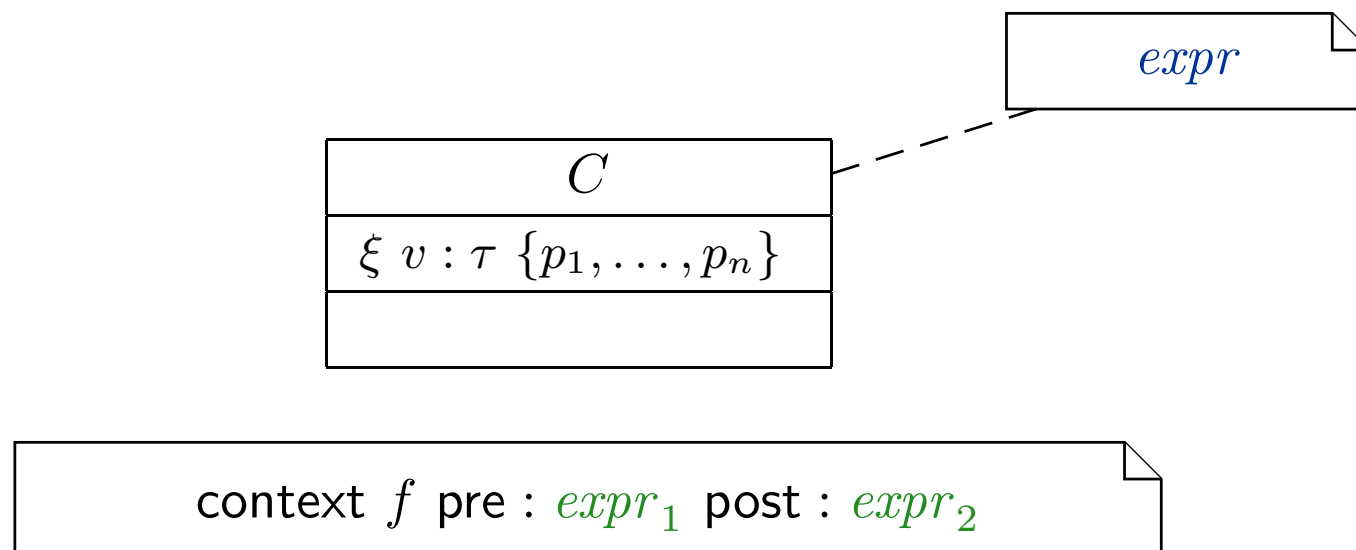


Where Shall We Put OCL Constraints?

- (ii) **Particular dedicated places** in class diagrams: (behav. feature: later)



For simplicity, we view the above as an abbreviation for



Invariants of a Class Diagram

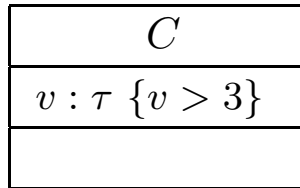
- Let \mathcal{CD} be a class diagram.
- As we (now) are able to recognise OCL constraints when we see them, we can define

$$Inv(\mathcal{CD})$$

as the set $\{\varphi_1, \dots, \varphi_n\}$ of OCL constraints **occurring** in notes in \mathcal{CD} — after **unfolding** all abbreviations (cf. next slides).

- As usual: $Inv(\mathcal{CD}) := \bigcup_{\mathcal{CD} \in \mathcal{CD}} Inv(\mathcal{CD})$.
- **Principally clear:** $Inv(\cdot)$ for any kind of diagram.

Invariant in Class Diagram Example



If \mathcal{CD} consists of only CD with the single class C , then

- $Inv(\mathcal{CD}) = Inv(CD) =$

Semantics of a Class Diagram

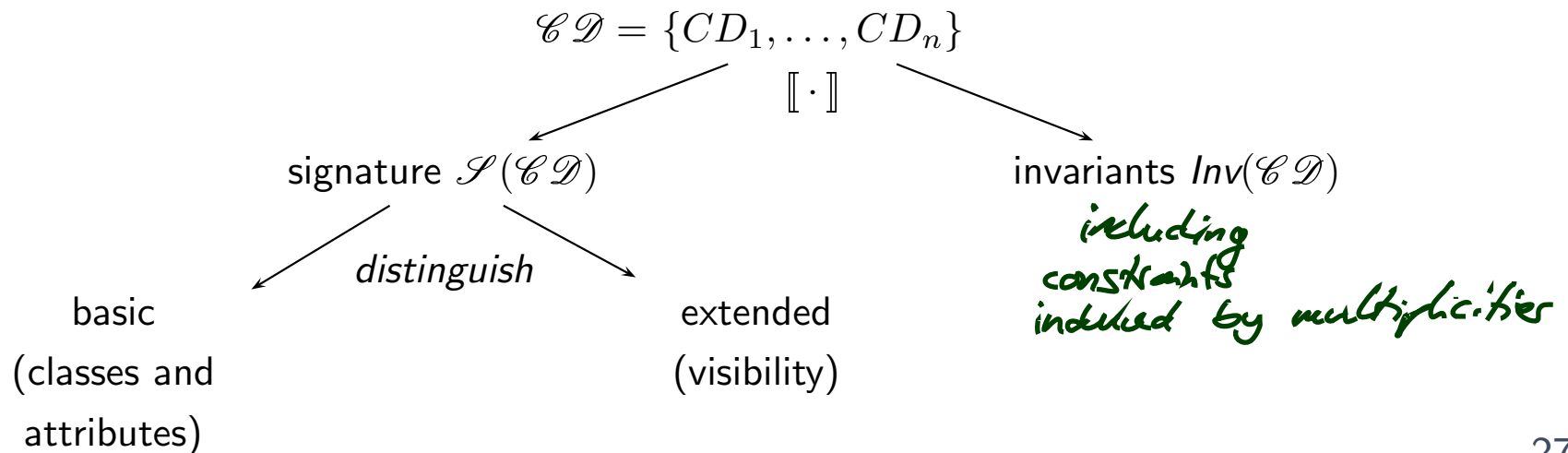
Definition. Let \mathcal{CD} be a set of class diagrams.

We say, the **semantics** of \mathcal{CD} is the signature it induces and the set of OCL constraints occurring in \mathcal{CD} , denoted

$$\llbracket \mathcal{CD} \rrbracket := \langle \mathcal{S}(\mathcal{CD}), \text{Inv}(\mathcal{CD}) \rangle.$$

Given a structure \mathcal{D} of \mathcal{S} (and thus of \mathcal{CD}), the class diagrams **describe** the system states $\Sigma_{\mathcal{D}}^{\mathcal{S}}$, of which **some** may satisfy $\text{Inv}(\mathcal{CD})$.

In pictures:



References

References

- [Ambler, 2005] Ambler, S. W. (2005). *The Elements of UML 2.0 Style*. Cambridge University Press.
- [OMG, 2007a] OMG (2007a). Unified modeling language: Infrastructure, version 2.1.2. Technical Report formal/07-11-04.
- [OMG, 2007b] OMG (2007b). Unified modeling language: Superstructure, version 2.1.2. Technical Report formal/07-11-02.