

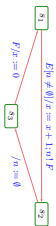
Software Design, Modelling and Analysis in UML

Lecture 13: Core State Machines III

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Where are we?



Where are we? $(\alpha, \varepsilon) \xrightarrow{\text{Consum, Send}} (\alpha', \varepsilon')$

- **Wanted:** a labelled transition relation on system configuration, labelled with the **consumed and sent events**, (α', ε') being the result (or effect) of **one object** u_x , taking a transition of its state machine from the current state mach. state $\sigma(u_x, S(C))$.
- **Have:** system configuration (α, ε) comprising current state machine state and stability flag for each object, and the ether.
- **Plan:**
 - (i) Introduce **transformer** as the semantics of action annotations. **Intuitively**, (α', ε') is the effect of applying the transformer of the taken transition.
 - (ii) Explain how to choose transitions depending of σ and when to stop taking transitions — the **run-to-completion "algorithm"**.

Contents & Goals

- **Last Lecture:**
 - Ether
 - System configuration
- **This Lecture:**
 - **Educational Objectives:** Capabilities for following tasks/questions:
 - What does this State Machine mean? What happens if I inject this event?
 - Can you please model the following behaviour?
 - What is: Signal, Event, Ether, Transformer, Step, RTC.
 - **Content:**
 - Transformer
 - Examples for transformer
 - Run-to-completion Step
 - Putting It All Together

System Configuration, Ether, Transformer

Transformer

not a function, to model non-determinism

Definition
 Let Σ, \mathcal{E} the set of system configurations over some $\mathcal{O}, \mathcal{S}_0, \mathcal{B}, \mathcal{H}$.
 We call a relation $\mathcal{T} \subseteq \Sigma \times \mathcal{E} \times \Sigma \times \mathcal{E}$ a **relation of system configurations**.

$$\mathcal{T} \subseteq \mathcal{O}(\mathcal{B}) \times (\mathcal{S}_0 \times \mathcal{B}) \times (\mathcal{S}_0 \times \mathcal{B})$$

 a (system configuration) **transformer**.
system configuration before executing the action

- In the following, we assume that each application of a transformer f to some system configuration (α, ε) for object u_x is associated with a set of **observations** $Obs(u_x | (\alpha, \varepsilon)) \subseteq \mathcal{O}(\mathcal{B}) \times \mathcal{E}$.
 - An observation $(u_x, \sigma, (E, \delta), \text{Msg}) \in Obs(u_x | (\alpha, \varepsilon))$ represents the information that, as a "side effect" of u_x executing ι , an event $(\iota, (E, \delta))$ has been sent from u_x to u_{id} .
- Special cases:** creation/destruction.

Why Transformers?

- Recall the (simplified) syntax of transition annotations:

$$\text{annot} ::= [\langle \text{event} \rangle \mid [\langle \text{guard} \rangle] \mid [\langle \text{action} \rangle]]$$
- **Clear:** $\langle \text{event} \rangle$ is from \mathcal{E} of the corresponding signature.
- **But:** What are $\langle \text{guard} \rangle$ and $\langle \text{action} \rangle$?
- UML can be viewed as being **parameterized** in **expression language** (providing $\langle \text{guard} \rangle$) and **action language** (providing $\langle \text{action} \rangle$).
- **Examples:**
 - **Expression Language:**
 - OCL
 - Java, C++, ... expressions
 - ...
 - **Action Language:**
 - UML Action Semantics, "Executable UML"
 - Java, C++, ... statements (plus some event send action)
 - ...

Transformers as Abstract Actions!

In the following, we assume that we're given

- an expression language $Expr$ for guards, and
 - an action language Act for actions,
- and that we're given
- a semantics for boolean expressions in form of a μ CCDL function

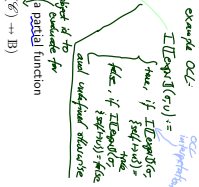
$$\llbracket \cdot \rrbracket : (\cdot) : Expr \rightarrow (\mathbb{S}^{\mathbb{S}} \times \mathcal{S}(\mathcal{C}) \rightarrow \mathbb{B})$$

which evaluates expressions in a given system configuration.

Assuming I to be partial is a way to treat "undefined" during runtime. If I is not defined (for instance because of dangling-reference navigation or division-by-zero), we want to go to a designated "error" system configuration.

a transformer for each action: for each $act \in Act$, we assume to have

$$t_{act} \subseteq \mathcal{S}(\mathcal{C}) \times (\mathbb{S}^{\mathbb{S}} \times Env) \times (\mathbb{S}^{\mathbb{S}} \times Env)$$



Expression/Action Language Examples

We can make the assumptions from the previous slide because instances exist:

- for OCL, we have the OCL semantics from Lecture 03. Simply remove the preimages which map to \perp .
- for Java, the operational semantics of the SWT lecture uniquely defines transformers for sequences of Java statements.

We distinguish the following kinds of transformers:

- **skip**: do nothing — recall: this is the default action
- **send**: modifies ε — interesting ε , because state machines are built around sending/consuming events
- **create/delete**: modify domain of σ — not specific to state machines, but let's discuss them here as we're at it
- **update**: modify own or other objects' local state — boring

Action Language

In the following we consider

$$Act_g := \{ skip \} \cup \{ \text{update}(expr_1, v, expr_2) \mid expr_1, expr_2 \in OCLExpr, v \in V \} \cup \{ \text{send}(expr, \varepsilon, expr_2) \mid expr_1, expr_2 \in OCLExpr, \varepsilon \in \mathcal{E} \} \cup \{ \text{create}(c, expr, v) \mid c \in C, expr \in OCLExpr, v \in V \} \cup \{ \text{delete}(expr) \mid expr \in OCLExpr \}$$

Expr_g: OCL expressions over \mathcal{P}

Transformer Examples: Presentation

abstract syntax	op $update(c, v, e)$	concrete syntax	$e, v \vdash e$
intuitive semantics	...		
well-typedness	...		
semantics	$\llbracket (c, \varepsilon) \rrbracket (c', \varepsilon') \in Env[Env_2] \text{ iff } \dots$ or $t_{op}[Env_1][c, \varepsilon] = \{ (c', \varepsilon') \}$ where ...		
observables	$O[update(c, v, e)] = \{ \dots \}$, not a relation, depends on choice		
(error) conditions	Not defined if ...		

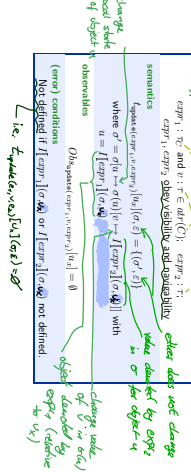
Transformer: Skip

abstract syntax	skip	concrete syntax	skip
intuitive semantics	do nothing		
well-typedness	/		
semantics	$\llbracket skip \rrbracket (c, \varepsilon) = \{ (c, \varepsilon) \}$		
observables	$O[skip][c, \varepsilon] = \emptyset$		
(error) conditions			

"if v_c exceeds v_d on (c, ε) , then the result is (c, ε) "

Transformer: Update

abstract syntax	update(c_1, v, c_2)	concrete syntax	$expr_1, v \vdash expr_2$
intuitive semantics	Update attribute v in the object denoted by $expr_1$ to the value denoted by $expr_2$.		
well-typedness	$expr_1 : \tau_c$ and $v : \tau_v \in \text{attr}(C)$, $expr_2 : \tau_v$		
semantics	$\llbracket update(c_1, v, c_2) \rrbracket (c, \varepsilon) = \{ (c', \varepsilon') \}$ where $c' = c[c_1 \mapsto \sigma(c_2)]$ or $\llbracket expr_2 \rrbracket (c, \varepsilon)$ with $\sigma = \llbracket expr_1 \rrbracket (c, \varepsilon)$		
observables	$O[update(c_1, v, c_2)](c, \varepsilon) = \emptyset$		
(error) conditions	Not defined if $\llbracket expr_1 \rrbracket (c, \varepsilon)$ or $\llbracket expr_2 \rrbracket (c, \varepsilon)$ not defined		



Update Transformer Example

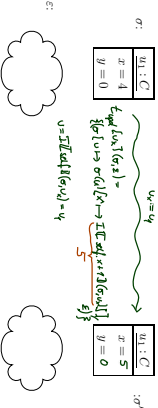
SMC:

S1

$f_x = x + 1$
 $\text{self } x$

S2

```
update(capt1, v, capt2)
 $f_{\text{update}}(\text{cap}_1, \text{cap}_2)(s) = (s[x] \leftarrow \sigma(s)[v]) \rightarrow [f_{\text{update}}](\sigma(s)) \cdot s$ 
 $v = [f_{\text{update}}](\sigma(s))$ 
```



$\sigma^2 = \sigma$

Transformer: Send

abstract syntax

$\text{send}(E(cap_1, \dots, cap_n), cap_{n+1})$

concrete syntax $\text{cap}_n \text{ ! } E(\text{cap}_1, \dots, \text{cap}_n)$

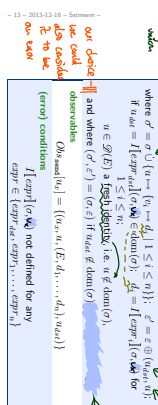
infixive semantics

Object $v_n : C$ sends event E to object cap_{n+1} . To create a fresh signal instance, fill in its attributes, and place it in the other well-synchronised cap_{n+1} .

well-synchronised $\text{cap}_{n+1} : \text{Type } C, D \in \mathcal{S} \wedge \mathcal{E}, E \in \mathcal{E}; \text{ all expressions obey stability and taggability in } C$

$\text{obj}(E) = \{(v_1, \dots, v_n) \mid \exists (s) \in \text{dom}(s) \cdot v_i = s[x_i] \text{ for } 1 \leq i \leq n\}$

semantics $\llbracket \text{send}(E(\text{cap}_1, \dots, \text{cap}_n), \text{cap}_{n+1}) \rrbracket (s) = \exists (s') \cdot s \rightarrow s' \wedge s' \in \text{dom}(s') \wedge \text{obj}(E) \subseteq \text{dom}(s') \wedge \llbracket \text{cap}_{n+1} \rrbracket (s')$



$\sigma^2 = \sigma$

Send Transformer Example

SMC:

S1

$\text{self } x$
 $\text{obj } E$
 cap_n

S2

```
send(E(cap_1, ..., cap_n), cap_{n+1})
 $\llbracket \text{send}(E(\text{cap}_1, \dots, \text{cap}_n), \text{cap}_{n+1}) \rrbracket (s) = \dots$ 
```



$\sigma^2 = \sigma$

References

[Harel and Gery, 1997] Harel, D. and Gery, E. (1997). Executable object modeling with statecharts. *IEEE Computer*, 30(7):31–42.

[OMG, 2007a] OMG (2007a). Unified modeling language: Infrastructure, version 2.1.2. Technical Report formal/07-11-04.

[OMG, 2007b] OMG (2007b). Unified modeling language: Superstructure, version 2.1.2. Technical Report formal/07-11-02.