

Software Design, Modelling and Analysis in UML

Lecture 14: Core State Machines IV

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Contents & Goals

Last Lecture:

- System configuration
- Transformer
- Action language: skip, update, send

This Lecture:

- Educational Objectives: Capabilities for following tasks/questions:
 - What does this State Machine mean? What happens if I inject this event?
 - Can you please model the following behaviour.
 - What is: Signal, Event, Ether, Transformer, Step, RTC.

Content:

- Transformers for Action Language
- Run-to-completion Step
- Putting It All Together

Transformer Cont'd

Transformer: Create

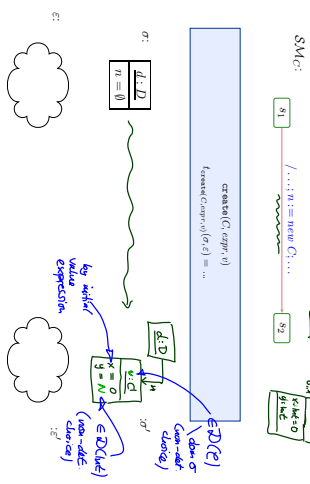
abstract syntax	create(C, expr, v)
concrete syntax	expr.v = new C
infixive semantics	Create an object of class C and assign it to attribute v of the object
denoted by expression expr.	
well-typedness	expr : T _D , v ∈ attr(D), attr(C) = {{v1 : T1, v2 : T2} 1 ≤ i ≤ n}
semantics	...
observables	...
(error) conditions	[[expr]](C, β) not defined

(4) 20 Apr: x := (new C) * + (new C) y

if needed
 obj := new C
 x := obj * x
 obj := obj * y
 obj := obj * z

• We use an "and assign" action for simplicity — it doesn't add or remove expressive power, but moving creation to the expression language raises all kinds of other problems such as order of evaluation (and thus creation!)
 • Also for simplicity: no parameters to construction (= parameters of constructor). Adding them is straightforward (but somewhat tedious).

Create Transformer Example



How To Choose New Identities?

- Re-use: choose any identity that is not alive now, i.e. not in dom(σ). *our choice*
- Doesn't depend on history.
- May "undangle" dangling references — may happen on some platforms.
- Fresh: choose any identity that has not been alive ever, i.e. not in dom(σ) and any predecessor in current run.
- Depends on history.
- Dangling references remain dangling — could mask "dirty" effects of platform.

Transformer: Create

abstract syntax	concrete syntax
<p>create(C; expr; v) Create an object of class C and assign it to attribute v of the object</p> <p>well-spreadness $expr : \tau_C, v \in \text{attr}(D), \text{attr}(C) = \{(v_1 : \tau_1, \text{expr}_i^j) \mid 1 \leq i \leq n\}$</p> <p>semantics $\langle \sigma, \varepsilon \rangle, (\sigma', \varepsilon') \in \text{step}$ is the newly created object iff $\sigma' = \sigma \uparrow v \uparrow (u_0 \mapsto \text{eval}(\text{expr}))$ $\varepsilon' = \varepsilon \uparrow v \uparrow (u_0 \mapsto \text{eval}(\text{expr}))$ if $\sigma' = \sigma \uparrow v \uparrow (u_0 \mapsto \text{eval}(\text{expr}))$ and u_0 is not in $\text{dom}(\sigma)$, then $u_0 = \llbracket \text{expr} \rrbracket(\sigma, \varepsilon), d_i = \llbracket \text{expr}_i^j \rrbracket(\sigma, \varepsilon)$ if $\text{expr}_i^j \neq \text{fresh}$ arbitrary value from $\mathcal{D}(\tau_i)$ otherwise</p> <p>observables $\text{Obs}_{\text{create}}[u_0] = \{(u_0, \perp, (\sigma, \varepsilon), h)\}$ <i>if class τ_C is not final</i></p> <p>(error) conditions $\llbracket \text{expr} \rrbracket(\sigma)$ not defined.</p>	

7.9

Transformer: Destroy

abstract syntax	concrete syntax
<p>destroy(expr) Destroy the object denoted by expression expr.</p> <p>well-spreadness $expr : \tau_C, C \in \mathcal{C}$</p> <p>semantics ...</p> <p>observables $\text{Obs}_{\text{destroy}}[u_0] = \{(u_0, \perp, (\perp, \emptyset), n)\}$</p> <p>(error) conditions $\llbracket \text{expr} \rrbracket(\sigma, \varepsilon)$ not defined.</p>	<i>delete expr</i>

8.9

What to Do With the Remaining Objects?

Assume object u_0 is destroyed...

- object v_1 may still refer to it via association r .
- allow dangling references?
- or remove u_0 from $\sigma(v_1, r)$?
- object u_0 may have been the last one linking to object u_2 .
- leave u_2 alone?
- or remove u_2 also? (*garbage collection!*)

Plus: (temporal extensions of) OCL may have dangling references.

Our choice: Dangling references and no garbage collection!
 This is in line with "expect the worst", because there are target platforms which don't provide garbage collection — and models shall (in general) be correct without assumptions on target platform.

But: the more "dirty" effects we see in the model, the more expensive it often is to analyse. Valid proposal for simple analysis: monotone frame semantics, no destruction at all.

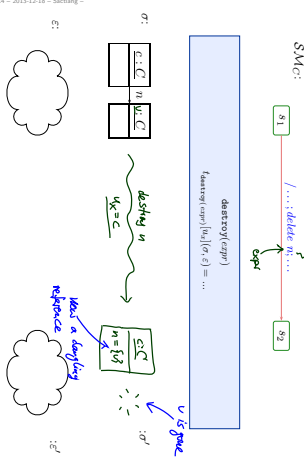
10.9

Transformer: Destroy

abstract syntax	concrete syntax
<p>destroy(expr) Destroy the object denoted by expression expr.</p> <p>well-spreadness $expr : \tau_C, C \in \mathcal{C}$</p> <p>semantics $\langle u_0 \rangle(\sigma, \varepsilon) = \langle r' \rangle(\sigma', \varepsilon')$ <i>function notations</i> where $\sigma' = \sigma \uparrow \text{dom}(\sigma) \setminus \{u_0\}$ with $u = \llbracket \text{expr} \rrbracket(\sigma, \varepsilon)$.</p> <p>observables $\text{Obs}_{\text{destroy}}[u_0] = \{(u_0, \perp, (\perp, \emptyset), n)\}$</p> <p>(error) conditions $\llbracket \text{expr} \rrbracket(\sigma, \varepsilon)$ not defined.</p>	

11.9

Destroy Transformer Example



9.9

Sequential Composition of Transformers

- Sequential composition** $t_1 \circ t_2$ of transformers t_1 and t_2 is canonically defined as $(\tau_2 \circ \tau_1)(u_0) \langle \sigma, \varepsilon \rangle = \tau_2(u_0) \langle \tau_1(\sigma), \varepsilon \rangle$ with observation

$$\text{Obs}_{(t_1 \circ t_2)[u_0]}(\sigma, \varepsilon) = \text{Obs}_{t_1}[u_0](\sigma, \varepsilon) \cup \text{Obs}_{t_2}[u_0](\tau_1(\sigma, \varepsilon))$$

Clear: not defined if one of the two intermediate "micro steps" is not defined.

Handwritten notes: $x = x' / j, \text{delete } u_1, j, u_1' / \tau$
 τ send (= delete (= update (p/d)))

12.9

Observation: our transformers are in principle the **denotational semantics** of the actions/ action sequences. The trivial case, to be precise.

Note: with the previous examples, we can capture while, $k = x - 1$, $k < x$, $k = x - 1$

- empty statements, skips,
 - assignments,
 - conditionals (by normalisation and auxiliary variables),
 - create/destroy,
- but not possibly diverging loops.

Our (Simple) Approach: if the action language is, e.g.: Java, then (syntactically) forbid loops and calls of recursive functions.

Other Approach: use full blown denotational semantics.

No show-stopper, because loops in the action annotation can be converted into transition cycles in the state machine.

Step and Run-to-completion Step

Definition. Let A be a set of actions and S a (not necessarily finite) set of states.

We call

$$\rightarrow \subseteq S \times A \times S$$

a (labelled) transition relation.

Let $S_0 \subseteq S$ be a set of initial states. A sequence

$$s_0 \xrightarrow{a_0} s_1 \xrightarrow{a_1} s_2 \xrightarrow{a_2} \dots$$

with $s_i \in S_i$, $a_i \in A$ is called **computation of the labelled transition system** (S, \rightarrow, S_0) if and only if

- **inflation:** $s_0 \in S_0$
- **consecution:** $(s_i, a_i, s_{i+1}) \in \rightarrow$ for $i \in \mathbb{N}_0$.

Note: for simplicity, we only consider infinite runs.

Active vs. Passive Classes/Objects

- **Note:** From now on, assume that all classes are **active** for simplicity. We'll later briefly discuss the Rhapsody framework which proposes a way how to integrate non-active objects.

- **Note:** The following RT-C "algorithm" follows [Harel and Gery, 1997] (i.e. the one realised by the Rhapsody code generation) **where** the standard is ambiguous or leaves choices.

From Core State Machines to LTS

Definition. Let $\mathcal{S}_0 = (\mathcal{S}_0, \mathcal{K}_0, \gamma_0, \text{act}, \sigma, \mathcal{E})$ be a signature with signals (all classes **active**) \mathcal{S}_0 , a structure of \mathcal{S}_0 , and $(EBM, \text{ready}, \Phi, \Theta, \Gamma)$ an ether over \mathcal{S}_0 and \mathcal{S}_0 . Assume there is one core state machine M_C per class $C \in \mathcal{E}$.

We say, the state machines **induce** the following labelled transition relation on states

$$S := (\mathcal{S}_0 \cup \{\#\}) \times EBM \text{ with actions } A := (\mathcal{E}^{\text{in}} \cup \{\text{error}\} \cup \{\text{L}, \text{R}\} \cup \{\text{err}, \text{err}'\}) \times \mathcal{E}^{\text{out}}$$

- $(\sigma, \varepsilon) \xrightarrow{\text{error}} (\sigma', \varepsilon')$ if and only if $\sigma' = \text{error state}$
- $(\sigma, \varepsilon) \xrightarrow{\text{consum.}} \#$ if an event with destination u is discarded.
- (i) an event is dispatched to u, i i.e. stable object processes an event, or (ii) run-to-completion processing by u commences. i.e. object u is not stable and continues to process an event.
- (iv) the environment interacts with object u .
- $\# \xrightarrow{\text{consum.}} \#$ if and only if $\#$ and $\text{cons} = \emptyset$, or an error condition occurs during consumption of cons .

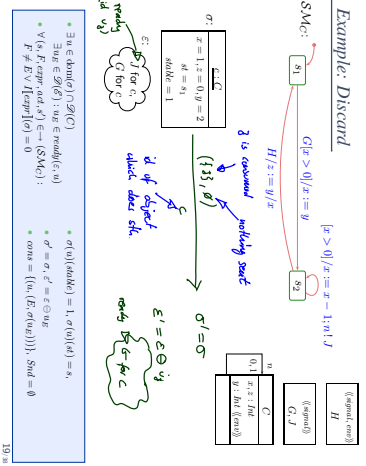
(i) Discarding An Event

if $(\sigma, \varepsilon) \xrightarrow{\text{consum.}} (\sigma', \varepsilon')$

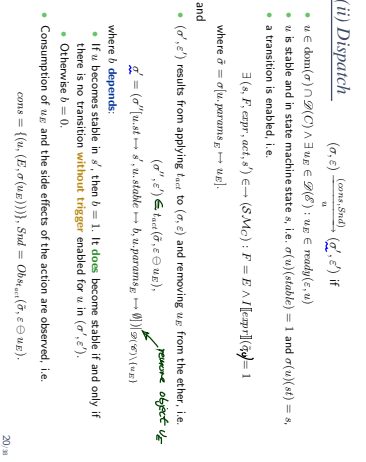
- an E -event (instance of signal E) is ready in ε for object u of a class \mathcal{K} , i.e. if $u \in \text{dom}(\sigma) \cap \mathcal{D}(C) \wedge \exists u \varepsilon \in \mathcal{D}(\mathcal{K})$; $u \varepsilon \in \text{ready}(C, u)$
 - u is stable and in state machine state s_i , i.e. $\sigma(u)(\text{stable}) = 1$ and $\sigma(u)(s) = s_i$
 - but there is no corresponding transition enabled (all transitions incident with current state of u either have other triggers or the guard is not satisfied)
- $$V(s_i, F, \text{app}, \text{act}, s') \in \neg (SM_C) : F \neq EV \wedge \text{app}[a] = 0$$

- and
- the system configuration doesn't change, i.e. $\sigma' = \sigma$
 - the event $u \varepsilon$ is removed from the ether, i.e. $\varepsilon' = \varepsilon \ominus u \varepsilon$
 - consumption of $u \varepsilon$ is observed, i.e. $\text{cons} = ((u, E, \sigma(u \varepsilon)))$; $\text{Stnd} = \emptyset$

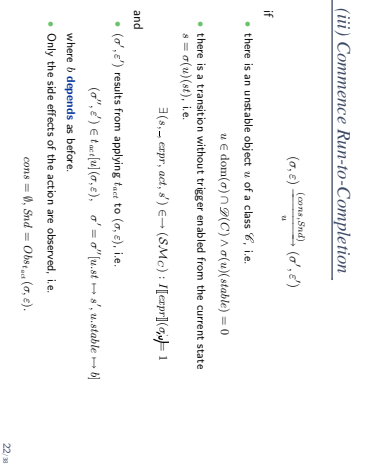
Example: Discard



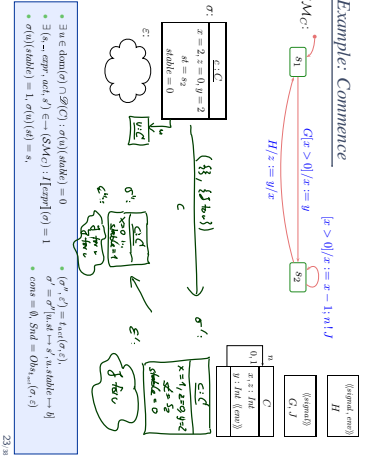
(ii) Dispatch



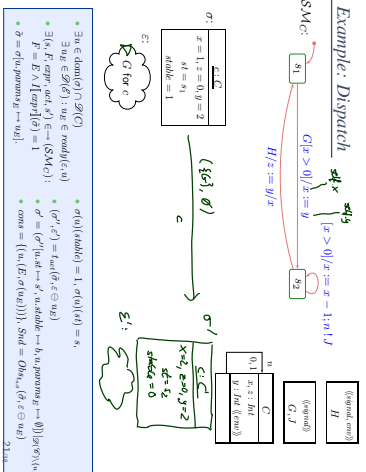
(iii) Commence Run-to-Completion



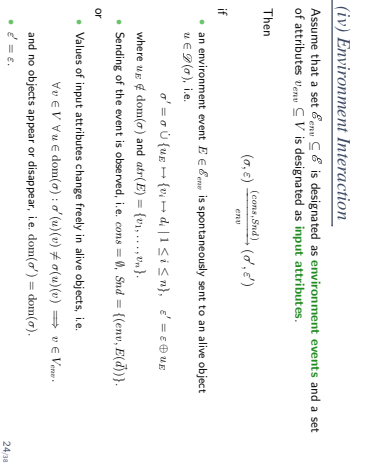
Example: Commence

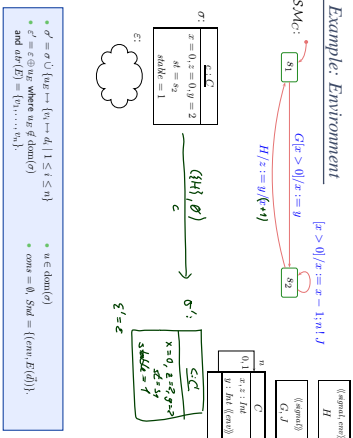


Example: Dispatch



(iv) Environment Interaction





Notions of Steps: The Step

Note: we call one evolution $(\sigma, \varepsilon) \xrightarrow{(cons, Stnd)} (\sigma', \varepsilon')$ a **step**.
Thus in our setting, a **step directly corresponds** to **one object** (namely v) takes a **single transition** between regular states. (We have to extend the concept of "single transition" for hierarchical state machines.)
That is: We're going for an interleaving semantics without true parallelism.
Remark: With only methods (later), the notion of step is not so clear.
For example, consider

- c_1 calls εO at c_2 , which calls εO at c_1 which in turn calls εO for c_2 .
- Is the completion of εO a step?
- Or the completion of εO ?
- Or doesn't it play a role?

It does play a role, because **constraints/invariants** are typically (= by convention) assumed to be evaluated at step boundaries, and sometimes the convention is meant to admit (temporary) violation in between steps.

(v) Error Conditions

if, in (ii) or (iii),

- $\llbracket \text{Error} \rrbracket$ is not defined for σ , or
- last is not defined for (σ, ε) ,

and

- consumption is observed according to (ii) or (iii), but $Stnd = \emptyset$.

Examples

State Machine (SMc):

- States: s_1, s_2
- Transitions: $s_1 \xrightarrow{E[exp] / x := x/0} s_2$, $s_1 \xrightarrow{E[trans] / last} s_2$

Notions of Steps: The Run-to-Completion Step

What is a **run-to-completion step**...?

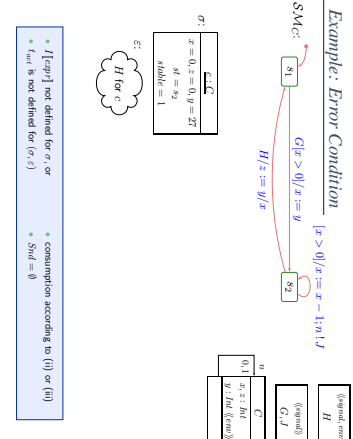
- Intuition:** a maximal sequence of steps, where the first step is a **dispatch** step and all later steps are **commence** steps.
- Note:** one step corresponds to one transition in the state machine.

A run-to-completion step is in general not syntactically definable — one transition may be taken multiple times during an RTC-step.

Example:

State Machine (SMc):

- States: s_1, s_2
- Transitions: $s_1 \xrightarrow{E[x > 0] / x := x - 1} s_2$



Notions of Steps: The Run-to-Completion Step Cont'd

Proposal: Let

$$(\sigma_0, \varepsilon_0) \xrightarrow{(cons, Stnd)} \dots \xrightarrow{(cons, Stnd)} (\sigma_n, \varepsilon_n), \quad n > 0,$$

be a finite (i), non-empty, maximal, consecutive sequence such that

- object v is alive in σ_0 ,
- $v_{in} = u$ and $(cons, Stnd)$ indicates dispatching to u , i.e. $cons = \{(c_i, v^i) \rightarrow \bar{d}\}$,
- there are no receptors by u in between, i.e. $cons \cap \{v\} \times Env(\varepsilon, \mathcal{D}) = \emptyset, \forall i > 1$,
- $v_{in-1} = u$ and u is stable only in σ_0 and σ_n , i.e. $\sigma_0(v)(stable) = \sigma_n(v)(stable) = 1$ and $\sigma_i(v)(stable) = 0$ for $0 < i < n$.

Let $0 = k_1 < k_2 < \dots < k_N = n$ be the maximal sequence of indices such that $u_{k_i} = u$ for $1 \leq i \leq N$. Then we call the sequence

$$(\sigma_0(v) \Rightarrow) \sigma_{k_1}(v), \sigma_{k_2}(v), \dots, \sigma_{k_N}(v) \quad (= \sigma_{k_i-1}(v))$$

a (i) **run-to-completion computation** of u (from (local) configuration $\sigma_0(v)$)

We say, object u can diverge on reception *cons* from (local) configuration $\sigma_0(u)$ if and only if there is an infinite, consecutive sequence

$$(\sigma_0, \varepsilon_0) \xrightarrow{(\text{cons}, \text{Send}_0)} (\sigma_1, \varepsilon_1) \xrightarrow{(\text{cons}, \text{Send}_1)} \dots$$

such that u doesn't become stable again.

- **Note:** disappearance of object not considered in the definitions. By the current definitions, it's neither divergence nor an RTC-step.

What people may **debate** on our definition of RTC-step is that it takes a **global** and **non-compositional** view. That is:

- in the projection onto a single object we still **see** the effect of interaction with other objects.
 - Adding classes (or even objects) may change the divergence behaviour of existing ones.
 - Compositional would be: the behaviour of a set of objects is determined by the behaviour of each object "in isolation".
- Our semantics and notion of RTC-step doesn't have this (often desired) property.

Can we give (syntactical) criteria such that any global run-to-completion step is an interleaving of local ones?

Maybe: **Strict interfaces.** (Proof left as exercise...)

- (A): Refer to private features only via "self".
- (B): Let objects only communicate by events, i.e. don't let them modify each other's local state via links at all.

Putting It All Together

The Missing Piece: Initial States

Recall: a labelled transition system is (S, \rightarrow, S_0) . We have

- S : system configurations (σ, ε)
- \rightarrow : labelled transition relation $(\sigma, \varepsilon) \xrightarrow{(\text{cons}, \text{Send}_0)} (\sigma', \varepsilon')$.
- S_0 : initial states S_0 .

Proposal:

Require a (finite) set of **object diagrams** $OD \in \mathcal{O}^{\mathcal{D}_0, \varepsilon}$ empty}.

And set

$$S_0 = \{(\sigma, \varepsilon) \mid \sigma \in G^{-1}(OD), OD \in \mathcal{O}^{\mathcal{D}_0, \varepsilon} \text{ empty}\}$$

Other Approach: (used by Rhapsody tool) multiplicity of classes. We can read that as an abbreviation for an object diagram.

Semantics of UML Model — So Far

The semantics of the UML model

$$\mathcal{M} = (\mathcal{C}_0, \mathcal{K}, \mathcal{O}_0)$$

where

- some classes in \mathcal{C}_0 are stereotyped as "signal" (standard), some signals and attributes are stereotyped as "external" (non-standard).
 - there is a 1-to-1 relation between classes and state machines
 - \mathcal{O}_0 is a set of object diagrams over \mathcal{C}_0 .
- is the **transition system** (S, \rightarrow, S_0) constructed on the previous slide.

The computations of \mathcal{M} are the computations of (S, \rightarrow, S_0) .

OCCL Constrains and Behaviour

- Let $\mathcal{M} = (\mathcal{C}_0, \mathcal{K}, \mathcal{O}_0)$ be a UML model.
- We call \mathcal{M} **consistent** iff for each OCCL constraint $\text{expr} \in \text{Inv}(\mathcal{C}_0)$, $\sigma \models \text{expr}$ for each "reasonable point" (σ, ε) of computations of \mathcal{M} . (Cf. exercises and tutorial for discussion of "reasonable point".)

Note: we could define $\text{Inv}(\mathcal{K})$ similar to $\text{Inv}(\mathcal{C}_0)$.

Pragmatics:

- In **UML-as-blueprint** mode, if \mathcal{K} doesn't exist yet, then $\mathcal{M} = (\mathcal{C}_0, \emptyset, \mathcal{O}_0)$ is typically asking the developer to provide \mathcal{K} such that $\mathcal{M}' = (\mathcal{C}_0, \mathcal{K}, \mathcal{O}_0)$ is consistent.
- If the developer makes a mistake, then \mathcal{M}' is inconsistent.
- **Not common:** if \mathcal{K} is given, then constraints are also considered when choosing transitions in the RTC-algorithm. In other words: even in presence of mistakes, the \mathcal{K} never move to inconsistent configurations.

References

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