

# Software Design, Modelling and Analysis in UML

## Lecture 02: Semantical Model

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### Contents & Goals

#### Last Lecture:

- Motivation: model-based development of things (houses, software) to cope with complexity; detect errors early
- Model-based (or -driven) Software Engineering
- UML Mode of the Lecture: Blueprint.

#### This Lecture:

- **Educational Objectives:** Capabilities for these tasks/questions:
  - Why is UML of the form it is?
  - Shall one feel bad if not using all diagrams during software development?
  - What is a signature, an object, a system state, etc.?
  - What's the purpose of signature, object, etc. in the course?
  - How do Basic Object System Signatures relate to UML class diagrams?

#### Content:

- Brief history of UML
- Basic Object System Signature, Structure, and System State

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### Why (of all things) UML?

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- [Kerens and Baining, 2008] compares as examples:
  - Pre-Note: being a **modelling** languages doesn't mean being graphical (or: being a visual formalism [Harel]).
  - Sets, Relations, Functions
  - Terms and Algebras
  - Propositional and Predicate Logic
  - Graphs
  - XML Schema, Entity Relation Diagrams, UML Class Diagrams
  - Finite Automata, Petri Nets, UML State Machines

• **Pro:** visual formalisms are found appealing and easier to **grasp**. Yet they are not necessarily easier to **write!**

• **Beware:** you may meet people who dislike visual formalisms just for being graphical — maybe because it's easier to "trick" people with a meaningless picture than with a meaningless formula.

More serious: it's maybe easier to misunderstand a picture than a formula.

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### A Brief History of UML

- Boxes/lines and finite automata are used to visualise software for ages.
- 1970's: **Software Crick**™
  - Idea: learn from engineering disciplines to handle growing complexity. Languages: Flowcharts, Nassi-Shneiderman, Entity-Relation Diagrams
- Mid 1980's: **Statecharts** [Harel, 1987], **StateMate**™ [Harel et al., 1990]

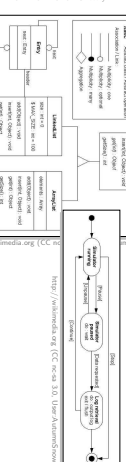


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- Mid 1980's: **Statecharts** [Harel, 1987], **StateMate**™ [Harel et al., 1990]
  - Inflation of notations and methods, most prominent:
- **Object-Modeling Technique (OMT)** [Fumbaugh et al., 1990]



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**Definition.** A Basic Object System Structure of  $\mathcal{S} = (\mathcal{C}, \mathcal{V}, \text{atr})$  is a domain function  $\mathcal{D}$  which assigns to each type a domain, i.e.

- $\tau \in \mathcal{S}$  is mapped to  $\mathcal{D}(\tau)$ .
- $C \in \mathcal{C}$  is mapped to an idyllic set  $\mathcal{D}(C)$  of (object) identities.

Note: Object identities only have the "-" operation; object identities of different classes are disjoint, i.e.  $\forall C, D \in \mathcal{C} : C \neq D \rightarrow \mathcal{D}(C) \cap \mathcal{D}(D) = \emptyset$ .

- $C_+$  and  $C_{0+}$  for  $C \in \mathcal{C}$  are mapped to  $\mathcal{D}(C)$ .

We use  $\mathcal{D}(\mathcal{C})$  to denote  $\bigcup_{C \in \mathcal{C}} \mathcal{D}(C)$ ; analogously  $\mathcal{D}(\mathcal{V})$ .

**Note:** We identify objects and object identities, because both uniquely determine each other (cf. OCL 2.0 standard).

**Wanted:** a structure for signature

$$\mathcal{S}_0 = (\{Int\}, \{C, D\}, \{x : Int, p : C_{0+}, n : C_+, \{C\} \mapsto \{n, n\}, D \mapsto \{x\}\})$$

Recall: by definition, seek a  $\mathcal{D}$  which maps

- $\tau \in \mathcal{S}$  to some  $\mathcal{D}(\tau)$ .
- $c \in \mathcal{C}$  to some identities  $\mathcal{D}(C)$  (infinite, disjoint for different classes).
- $C_+$  and  $C_{0+}$  for  $C \in \mathcal{C}$  to  $\mathcal{D}(C_{0+}) = \mathcal{D}(C) = 2^{\mathcal{D}(C)}$ .

$$\begin{aligned} \mathcal{D}(Int) &= \mathbb{Z} \\ \mathcal{D}(C) &= \mathcal{M}^{\mathbb{Z}} \times \{0\} = \{1, c_{-1}, \dots\} \\ \mathcal{D}(D) &= \mathcal{M}^{\mathbb{Z}} \times \mathbb{R} = \{1, b_{-2}, b_{-3}, \dots\} \\ \mathcal{D}(C_{0+}) &= \mathcal{D}(C) = 2^{\mathcal{D}(C)} \\ \mathcal{D}(C_+) &= \mathcal{D}(C) = 2^{\mathcal{D}(C)} \\ \mathcal{D}(D_{0+}) &= \mathcal{D}(D) = 2^{\mathcal{D}(D)} \end{aligned}$$

System State

**Definition.** Let  $\mathcal{S}$  be a structure of  $\mathcal{S} = (\mathcal{C}, \mathcal{V}, \text{atr})$ . A system state of  $\mathcal{S}$  wrt.  $\mathcal{S}$  is a type-consistent mapping  $\sigma : \mathcal{D}(\mathcal{C}) \rightarrow \mathcal{V} \rightarrow (\mathcal{D}(\mathcal{S}) \cup \mathcal{D}(\mathcal{V}))$ . That is, for each  $u \in \mathcal{D}(C)$ ,  $C \in \mathcal{C}$ , if  $u \in \text{dom}(\sigma)$

- $\text{dom}(\sigma(u)) = \text{atr}(C)$
- $\sigma(u)(v) \in \mathcal{D}(\tau)$  if  $v : \tau, \tau \in \mathcal{S}$
- $\sigma(u)(v) \in \mathcal{D}(D_+)$  if  $v : D_+, n : D_+$ , with  $D \in \mathcal{C}$

We call  $u \in \mathcal{D}(\mathcal{C})$  alive in  $\sigma$  if and only if  $u \in \text{dom}(\sigma)$ . We use  $\Sigma_{\mathcal{S}}$  to denote the set of all system states of  $\mathcal{S}$  wrt.  $\mathcal{S}$ .

System State Example

**Signature, Structure:**

$$\mathcal{S}_0 = (\{Int\}, \{C, D\}, \{x : Int, p : C_{0+}, n : C_+, \{C\} \mapsto \{n, n\}, D \mapsto \{x\}\})$$

$$\mathcal{D}(Int) = \mathbb{Z}, \quad \mathcal{D}(C) = \{1, c_1, 2c_1, 3c_1, \dots\}, \quad \mathcal{D}(D) = \{1, d_1, 2d_1, 3d_1, \dots\}$$

**Wanted:**  $\sigma : \mathcal{D}(\mathcal{C}) \rightarrow \mathcal{V} \rightarrow (\mathcal{D}(\mathcal{S}) \cup \mathcal{D}(\mathcal{V}))$  such that for all  $u \in \text{dom}(\sigma)$

- $\text{dom}(\sigma(u)) = \text{atr}(C)$ .
- $\sigma(u)(v) \in \mathcal{D}(\tau)$  if  $v : \tau, \tau \in \mathcal{S}$ .
- $\sigma(u)(v) \in \mathcal{D}(D_+)$  if  $v : D_+, n : D_+$ , with  $D \in \mathcal{C}$ .

**Concrete example:**

$$\sigma = \{ \{c_1 \mapsto 2, d_1 \mapsto \{1, n\}\}, \{2c_1 \mapsto 3, d_1 \mapsto \{2, n\}\}, \dots \}$$

System State Example

**Signature, Structure:**

$$\mathcal{S}_0 = (\{Int\}, \{C, D\}, \{x : Int, p : C_{0+}, n : C_+, \{C\} \mapsto \{n, n\}, D \mapsto \{x\}\})$$

$$\mathcal{D}(Int) = \mathbb{Z}, \quad \mathcal{D}(C) = \{1, c_1, 2c_1, 3c_1, \dots\}, \quad \mathcal{D}(D) = \{1, d_1, 2d_1, 3d_1, \dots\}$$

**Wanted:**  $\sigma : \mathcal{D}(\mathcal{C}) \rightarrow \mathcal{V} \rightarrow (\mathcal{D}(\mathcal{S}) \cup \mathcal{D}(\mathcal{V}))$  such that

- $\text{dom}(\sigma(u)) = \text{atr}(C)$ .
- $\sigma(u)(v) \in \mathcal{D}(\tau)$  if  $v : \tau, \tau \in \mathcal{S}$ .
- $\sigma(u)(v) \in \mathcal{D}(D_+)$  if  $v : D_+, n : D_+$ , with  $D \in \mathcal{C}$ .

**Concrete, explicit:**

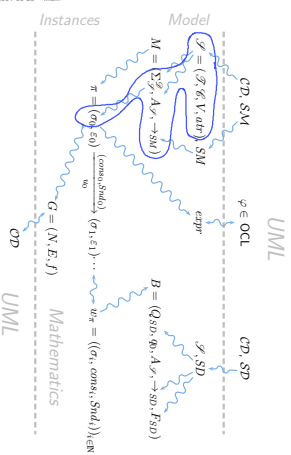
$$\sigma = \{1, c_1 \mapsto \{p \mapsto 0, n \mapsto \{5, c_1\}\}, 5, c_1 \mapsto \{p \mapsto 0, n \mapsto 0\}, 1, d_1 \mapsto \{x \mapsto 23\}\}$$

**Alternative, symbolic system state**

$$\sigma = \{c_1 \mapsto \{p \mapsto 0, n \mapsto \{c_2\}\}, c_2 \mapsto \{p \mapsto 0, n \mapsto 0\}, d_1 \mapsto \{x \mapsto 23\}\}$$

You Are Here

## Course Map



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