Software Design, Modelling and Analysis in UML

Lecture 11: Core State Machines I

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The Rest

Recapitulation: Consider the following association:

 $\langle r:\langle role_1:C_1,\mu_1,P_1,\xi_1,\nu_1,o_1\rangle,\ldots,\langle role_n:C_n,\mu_n,P_n,\xi_n,\nu_n,o_n\rangle\rangle$

- Association name r and role names/types $role_i/C_i$ induce extended system states λ .
- Multiplicity μ is considered in OCL syntax.
- Visibility ξ/Navigability ν: well-typedness

Now the rest:

- Multiplicity \(\mu\): we propose to view them as constraints.
- Properties P_i: even more typing.
- Ownership o: getting closer to pointers/references.

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Contents & Goals

Last Lecture:

Associations (up to some rest)

- This Lecture:
- Educational Objectives: Capabilities for following tasks/questions. What does this State Machine mean? What happens if I inject this event?
 Can you please model the following behaviour:
 What is: Signal, Event, Ether, Transformer, Step, RTC.
- Content:
- Associations cont'd, back to main track
 Core State Machines
 UML State Machine syntax

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Associations: The Rest

Visibility

Visibility of role-names is treated similar to attributes, by typing rules. Question: given Selfac OK

is the following OCL expression well-typed or not (wrt. visibility):

 ${\tt context}\ C\ {\tt inv}: self.role.x>0$

Basically the same rule as before (similar for other multiplicities):

 $role(expr_1(w)): \tau_C \rightarrow \tau_D$ role(w) : $\tau_C \rightarrow \tau_D$ $\mu = 0..1 \text{ or } \mu = 1, \ expr_1(w) : \tau_C,$ $w: \tau_{C_1}$, and $C_1 = C$ or $\underline{\xi} = +$ $\mu = 0..1 \text{ or } \mu = 1$,

Navigability

Navigability is similar to visibility: expressions over non-navigable association ends ($\nu=\times$) are basically type-correct, but forbidden.

Question: given

D

is the following OCL expression well-typed or not (wrt. navigability)?

 ${\tt context}\ D\ {\tt inv}: self.role.x > 0$

The standard says: navigation is...

'-': ...possible '>': ...efficient 'x': ...not possible

But: Pointers/references can faithfully be modelled by UML associations So: In general, UML associations are different from pointers/references!

The Rest of the Rest

Recapitulation: Consider the following association:

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- Multiplicity μ is considered in OCL syntax. Association name r and role names/types $role_i/C_i$ induce extended system states λ .
- Visibility ξ/Navigability ν: well-typedness

Now the rest

- Multiplicity μ: we propose to view them as constraints.
- Properties P_i: even more typing.
- Ownership o: getting closer to pointers/references.
- Diamonds: exercise.

Multiplicities as Constraints Example

$$\begin{split} \mu_{\text{OCL}}^{G}(role) &= \text{context } C \text{ inv :} \\ (N_{1} \leq role -> \text{size}() \leq N_{2}) \text{ or } \dots \text{ or } (N_{2k-1} \leq role -> \text{size}() \leq N_{2k}) \end{split}$$

but.
$$CD: robe_1 C$$
 So equiphed to $CD: robe_1 C$ So $CD: robe_1$

0.0,4.1



- * { constact C inv: 46 releptoral 64 or 17 trolleptoral 1617, (x)}

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Multiplicities as Constraints

Multiplicities as Constraints

Recall: The multiplicity of an association end is a term of the form:

$$\mu ::= \ast \mid N \mid N..M \mid N..\ast \mid \mu, \mu \tag{$N,M \in \mathbb{N}$}$$

Proposal: View multiplicities (except 0..1, 1) as additional invariants/constraints

Recall: we can normalize each multiplicity μ to the form

$$\mu = \underbrace{N_1..N_2}_{N_1..N_2}, \ldots, \underbrace{N_{2k-1}..N_{2k}}_{N_2}$$

where $N_i \leq N_{i+1}$ for $1 \leq i \leq 2k$, $N_1, \dots, N_{2k-1} \in \mathbb{N}$, $N_{2k} \in \mathbb{N} \cup \{*\}$.

Note: in n-ary associations with n > 2, there is redundancy.

And define

for each $\mu \neq 0..1$, $\mu \neq 1$,

 $\langle r:\dots,\langle role:D,\mu,\dots,\dots\rangle, \langle role':C,\dots,\dots\rangle \in V \text{ or } \langle r:\dots,\langle role:C,\dots,\dots\rangle, \langle role':C,\dots,\dots\rangle \in V, role \neq role'.$

For $\mu=0$: constant C inv: ∞l is landformed (edu.) $\mu_{\mathsf{OCL}}^C(mle) := \mathsf{context}\ C\ \mathsf{inv} : \mathsf{not}(\mathsf{ocllsUndefined}(role))$

Define $\mu_{\mathsf{OCL}}^C(role) := \mathsf{context}\ C$ inv :

 $(N_1 \leq role \text{ -> size}() \leq N_2) \text{ or } \dots \text{ or } (N_{2k-1} \leq role \text{ -> size}() \underbrace{\leq N_{2k}}_{\text{omit if } N_{2k} = *})$

 $\text{where } N_i \leq N_{i+1} \text{ for } 1 \leq i \leq 2k, \quad N_1, \ldots, N_{2k-1} \in \mathbb{N}, \quad N_{2k} \in \mathbb{N} \cup \{*\}.$

 $\mu = N_1..N_2, ..., N_{2k-1}..N_{2k}$

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Why Multiplicities as Constraints?

More precise, can't we just use types? (cf. Slide 26)

- many programming language have direct correspondences (the first corresponds to type pointer, the second to type reference) therefore treated specially.
- problem with our approach, we have $\mu_{OCL} = true$ anyway. could be represented by a set data-structure type without fixed bounds — no
- e $\mu=0..3$: 3 use array of size $\mathbf{4}$ —if model behaviour (or the implementation) adds 5th identity, we'll get a runtime error, and thereby see that the constraint is violated. Principally acceptable, but checks for array bounds everywhere...?
- could be represented by an array of size? but few programming languages/ data structure libraries allow lower bounds for array, clother than 0). If we have 5 identifies and the model behaviour removes one, this should be a violation of the constraints imposed by the model.

 The implementation which dose this removal is wrong. How do we see this..?

Multiplicities Never as Types...?

Well, if the target platform is known and fixed and the target platform has, for instance,

- range-checked arrays with positions $0,\ldots,N$,

then we could simply restrict the syntax of multiplicities to

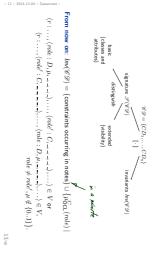
 $\mu ::= 1 \mid 0..N \mid *$

In general, unfortunately, we don't know.

and don't think about constraints (but use the obvious 1-to-1 mapping to types).

Multiplicities as Constraints of Class Diagram

Recall/Later:



Properties

We don't want to cover association **properties** in detail, only some observations (assume binary associations):

[Charles 1 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2	ordered, sequence	bag	unique	Property
does not allow is a significant is significant.	an r -link is a sequence of object identities (possibly including duplicates)	one object may have multiple r-links to a single other object	one object has at most one r-link to a single other object	Intuition
Ryphotological	have $\lambda(r)$ yield sequences	have $\lambda(r)$ yield multi-sets	current setting	Semantical Effect

Back to the Main Track

Not clear to me:

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Actually, ownership is seldom seen in UML diagrams. Again: if target platform is clear, one may well live without (d. [OMG, 2007b, 42] for more details). So: if multiplicity of n l e is 0.1 or 1, then the picture above is very close to concepts of pointers/references.

-		\geq	$\setminus \setminus$		\setminus	۲.
	SIN Stay!	does not allow is	an r -link is a sequence of object identities (possibly including duplicates)	one object may have multiple r -links to a single other object	one object has at most one r -link to a single other object	Intuition
		Rurahal total	have $\lambda(r)$ yield sequences	have $\lambda(r)$ yield multi-sets	current setting	Semantical Effect

Ownership

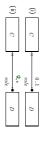
Intuitively it says:

Association r is not a "thing on its own" (i.e. provided by λ), but association end "role" is owned by C (1). (That is, it's stored inside C object and provided by σ).

Recall: on some earlier slides we said, the extension of the signature is only to study associations in "full beauty".
For the remainder of the course, we should look for something simpler...

Back to the main track:

from now on, we only use associations of the form



(And we may omit the non-navigability and ownership symbols.)

- ullet Form (i) introduces $\underline{role:C_{0,1}}$, and form (ii) introduces $\underline{role:C_{\star}}$ in V.
- In both cases, role ∈ atr(C).

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• We drop λ and go back to our nice σ with $\sigma(u)(role) \subseteq \mathscr{D}(D)$.

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Properties

We don't want to cover association **properties** in detail, only some observations (assume binary associations):

Property	Intuition	Semantical Effect
unique	one object has at most one r -link to a single other object	current setting
bag	one object may have multiple r-links to a single other object	have $\lambda(r)$ yield multi-sets
ordered, sequence	an r -link is a sequence of object identities (possibly including duplicates)	have $\lambda(r)$ yield sequences

ordered, sequence	bag	unique	Property
$\tau_D \rightarrow Seq(\tau_C)$	$\tau_D \rightarrow Bag(\tau_C)$	$\tau_D \rightarrow Set(\tau_C)$	OCL Typing of expression $rate(expr)$

For subsets, redefines, union, etc. see [OMG, 2007a, 127].

OCL Constraints in (Class) Diagrams

Where Shall We Put OCL Constraints?

OCL in Notes: Conventions

expr



text can principally be everything, in particular comments and constraints.

Sometimes, content is explicitly classified for clarity:

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Invariants of a Class Diagram

Let CD be a class diagram.

(ii) Particular dedicated places in class diagrams: (behav. feature: later)

 $..., p_n$ {pre : $expr_1$

Where Shall We Put OCL Constraints?

As we (now) are able to recognise OCL constraints when we see them, we can define

as the set $\{\varphi_1,\dots,\varphi_n\}$ of OCL constraints occurring in notes in \mathcal{CD} — after unfolding all abbreviations (cf. next slides).

- As usual: $Inv(\mathscr{CP}) := \bigcup_{\mathcal{CD} \in \mathscr{CP}} Inv(\mathcal{CD})$. Principally clear: $Inv(\cdot)$ for any kind of diagram.

For simplicity, we view the above as an abbreviation for

expr

 $\mathtt{context}\ f\ \mathsf{pre}: expr_1\ \mathsf{post}: expr_2$

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context C inv: expr

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Invariant in Class Diagram Example



If $\mathscr{C}\mathscr{D}$ consists of only $\mathscr{C}\mathscr{D}$ with the single class C, then $\bullet \ \, Inv(\mathscr{C}\mathscr{D}) = Inv(\mathscr{C}\mathscr{D}) = \ \, ...$

Semantics of a Class Diagram

We say, the semantics of $\mathscr{C}\mathscr{D}$ is the signature it induces and the set of OCL constraints occurring in $\mathscr{C}\mathscr{D}$, denoted Definition. Let \mathscr{CD} be a set of class diagrams.

 $[\![\mathscr{C}\mathscr{D}]\!] := \langle \mathscr{S}(\mathscr{C}\mathscr{D}), \mathit{Inv}(\mathscr{C}\mathscr{D}) \rangle.$

Given a structure \mathscr{D} of \mathscr{S} (and thus of $\mathscr{C}\mathscr{D}$), the class diagrams describe the system states $\Sigma_\mathscr{S}^2$, of which some may satisfy $Inv(\mathscr{C}\mathscr{D})$.

In pictures



UML State Machines

Brief History:

Rooted in Moore/Mealy machines, Transition Systems

ines, Transition Systems

| State | St

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Note: there is a common core, but each dialect interprets some constructs subtly different [Crane and Dingel, 2007]. (Would be too easy otherwise...)

(xii) Later: Hierarchical state machines.

Late 1990's: tool Rhapsody with code-generation for state machines.

Flanel 1987]: Statecharts as a concise notation introduces in particular higgoritical gates,
Manifest in tool Statecharte (Hard et al., 1990) (simulation, code: https://doi.org/10.1001/j.minie, etc.
From UML 1.2 or State Machines (1-, SMc Care Dynna)

(not the official name, but understood: UML-Statecharts)

Pragmatics

Recall: a UML model is an image or pre-image of a software system.

of system states. A set of class diagrams \mathscr{CD} with invariants $\mathit{Inv}(\mathscr{CD})$ describes the structure

Together with the invariants it can be used to state:

- **Pre-image**: Dear programmer, please provide an implementation which uses only system states that satisfy $Inv(\mathscr{CQ})$.
- Post-image: Dear user/maintainer, in the existing system, only system states which satisfy $Inv(\mathscr{CD})$ are used.

(The exact meaning of "use" will become clear when we study behaviour — intuitively: the system states that are reachable from the initial system state(s) by calling methods or firing transitions in state-machines.)

Example: highly abstract model of traffic lights controller.



Constraints vs. Types

Find the 10 differences: $\mathcal{D}(T) = \{3\}$ $\cup \{n \in \mathbb{N} \mid n > 17\}$

- x=4 is well-typed in the left context, a system state satisfying $x=4\,$
- violates the constraints of the diagram. x=4 is not even well-typed in the right context, there cannot be a system state with $\sigma(u)(z)=4$ because $\sigma(u)(x)$ is supposed to be in $\mathscr{D}(T)$ (by definition of system state).

Rule-of-thumb:

- If something "feels like" a type (one criterion: has a natural correspondence in the application domain), then make it a type.
 If something is a requirement or restriction of an otherwise useful type, then make it a constraint.

(x) Def: Ether (aka. event pool) (yi) Def: System configuration. (yii) Def: Event. (yii) Def: Transformer. (x) Def: Transformer. Roadmap: Chronologically (x) Transition relation induced by core state machine.(xi) Def.: step, run-to-completion step. (iii) Def.: Core state machine.(iv) Map UML State Machine Diagrams to core state machines. (i) What do we (have to) cover? UML State Machine Diagrams Syntax. (ii) Def.: Signature with signals. Semantics: The Basic Causality Model state chart diguram

UML State Machines

 $E[n \neq \emptyset]/x := x + 1; n! F$



UML State Machines: Syntax

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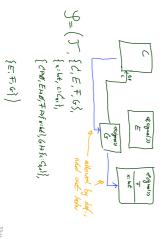
Signature With Signals

is called signature (with signals) if and only if is a signature (as before). Definition. A tuple $\mathcal{S} = (\mathcal{T}, \mathcal{C}, V, atr, \mathcal{E}), \qquad \mathcal{E} \subseteq \mathcal{C} \text{ a set of signals},$ $(\mathcal{T},\mathcal{C},V,atr)$

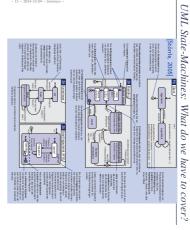
 $\mbox{\bf Note:}$ Thus conceptually, a signal is a class and can have attributes of plain type and associations.

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Signature With Signals: Example



UML State-Machines: What do we have to cover?



basic/leaf stan...

transitions,
then extend to cover the complicated rest.

Proven approach:

Start out simple, consider the essence, namely

absic/leaf states

transitions,

Proven approach:

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Core State Machine

 $\begin{array}{ll} s \; S \; \text{is a non-empty, finite set of (basic) states,} \\ s \; s_0 \in S \; \text{is an initial state,} \quad \int\limits_{c}^{cd} \frac{d}{c} \; \mathcal{G}_{p}^{m-d} \\ s \; \text{ and} \quad \int\limits_{c}^{cd} \frac{d}{c} \int\limits_{c}^{c} \frac{d}{c} \int\limits_{$ Definition. A core state machine over signature $\mathscr{S}=(\mathscr{T},\mathscr{C},V,atr,\mathscr{E})$ is a tuple We assume a set $Expr_{\mathscr{S}}$ of boolean expressions (may be OCL, may be something else) and a set $Act_{\mathscr{S}}$ of actions over \mathscr{S} . is a labelled transition relation. $M=(S,s_0,\to)$

From UML to Core State Machines: By Example

• $event \in \mathcal{E}$, • $guard \in Expr_{\mathscr{S}}$ • $action \in Act_{\mathscr{S}}$ maps to UML state machine diagram \mathcal{SM} : $M(\mathcal{SM}) = \underbrace{\{\{s_1, s_2\}, s_1, \{s_1, event, guard, action, s_2\}\}}_{S} \underbrace{\{s_1, event, guard, action, s_2\}\}}_{S}$ $annot ::= \left[\quad \langle event \rangle [\ ' \ ' \ \langle event \rangle]^* \quad [\ ' [' \ \langle guard \rangle \ ']' \] \quad [\ ' /' \ \langle action \rangle] \quad] \right]$ 81 (default: true, assumed to be in $Expr_{\mathscr{S}}$) (default: skip, assumed to be in $Act_{\mathscr{S}}$) s_2 35/48

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