

Contents & Goals

Last Lecture:

- Basic causality model
- Ether

This Lecture:

- Educational Objectives: Capabilities for following tasks/questions.
 - What does this State Machine mean? What happens if I inject this event?
 - Can you please model the following behaviour?
 - What is: Signal, Event, Ether, Transformer, Step, RTC

Content:

- System configuration
- Transformer
- Example for transformer

Ether aka. Event Pool

Definition. Let $\mathcal{S} = (\mathcal{S}, \mathcal{E}, Y, \text{act}, \emptyset)$ be a signature with signals and \mathcal{S} a structure.

We call a tuple $(Eh, \text{ready}, \oplus, [-])$ an ether over \mathcal{S} and \mathcal{S} if and only if it provides

- a ready operation which yields a set of signals that are ready for a given object, i.e.

$$\text{ready} : Eh \times \mathcal{S}(\theta) \rightarrow 2^{\mathcal{S}(\theta)}$$
- a operation to insert an event designed for a given object, i.e.

$$\oplus : Eh \times \mathcal{S}(\theta) \times \mathcal{S}(\theta) \rightarrow Eh$$
- a operation to remove an event, i.e.

$$\ominus : Eh \times \mathcal{S}(\theta) \rightarrow Eh$$
- a operation to clear the ether for a given object, i.e.

$$[-] : Eh \times \mathcal{S}(\theta) \rightarrow Eh.$$

Ether: Examples



- A (single, global, shared, reliable) FIFO queue is an ether.
 - $Eh \cong (\mathcal{S}(\mathcal{E}) \times \mathcal{S}(\mathcal{E}))^*$ eg. $e = (v, a), (v, b), (v, c)$
 - the set of all finite sequences of pairs $(\text{val}, \text{obj}) \in \mathcal{S}(\mathcal{E})$
 - ready: $(\text{val}, v) = \{(v, a)\}$ if $v = a$
 - $\oplus((v, a), e) = e \cdot (v, a)$ if $v = a$
 - $\oplus((v, a), e) = \{\}$ if $v \neq a$
 - $[-]$ remove all (val, obj) from e that originate from v
 - $\ominus((v, a), e) = e$ if $v \neq a$
 - $\ominus((v, a), e) = e \cdot \text{obj}$ if $v = a$
- One FIFO queue per active object is an ether.
- Lazy queue (\oplus becomes a relation then)
- One-place buffer.
- Priority queue.
- Multi-queues (one per sender).
- Trivial example: sink, "black hole".
- ...

System Configuration, Ether, Transformer

15.3.12 StateMachine (owg, 2007b, 561)

- The order of dequeuing is **not defined**, leaving open the possibility of modeling different, priority-based schemes.
- Run-to-completion may be implemented in various ways. [-]

The standard distinguishes, e.g.: **SignalEvent** [OMG, 2007b, 450], **Reception** [OMG, 2007b, 447].

On **signalEvents**, it says

A **signal event** represents the receipt of an asynchronous signal instance. A signal event may, for example, cause a state machine to trigger a transition. [OMG, 2007b, 449] [...]

Semantic Variation Points

The means by which requests are transported to their target depend on the type of requesting action, the target, and properties of the communication medium, and numerous other factors. In some cases, this is instantaneous and completely reliable while in others it may involve transmission delays of variable duration, loss of requests, reordering, or duplication. [See also the discussion on page 421.] [OMG, 2007b, 450]

Our **ether** is a general representation of the possible choices.

Often seen **minimal requirement**: order of sending by one object is preserved. But: we'll later briefly discuss "discarding" of events.

Events Are Instances of Signals

Definition. Let \mathcal{S}_0 be a structure of the signature with signals $\mathcal{S}_0 = (\mathcal{S}_0, \mathcal{R}_0, \mathcal{V}_0, \text{attr}_0, \mathcal{E})$ and let $E \in \mathcal{E}_0$ be a signal.

Let $\text{atr}(E) = (n_1, \dots, n_k)$. We call

$$e = (E, \{r_1 \mapsto d_1, \dots, r_k \mapsto d_k\})$$

or shorter (if mapping is clear from context)

$$(E, (d_1, \dots, d_k)) \text{ or } (E, \vec{d})$$

an event (or an instance) of signal E (if type-consistent).

We use $\text{Inst}(\mathcal{E}_0, \mathcal{S}_0)$ to denote the set of all events in \mathcal{S}_0 wrt. \mathcal{S}_0 .

As we always try to maximize confusion...

- By our existing naming convention, $u \in \mathcal{U}(E)$ is also called **instance of the (signal) class** E in system configuration (σ, \mathcal{E}) if $u \in \text{dom}(\sigma)$.
- The corresponding event is then $(E, \sigma(u))$.

Signals? Events...? Ether...?!

The idea is the following:

- Signals** are types (classes).
- Instances of signals (in the standard sense) are kept in the **system state** component σ of system configurations (σ, \mathcal{E}) .
- Identities** of signal instances are kept in the **ether**.
- Each signal instance is in particular an event — somehow "a recording that this signal occurred" (without caring for its identity)
- The main difference between **signal instance** and **event**: Events don't have an identity.
- Why is this useful? In particular for **reflective** descriptions of behaviour, we are typically not interested in the identity of a signal instance, but only whether it is an " E " or " F ", and which parameters it carries.

System Configuration

Definition. Let $\mathcal{S}_0 = (\mathcal{S}_0, \mathcal{R}_0, \mathcal{V}_0, \text{attr}_0, \mathcal{E})$ be a signature with signals, \mathcal{S}_0 a structure of \mathcal{S}_0 , $(\mathcal{B}_0, \text{ready}, \mathcal{E}, \{\cdot\})$ an ether over \mathcal{S}_0 and \mathcal{S}_0 . Furthermore assume there is one core state machine M_C per class $C \in \mathcal{C}$. A system configuration over $\mathcal{S}_0, \mathcal{S}_0, \mathcal{B}_0$ and \mathcal{E} is a pair

a new class
for each class

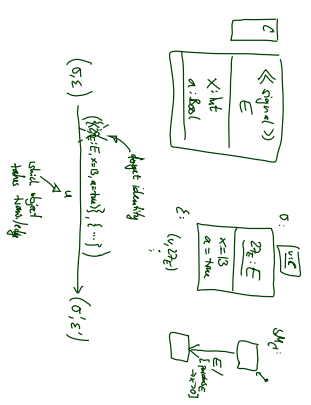
$$\mathcal{S} = (\mathcal{S}_0 \cup \{S_{StC} \mid C \in \mathcal{C}\}, \mathcal{R}_0, \mathcal{V}_0)$$

$$\mathcal{V}_0 \cup \{(\text{stable} : \text{Bool}, \text{true} \Rightarrow \text{true} \Rightarrow \text{true}) \mid C \in \mathcal{C}\}$$

$$\cup \{(\text{params} : S_{StC} + \mathcal{R}_0, \emptyset) \mid C \in \mathcal{C}\}$$

$$\cup \{(\text{stable}, \text{stC}) \mid C \in \mathcal{C}\} \cup \{(\text{params}, \text{stC}) \mid C \in \mathcal{C}\}$$

where $\mathcal{S}_{StC} = (\mathcal{S}_0 \cup \{S_{StC} \mid C \in \mathcal{C}\}, \mathcal{R}_0, \mathcal{V}_0)$ is the signature with signals, \mathcal{S}_0 a structure of \mathcal{S}_0 , $(\mathcal{B}_0, \text{ready}, \mathcal{E}, \{\cdot\})$ an ether over \mathcal{S}_0 and \mathcal{S}_0 . Furthermore assume there is one core state machine M_C per class $C \in \mathcal{C}$. A system configuration over $\mathcal{S}_0, \mathcal{S}_0, \mathcal{B}_0$ and \mathcal{E} is a pair



System Configuration: Example

$\mathcal{S}_0 = (\mathcal{S}_0, \mathcal{R}_0, \mathcal{V}_0, \text{attr}_0, \mathcal{E})$, $\mathcal{S}_0 = (\mathcal{S}_0, \mathcal{R}_0, \mathcal{V}_0, \text{attr}_0, \mathcal{E})$ where

- $\mathcal{S} = (\mathcal{S}_0 \cup \{S_{StC} \mid C \in \mathcal{C}\}, \mathcal{R}_0, \mathcal{V}_0)$
- $\mathcal{V}_0 \cup \{(\text{stable} : \text{Bool}, \text{true} \Rightarrow \text{true} \Rightarrow \text{true}) \mid C \in \mathcal{C}\}$
- $\cup \{(\text{params} : S_{StC} + \mathcal{R}_0, \emptyset) \mid C \in \mathcal{C}\}$
- $\cup \{(\text{stable}, \text{stC}) \mid C \in \mathcal{C}\} \cup \{(\text{params}, \text{stC}) \mid C \in \mathcal{C}\}$

for each $w \in \text{dom}(\sigma)$ and $r \in \mathcal{V}_0$.

System Configuration Step-by-Step

- We start with some signature with signals $\mathcal{S}_0 = (\mathcal{S}_0, \mathcal{E}_0, V_0, \text{atr}_0, \mathcal{E})$.
- A **system configuration** is a pair (σ, ε) which comprises a system state σ wrt. \mathcal{S} (not wrt. \mathcal{S}_0).
- Such a **system state** σ wrt. \mathcal{S} provides, for each object $u \in \text{dom}(\sigma)$,
 - values for the **explicit attributes** in V_0
 - values for a number of **implicit attributes**, namely
 - a **stability flag**, i.e. $\sigma(u)(\text{stable})$ is a boolean value,
 - a **current (state machine) state**, i.e. $\sigma(u)(s)$ denotes one of the states of core state machine M_C ,
 - a temporary association to access **event parameters** for each class, i.e. $\sigma(u)(\text{params } \varepsilon)$ is defined for each $E \in \mathcal{E}$.
- For convenience require: there is **no link to an event** except for params_E .

Stability

Definition:
Let (σ, ε) be a system configuration over some $\mathcal{S}_0, \mathcal{S}_0, E, H$.
We call an object $u \in \text{dom}(\sigma) \cap \mathcal{D}(E_0)$ **stable** in σ if and only if

$$\sigma(u)(\text{stable}) = \text{true}$$

Why Transformers?

- Recall the (simplified) syntax of transition annotations:


```
annot ::= [ (event) [ T (guard) T ] [ T (action) ] ]
```
- **Clear:** (event) is from \mathcal{E} of the corresponding signature.
- **But:** What are (guard) and (action)?
- UML can be viewed as being **parameterized** in **expression language** (providing (guard)) and **action language** (providing (action)).
- **Examples:**
 - **Expression Language:**
 - OCL
 - Java, C++, ... expressions
 - ...
 - **Action Language:**
 - UML Action Semantics, "Executable UML"
 - Java, C++, ... statements (plus some event send action)
 - ...

Transformer

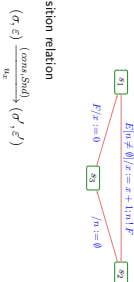
Definition:
Let $\Sigma_{\mathcal{S}}$ the set of system configurations over some $\mathcal{S}_0, \mathcal{S}_0, E, H$.
We call a relation t **system configuration transformer** if and only if

$$t \subseteq \mathcal{D}(E) \times (\Sigma_{\mathcal{S}} \times E, H) \times (\Sigma_{\mathcal{S}} \times E, H)$$

a (system configuration) **transformer** - system configuration transformer

- In the following, we assume that each application of a transformer t to some system configuration (σ, ε) of some object u_x is associated with a **system configuration** (σ', ε') of some object u_x .
 - An observation $(\text{params}, u_x, (E, \delta), u_x, \varepsilon) \in \text{Obs}(u_x)(\sigma, \varepsilon)$ represents the information that, as a "side effect" of u_x executing t , an event $(\delta) (E, \delta)$ has been sent from u_x to u_{dest} .
- Special cases:** creation/destruction

Where are we?



- **Wanted:** a labelled transition relation $(\sigma, \varepsilon) \xrightarrow[\text{tr}]{(\text{params}, \text{Send})} (\sigma', \varepsilon')$
- on system configuration. Labelled with the **consumed** and **sent** events, (σ', ε') being the result (or effect) of **one object** u_x taking a transition of its state machine from the current state machine state $\sigma(u_x)(s)$.
- **Have:** system configuration, (σ, ε) comprising current state machine state and stability flag for each object, and the other:
 - **Plan:**
 - (i) Introduce **transformer** as the semantics of action annotations. **Intuitively**, (σ', ε') is the effect of applying the transformer of the taken transition.
 - (ii) Explain how to choose transitions depending on ε and when to stop taking transitions — die **run to completion algorithm**.

Transformers as Abstract Actions!

- In the following, we assume that we're given
- an **expression language** E_{Expr} for guards, and
 - an **action language** A_{Act} for actions,
- and that we're given
- a **semantics** for boolean expressions in form of a partial function
- $$I[\cdot](\cdot, \cdot) : E_{Expr} \rightarrow (\Sigma_{\mathcal{S}} \times \mathcal{D}(E)) \rightarrow \mathbb{B}$$
- which evaluates expressions in a given system configuration.
- Assuming I to be partial is a way to treat "undefined" during runtime. If I is not defined (for instance because of dangling-reference navigation or division-by-zero), we want to go to a designated "error" system configuration.
- a **transformer** for each action: for each $\text{act} \in A_{Act}$, we assume to have
- $$t_{\text{act}} \subseteq \mathcal{D}(E) \times (\Sigma_{\mathcal{S}} \times E, H) \times (\Sigma_{\mathcal{S}} \times E, H)$$

example:
OCL
 $I[\text{Exp}](\sigma, \varepsilon) =$
true, if $\sigma(u_x)(\text{Exp}) = \text{true}$
false, if $\sigma(u_x)(\text{Exp}) = \text{false}$
undefined, otherwise

We can make the assumptions from the previous slide because instances exist:

- for OCL, we have the OCL semantics from Lecture 03. Simply remove the pre-images which map to \perp, \dots
- for Java, the operational semantics of the SWT lecture uniquely defines transformers for sequences of Java statements.

We distinguish the following kinds of transformers:

- **skip**: do nothing — recall: this is the default action
- **send**: modifies ε — interesting, because state machines are built around sending/consuming events
- **create/destroy**: modify domain of σ — not specific to state machines, but let's discuss them here as we're at it
- **update**: modify own or other objects' local state — boring

In the following we use

$$Act_2 ::= \{ skip \}$$

$$v \{ update(Expr_1, v, Expr_2) \mid Expr_1, Expr_2 \in OCLExp, v \in V \}$$

$$v \{ send(Expr_1, E, Expr_2) \mid Expr_1, Expr_2 \in OCLExp, E \in E \}$$

$$v \{ create(C, Expr_1, v) \mid C \in C \setminus E, Expr_1 \in OCLExp, v \in V \}$$

$$v \{ destroy(Expr) \mid Expr \in OCLExp \}$$

Errors: OCL expressions

new xp

$$v ::= new C_i$$

$$\neq \{ v \# null \} \dots$$

abstract syntax op	concrete syntax
intuitive semantics	\dots
well-typedness	\dots
semantics	$((\sigma, \varepsilon), (c', \varepsilon')) \in \tau_{op}[u_x]$ iff \dots
observables	$\tau_{op}[u_x](\sigma, \varepsilon) = \{ (\sigma', \varepsilon') \mid \text{where } \dots \}$
(error) conditions	$Obs_{op}[u_x] = \{ \dots \}$, not a relation, depends on choice Not defined if \dots

Transformer: Skip

abstract syntax skip	concrete syntax skip
intuitive semantics	do nothing
well-typedness	\dots
semantics	$\tau_{skip}[(\sigma, \varepsilon)] = \{ (\sigma, \varepsilon) \}$
observables	$Obs_{skip}[u_x](\sigma, \varepsilon) = \emptyset$
(error) conditions	

Transformer: Update

abstract syntax update(Expr ₁ , v, Expr ₂)	concrete syntax Expr ₁ . v := Expr ₂
intuitive semantics Update attribute value denoted by Expr ₁ to the value denoted by Expr ₂ .	
well-typedness Expr ₁ , Expr ₂ obey visibility and navigability	
semantics $\tau_{update(Expr_1, v, Expr_2)}[(\sigma, \varepsilon)] = \{ (\sigma', \varepsilon') \mid \tau_{update(Expr_1, v, Expr_2)}[(\sigma, \varepsilon)] \text{ with } \sigma' = \tau_{update(Expr_1, v, Expr_2)}[\sigma]$	
observables $Obs_{update(Expr_1, v, Expr_2)}[(\sigma, \varepsilon)] = \emptyset$	
(error) conditions Not defined if $\tau_{update(Expr_1, v, Expr_2)}[(\sigma, \varepsilon)]$ or $\tau_{update(Expr_1, v, Expr_2)}[(\sigma, \varepsilon)]$ not defined.	

References

[Harel and Gery, 1997] Harel, D. and Gery, E. (1997). Executable object modeling with statecharts. *IEEE Computer*, 30(7):31-42.

[OMG, 2007a] OMG. (2007a). Unified modeling language: Infrastructure, version 2.1.2. Technical Report formal/07-11-04.

[OMG, 2007b] OMG. (2007b). Unified modeling language: Superstructure, version 2.1.2. Technical Report formal/07-11-02.