

Software Design, Modelling and Analysis in UML

Lecture 14: Core State Machines IV

2014-12-18

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Contents & Goals

Last Lecture:

- System configuration
- Transformer
- Action language: skip, update

This Lecture:

- **Educational Objectives:** Capabilities for following tasks/questions.
 - What does this State Machine mean? What happens if I inject this event?
 - Can you please model the following behaviour.
 - What is: Signal, Event, Ether, Transformer, Step, RTC.
- **Content:**
 - Action Language: send (create/destroy later)
 - Run-to-completion Step
 - Putting It All Together

Transformer Cont'd

Transformer: Skip

abstract syntax		concrete syntax
skip		<i>skip</i>
intuitive semantics	<i>do nothing</i>	
well-typedness	./.	
semantics	$t_{\text{skip}}[u_x](\sigma, \varepsilon) = \{(\sigma, \varepsilon)\}$	
observables	$Obs_{\text{skip}}[u_x](\sigma, \varepsilon) = \emptyset$	
(error) conditions		

Transformer: Update

abstract syntax

$\text{update}(expr_1, v, expr_2)$

concrete syntax

$expr_1.v := expr_2$

intuitive semantics

Update attribute v in the object denoted by $expr_1$ to the value denoted by $expr_2$.

well-typedness

$expr_1 : \tau_C$ and $v : \tau \in \text{atr}(C)$; $expr_2 : \tau$;
 $expr_1, expr_2$ obey visibility and navigability!

semantics

$t_{\text{update}(expr_1, v, expr_2)}[u_x](\sigma, \varepsilon) = \{(\sigma', \varepsilon)\}$

where $\sigma' = \sigma[u \mapsto \sigma(u)[v \mapsto I[expr_2](\sigma, u_x)]]$
 with $u = I[expr_1](\sigma, u_x)$.

observables

$Obs_{\text{update}(expr_1, v, expr_2)}[u_x] = \emptyset$

(error) conditions

Not defined if $I[expr_1](\sigma, \overset{v_x}{\beta})$ or $I[expr_2](\sigma, \overset{u_x}{\beta})$ not defined.

change local state of object u

ε does not change

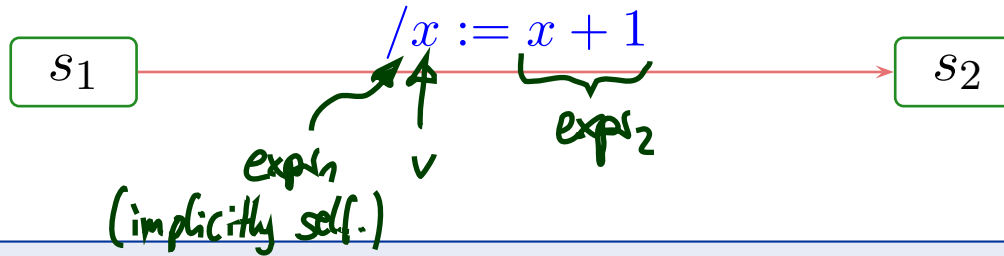
change value of v in $\sigma(u)$

object denoted by $expr_1$ (relative to u_x)

value denoted by $expr_2$ (relative to u_x)

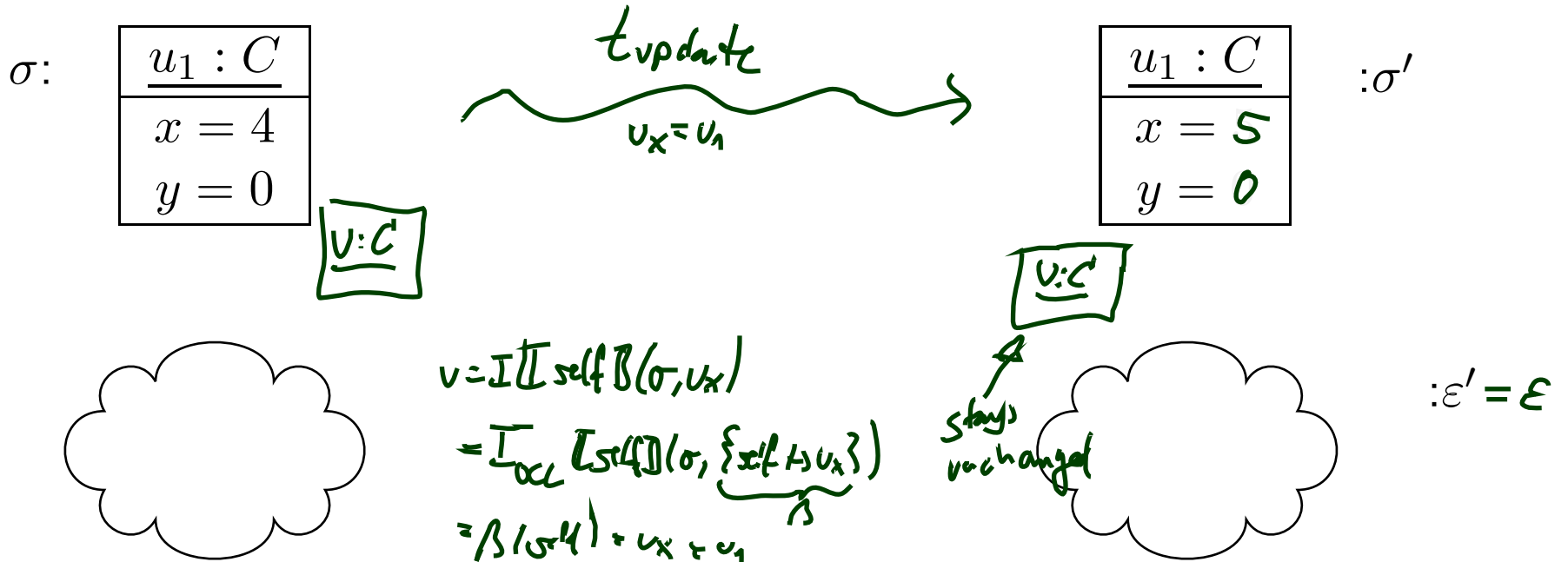
Update Transformer Example

SM_C :



$$t_{\text{update}(expr_1, v, expr_2)}[u_x](\sigma, \varepsilon) = (\sigma' = \sigma[u \mapsto \sigma(u)[v \mapsto I[expr_2](\sigma, u_x)]], \varepsilon), u = I[expr_1](\sigma, u_x)$$

$$I[x+1](\sigma, u_x) = I[x+1](\sigma, u_x) = 5$$



Transformer: Send

abstract syntax

$\text{send}(E(\text{expr}_1, \dots, \text{expr}_n), \text{expr}_{dst})$

concrete syntax

$\text{expr}_{dst} ! E(\text{expr}_1, \dots, \text{expr}_n)$

intuitive semantics

Object $u_x : C$ sends event E to object expr_{dst} , i.e. create a fresh signal instance, fill in its attributes, and place it in the ether.

well-typedness

$\text{expr}_{dst} : \tau_D, C, D \in \mathcal{C} \setminus \mathcal{E}; E \in \mathcal{E}; \text{atr}(E) = \{v_1 : \tau_1, \dots, v_n : \tau_n\};$
 $\text{expr}_i : \tau_i, 1 \leq i \leq n;$

all expressions obey visibility and navigability in C

semantics

$(\sigma', \varepsilon') \in t_{\text{send}(E(\text{expr}_1, \dots, \text{expr}_n), \text{expr}_{dst})}[u_x](\sigma, \varepsilon)$

iff $\sigma' = \sigma \dot{\cup} \{u \mapsto \{v_i \mapsto d_i \mid 1 \leq i \leq n\}\}; \varepsilon' = \varepsilon \oplus (u_{dst}, u);$
 if $u_{dst} = I[\text{expr}_{dst}](\sigma, u_x) \in \text{dom}(\sigma); d_i = I[\text{expr}_i](\sigma, u_x)$ for
 $1 \leq i \leq n;$

$u \in \mathcal{D}(E)$ a fresh identity, i.e. $u \notin \text{dom}(\sigma),$

and where $(\sigma', \varepsilon') = (\sigma, \varepsilon)$ if $u_{dst} \notin \text{dom}(\sigma).$

observables

$\text{Obs}_{\text{send}}[u_x] = \{(u_x, u, (E, d_1, \dots, d_n), u_{dst})\}$

(error) conditions

$I[\text{expr}](\sigma, u_x)$ not defined for any
 $\text{expr} \in \{\text{expr}_{dst}, \text{expr}_1, \dots, \text{expr}_n\}$

disjunct union

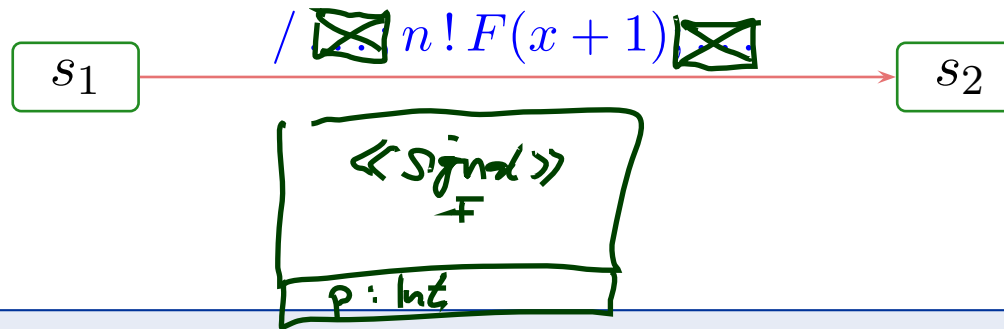
new signal instance

do nothing if u_{dst} not alive in σ

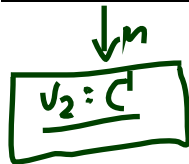
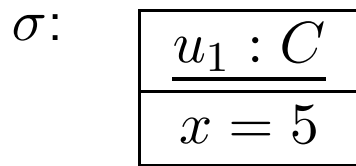
our choice!
 we could also just send, or consider it an error condition

Send Transformer Example

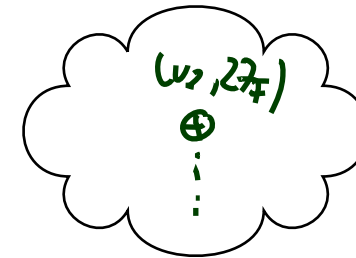
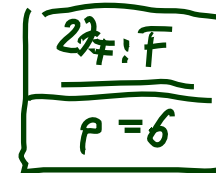
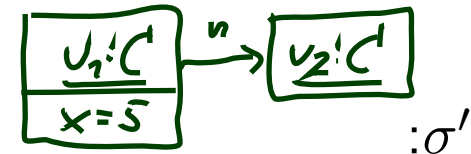
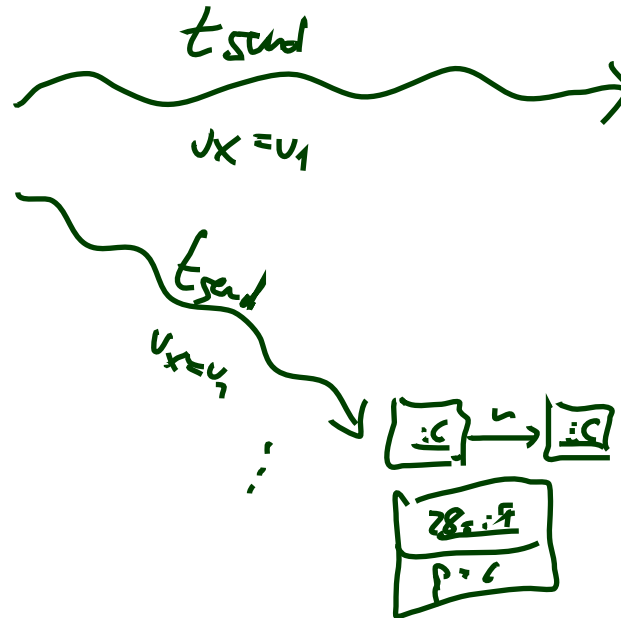
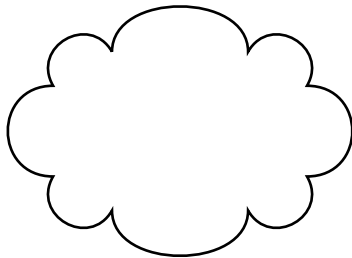
SM_C :



$t_{\text{send}}(\text{expr}_{\text{src}}, E(\text{expr}_1, \dots, \text{expr}_n), \text{expr}_{\text{dst}})[u_x](\sigma, \varepsilon) \ni (\sigma', \varepsilon')$ iff $\varepsilon' = \varepsilon \oplus (u_{\text{dst}}, u)$;
 $\sigma' = \sigma \dot{\cup} \{u \mapsto \{v_i \mapsto d_i \mid 1 \leq i \leq n\}\}$; $u_{\text{dst}} = I[\text{expr}_{\text{dst}}](\sigma, u_x) \in \text{dom}(\sigma)$;
 $d_i = I[\text{expr}_i](\sigma, u_x), 1 \leq i \leq n$; $u \in \mathcal{D}(E)$ a fresh identity;



ε :



$:\varepsilon' = \varepsilon \oplus (u_2, 277)$

Sequential Composition of Transformers

- **Sequential composition** $t_1 \circ t_2$ of transformers t_1 and t_2 is canonically defined as

$$(t_2 \circ t_1)[u_x](\sigma, \varepsilon) = t_2[u_x](t_1[u_x](\sigma, \varepsilon))$$

with observation

$$Obs_{(t_2 \circ t_1)}[u_x](\sigma, \varepsilon) = Obs_{t_1}[u_x](\sigma, \varepsilon) \cup Obs_{t_2}[u_x](t_1(\sigma, \varepsilon)).$$

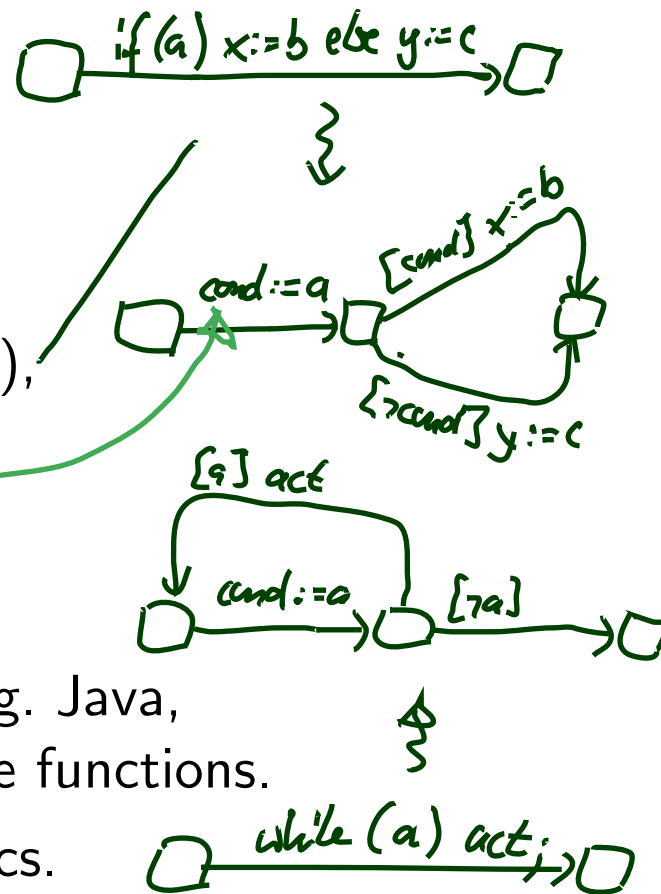
- **Clear:** not defined if one the two intermediate “micro steps” is not defined.

Transformers And Denotational Semantics

Observation: our transformers are in principle the **denotational semantics** of the actions/action sequences. The trivial case, to be precise.

Note: with the previous examples, we can capture

- empty statements, skips,
 - assignments,
 - conditionals (by normalisation and auxiliary variables),
 - create/destroy,
- but not **possibly diverging loops**.



Our (Simple) Approach: if the action language is, e.g. Java, then (**syntactically**) forbid loops and calls of recursive functions.

Other Approach: use full blown denotational semantics.

No show-stopper, because loops in the action annotation can be converted into transition cycles in the state machine.

Step and Run-to-completion Step

Transition Relation, Computation

Definition. Let A be a set of **actions** and S a (not necessarily finite) set of **states**.

We call

$$\rightarrow \subseteq S \times A \times S$$

a (labelled) **transition relation**.

Let $S_0 \subseteq S$ be a set of **initial states**. A sequence

$$s_0 \xrightarrow{a_0} s_1 \xrightarrow{a_1} s_2 \xrightarrow{a_2} \dots$$

with $s_i \in S$, $a_i \in A$ is called **computation** of the **labelled transition system** (S, \rightarrow, S_0) if and only if

- **initiation:** $s_0 \in S_0$
- **consecution:** $(s_i, a_i, s_{i+1}) \in \rightarrow$ for $i \in \mathbb{N}_0$.

Active vs. Passive Classes/Objects

- **Note:** From now on, assume that all classes are **active** for simplicity.

We'll later briefly discuss the Rhapsody framework which proposes a way how to integrate non-active objects.

- **Note:** The following RTC “algorithm” follows [?] (i.e. the one realised by the Rhapsody code generation) where the standard is ambiguous or leaves choices.

From Core State Machines to LTS

Definition. Let $\mathcal{S}_0 = (\mathcal{I}_0, \mathcal{C}_0, V_0, atr_0, \mathcal{E})$ be a signature with signals (all classes **active**), \mathcal{D}_0 a structure of \mathcal{S}_0 , and $(Eth, ready, \oplus, \ominus, [\cdot])$ an ether over \mathcal{S}_0 and \mathcal{D}_0 .

Assume there is one core state machine M_C per class $C \in \mathcal{C}$.

We say, the state machines **induce** the following labelled transition relation on states $S := \left(\sum_{\mathcal{C}} \mathcal{D}(\mathcal{C}) \dot{\cup} \{\#\} \times Eth \right)$ with actions $A :=$

$$\left(2^{\mathcal{D}(\mathcal{C})} \times (\mathcal{D}(\mathcal{E}) \dot{\cup} \{\perp\}) Evs(\mathcal{E}, \mathcal{D}) \times \mathcal{D}(\mathcal{C}) \right)^2 \times \mathcal{D}(e): \left(\sum_{\mathcal{C}} \mathcal{D}(\mathcal{C}) \times Eth \right) \dot{\cup} \{\#\}$$

- $(\sigma, \varepsilon) \xrightarrow[\underbrace{\quad}_u]{(cons, Snd)} (\sigma', \varepsilon')$ if and only if
 - (i) an event with destination u is discarded,
 - (ii) an event is dispatched to u , i.e. stable object processes an event, or
 - (iii) run-to-completion processing by u commences, i.e. object u is not stable and continues to process an event,
 - (iv) the environment interacts with object u ,
- $s \xrightarrow{(cons, \emptyset)} \#$ if and only if
 - (v) $s = \#$ and $cons = \emptyset$, or an error condition occurs during consumption of $cons$.

(i) Discarding An Event

$$(\sigma, \varepsilon) \xrightarrow[u]{(cons, Snd)} (\sigma', \varepsilon')$$

if

- an E -event (instance of signal E) is ready in ε for object u of a class \mathcal{C} , i.e. if

$$u \in \text{dom}(\sigma) \cap \mathcal{D}(C) \wedge \exists u_E \in \mathcal{D}(E) : u_E \in \text{ready}(\varepsilon, u)$$

- u is stable and in state machine state s , i.e. $\sigma(u)(\text{stable}) = 1$ and $\sigma(u)(st) = s$,
- but there is no corresponding transition enabled (all transitions incident with current state of u either have other triggers or the guard is not satisfied)

$$\forall (s, F, \text{expr}, \text{act}, s') \in \rightarrow (SM_C) : F \neq E \vee I[\text{expr}](\overset{\sim}{\sigma}, u) = 0$$

← current state assumed above *← see (ii)*

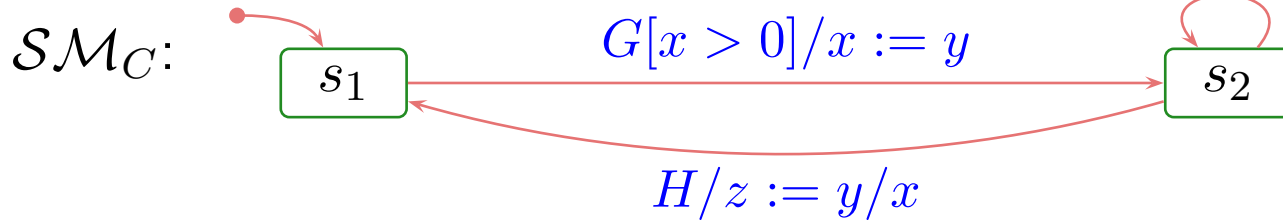
and

- the system configuration ~~doesn't~~ changes, i.e. $\sigma' = \sigma \setminus \{u_E \mapsto \sigma(u_E)\}$
- the event u_E is removed from the ether, i.e.

$$\varepsilon' = \varepsilon \ominus u_E,$$

Example: Discard

$[x > 0]/x := x - 1; n! J$



$\langle\langle signal, env \rangle\rangle$
 H

$\langle\langle signal \rangle\rangle$
 G, J

n

	C
0, 1	$x, z : Int$ $y : Int \langle\langle env \rangle\rangle$

σ :

$c : C$
$x = 1, z = 0, y = 2$ $st = s_1$ $stable = 1$

J
 G

$(v, E), \emptyset$
 c

not changed

$c : C$
$- - -$

G

σ'

ε :
 $ready(\varepsilon, c)$

J for c ,
 G for c

$(j.c). (g.c)$

(c, g)

ε'
 $\{ready(\varepsilon', c) = g\}$

- $\exists u \in \text{dom}(\sigma) \cap \mathcal{D}(C) \checkmark$
- $\exists u_E \in \mathcal{D}(\mathcal{E}) : u_E \in \text{ready}(\varepsilon, u) \checkmark$
- $\forall (s, F, \text{expr}, \text{act}, s') \in \rightarrow (SM_C) :$
 $F \neq E \vee I[\text{expr}](\sigma) = 0 \checkmark$

- $\sigma(u)(\text{stable}) = 1 \checkmark / \sigma(u)(\text{st}) = s_j \checkmark$
- $\sigma' = \sigma, \varepsilon' = \varepsilon \ominus u_E$
- $\text{cons} = \{(u, (E, \sigma(u_E)))\}, \text{Snd} = \emptyset$

(ii) Dispatch

$$(\sigma, \varepsilon) \xrightarrow[u]{(cons, Snd)} (\sigma', \varepsilon') \text{ if}$$

- $u \in \text{dom}(\sigma) \cap \mathcal{D}(C) \wedge \exists u_E \in \mathcal{D}(E) : u_E \in \text{ready}(\varepsilon, u)$
- u is stable and in state machine state s , i.e. $\sigma(u)(\text{stable}) = 1$ and $\sigma(u)(st) = s$,
- a transition is enabled, i.e.

$$\exists (s, F, \text{expr}, \text{act}, s') \in \rightarrow (\mathcal{SM}_C) : F = E \wedge I[\![\text{expr}]\!](\tilde{\sigma}) = 1$$

where $\tilde{\sigma} = \sigma[u.\text{params}_E \mapsto u_E]$.

and

- (σ', ε') results from applying t_{act} to (σ, ε) and removing u_E from the ether, i.e.

$$\begin{aligned} (\sigma'', \varepsilon') &\in \overset{[u]}{t_{act}}(\tilde{\sigma}, \varepsilon \ominus u_E), \\ \sigma' &= (\sigma''[u.st \mapsto s', u.\text{stable} \mapsto b, u.\text{params}_E \mapsto \emptyset])|_{\mathcal{D}(C) \setminus \{u_E\}} \end{aligned}$$

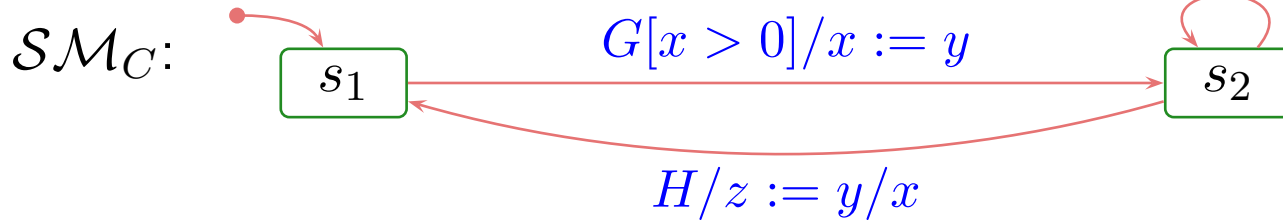
where b **depends**:

- If u becomes stable in s' , then $b = 1$. It **does** become stable if and only if there is no transition **without trigger** enabled for u in (σ', ε') .
- Otherwise $b = 0$.
- Consumption of u_E and the side effects of the action are observed, i.e.

$$cons = \{(u, (E, \sigma(u_E)))\}, Snd = \text{Obs}_{t_{act}}^{\{u\}}(\tilde{\sigma}, \varepsilon \ominus u_E).$$

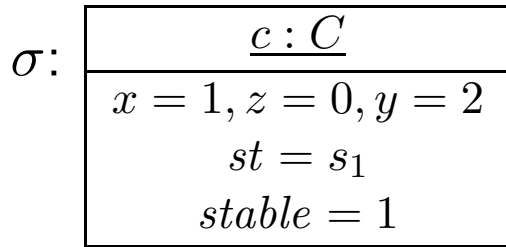
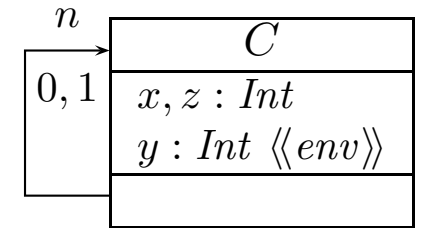
Example: Dispatch

$[x > 0]/x := x - 1; n! J$

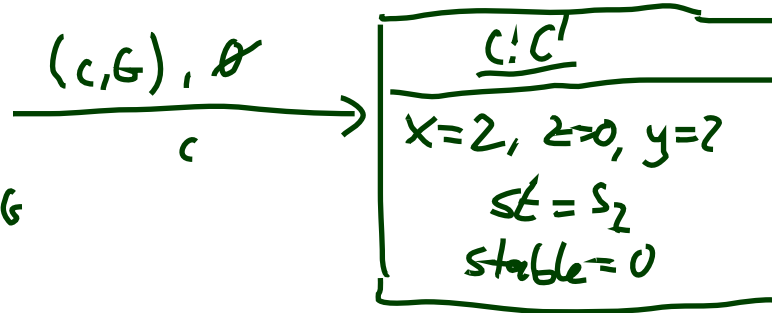


$\langle\langle signal, env \rangle\rangle$
 H

$\langle\langle signal \rangle\rangle$
 G, J



σ
params_G



σ'



$ready(\varepsilon, \varepsilon) = g$

empty FIFO
 $\varepsilon' = \varepsilon$

- $\exists u \in \text{dom}(\sigma) \cap \mathcal{D}(C) \checkmark$
- $\exists u_E \in \mathcal{D}(E) : u_E \in \text{ready}(\varepsilon, u) \checkmark$
- $\exists (s, F, \text{expr}, \text{act}, s') \in \rightarrow (SM_C) :$
 $F = E \wedge I[\text{expr}](\tilde{\sigma}) = 1 \checkmark$
- $\tilde{\sigma} = \sigma[u.params_E \mapsto u_E]$
- $\sigma(u)(stable) = 1 \checkmark \sigma(u)(st) = s, \checkmark$
- $(\sigma'', \varepsilon') = t_{act}(\tilde{\sigma}, \varepsilon \ominus u_E)$
- $\sigma' = (\sigma''[u.st \mapsto s', u.stable \mapsto b, u.params_E \mapsto \emptyset])|_{\mathcal{D}(C) \setminus \{u_E\}}$
- $cons = \{(u, (E, \sigma(u_E)))\}, Snd = Obs_{t_{act}}(\tilde{\sigma}, \varepsilon \ominus u_E)$

(iii) Commence Run-to-Completion

$$(\sigma, \varepsilon) \xrightarrow[u]{(cons, Snd)} (\sigma', \varepsilon')$$

if

- there is an unstable object u of a class \mathcal{C} , i.e.

$$u \in \text{dom}(\sigma) \cap \mathcal{D}(C) \wedge \sigma(u)(stable) = 0$$

- there is a transition without trigger enabled from the current state $s = \sigma(u)(st)$, i.e.

$$\exists (s, -, expr, act, s') \in \rightarrow (\mathcal{SM}_C) : I[[expr]](\sigma) = 1$$

\nwarrow not $\tilde{\sigma}$

and

- (σ', ε') results from applying t_{act} to (σ, ε) , i.e.

$$(\sigma'', \varepsilon') \in t_{act}[u](\sigma, \varepsilon), \quad \sigma' = \sigma''[u.st \mapsto s', u.stable \mapsto b]$$

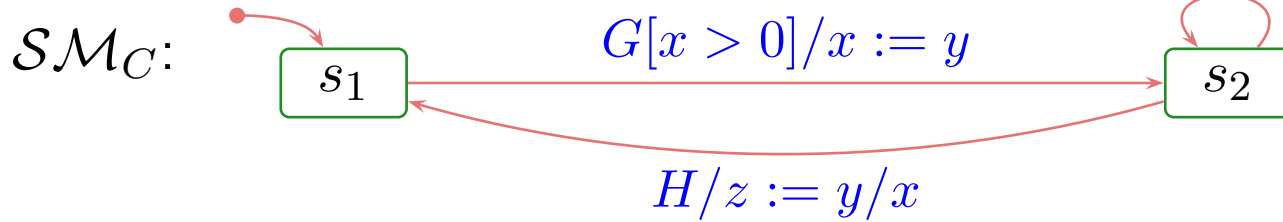
where b **depends** as before.

- Only the side effects of the action are observed, i.e.

$$cons = \emptyset, Snd = Obs_{t_{act}}(\sigma, \varepsilon).$$

Example: Commence

$[x > 0]/x := x - 1; n! J$



$\langle\langle signal, env \rangle\rangle$
 H

$\langle\langle signal \rangle\rangle$
 G, J

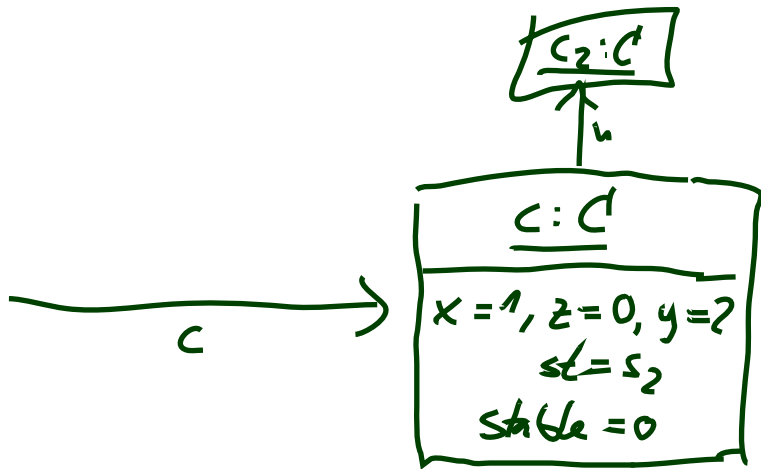
n	C
$0, 1$	$x, z : Int$ $y : Int \langle\langle env \rangle\rangle$

σ :

$c : C$
$x = 2, z = 0, y = 2$ $st = s_2$ $stable = 0$

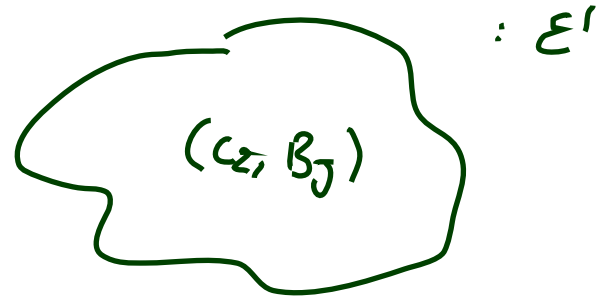
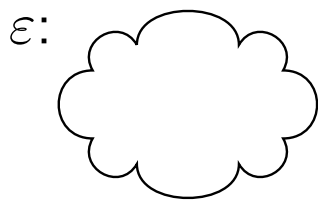
\uparrow_n

$C_2 : C$



σ'

$\{B_J : J\}$



- $\exists u \in \text{dom}(\sigma) \cap \mathcal{D}(C) : \sigma(u)(stable) = 0 \checkmark$
- $\exists (s, _, expr, act, s') \in \rightarrow (SM_C) :$
 $I[\![expr]\!](\sigma) = 1 \checkmark$
- ~~$\sigma(u)(stable) = 1$~~ $\sigma(u)(st) = s, \checkmark$
- $(\sigma'', \varepsilon') = t_{act}(\sigma, \varepsilon),$
 $\sigma' = \sigma''[u.st \mapsto s', u.stable \mapsto b]$
- $cons = \emptyset, Snd = Obs_{t_{act}}(\sigma, \varepsilon)$

(iv) Environment Interaction

Assume that a set $\mathcal{E}_{env} \subseteq \mathcal{E}$ is designated as **environment events** and a set of attributes $v_{env} \subseteq V$ is designated as **input attributes**.

Then

$$(\sigma, \varepsilon) \xrightarrow[env]{(cons, Snd)} (\sigma', \varepsilon')$$

if

- environment event $E \in \mathcal{E}_{env}$ is spontaneously sent to an alive object $u \in \mathcal{D}(\sigma)$, i.e.

$$\sigma' = \sigma \dot{\cup} \{u_E \mapsto \{v_i \mapsto d_i \mid 1 \leq i \leq n\}, \quad \varepsilon' = \varepsilon \oplus u_E$$

where $u_E \notin \text{dom}(\sigma)$ and $\text{atr}(E) = \{v_1, \dots, v_n\}$.

- Sending of the event is observed, i.e. $cons = \emptyset$, $Snd = \{(env, E(\vec{d}))\}$.

or

- Values of input attributes change freely in alive objects, i.e.

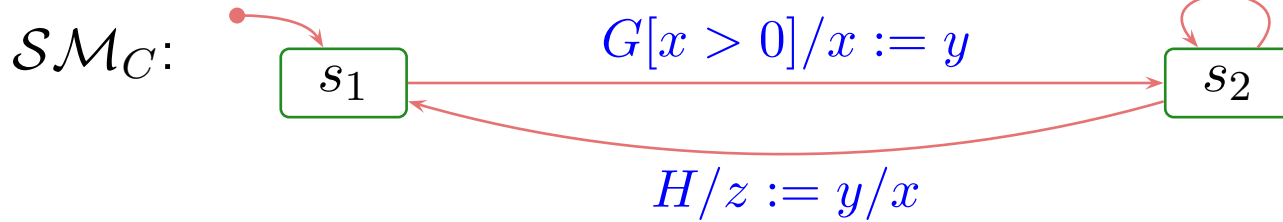
$$\forall v \in V \forall u \in \text{dom}(\sigma) : \sigma'(u)(v) \neq \sigma(u)(v) \implies v \in V_{env}.$$

and no objects appear or disappear, i.e. $\text{dom}(\sigma') = \text{dom}(\sigma)$.

- $\varepsilon' = \varepsilon$.

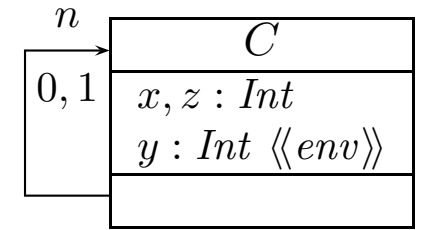
Example: Environment

$[x > 0]/x := x - 1; n! J$



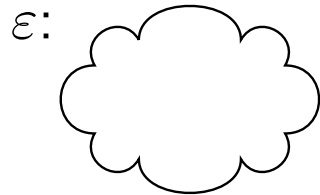
$\langle\langle \text{signal}, \text{env} \rangle\rangle$
 H

$\langle\langle \text{signal} \rangle\rangle$
 G, J



σ :

$\underline{c} : C$
$x = 0, z = 0, y = 2$
$st = s_2$
$stable = 1$



- $\sigma' = \sigma \dot{\cup} \{u_E \mapsto \{v_i \mapsto d_i \mid 1 \leq i \leq n\}\}$
- $\varepsilon' = \varepsilon \oplus u_E$ where $u_E \notin \text{dom}(\sigma)$
- and $\text{atr}(E) = \{v_1, \dots, v_n\}$.
- $u \in \text{dom}(\sigma)$
- $\text{cons} = \emptyset,$
- $\text{Snd} = \{(\text{env}, E(\vec{d}))\}.$

(v) Error Conditions

$$s \xrightarrow[u]{(cons, Snd)} \#$$

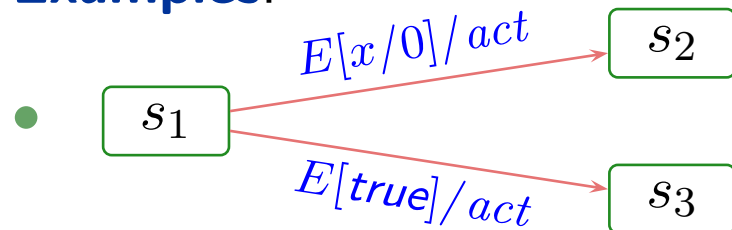
if, in (i) or (iii),

- $I[\![expr]\!]$ is not defined for σ , or
- t_{act} is not defined for (σ, ε) ,

and

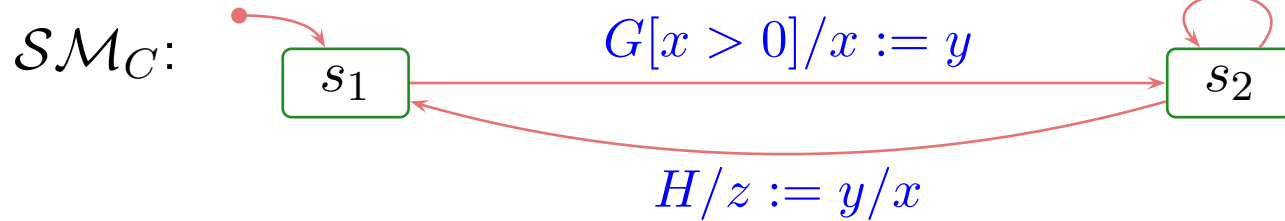
- consumption **is observed** according to (ii) or (iii), but $Snd = \emptyset$.

Examples:



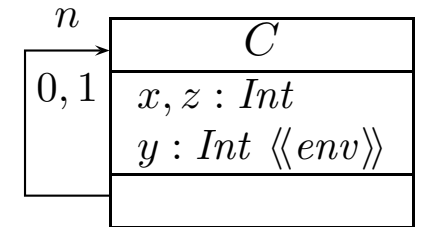
Example: Error Condition

$[x > 0]/x := x - 1; n! J$



$\langle\langle \text{signal}, \text{env} \rangle\rangle$
 H

$\langle\langle \text{signal} \rangle\rangle$
 G, J



σ :

$c : C$
$x = 0, z = 0, y = 27$
$st = s_2$
$stable = 1$

ε :

- $I[\text{expr}]$ not defined for σ , or
- t_{act} is not defined for (σ, ε)
- consumption according to (ii) or (iii)
- $Snd = \emptyset$

Notions of Steps: The Step

Note: we call one evolution $(\sigma, \varepsilon) \xrightarrow[u]{(cons, Snd)} (\sigma', \varepsilon')$ a **step**.

Thus in our setting, **a step directly corresponds** to

one object (namely u) takes **a single transition** between regular states.

(We have to extend the concept of “single transition” for hierarchical state machines.)

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Remark: With only methods (later), the notion of step is not so clear.

For example, consider

- c_1 calls $f()$ at c_2 , which calls $g()$ at c_1 which in turn calls $h()$ for c_2 .
- Is the completion of $h()$ a step?
- Or the completion of $f()$?
- Or doesn’t it play a role?

It does play a role, because **constraints/invariants** are typically (= by convention) assumed to be evaluated at step boundaries, and sometimes the convention is meant to admit (temporary) violation in between steps.

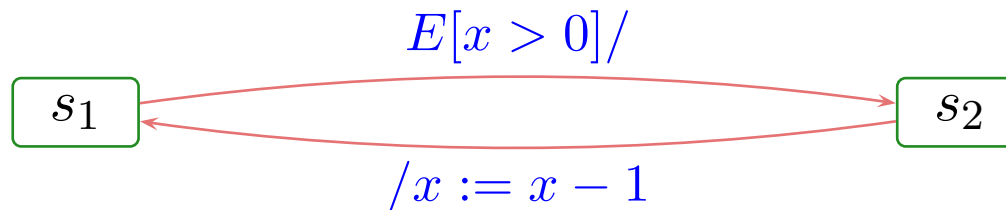
Notions of Steps: The Run-to-Completion Step

What is a **run-to-completion** step...?

- **Intuition**: a maximal sequence of steps, where the first step is a **dispatch** step and all later steps are **commence** steps.
- **Note**: one step corresponds to one transition in the state machine.

A run-to-completion step is in general not syntactically definable — one transition may be taken multiple times during an RTC-step.

Example:



σ :

$\underline{:C}$
$x = 2$

ε :

Notions of Steps: The RTC Step Cont'd

Proposal: Let

$$(\sigma_0, \varepsilon_0) \xrightarrow[u_0]{(cons_0, Snd_0)} \dots \xrightarrow[u_{n-1}]{(cons_{n-1}, Snd_{n-1})} (\sigma_n, \varepsilon_n), \quad n > 0,$$

be a finite (!), non-empty, maximal, consecutive sequence such that

- object u is alive in σ_0 ,
- $u_0 = u$ and $(cons_0, Snd_0)$ indicates dispatching to u , i.e. $cons = \{(u, \vec{v} \mapsto \vec{d})\}$,
- there are no receptions by u in between, i.e.

$$cons_i \cap \{u\} \times Evs(\mathcal{E}, \mathcal{D}) = \emptyset, i > 1,$$

- $u_{n-1} = u$ and u is stable only in σ_0 and σ_n , i.e.

$$\sigma_0(u)(stable) = \sigma_n(u)(stable) = 1 \text{ and } \sigma_i(u)(stable) = 0 \text{ for } 0 < i < n,$$

Notions of Steps: The RTC Step Cont'd

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Let $0 = k_1 < k_2 < \dots < k_N = n$ be the maximal sequence of indices such that $u_{k_i} = u$ for $1 \leq i \leq N$.

Notions of Steps: The RTC Step Cont'd

Proposal: Let

$$(\sigma_0, \varepsilon_0) \xrightarrow[u_0]{(cons_0, Snd_0)} \dots \xrightarrow[u_{n-1}]{(cons_{n-1}, Snd_{n-1})} (\sigma_n, \varepsilon_n), \quad n > 0,$$

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Let $0 = k_1 < k_2 < \dots < k_N = n$ be the maximal sequence of indices such that $u_{k_i} = u$ for $1 \leq i \leq N$. Then we call the sequence

$$(\sigma_0(u) =) \quad \sigma_{k_1}(u), \sigma_{k_2}(u) \dots, \sigma_{k_N}(u) \quad (= \sigma_{n-1}(u))$$

a (!) **run-to-completion computation** of u (from (local) configuration $\sigma_0(u)$).