Software Design, Modelling and Analysis in UML

Lecture 20: Live Sequence Charts

2015-02-03

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Contents & Goals

Last Lecture:

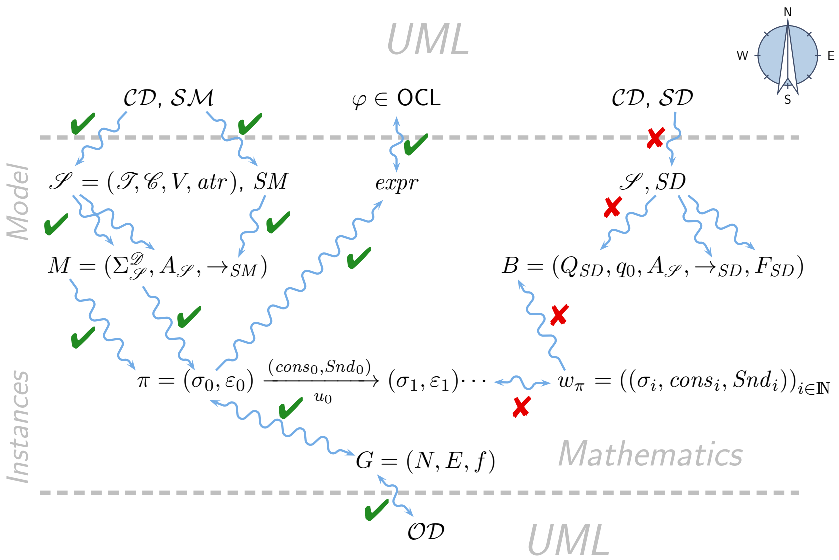
- Hierarchical State Machines completed.
- Behavioural feature (aka. methods).

This Lecture:

- **Educational Objectives:** Capabilities for following tasks/questions.
  - What does this LSC mean?
  - Are this UML model's state machines consistent with the interactions?
  - Please provide a UML model which is consistent with this LSC.
  - What is: activation, hot/cold condition, pre-chart, etc.?
- **Content:**
  - Reflective description of behaviour.
  - LSC concrete and abstract syntax.
  - LSC semantics.

You are here.

Course Map



Motivation: Reflective, Dynamic Descriptions of Behaviour

Recall: Constructive vs. Reflective Descriptions

[Harel, 1997] proposes to distinguish constructive and reflective descriptions:

- "*A language is* **constructive** *if it contributes to the dynamic semantics of the model. That is, its constructs contain information needed in executing the model or in translating it into executable code.*"

  A constructive description tells **how** things are computed (which can then be desired or undesired).

- "*Other languages are* **reflective** *or* **assertive**, *and can be used by the system modeler to capture parts of the thinking that go into building the model – behavior included –, to derive and present views of the model, statically or during execution, or to set constraints on behavior in preparation for verification.*"

  A reflective description tells **what** shall or shall not be computed.

Note: No sharp boundaries!

Recall: What is a Requirement?

Recall:

- The **semantics** of the **UML model** $\mathcal{M} = (\mathscr{CD}, \mathscr{SM}, \mathscr{OD})$ is the **transition system** $(S, \to, S_0)$ constructed according to discard/dispatch/commence-rules.
- The **computations of** $\mathcal{M}$, denoted by $[\![\mathcal{M}]\!]$, are the computations of $(S, \to, S_0)$.

Now:

A reflective description tells **what** shall or shall not be computed.

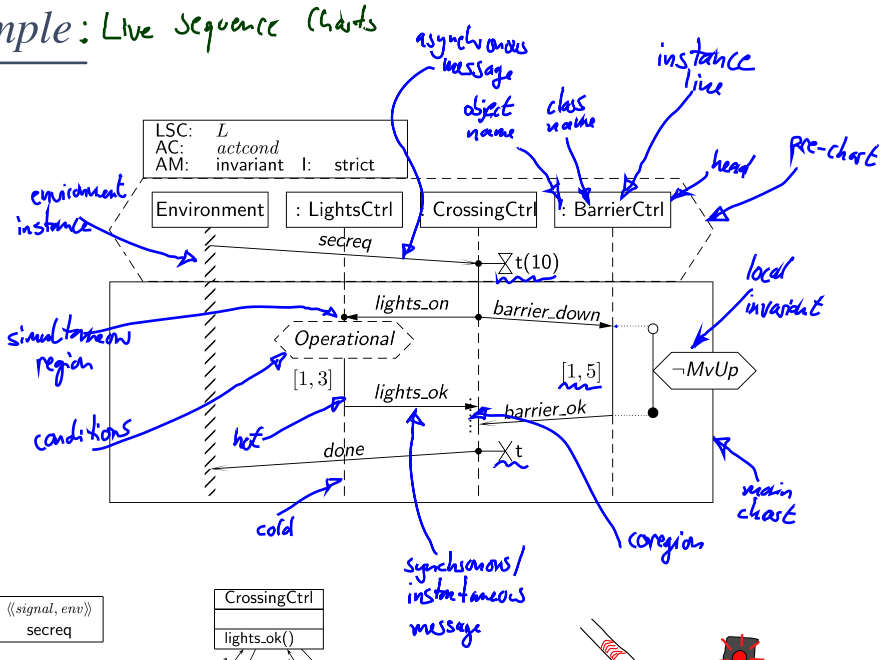
More formally: a requirement ϑ is a property of computations; something which is either satisfied or not satisfied by a computation

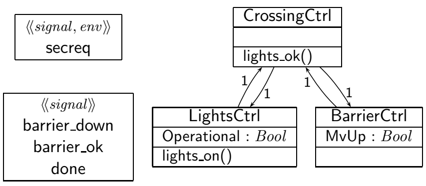
$$\pi = (\sigma_0, \varepsilon_0) \xrightarrow{(cons_0, Snd_0)} (\sigma_1, \varepsilon_1) \xrightarrow{(cons_1, Snd_1)} \cdots \in [\![\mathcal{M}]\!],$$

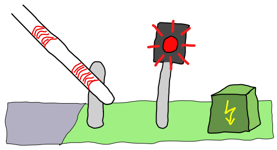
denoted by $\pi \models \vartheta$ and $\pi \not\models \vartheta$, resp.
Simplest case: OCL constraint.

Live Sequence Charts — Concrete Syntax

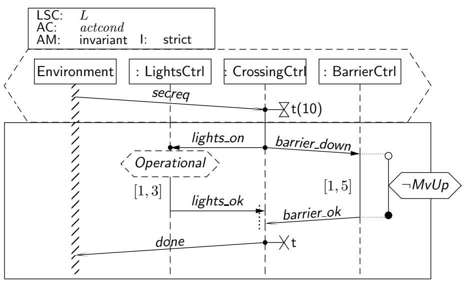
Example: Live Sequence Charts

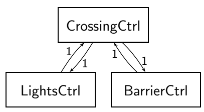


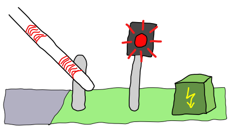




Example: What Is Required?







- **Whenever** the CrossingCtrl has consumed a ‘secreq’ event
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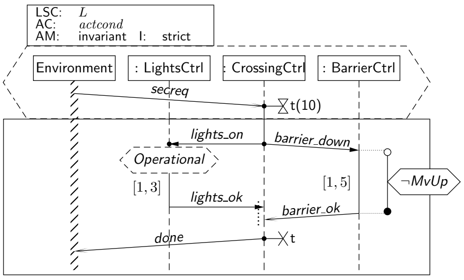
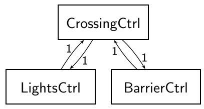
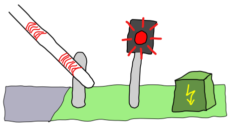
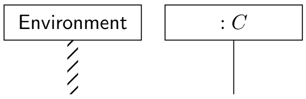
Building Blocks







- **Instance Lines:**



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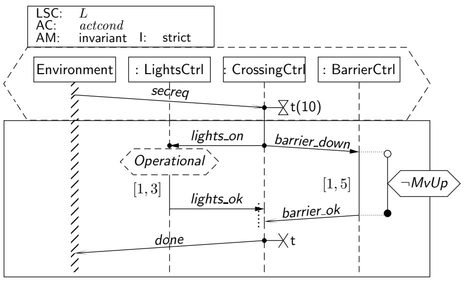
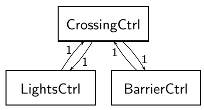
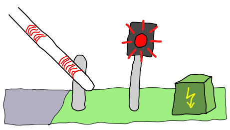
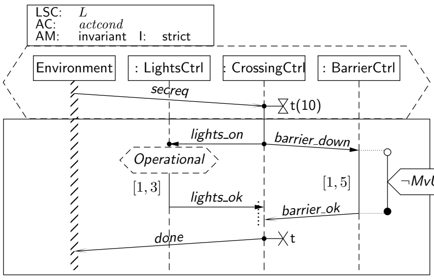


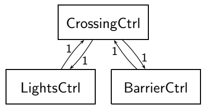


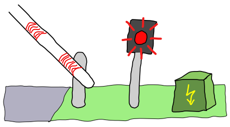


- **Messages:** (asynchronous or synchronous/instantaneous)

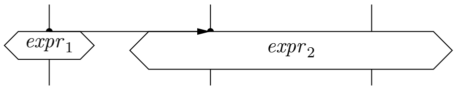
Building Blocks

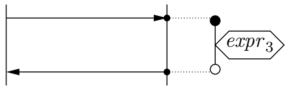






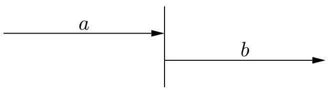
- **Conditions and Local Invariants:** $(expr_1, expr_2, expr_3 \in Expr_{\mathscr{S}})$

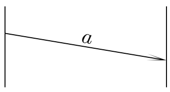




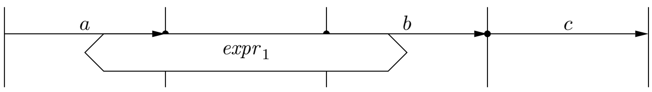
Intuitive Semantics: A Partial Order on Simclasses

(i) **Strictly After:**

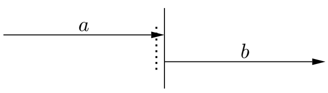




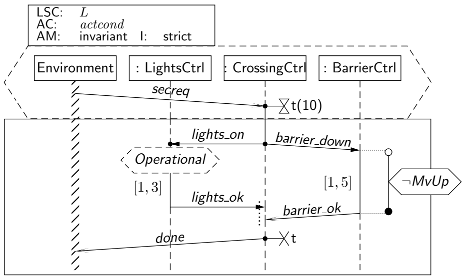
(ii) **Simultaneously:** (simultaneous region)

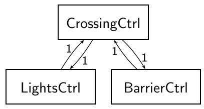


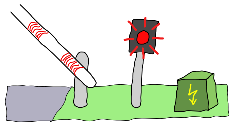
(iii) **Explicitly Unordered:** (co-region)



Partial Order Requirements







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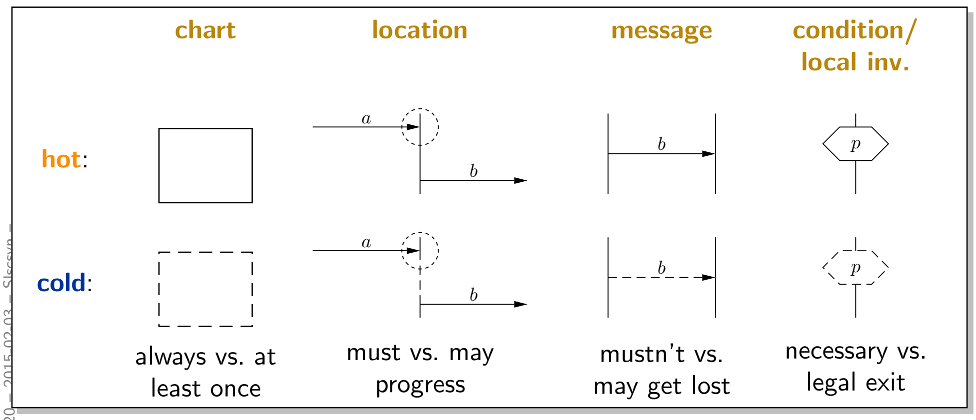
LSC Specialty: Modes

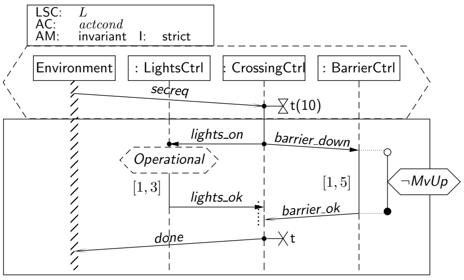
With LSCs,

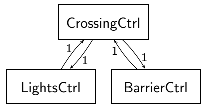
- whole charts,
- locations, and
- elements

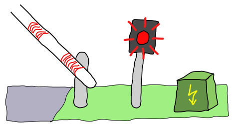
have a **mode** — one of **hot** or **cold** (graphically indicated by outline).



Example: Modes







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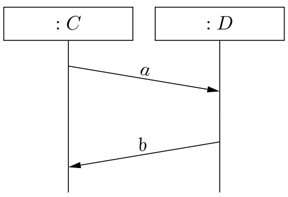
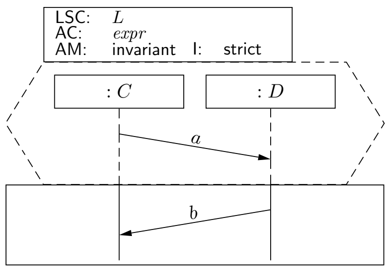
LSC Specialty: Activation

One **major defect** of **MSCs and SDs**: they don't say **when** the scenario has to/may be observed.



LSCs: Activation condition (AC $\in Expr_{\mathscr{S}}$), activation mode (AM $\in \{init, inv\}$), and pre-chart.



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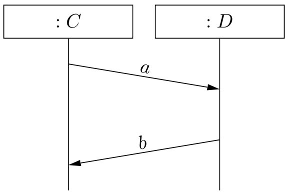

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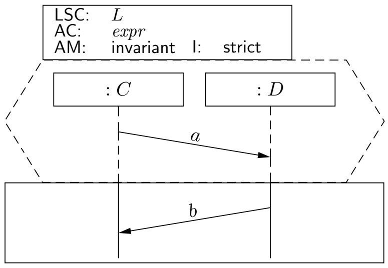
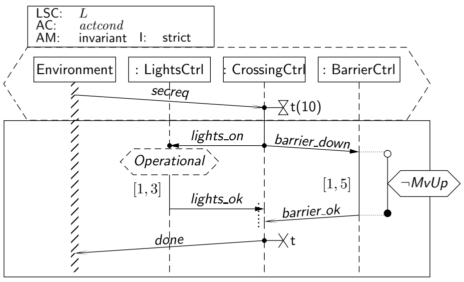


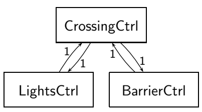
Intuition: (universal case)

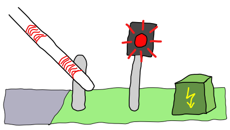
- given a computation π, **whenever** $expr$ holds in a configuration $(\sigma_i, \varepsilon_i)$ of ξ
  - which is initial, i.e. $k = 0$, or (AM $= initial$)
  - whose k is not further restricted, (AM $= invariant$)

  and if the pre-chart is observed from k to $k + n$,
  then the main-chart has to follow from $k + n + 1$.

Example: What Is Required?







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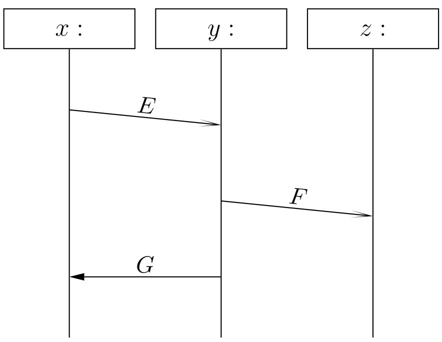
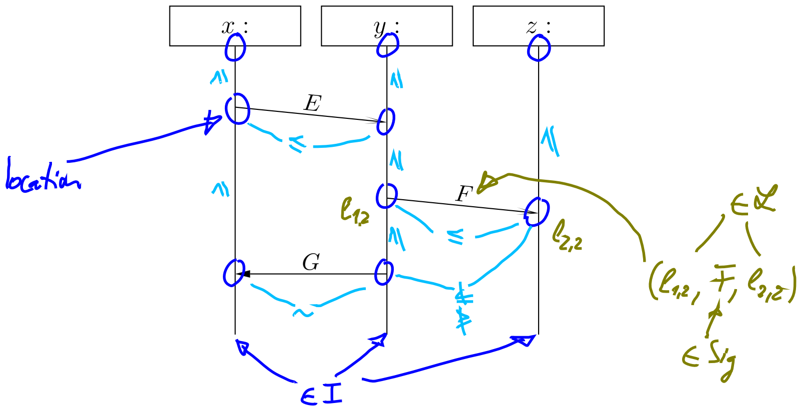
Live Sequence Charts — Semantics in a Nutshell

Restricted Syntax



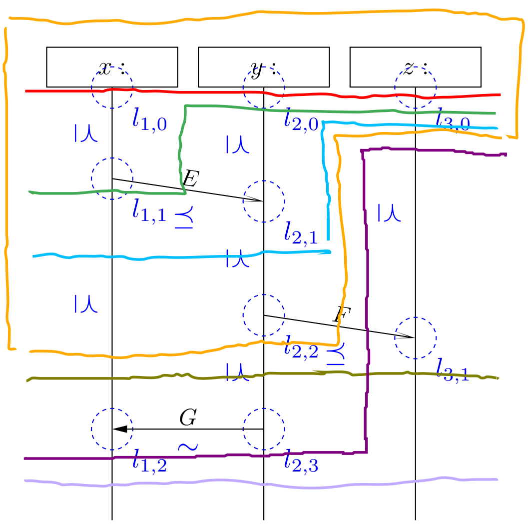
Restricted Abstract Syntax



$$(I, (\mathscr{L}, \preceq), \sim, \mathscr{S}, \mathsf{Msg})$$

instance lines, locations, partial, simultaneity, signature, message

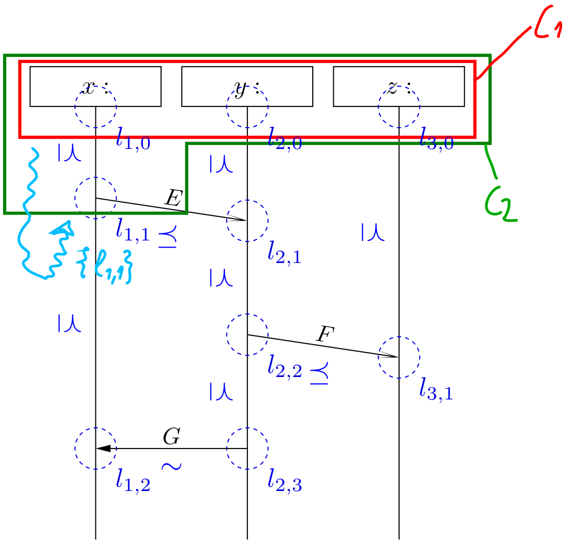
Cuts



A set $C \subseteq \mathscr{L}$ is called cut iff

- downward closed wrt. $\preceq$
- closed wrt. $\sim$
- at least one loc. per instance line (if more than one, then unordered)

Firedsets

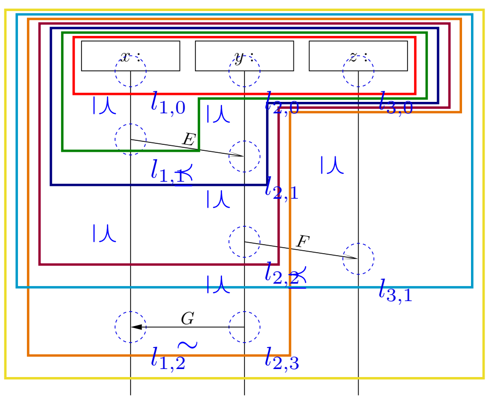


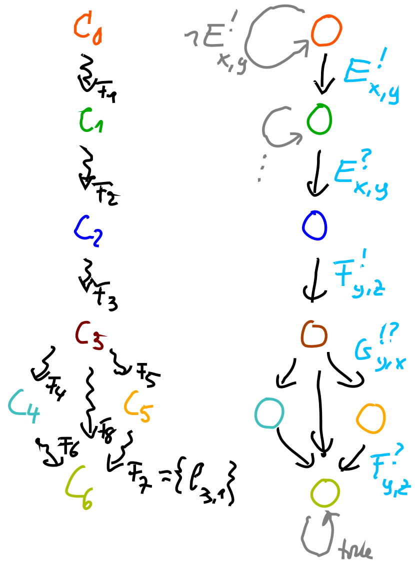
$C \rightsquigarrow_F C'$ iff

- $F \neq \emptyset$
- $C' \setminus C = F$
- for all event receptions in F, the sendings are in C
- direct successor:

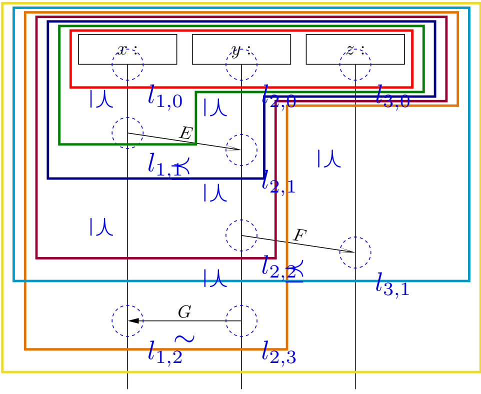
$\forall l \in F\ \exists l' \in \mathcal{L} \bullet l' \preceq l$
$\wedge \forall l'' \in \mathcal{L} \bullet l'' \preceq l$
$\Rightarrow l'' \preceq l'$

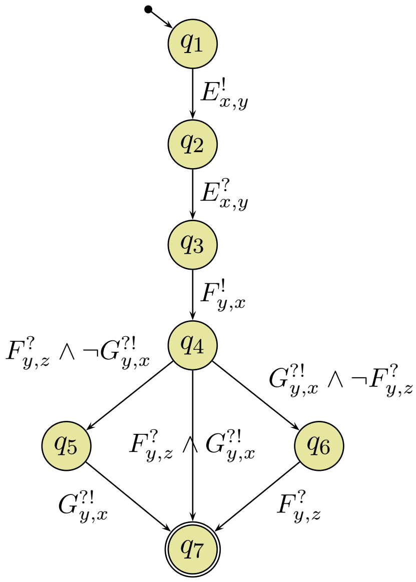
Towards Automata



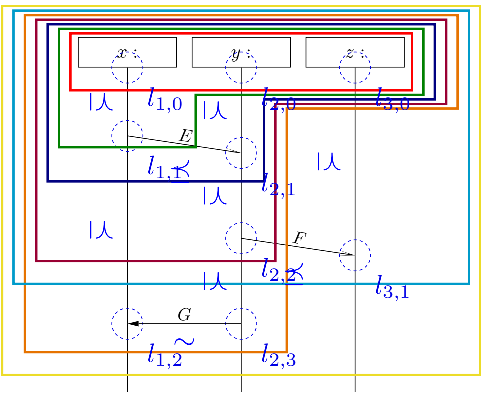


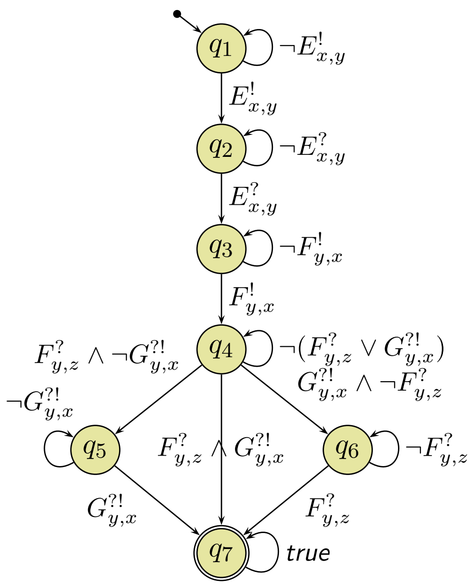
Alphabet — Progress Transitions



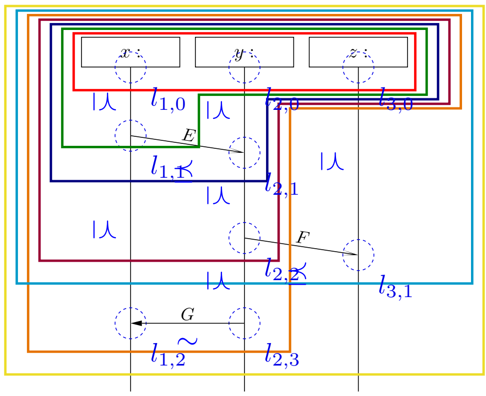


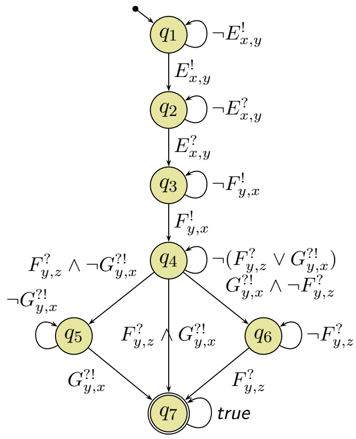
Loops





Language





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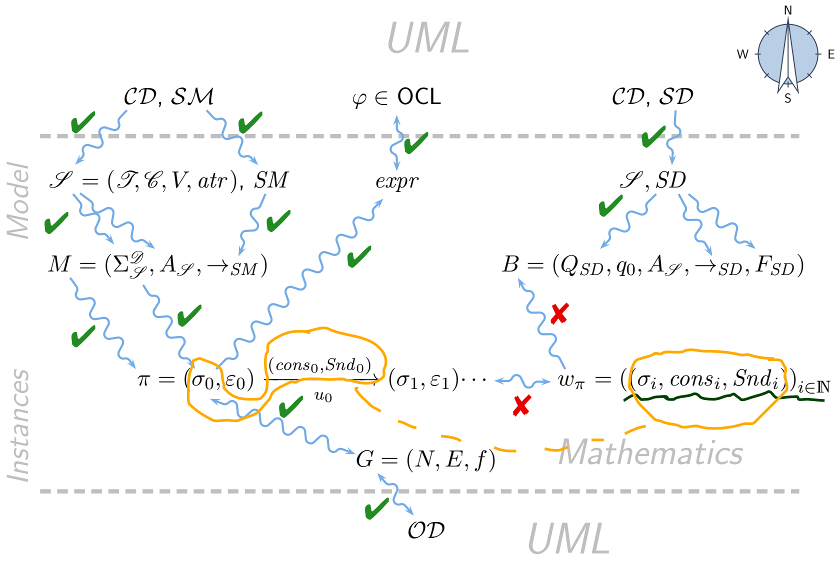
Course Map



Language of a Model

Words over Signature

Definition. Let $\mathscr{S} = (\mathscr{T}, \mathscr{C}, V, atr, \mathscr{E})$ be a signature and $\mathscr{D}$ a structure of $\mathscr{S}$. A **word** over $\mathscr{S}$ and $\mathscr{D}$ is an infinite sequence

$$(\sigma_i, cons_i, Snd_i)_{i \in \mathbb{N}_0} \in \left(\Sigma_{\mathscr{S}}^{\mathscr{D}} \times 2^{\mathscr{D}(\mathscr{C}) \times Evs(\mathscr{E},\mathscr{D}) \times \mathscr{D}(\mathscr{C})} \times 2^{\mathscr{D}(\mathscr{C}) \times Evs(\mathscr{E},\mathscr{D}) \times \mathscr{D}(\mathscr{C})}\right)^{\omega}.$$

The Language of a Model

Recall: A UML model $\mathcal{M} = (\mathscr{CD}, \mathscr{SM}, \mathscr{OD})$ and a structure $\mathscr{D}$ denotes a set $[\![\mathcal{M}]\!]$ of (initial and consecutive) **computations** of the form

$$(\sigma_0, \varepsilon_0) \xrightarrow{a_0} (\sigma_1, \varepsilon_1) \xrightarrow{a_1} (\sigma_2, \varepsilon_2) \xrightarrow{a_2} \ldots \text{ where}$$

$$a_i = (cons_i, Snd_i, u_i) \in \underbrace{2^{\mathscr{D}(\mathscr{C}) \times Evs(\mathscr{E},\mathscr{D}) \times \mathscr{D}(\mathscr{C})} \times 2^{\mathscr{D}(\mathscr{C}) \times Evs(\mathscr{E},\mathscr{D}) \times \mathscr{D}(\mathscr{C})}}_{=:\tilde{A}} \times \mathscr{D}(\mathscr{C}).$$

For the connection between models and interactions, we **disregard** the configuration of **the ether** and **who** made the step, and define as follows:

Definition. Let $\mathcal{M} = (\mathscr{CD}, \mathscr{SM}, \mathscr{OD})$ be a UML model and $\mathscr{D}$ a structure. Then

$$\mathcal{L}(\mathcal{M}) := \{(\sigma_i, cons_i, Snd_i)_{i \in \mathbb{N}_0} \in (\Sigma_{\mathscr{S}}^{\mathscr{D}} \times \tilde{A})^{\omega} \mid$$
$$\exists\, (\varepsilon_i, u_i)_{i \in \mathbb{N}_0} : (\sigma_0, \varepsilon_0) \xrightarrow[u_0]{(cons_0, Snd_0)} (\sigma_1, \varepsilon_1) \cdots \in [\![\mathcal{M}]\!]\}$$

is the **language** of $\mathcal{M}$.

Example: The Language of a Model

$$\mathcal{L}(\mathcal{M}) := \{(\sigma_i, cons_i, Snd_i)_{i \in \mathbb{N}_0} \in (\Sigma_{\mathscr{S}}^{\mathscr{D}} \times \tilde{A})^\omega \mid \exists\, (\varepsilon_i, u_i)_{i \in \mathbb{N}_0} : (\sigma_0, \varepsilon_0) \xrightarrow[u_0]{(cons_0, Snd_0)} (\sigma_1, \varepsilon_1) \cdots \in [\![\mathcal{M}]\!]\}$$

Signal and Attribute Expressions

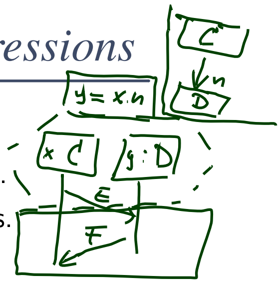
- Let $\mathscr{S} = (\mathscr{T}, \mathscr{C}, V, atr, \mathscr{E})$ be a signature and X a set of logical variables,
- The signal and attribute expressions $Expr_{\mathscr{S}}(\mathscr{E}, X)$ are defined by the grammar:

$$\psi ::= \textit{true} \mid expr \mid E^!_{x,y} \mid E^?_{x,y} \mid \neg\psi \mid \psi_1 \vee \psi_2 \mid E^{!?}_{x,y}$$

where $expr : Bool \in Expr_{\mathscr{S}}$, $E \in \mathscr{E}$, $x, y \in X$.

↖ set of variables

Satisfaction of Signal and Attribute Expressions



- Let $(\sigma, cons, Snd) \in \Sigma_{\mathscr{S}}^{\mathscr{D}} \times \tilde{A}$ be a triple consisting of **system state**, **consume set**, and **send set**.
- Let $\beta : X \to \mathscr{D}(\mathscr{C})$ be a valuation of the logical variables.

Then

- $(\sigma, cons, Snd) \models_\beta \mathit{true}$
- $(\sigma, cons, Snd) \models_\beta \neg\psi$ if and only if not $(\sigma, cons, Snd) \models_\beta \psi$
- $(\sigma, cons, Snd) \models_\beta \psi_1 \vee \psi_2$ if and only if $(\sigma, cons, Snd) \models_\beta \psi_1$ or $(\sigma, cons, Snd) \models_\beta \psi_2$
- $(\sigma, cons, Snd) \models_\beta expr$ if and only if $I[\![expr]\!](\sigma, \beta) = 1$
- $(\sigma, cons, Snd) \models_\beta E^!_{x,y}$ if and only if $\exists\, \vec{d} \bullet (\beta(x), (E, \vec{d}), \beta(y)) \in Snd$
- $(\sigma, cons, Snd) \models_\beta E^?_{x,y}$ if and only if $\exists\, \vec{d} \bullet (\beta(x), (E, \vec{d}), \beta(y)) \in cons$

Observation: semantics of models **keeps track** of sender and receiver at sending and consumption time. We disregard the event identity.
Alternative: keep track of event identities.

TBA over Signature

Definition. A TBA

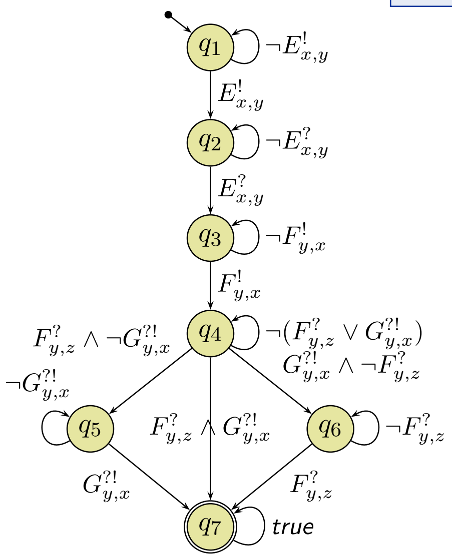
$$\mathcal{B} = (Expr_{\mathcal{B}}(X), X, Q, q_{ini}, \to, Q_F)$$

where $Expr_{\mathcal{B}}(X)$ is the set of **signal and attribute expressions** $Expr_{\mathscr{S}}(\mathscr{E}, X)$ over signature $\mathscr{S}$ is called **TBA over $\mathscr{S}$**.

- Any word over $\mathscr{S}$ and $\mathscr{D}$ is then a word for $\mathcal{B}$.
(By the satisfaction relation defined on the previous slide; $\mathscr{D}(X) = \mathscr{D}(\mathscr{C})$.)
- Thus a TBA over $\mathscr{S}$ accepts words of models with signature $\mathscr{S}$.
(By the previous definition of TBA.)

TBA over Signature Example

$(\sigma, cons, Snd) \models_\beta expr$ iff $I[\![expr]\!](\sigma, \beta) = 1$;
$(\sigma, cons, Snd) \models_\beta E^!_{x,y}$ iff $(\beta(x), (E, \vec{d}), \beta(y)) \in Snd$

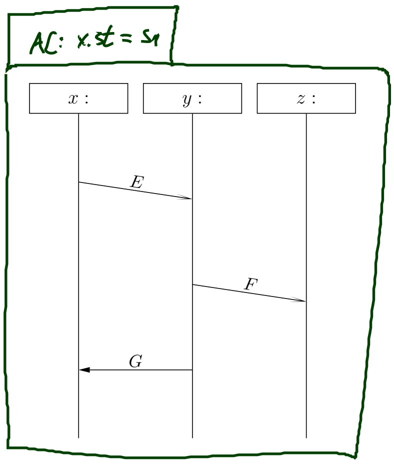


– 20 – 2015-02-03 – Smodellang –

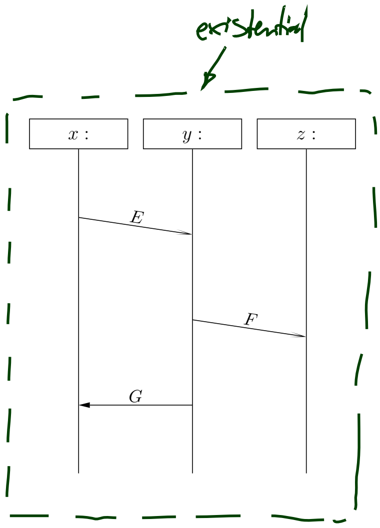
Activation, Chart Mode

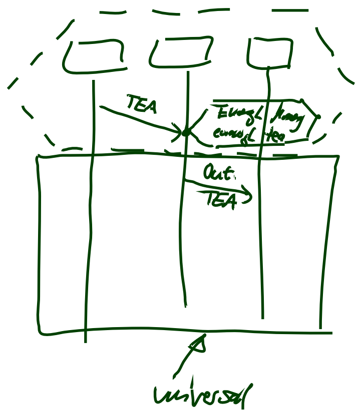
– 20 – 2015-02-03 – main –

Activation Condition

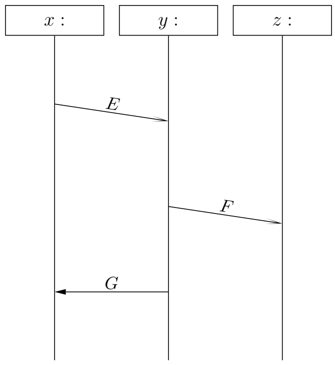


Universal vs. Existential Charts



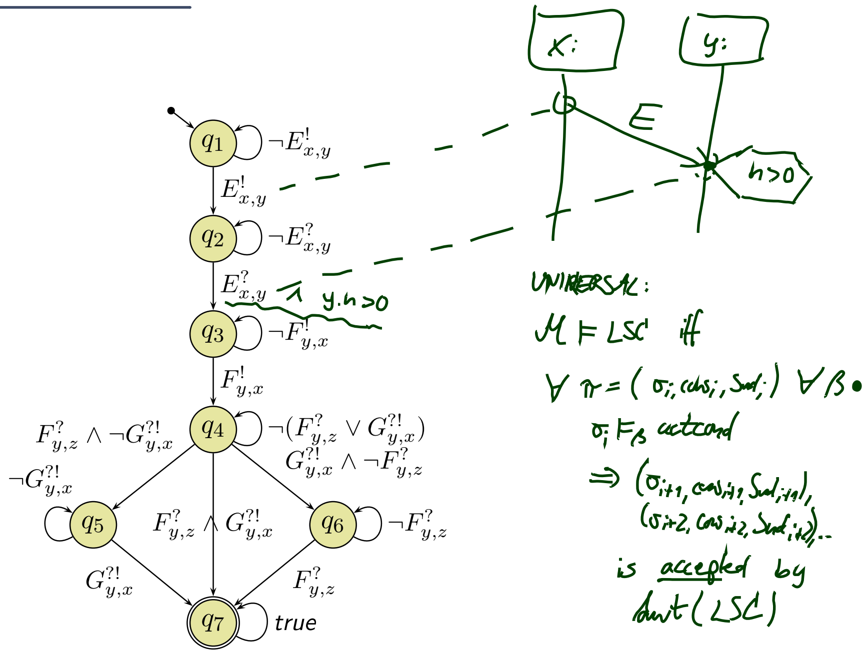


Prechart



Conditions

Conditions



Back to UML: Interactions

Model Consistency wrt. Interaction

- We assume that the set of interactions $\mathscr{I}$ is partitioned into two (possibly empty) sets of **universal** and **existential** interactions, i.e.

$$\mathscr{I} = \mathscr{I}_\forall \,\dot{\cup}\, \mathscr{I}_\exists.$$

Definition. A model

$$\mathcal{M} = (\mathscr{C}\mathscr{D}, \mathscr{S}\mathscr{M}, \mathscr{O}\mathscr{D}, \mathscr{I})$$

is called **consistent** (more precise: the constructive description of behaviour is consistent with the reflective one) if and only if

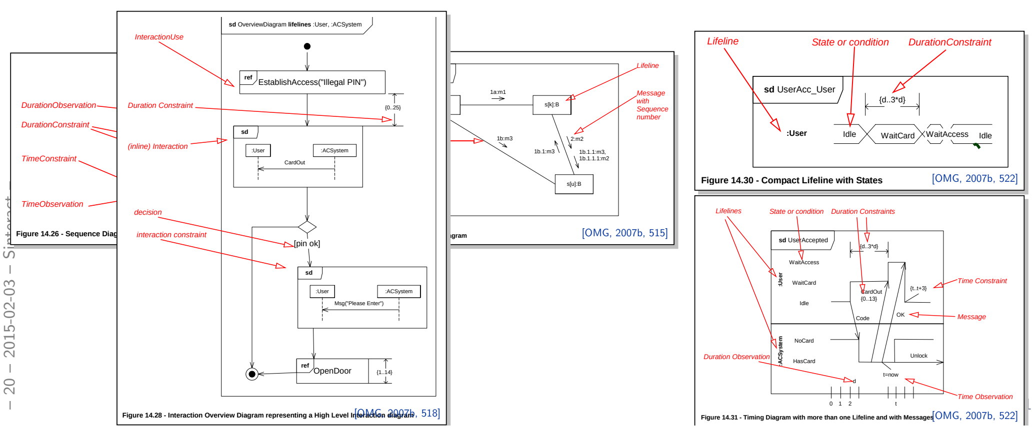
$$\forall \mathcal{I} \in \mathscr{I}_\forall : \mathcal{L}(\mathcal{M}) \subseteq \mathcal{L}(\mathcal{I})$$

and

$$\forall \mathcal{I} \in \mathscr{I}_\exists : \mathcal{L}(\mathcal{M}) \cap \mathcal{L}(\mathcal{I}) \neq \emptyset.$$

Interactions as Reflective Description

- In UML, reflective (temporal) descriptions are subsumed by **interactions**.
- A UML model $\mathcal{M} = (\mathscr{C}\mathscr{D}, \mathscr{S}\mathscr{M}, \mathscr{O}\mathscr{D}, \mathscr{I})$ has a set of interactions $\mathscr{I}$.
- An interaction $\mathcal{I} \in \mathscr{I}$ can be (OMG claim: equivalently) **diagrammed** as
  - **sequence diagram**, **timing diagram**, or
  - **communication diagram** (formerly known as collaboration diagram).



Interactions as Reflective Description

- In UML, reflective (temporal) descriptions are subsumed by **interactions**.
- A UML model $\mathcal{M} = (\mathscr{CD}, \mathscr{SM}, \mathscr{OD}, \mathscr{I})$ has a set of interactions $\mathscr{I}$.
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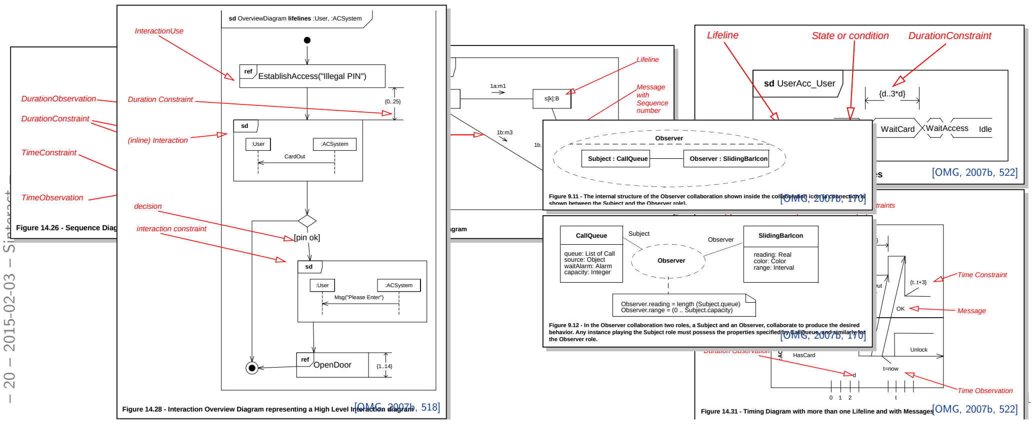


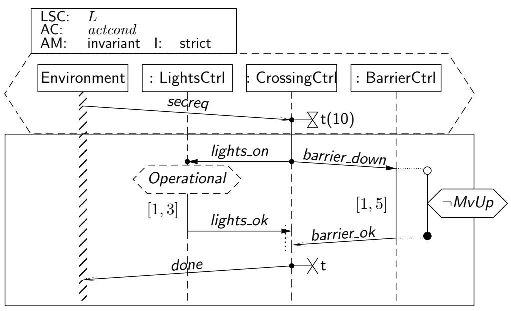
Why Sequence Diagrams?

Most Prominent: Sequence Diagrams — with **long history**:

- **Message Sequence Charts**, standardized by the ITU in different versions, often accused to lack a formal semantics.
- **Sequence Diagrams** of UML 1.x

Most severe **drawbacks** of these formalisms:

- unclear **interpretation**: example scenario or invariant?
- unclear **activation**: what triggers the requirement?
- unclear **progress** requirement: must all messages be observed?
- **conditions** merely comments
- no means to express **forbidden scenarios**



Thus: Live Sequence Charts

- **SDs of UML 2.x** address **some** issues, yet the standard exhibits unclarities and even contradictions [Harel and Maoz, 2007, Störrle, 2003]
- For the lecture, we consider **Live Sequence Charts** (LSCs) [Damm and Harel, 2001, Klose, 2003, Harel and Marelly, 2003], who have a common fragment with UML 2.x SDs [Harel and Maoz, 2007]
- **Modelling guideline**: stick to that fragment.

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