# Software Design, Modelling and Analysis in UML

# Lecture 10: Class Diagrams V

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### Associations in General

Recall: We consider associations of the following form:

 $\langle r:\langle role_1:C_1,\mu_1,P_1,\xi_1,\nu_1,o_1\rangle,\ldots,\langle role_n:C_n,\mu_n,P_n,\xi_n,\nu_n,o_n\rangle\rangle$ 

Only these parts are relevant for extended system states:

 $\langle r: \langle role_1: C_1, \_, P_1, \_, \_ - \rangle, \ldots, \langle role_n: C_n, \_, P_n, \_, \_ - \rangle$ 

(recall: we assume  $P_1=P_n=\{\mathtt{unique}\}$ ).

The UML standard thinks of associations as n-ary relations which "live on their own" in a system state.

That is, links (= association instances)

- do not belong (in general) to certain objects (in contrast to pointers, e.g.)
- are "first-class citizens" next to objects,
- are (in general) not directed (in contrast to pointers).

### Contents & Goals

### Last Lectures:

associations syntax and semantics

#### This Lecture:

Educational Objectives: Capabilities for following tasks/questions.

Association Semantics: The System State Aspect

- Please explain this class diagram with associations.
   Which annotations of an association arrow are semantically relevant?
   What's a role name? What's it good for?
- What is "multiplicity"? How did we treat them semantically?
   What is "reading direction", "navigability", "ownership", . . .?
   What's the difference between "aggregation" and "composition"?
- Associations and OCL
- Btw.: where do we put OCL constraints?

### Links in System States

 $\langle r: \langle role_1: C_1, \_, P_1, \_, \_, \_ \rangle, \ldots, \langle role_n: C_n, \_, P_n, \_, \_ \rangle$ 

Only for the course of Lectures 9/10 we change the definition of system states:

 a type-consistent mapping A system state of  ${\mathscr S}$  wrt.  ${\mathscr D}$  is a pair  $(\sigma,\lambda)$  consisting of Definition. Let  $\mathscr D$  be a structure of the (extended) signature  $\mathscr S=(\mathscr T,\mathscr C,V,atr).$ 

 $\sigma: \mathscr{D}(\mathscr{C}) \nrightarrow (atr(\mathscr{C}) \nrightarrow \mathscr{D}(\mathscr{T})),$ 

• a mapping  $\lambda$  which assigns each association  $\langle r:\langle role_1:C_1\rangle,\ldots,\langle role_n:C_n\rangle\rangle\in V$  a relation

 $\lambda(r) \subseteq \mathscr{D}(C_1) \times \cdots \times \mathscr{D}(C_n)$ 

(i.e. a set of type-consistent n-tuples of identities)

Association/Link Example



$$\begin{split} \mathscr{S} &= (\{Int\}, \{C, D\}, \{x: Int, \\ \langle A.C.D: \langle c: C, 0, *, *, *, \{unique\}, \times, 1\rangle, \\ \langle n: D, 0, *, *, \{unique\}, \times, 1\rangle, \\ \{C \mapsto \emptyset, D \mapsto \{x\}\} ) \end{split}$$

A system state of  ${\mathscr S}$  (some reasonable  ${\mathscr D}$ ) is  $(\sigma,\lambda)$  with:

 $\sigma = \{1_C \mapsto \emptyset, 3_D \mapsto \{x \mapsto 1\}, 7_D \mapsto \{x \mapsto 2\}\}$  $\lambda = \{A.C.D \mapsto \{(1_C, 3_D), (1_C, 7_D)\}\}$ 

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# Extended System States and Object Diagrams

Legitimate question: how do we represent system states such as

 $\sigma = \{1_C \mapsto \emptyset, 3_D \mapsto \{x \mapsto 1\}, 7_D \mapsto \{x \mapsto 2\}\}$  $\lambda = \{A\_C\_D \mapsto \{(1_C, 3_D), (1_C, 7_D)\}\}$ 

as object diagram?

OCL and Associations: Syntax

Recall: OCL syntax as introduced in Lecture 03, interesting part:

$$\begin{array}{ccc} expr := \dots & | r_1(expr_1) & : \tau_C \rightarrow \tau_D & r_1 : D_{0,1} \in atr(C) \\ | r_2(expr_1) & : \tau_C \rightarrow Set(\tau_D) & r_2 : D_* \in atr(C) \end{array}$$

#### Now becomes

 $\langle r:\dots,\langle role:D,\mu,\dots,\dots\rangle,\dots\rangle\in V \text{ or } \\ \langle r:\dots,\langle role':C,\dots,\dots\rangle\in V, role\neq role'.$  $expr ::= \dots$  $\begin{array}{ll} |\ role(expr_1) &: \tau_C \to \tau_D & \mu = 0..1 \ \text{or} \ \mu = 1 \\ |\ role(expr_1) &: \tau_C \to Set(\tau_D) & \text{otherwise} \end{array}$ 

- Association name as such doesn't occur in OCL syntax, role names do.
   expr<sub>1</sub> has to denote an object of a class which "participates" in the association.

Associations and OCL

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# OCL and Associations Syntax: Example

 $\begin{array}{l} \langle r:\dots,\langle role:D,\mu,\dots,\dots\rangle, role':C,\dots,\dots\rangle\in V \text{ or } \\ \langle r:\dots,\langle role':C,\dots,\dots\rangle,\langle role:D,\mu,\dots,\dots\rangle\in V, role\neq role'. \end{array}$  $\begin{array}{ll} \textit{expr} ::= \dots & | \ \textit{role} (\textit{expr}_1) & : \tau_C \to \tau_D & \mu = 0..1 \ \textit{or} \ \mu = 1 \\ | \ \textit{role} (\textit{expr}_1) & : \tau_C \to \textit{Set} (\tau_D) & \text{otherwise} \end{array}$ 

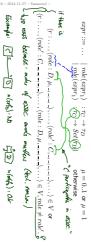


### OCL and Associations: Syntax

# Recall: OCL syntax as introduced in Lecture 03, interesting part:



### Now becomes



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## OCL and Associations: Semantics

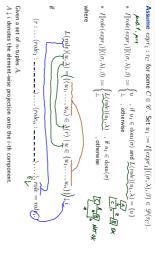
### Recall: (Lecture 03)



### $I[\![role(\mathit{expr}_1)]\!]((\sigma,\lambda),\beta)$

- We cannot simply write \(\sigma(u)(\pi let)\).
   Recalt: \(\pi de \) is \(\frac{f(\pi)}{n}\) the momenth not an attribute of object \(u\) (not in \(\sigma r(C)\)).
   What we have \(\frac{k}{n}\) (a \(\pi/r)\) (not with \(\pi de t)\) but it yields a set of \(\pi \- \text{tuples}\), of which some relate \(u\) and other some instances of \(D\).
- role denotes the position of the D's in the tuples constituting the value of r.

# OCL and Associations: Semantics Cont'd



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### The Rest

## Recapitulation: Consider the following association:

 $\langle r: \langle role_1: C_1, \mu_1, P_1, \xi_1, \nu_1, o_1 \rangle, \ldots, \langle role_n: C_n, \mu_n, P_n, \xi_n, \nu_n, o_n \rangle \rangle$ 

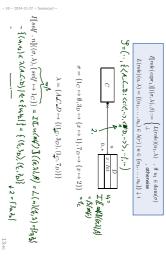
- Association name r and role names/types  $role_i/C_i$  induce extended system states  $\lambda$ .
- Multiplicity  $\mu$  is considered in OCL syntax.
- Visibility ξ/Navigability ν: well-typedness.

#### Now the rest:

- Multiplicity \(\mu\): we propose to view them as constraints.
- Properties P<sub>i</sub>: even more typing.
- Ownership o: getting closer to pointers/references.
   Diamonds: exercise.

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# OCL and Associations Example



Associations: The Rest

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Rhapsody Demo

References

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[OMG, 2007b] OMG (2007b). Unified modeling language: Superstructure, version 2.1.2. Technical Report formal/07-11-02.

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