

# *Software Design, Modelling and Analysis in UML*

## *Lecture 20: Live Sequence Charts*

*2015-02-03*

Prof. Dr. Andreas Podelski, **Dr. Bernd Westphal**

Albert-Ludwigs-Universität Freiburg, Germany

# *Contents & Goals*

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## Last Lecture:

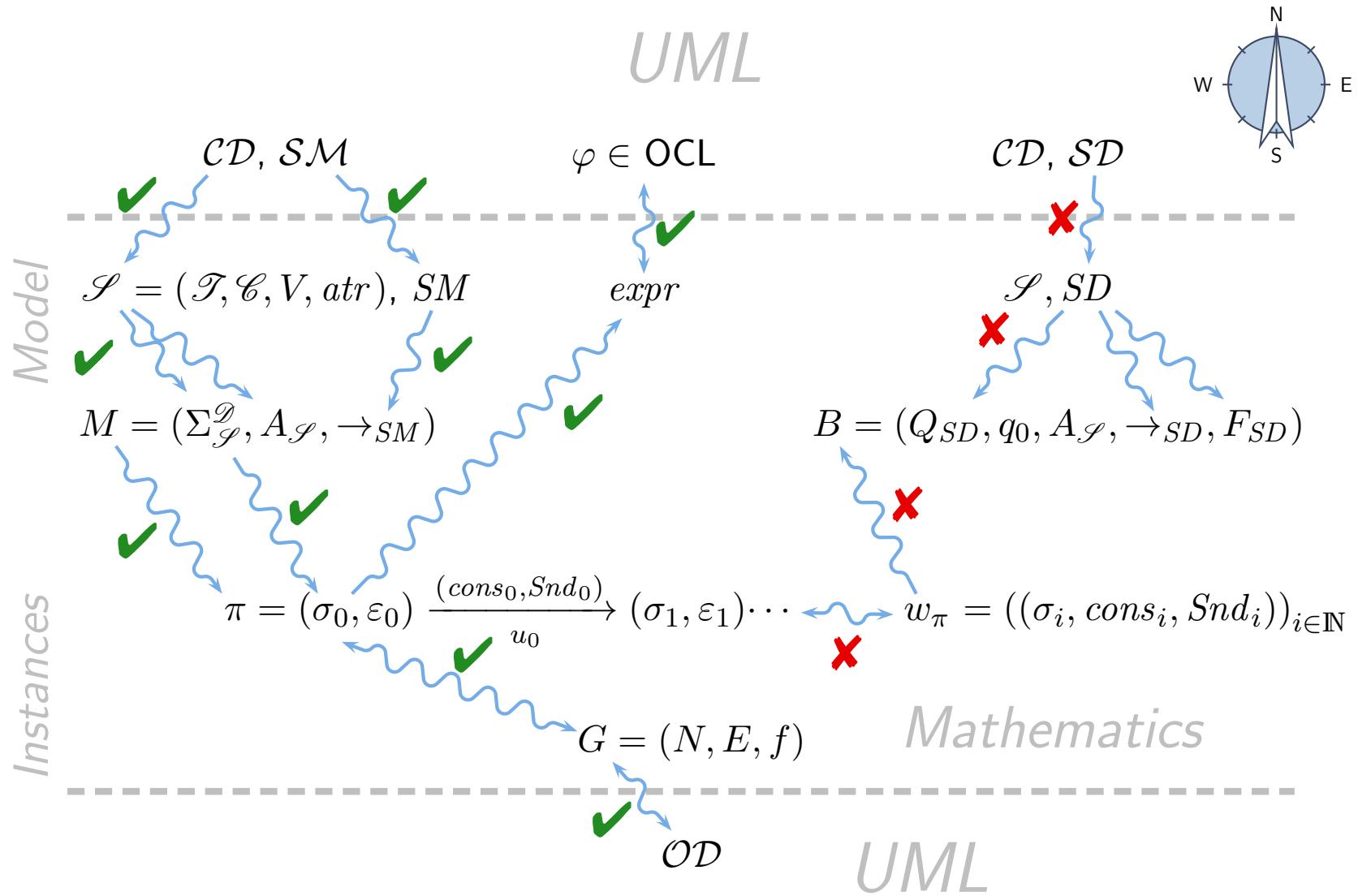
- Hierarchical State Machines completed.
- Behavioural feature (aka. methods).

## This Lecture:

- **Educational Objectives:** Capabilities for following tasks/questions.
  - What does this LSC mean?
  - Are this UML model's state machines consistent with the interactions?
  - Please provide a UML model which is consistent with this LSC.
  - What is: activation, hot/cold condition, pre-chart, etc.?
- **Content:**
  - Reflective description of behaviour.
  - LSC concrete and abstract syntax.
  - LSC semantics.

*You are here.*

# Course Map



# *Motivation: Reflective, Dynamic Descriptions of Behaviour*

# *Recall: Constructive vs. Reflective Descriptions*

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[Harel, 1997] proposes to distinguish constructive and reflective descriptions:

- “A language is **constructive** if it contributes to the dynamic semantics of the model. That is, its constructs contain information needed in executing the model or in translating it into executable code.”

A constructive description tells **how** things are computed (which can then be desired or undesired).

- “Other languages are **reflective** or **assertive**, and can be used by the system modeler to capture parts of the thinking that go into building the model – behavior included –, to derive and present views of the model, statically or during execution, or to set constraints on behavior in preparation for verification.”

A reflective description tells **what** shall or shall not be computed.

**Note:** No sharp boundaries!

# Recall: What is a Requirement?

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## Recall:

- The **semantics** of the **UML model**  $\mathcal{M} = (\mathcal{CD}, \mathcal{SM}, \mathcal{OD})$  is the **transition system**  $(S, \rightarrow, S_0)$  constructed according to discard/dispatch/commence-rules.
- The **computations** of  $\mathcal{M}$ , denoted by  $\llbracket \mathcal{M} \rrbracket$ , are the computations of  $(S, \rightarrow, S_0)$ .

## Now:

A reflective description tells **what** shall or shall not be computed.

**More formally:** a requirement  $\vartheta$  is a property of computations; something which is either satisfied or not satisfied by a computation

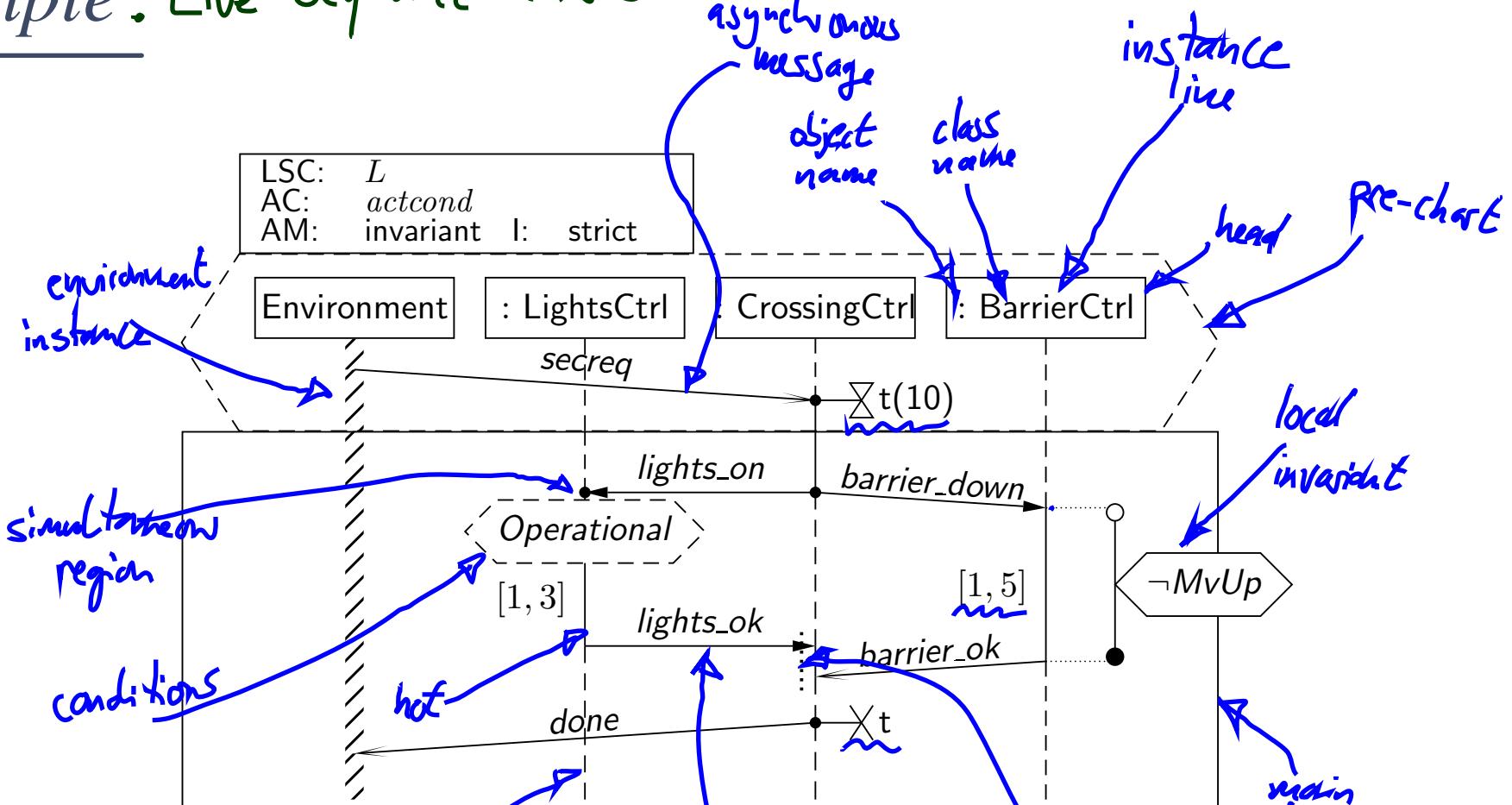
$$\pi = (\sigma_0, \varepsilon_0) \xrightarrow{(cons_0, Snd_0)} (\sigma_1, \varepsilon_1) \xrightarrow{(cons_1, Snd_1)} \dots \in \llbracket \mathcal{M} \rrbracket,$$

denoted by  $\pi \models \vartheta$  and  $\pi \not\models \vartheta$ , resp.

Simplest case: OCL constraint.

## *Live Sequence Charts — Concrete Syntax*

# Example: Live Sequence Charts

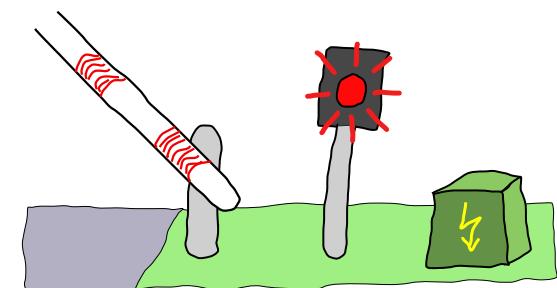


`⟨⟨signal, env⟩⟩`  
secreq

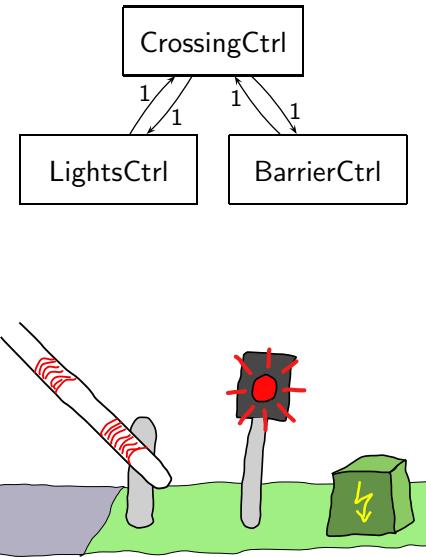
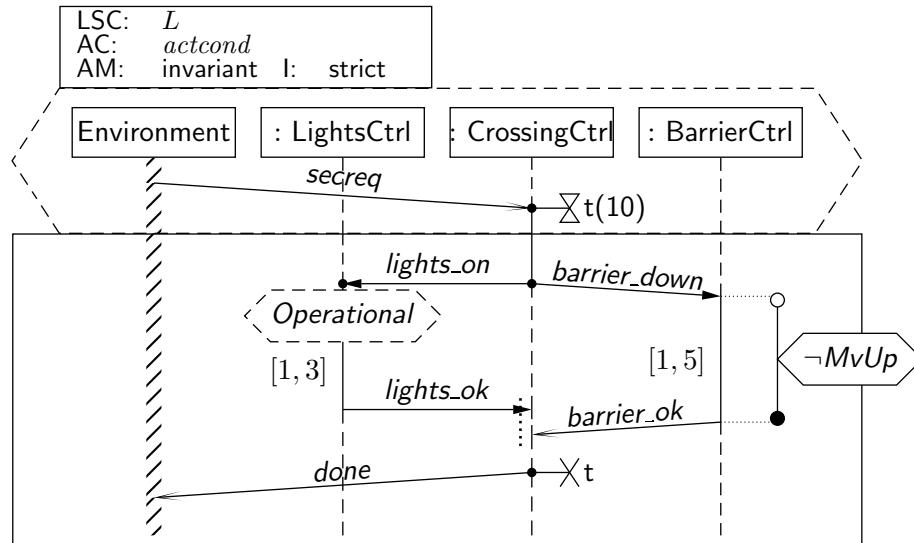
CrossingCtrl  
lights\_ok()

`⟨⟨signal⟩⟩`  
barrier\_down  
barrier\_ok  
done

LightsCtrl  
Operational : Bool  
lights\_on()  
BarrierCtrl  
MvUp : Bool

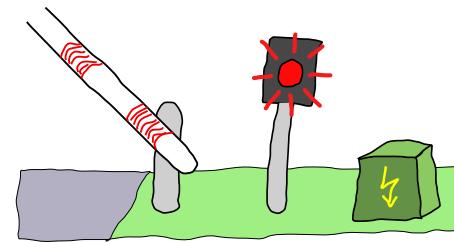
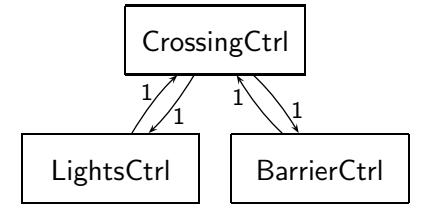
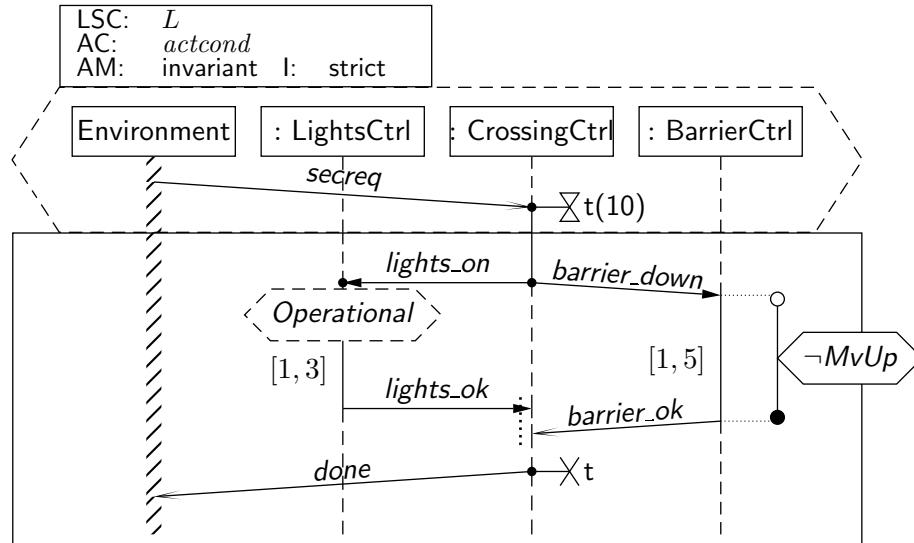


# Example: What Is Required?

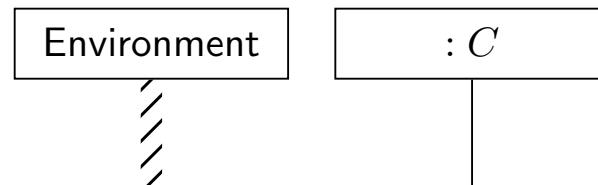


- Whenever the CrossingCtrl has consumed a 'secreq' event
- then it shall finally send 'lights\_on' and 'barrier\_down' to LightsCtrl and BarrierCtrl,
- if LightsCtrl is not 'operational' when receiving that event,  
the rest of this scenario doesn't apply; maybe there's another LSC for that case.
- if LightsCtrl is 'operational' when receiving that event,  
it shall reply with 'lights\_ok' within 1–3 time units,
- the BarrierCtrl shall reply with 'barrier\_ok' within 1–5 time units, during this time  
(dispatch time not included) it shall not be in state 'MvUp',
- 'lights\_ok' and 'barrier\_ok' may occur in any order.
- After having consumed both, CrossingCtrl may reply with 'done' to the environment.

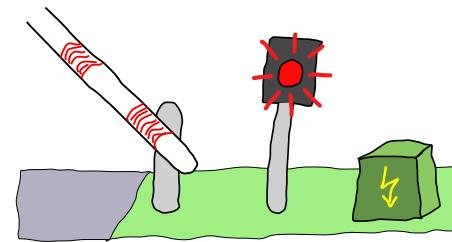
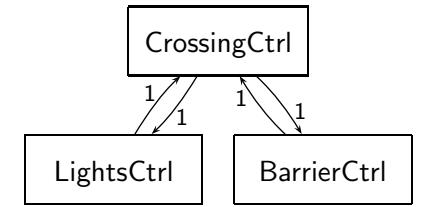
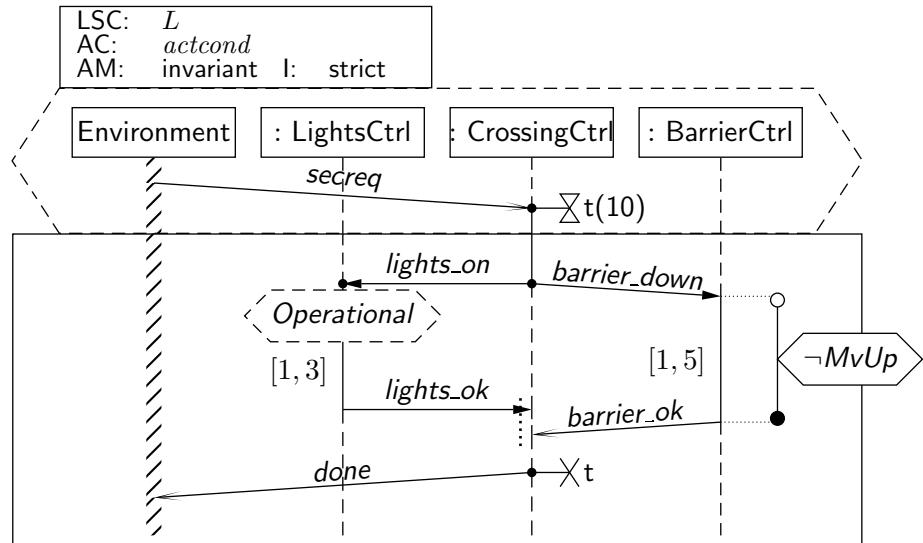
# Building Blocks



- Instance Lines:

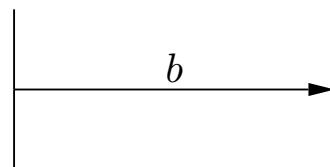
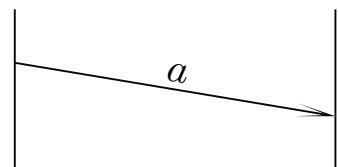


# *Building Blocks*

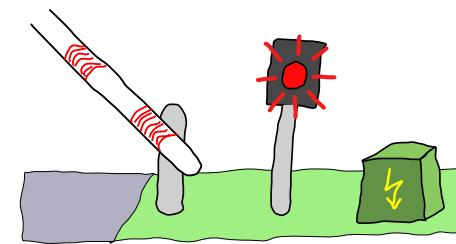
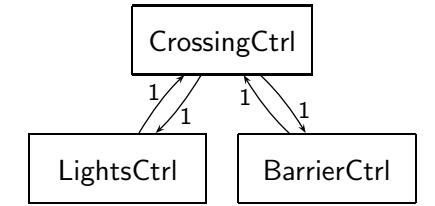
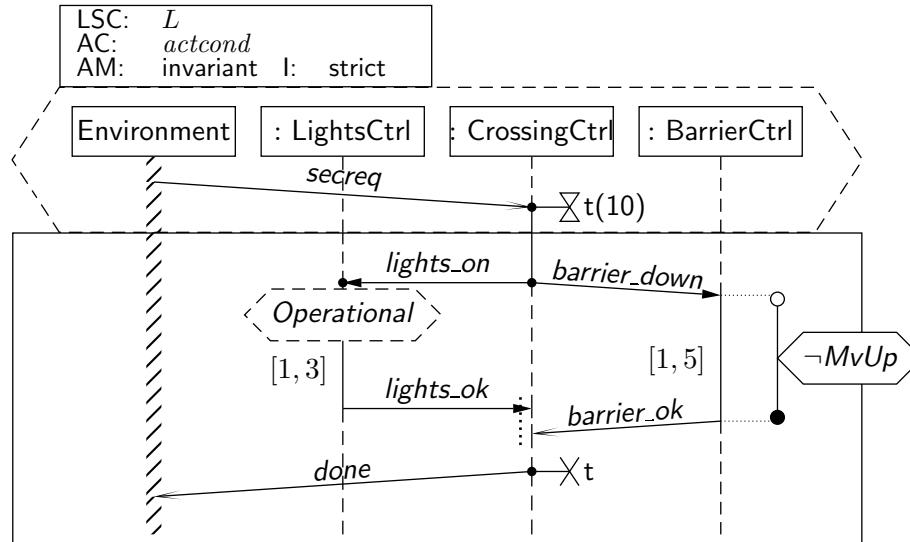


- **Messages:** (asynchronous or synchronous/instantaneous)

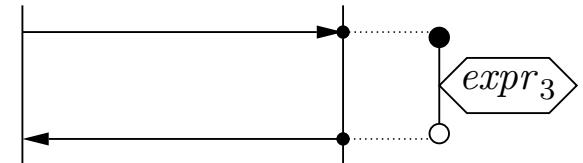
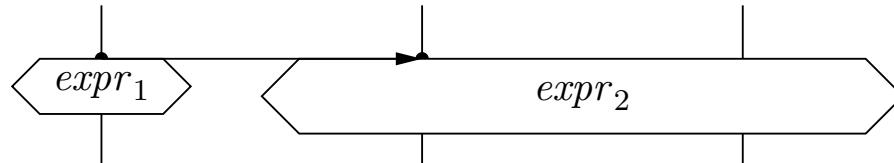
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# Building Blocks



- Conditions and Local Invariants: ( $expr_1, expr_2, expr_3 \in Expr_{\mathcal{S}}$ )



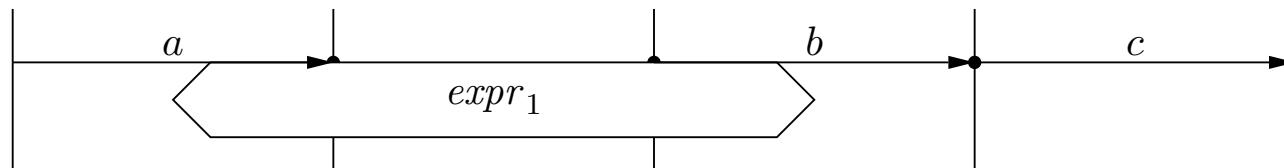
# *Intuitive Semantics: A Partial Order on Simclasses*

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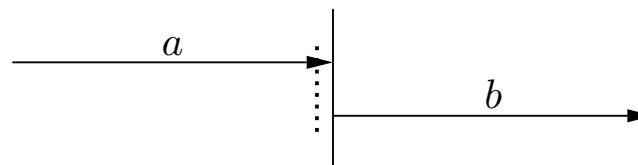
(i) **Strictly After:**



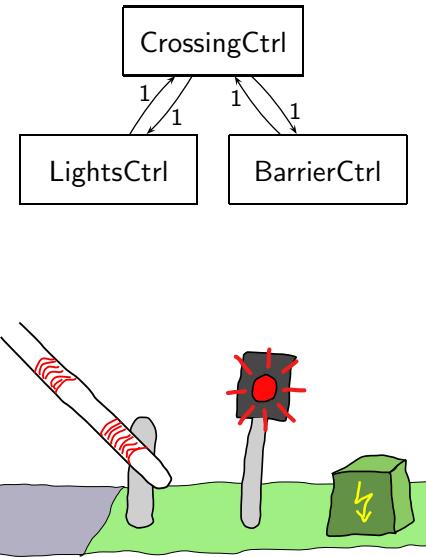
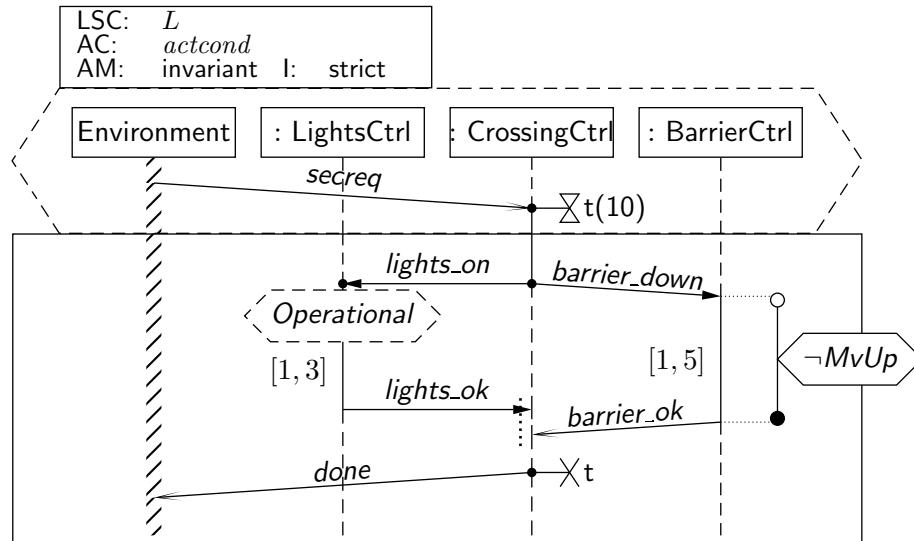
(ii) **Simultaneously:** (simultaneous region)



(iii) **Explicitly Unordered:** (co-region)



# Partial Order Requirements



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the rest of this scenario doesn’t apply; maybe there’s another LSC for that case.
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(dispatch time not included) it shall not be in state ‘MvUp’,
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# LSC Specialty: Modes

With LSCs,

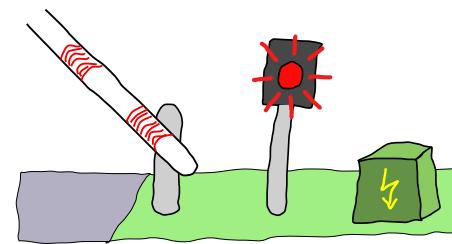
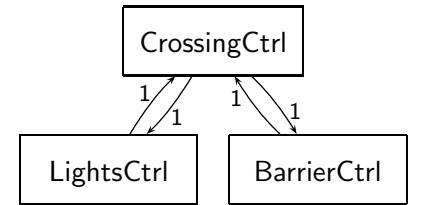
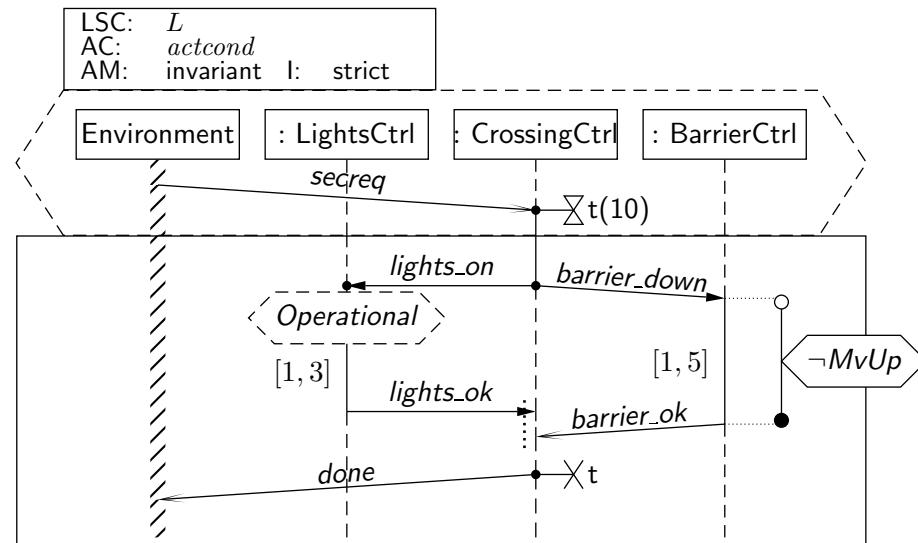
- whole charts,
- locations, and
- elements

have a **mode** — one of **hot** or **cold** (graphically indicated by outline).

	chart	location	message	condition/ local inv.
hot:				
cold:				

always vs. at least once      must vs. may progress      mustn't vs. may get lost      necessary vs. legal exit

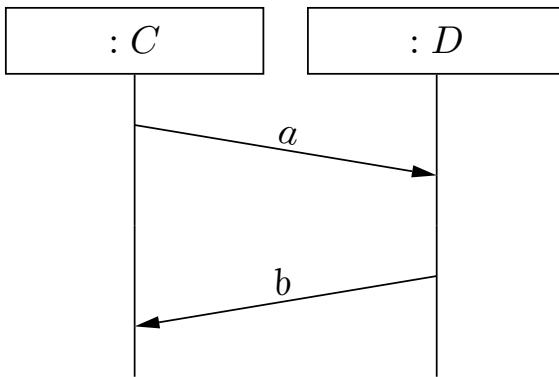
## *Example: Modes*



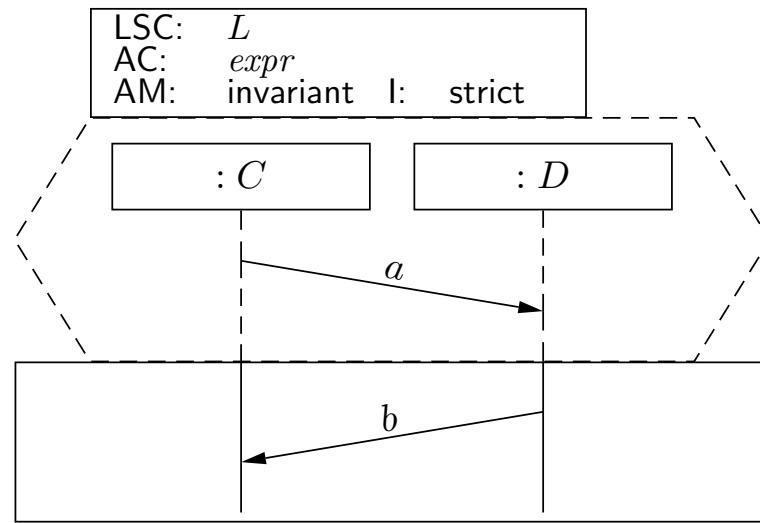
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# LSC Specialty: Activation

One **major defect** of **MSCs and SDs**: they don't say **when** the scenario has to/may be observed.

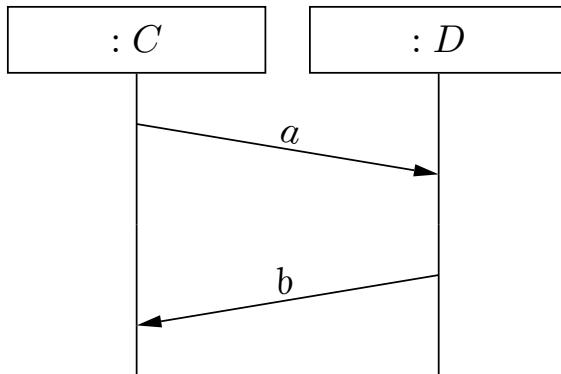


**LSCs:** Activation condition ( $AC \in Expr_{\mathcal{S}}$ ), activation mode ( $AM \in \{init, inv\}$ ), and pre-chart.

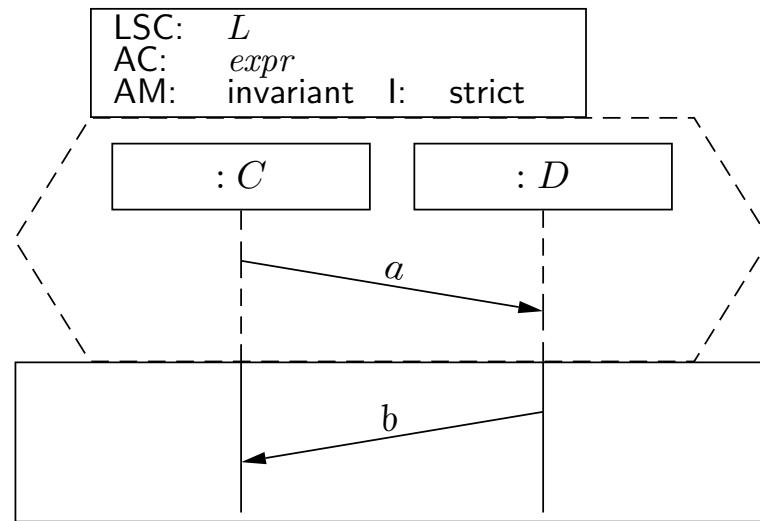


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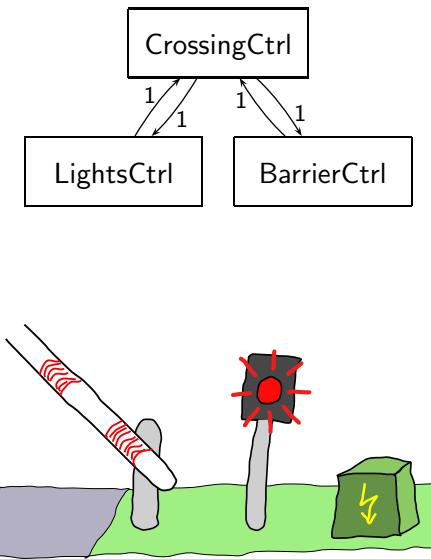
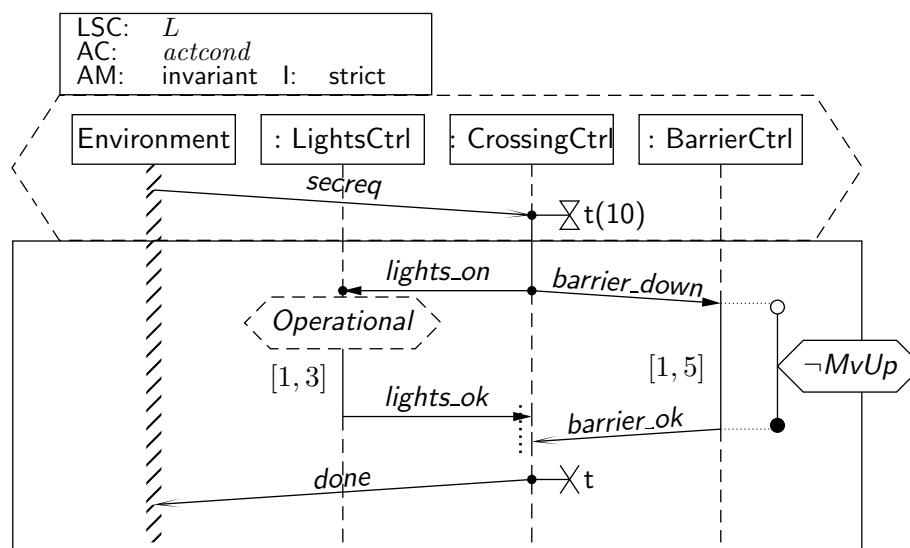
**LSCs**: Activation condition ( $AC \in Expr_{\mathcal{S}}$ ), activation mode ( $AM \in \{init, inv\}$ ), and pre-chart.



**Intuition:** (universal case)

- given a computation  $\pi$ , **whenever**  $expr$  holds in a configuration  $(\sigma_i, \varepsilon_i)$  of  $\xi$ 
  - which is initial, i.e.  $k = 0$ , or  $(AM = initial)$
  - whose  $k$  is not further restricted,  $(AM = invariant)$
- **and if** the pre-chart is observed from  $k$  to  $k + n$ ,  
**then** the main-chart has to follow from  $k + n + 1$ .

# Example: What Is Required?

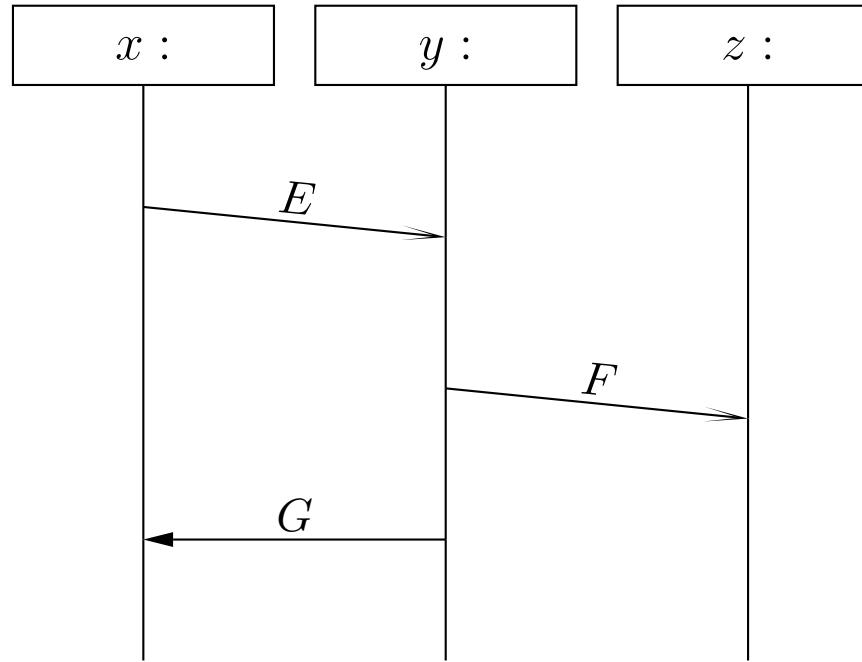


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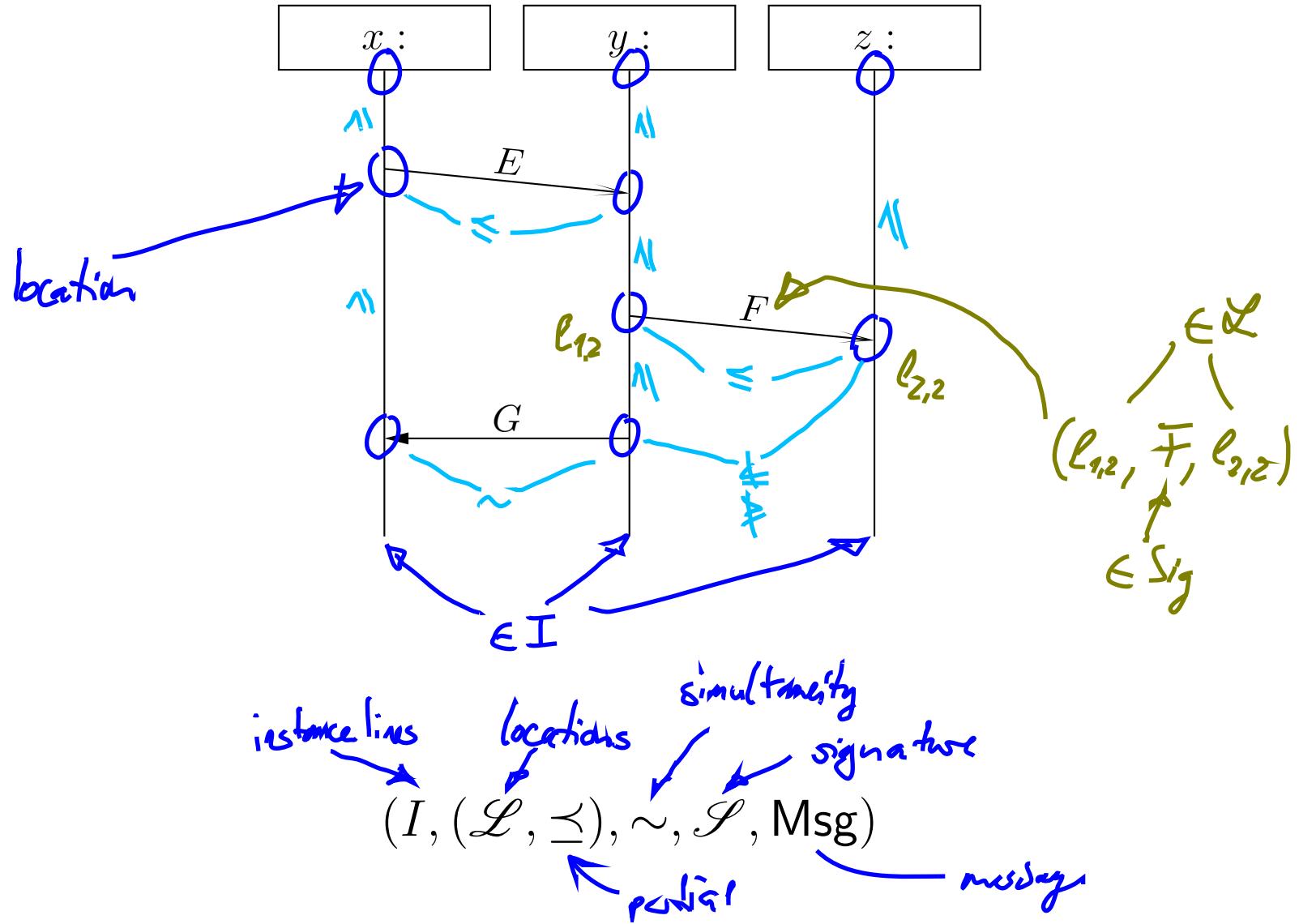
## *Live Sequence Charts — Semantics in a Nutshell*

# *Restricted Syntax*

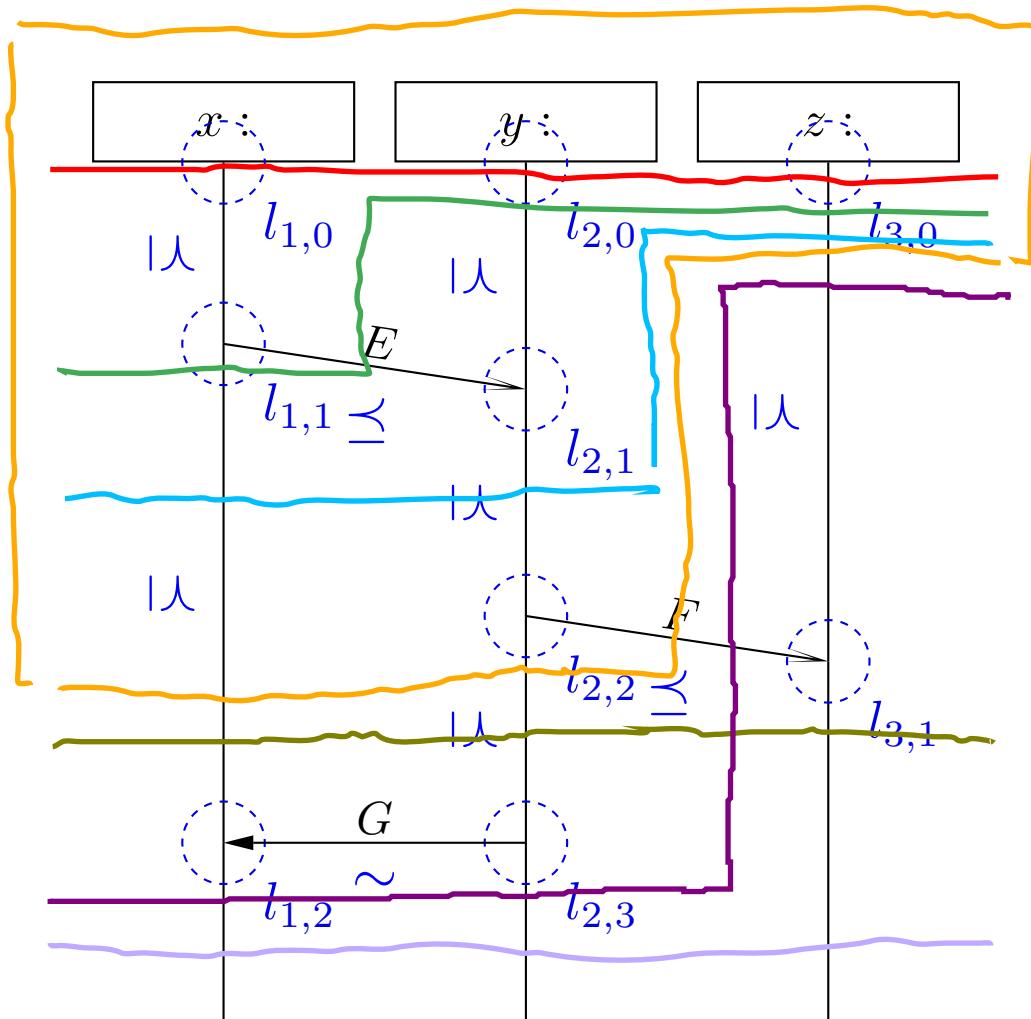
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# Restricted Abstract Syntax



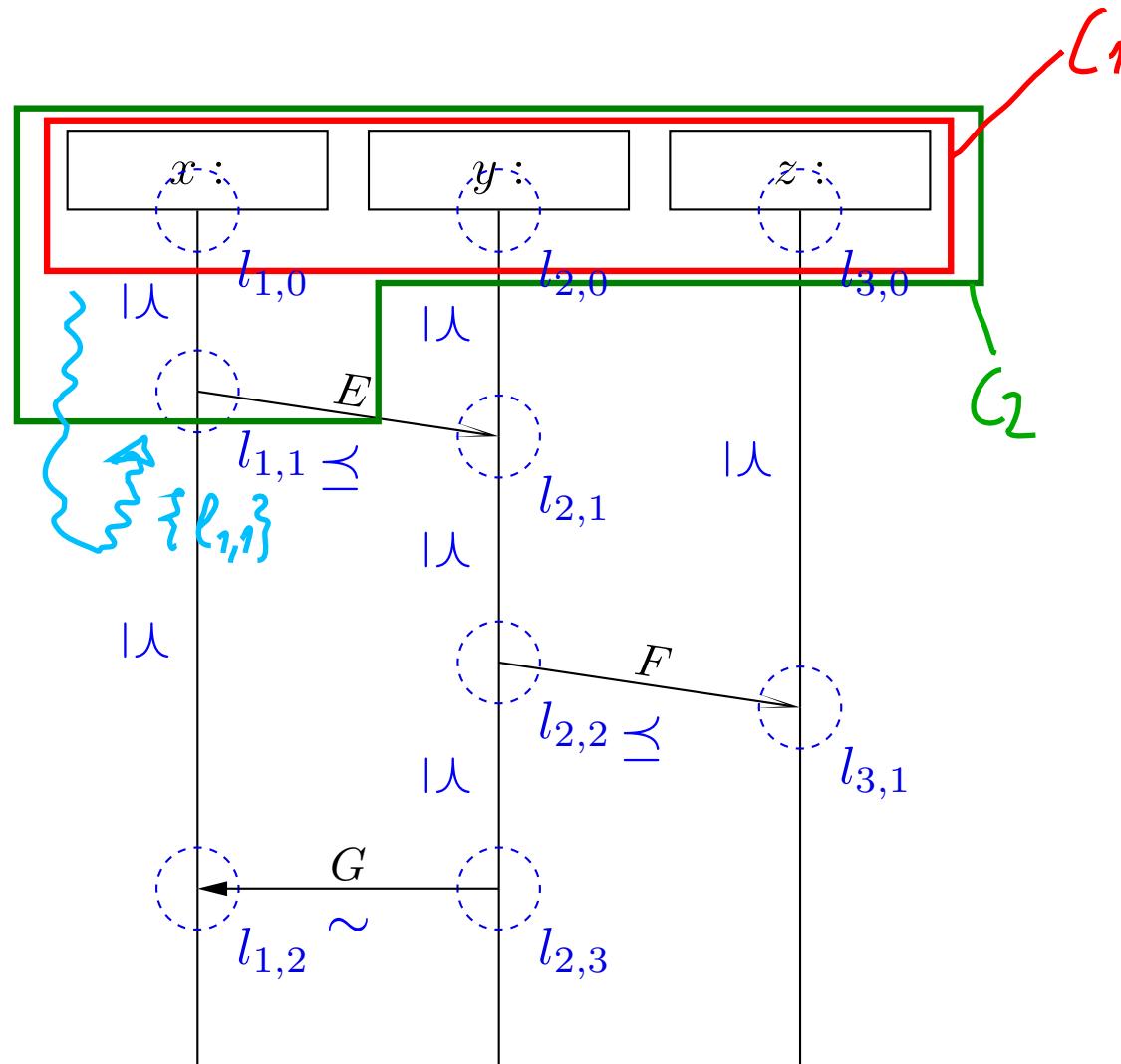
# Cuts



- A set  $C \subseteq \mathcal{L}$  is called cut iff
- downward closed w.r.t.  $\leq$
  - closed w.r.t.  $\sim$
  - at least one loc. per instance line (if more than one, then unordered)

# Firedsets

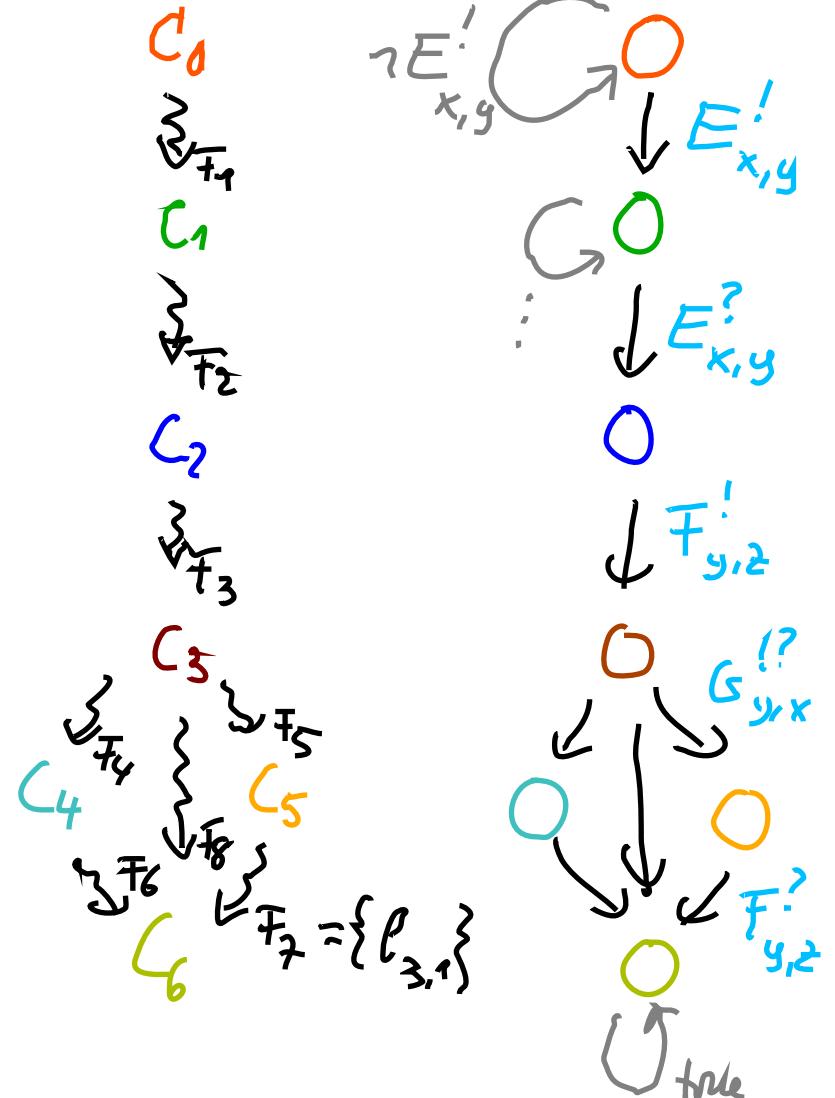
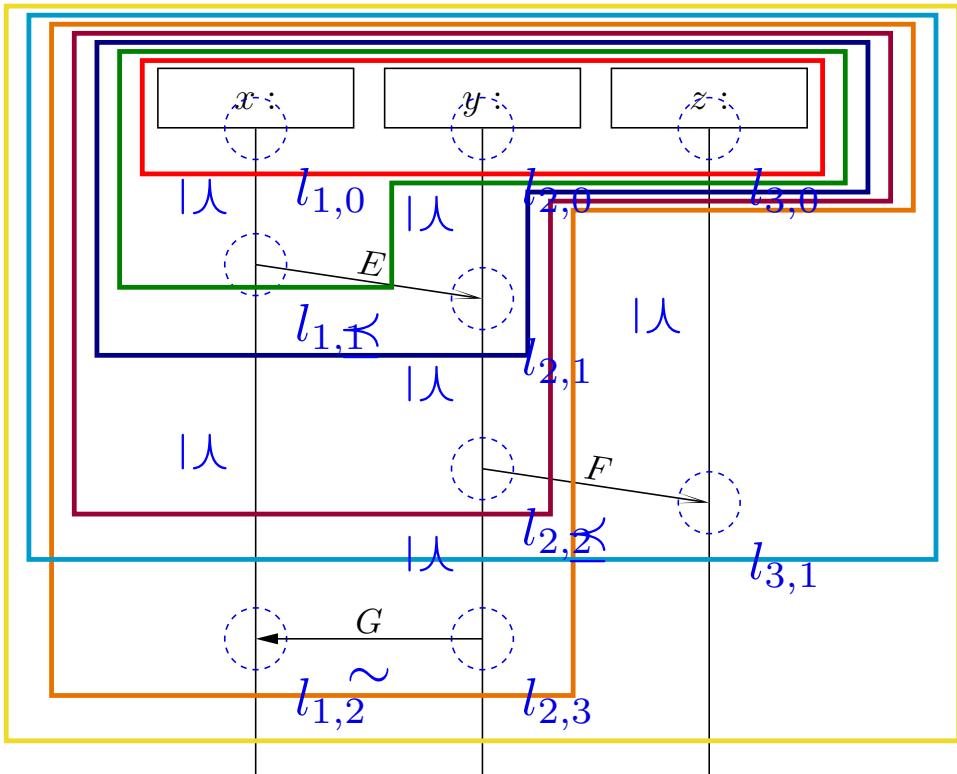
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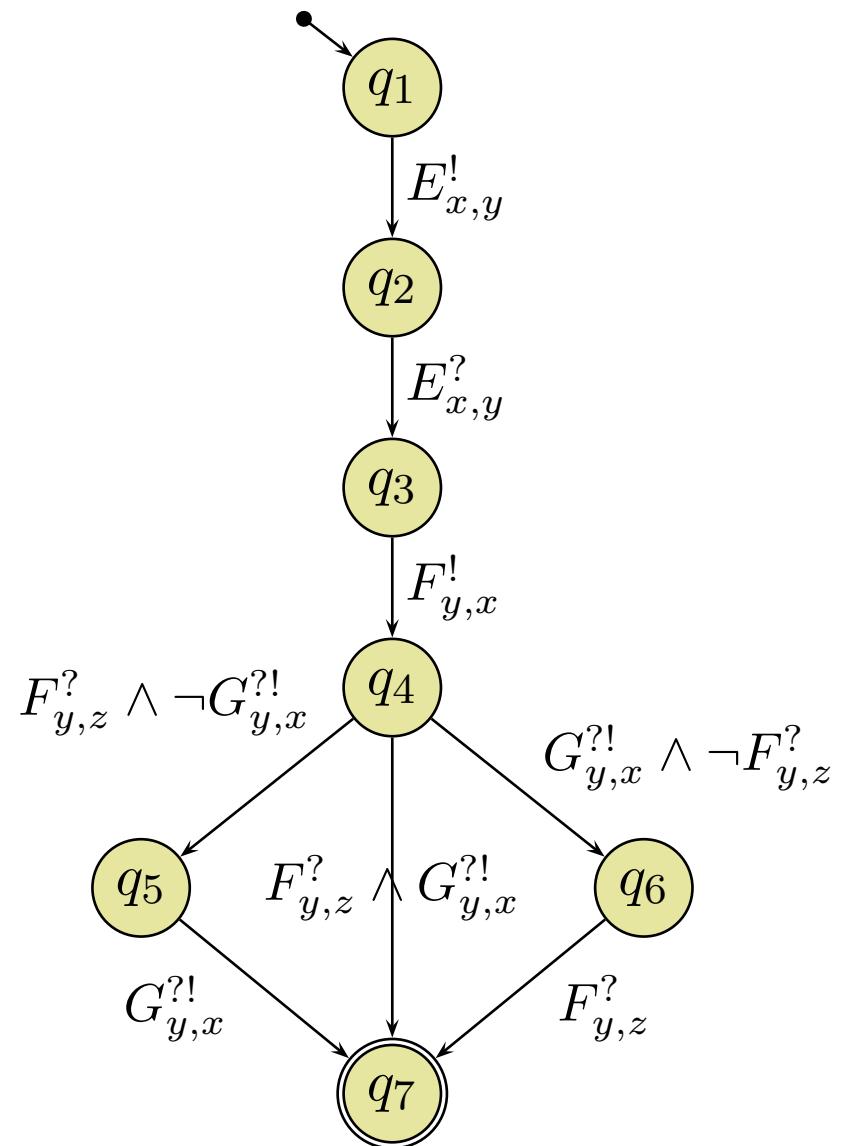
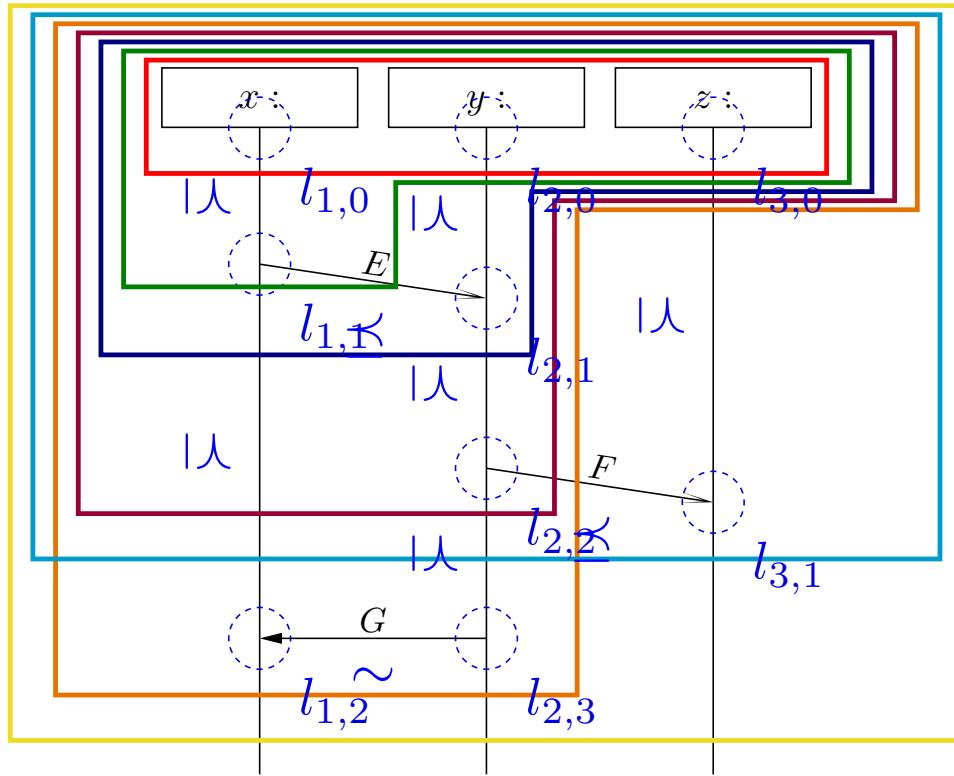
$C \sqsupseteq_F C'$  iff

- $F \neq \emptyset$
  - $C' \setminus C = F$
  - for all event receptions in  $F$ , the standings are in  $C$
  - direct successor:
- $$\forall l \in F \exists l' \in C \cdot l' \leq l$$
- $$\wedge \forall l'' \in C \cdot l'' \leq l \Rightarrow l'' \leq l'$$

# Towards Automata

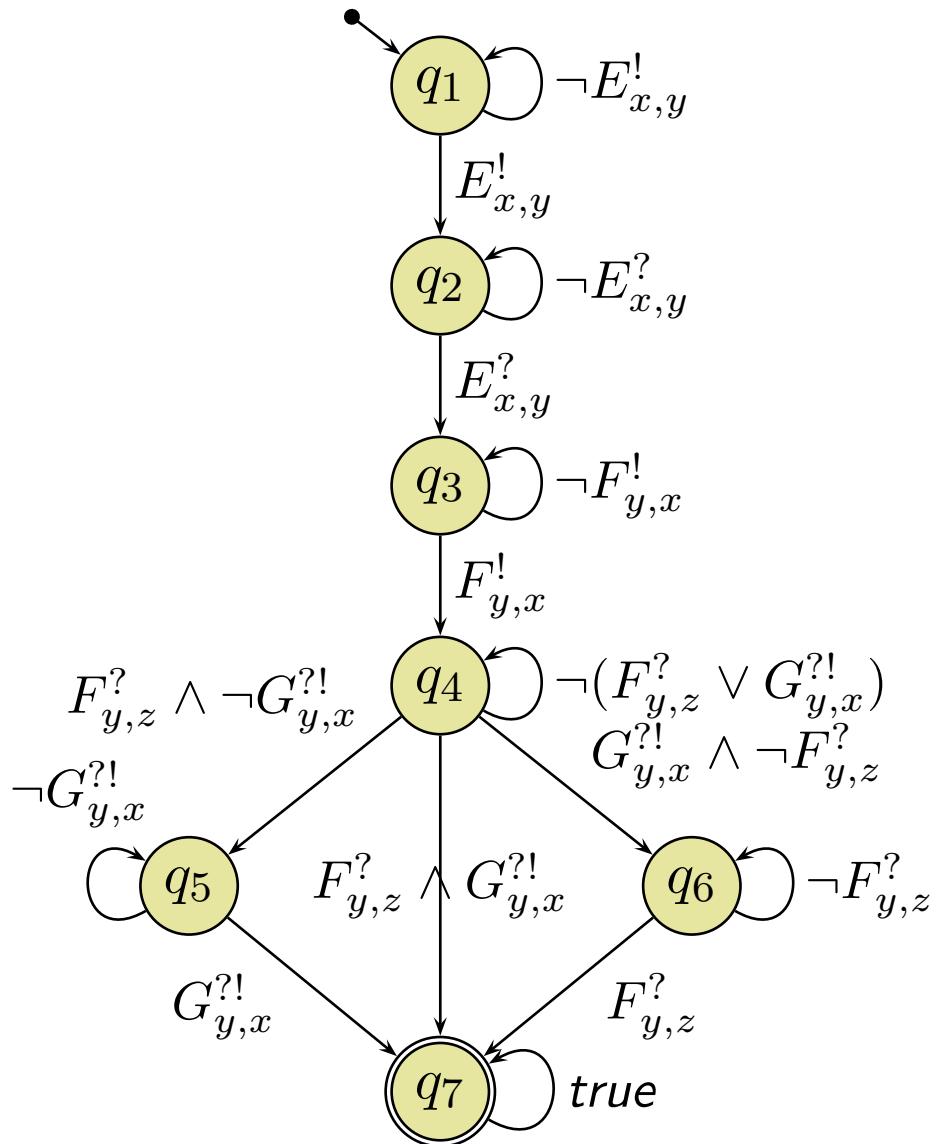
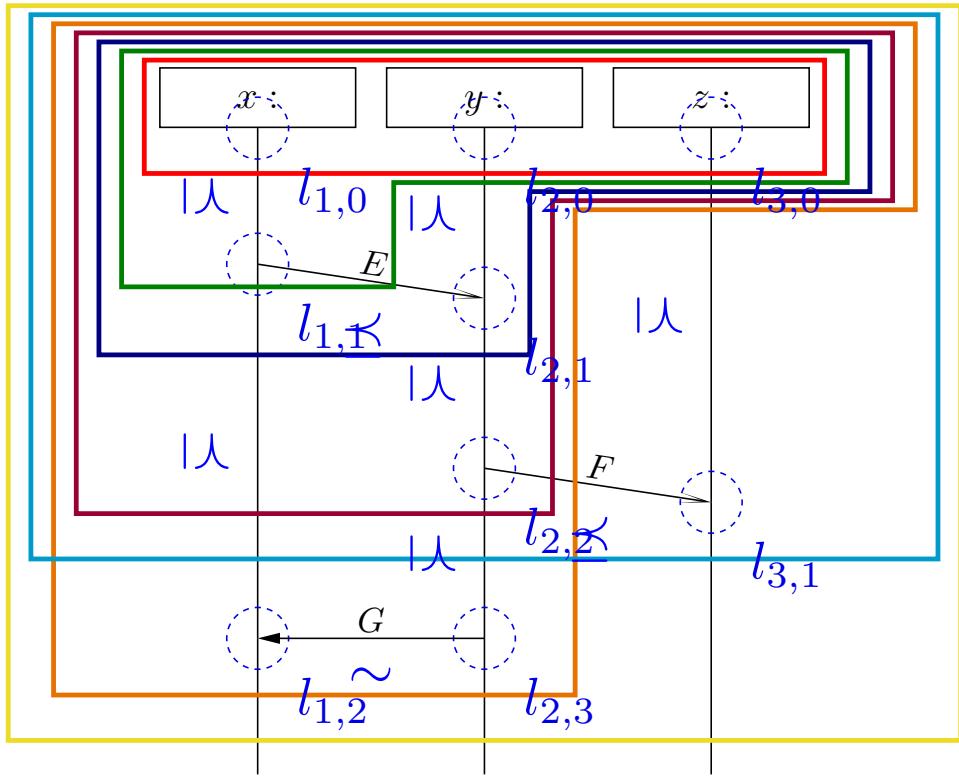


# Alphabet — Progress Transitions

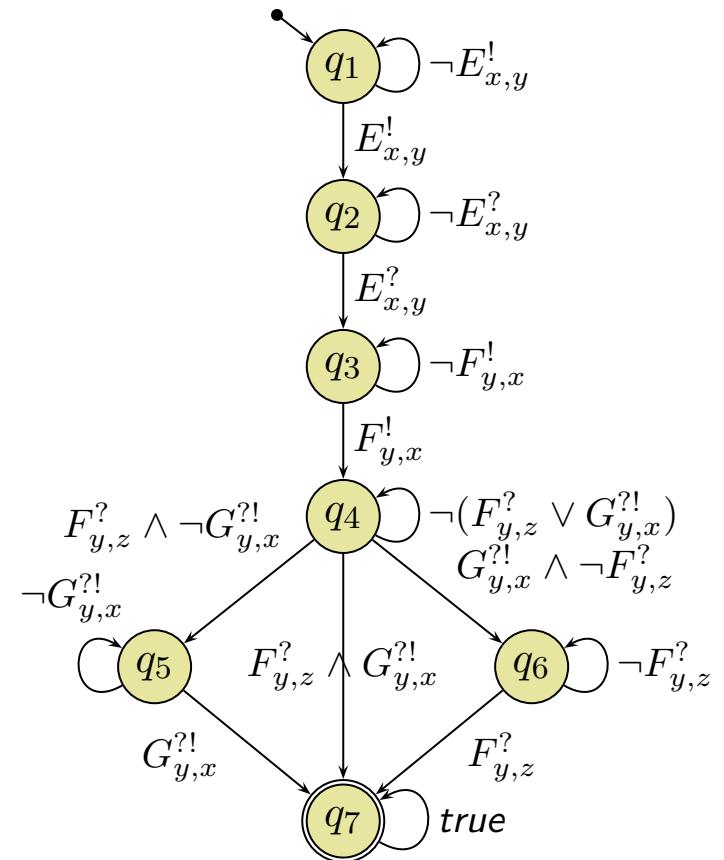
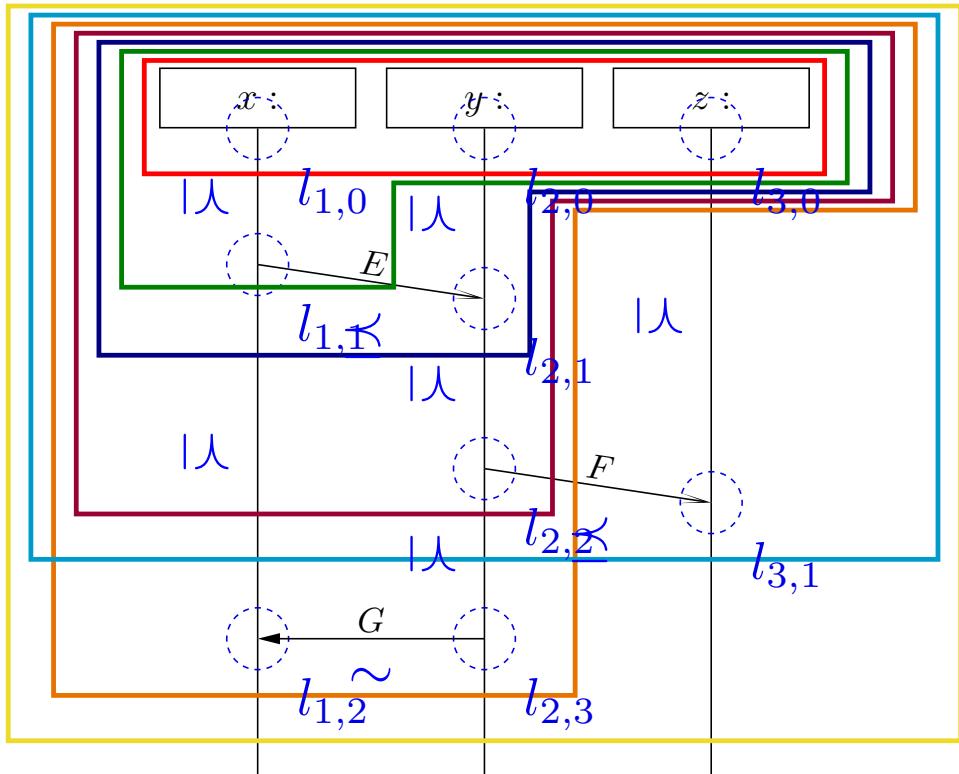


# Loops

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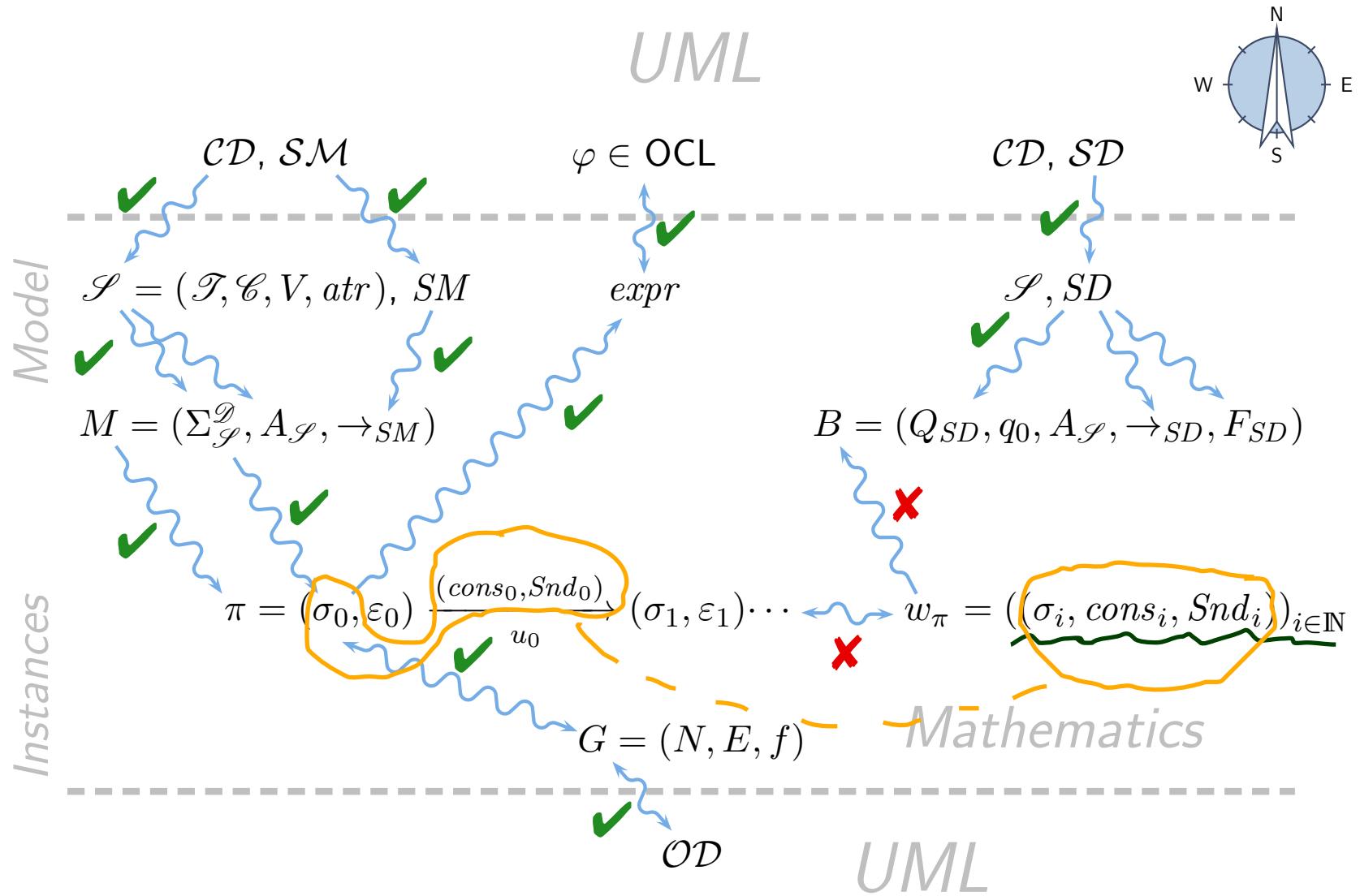


# Language



*You are here.*

# Course Map



## *Language of a Model*

# Words over Signature

**Definition.** Let  $\mathcal{S} = (\mathcal{T}, \mathcal{C}, V, atr, \mathcal{E})$  be a signature and  $\mathcal{D}$  a structure of  $\mathcal{S}$ . A **word** over  $\mathcal{S}$  and  $\mathcal{D}$  is an infinite sequence

$$(\sigma_i, cons_i, Snd_i)_{i \in \mathbb{N}_0} \\ \in \left( \Sigma_{\mathcal{S}}^{\mathcal{D}} \times 2^{\mathcal{D}(\mathcal{C}) \times Evs(\mathcal{E}, \mathcal{D}) \times \mathcal{D}(\mathcal{C})} \times 2^{\mathcal{D}(\mathcal{C}) \times Evs(\mathcal{E}, \mathcal{D}) \times \mathcal{D}(\mathcal{C})} \right)^{\omega}.$$

# The Language of a Model

**Recall:** A UML model  $\mathcal{M} = (\mathcal{CD}, \mathcal{SM}, \mathcal{OD})$  and a structure  $\mathcal{D}$  denotes a set  $[\![\mathcal{M}]\!]$  of (initial and consecutive) **computations** of the form

$$(\sigma_0, \varepsilon_0) \xrightarrow{a_0} (\sigma_1, \varepsilon_1) \xrightarrow{a_1} (\sigma_2, \varepsilon_2) \xrightarrow{a_2} \dots \text{ where}$$

$$a_i = (cons_i, Snd_i, u_i) \in \underbrace{2^{\mathcal{D}(\mathcal{C}) \times Evs(\mathcal{E}, \mathcal{D}) \times \mathcal{D}(\mathcal{C})}}_{=: \tilde{A}} \times 2^{\mathcal{D}(\mathcal{C}) \times Evs(\mathcal{E}, \mathcal{D}) \times \mathcal{D}(\mathcal{C})} \times \mathcal{D}(\mathcal{C}).$$

For the connection between models and interactions, we **disregard** the configuration of **the ether** and **who** made the step, and define as follows:

**Definition.** Let  $\mathcal{M} = (\mathcal{CD}, \mathcal{SM}, \mathcal{OD})$  be a UML model and  $\mathcal{D}$  a structure. Then

$$\begin{aligned} \mathcal{L}(\mathcal{M}) := \{ & (\sigma_i, cons_i, Snd_i)_{i \in \mathbb{N}_0} \in (\Sigma_{\mathcal{S}}^{\mathcal{D}} \times \tilde{A})^\omega \mid \\ & \exists (\varepsilon_i, u_i)_{i \in \mathbb{N}_0} : (\sigma_0, \varepsilon_0) \xrightarrow[u_0]{(cons_0, Snd_0)} (\sigma_1, \varepsilon_1) \dots \in [\![\mathcal{M}]\!] \} \end{aligned}$$

is the **language** of  $\mathcal{M}$ .

# *Example: The Language of a Model*

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$$\begin{aligned}\mathcal{L}(\mathcal{M}) := \{ & (\sigma_i, cons_i, Snd_i)_{i \in \mathbb{N}_0} \in (\Sigma_{\mathcal{S}}^{\mathcal{D}} \times \tilde{A})^\omega \mid \\ & \exists (\varepsilon_i, u_i)_{i \in \mathbb{N}_0} : (\sigma_0, \varepsilon_0) \xrightarrow[u_0]{(cons_0, Snd_0)} (\sigma_1, \varepsilon_1) \dots \in \llbracket \mathcal{M} \rrbracket\}\end{aligned}$$

# Signal and Attribute Expressions

---

- Let  $\mathcal{S} = (\mathcal{I}, \mathcal{C}, V, \text{attr}, \mathcal{E})$  be a signature and  $X$  a set of logical variables,
- The signal and attribute expressions  $\text{Expr}_{\mathcal{S}}(\mathcal{E}, X)$  are defined by the grammar:

$$\psi ::= \text{true} \mid \text{expr} \mid E_{x,y}^! \mid E_{x,y}^? \mid \neg\psi \mid \psi_1 \vee \psi_2 \mid E_{x,y}^{!?}$$

where  $\text{expr} : \text{Bool} \in \text{Expr}_{\mathcal{S}}$ ,  $E \in \mathcal{E}$ ,  $x, y \in X$ .

↗ set of variables

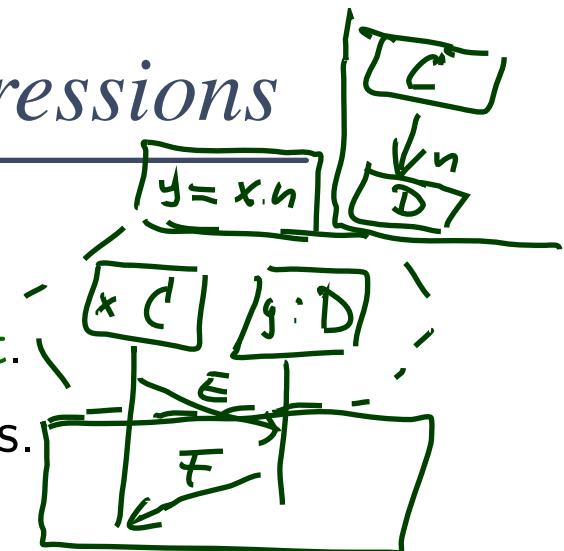
# Satisfaction of Signal and Attribute Expressions

- Let  $(\sigma, cons, Snd) \in \Sigma_{\mathcal{S}}^{\mathcal{D}} \times \tilde{A}$  be a triple consisting of **system state**, **consume set**, and **send set**.
- Let  $\beta : X \rightarrow \mathcal{D}(\mathcal{C})$  be a valuation of the logical variables.

Then

- $(\sigma, cons, Snd) \models_{\beta} \text{true}$
- $(\sigma, cons, Snd) \models_{\beta} \neg\psi$  if and only if not  $(\sigma, cons, Snd) \models_{\beta} \psi$
- $(\sigma, cons, Snd) \models_{\beta} \psi_1 \vee \psi_2$  if and only if  

$$(\sigma, cons, Snd) \models_{\beta} \psi_1 \text{ or } (\sigma, cons, Snd) \models_{\beta} \psi_2$$
- $(\sigma, cons, Snd) \models_{\beta} \text{expr}$  if and only if  $I[\text{expr}](\sigma, \beta) = 1$
- $(\sigma, cons, Snd) \models_{\beta} E_{x,y}^!$  if and only if  $\exists \vec{d} \bullet (\beta(x), (E, \vec{d}), \beta(y)) \in Snd$
- $(\sigma, cons, Snd) \models_{\beta} E_{x,y}^?$  if and only if  $\exists \vec{d} \bullet (\beta(x), (E, \vec{d}), \beta(y)) \in cons$



**Observation:** semantics of models **keeps track** of sender and receiver at sending and consumption time. We disregard the event identity.

**Alternative:** keep track of event identities.

# TBA over Signature

**Definition.** A TBA

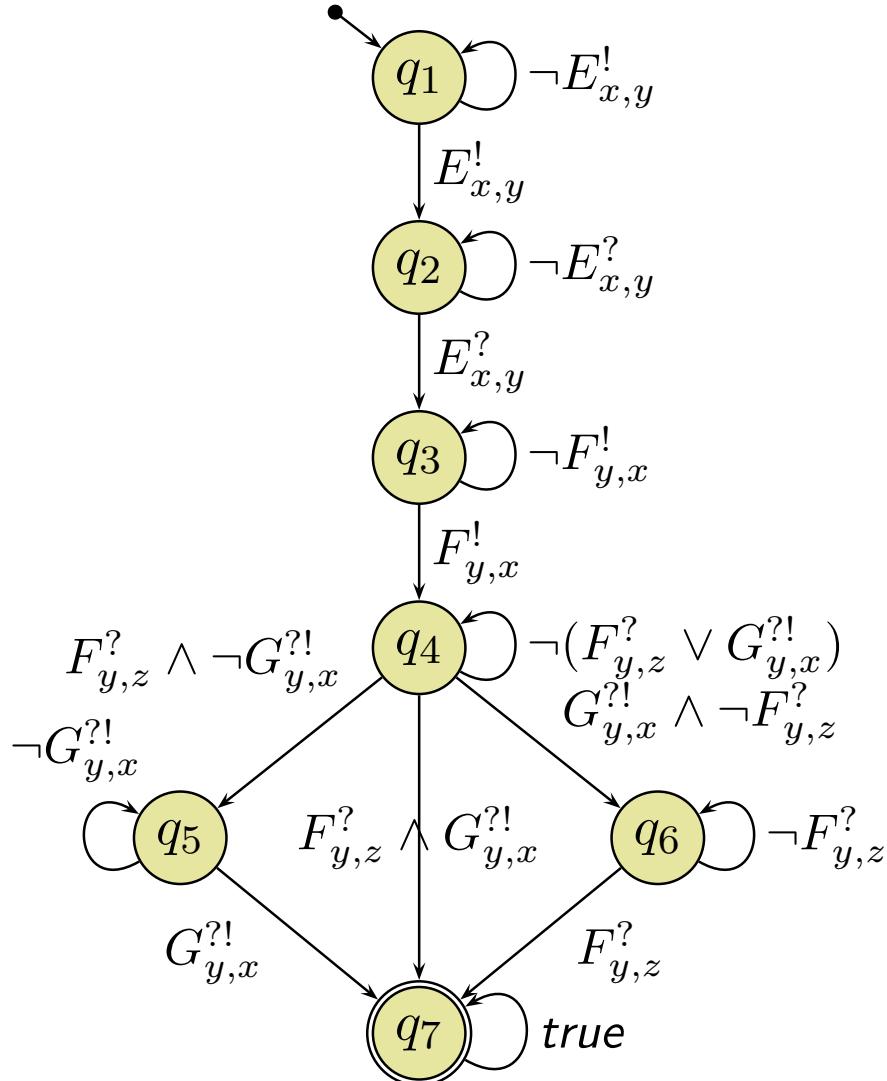
$$\mathcal{B} = (\text{Expr}_{\mathcal{B}}(X), X, Q, q_{ini}, \rightarrow, Q_F)$$

where  $\text{Expr}_{\mathcal{B}}(X)$  is the set of **signal and attribute expressions**  
 $\text{Expr}_{\mathcal{S}}(\mathcal{E}, X)$  over signature  $\mathcal{S}$  is called **TBA over  $\mathcal{S}$** .

- Any word over  $\mathcal{S}$  and  $\mathcal{D}$  is then a word for  $\mathcal{B}$ .  
(By the satisfaction relation defined on the previous slide;  $\mathcal{D}(X) = \mathcal{D}(\mathcal{C})$ .)
- Thus a TBA over  $\mathcal{S}$  accepts words of models with signature  $\mathcal{S}$ .  
(By the previous definition of TBA.)

# TBA over Signature Example

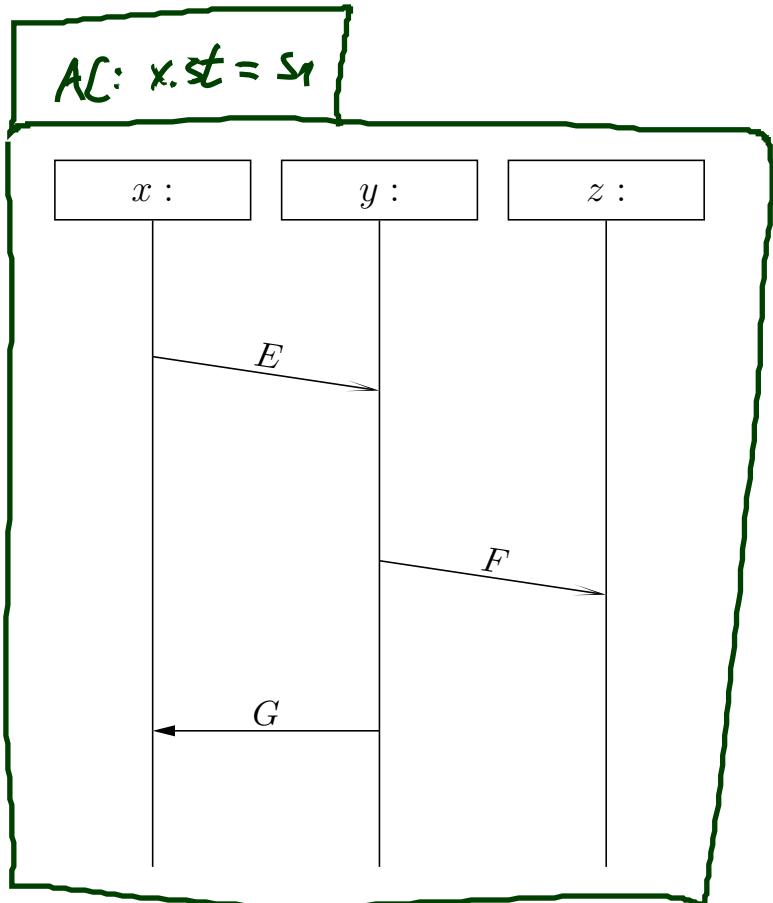
$(\sigma, \text{cons}, \text{Snd}) \models_{\beta} \text{expr}$  iff  $I[\![\text{expr}]\!](\sigma, \beta) = 1$ ;  
 $(\sigma, \text{cons}, \text{Snd}) \models_{\beta} E_{x,y}^!$  iff  $(\beta(x), (E, \vec{d}), \beta(y)) \in \text{Snd}$



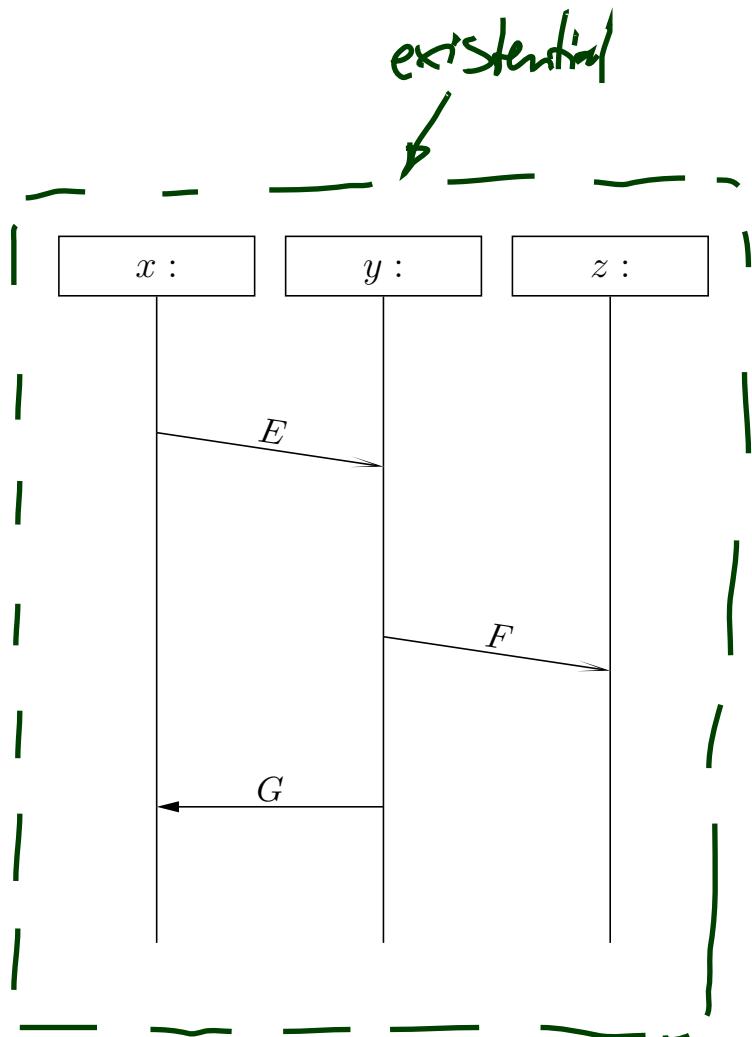
## *Activation, Chart Mode*

# Activation Condition

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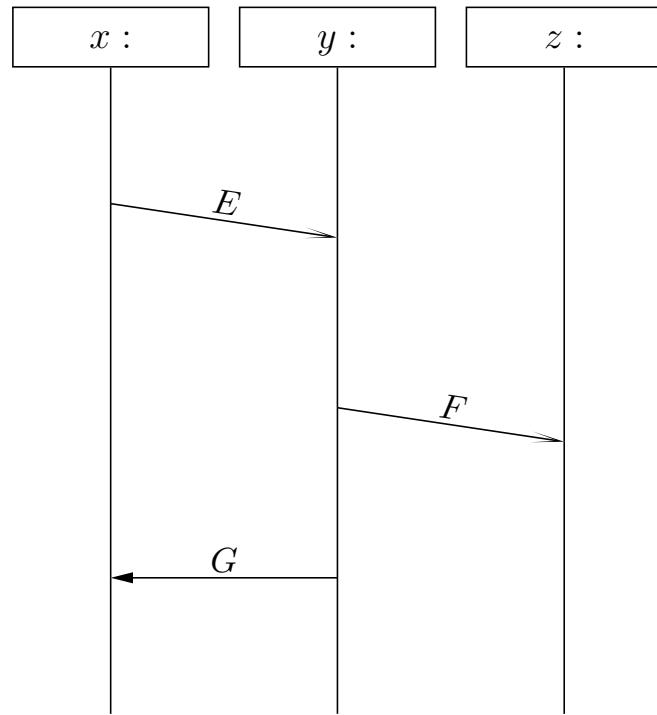


# *Universal vs. Existential Charts*



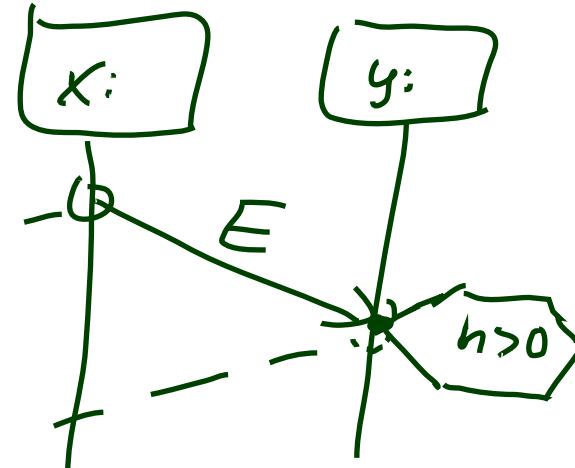
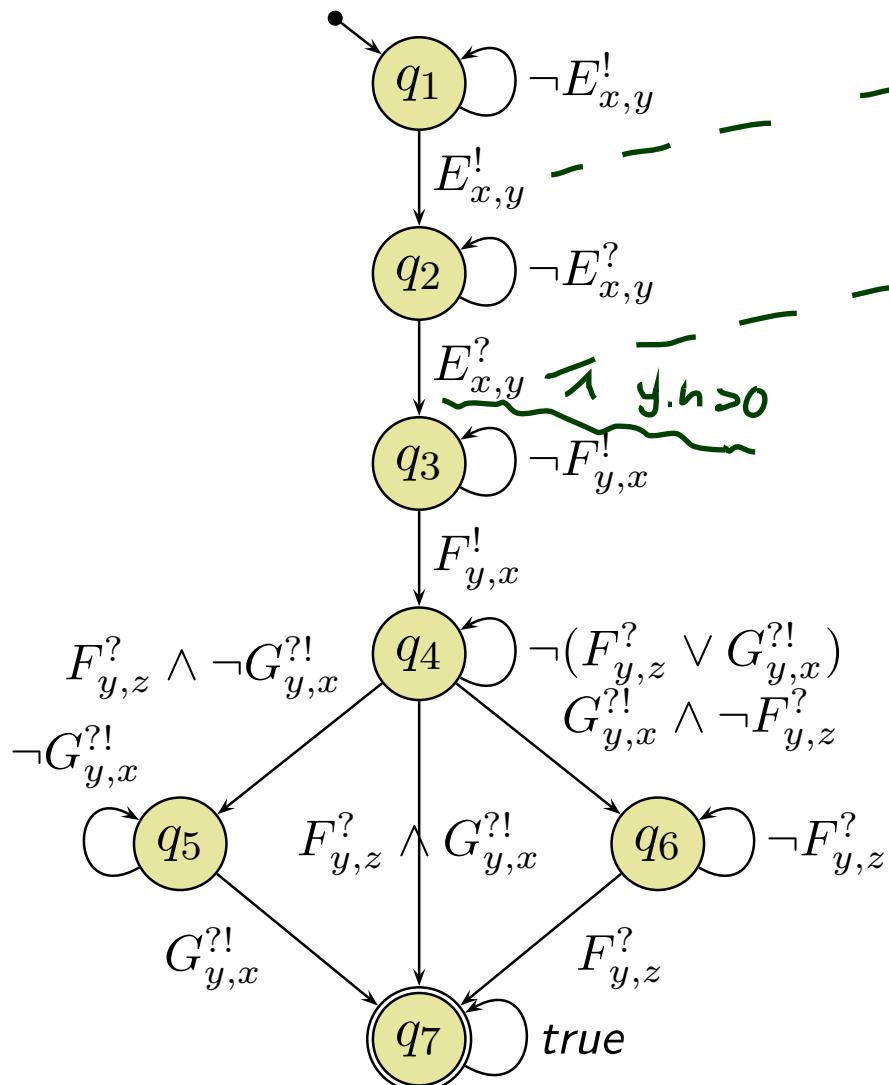
# *Prechart*

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## *Conditions*

# Conditions



UNIVERSAL:

$\mathcal{M} \models \text{LSC} \quad \text{iff}$

$\forall \pi = (\sigma_i, \text{obs}_i, \text{Snd}_i) \quad \pi \models \text{LSC}$

$\sigma_i, \pi_\beta$  *act and*

$\Rightarrow (\sigma_{i+1}, \text{obs}_{i+1}, \text{Snd}_{i+1}),$   
 $(\sigma_{i+2}, \text{obs}_{i+2}, \text{Snd}_{i+2}), \dots$

is accepted by  
 $\text{dmt(LSC)}$

## *Back to UML: Interactions*

# *Model Consistency wrt. Interaction*

- We assume that the set of interactions  $\mathcal{I}$  is partitioned into two (possibly empty) sets of **universal** and **existential** interactions, i.e.

$$\mathcal{I} = \mathcal{I}_{\forall} \dot{\cup} \mathcal{I}_{\exists}.$$

**Definition.** A model

$$\mathcal{M} = (\mathcal{CD}, \mathcal{SM}, \mathcal{OD}, \mathcal{I})$$

is called **consistent** (more precise: the constructive description of behaviour is consistent with the reflective one) if and only if

$$\forall \mathcal{I} \in \mathcal{I}_{\forall} : \mathcal{L}(\mathcal{M}) \subseteq \mathcal{L}(\mathcal{I})$$

and

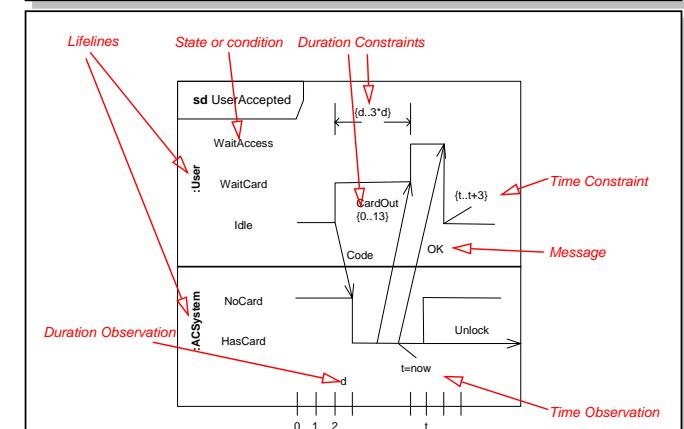
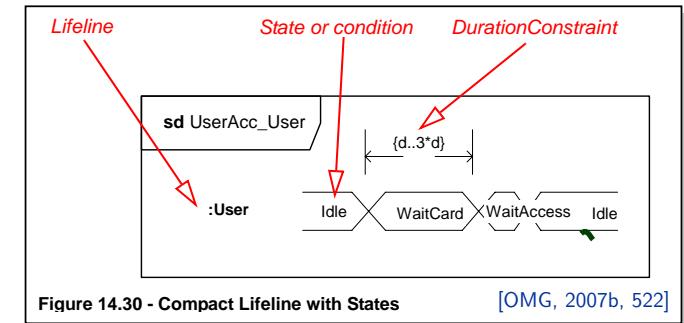
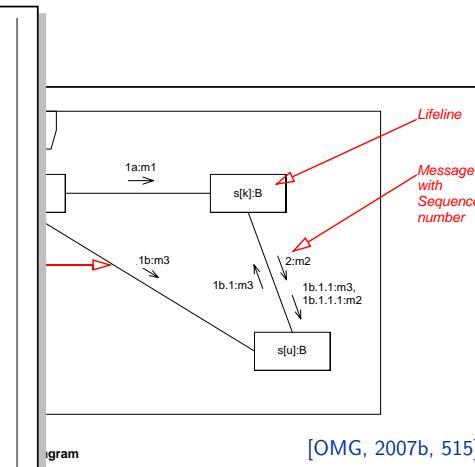
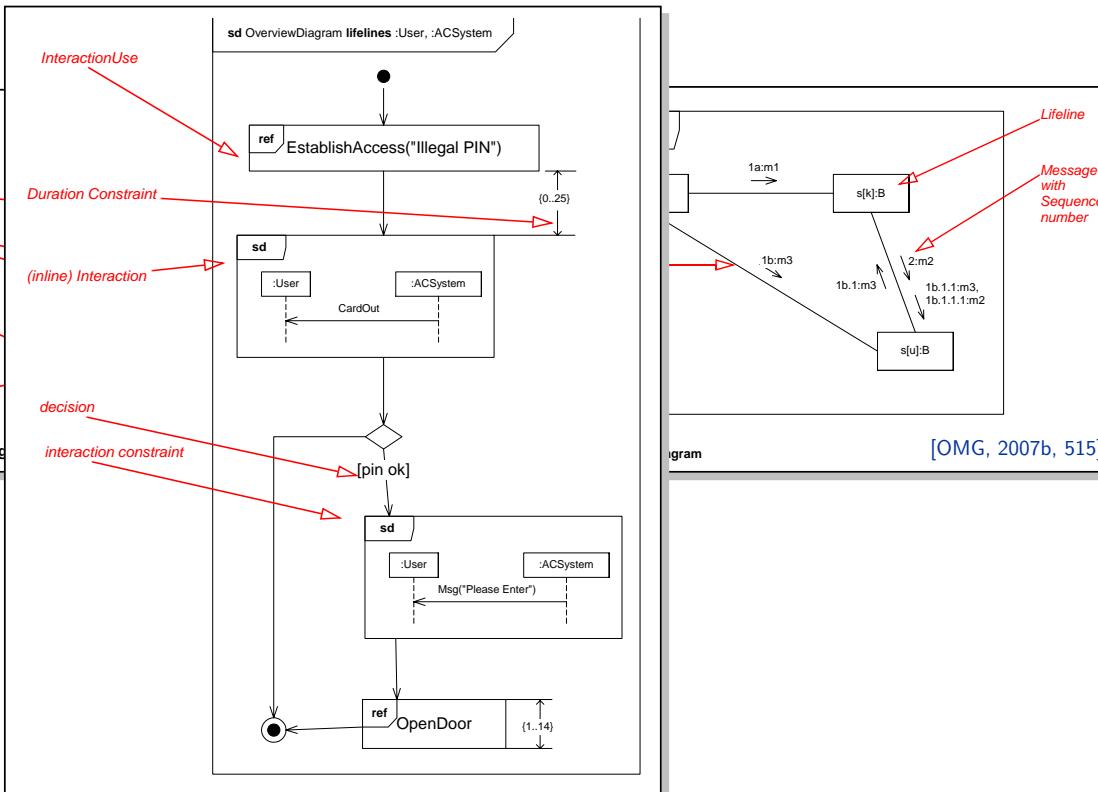
$$\forall \mathcal{I} \in \mathcal{I}_{\exists} : \mathcal{L}(\mathcal{M}) \cap \mathcal{L}(\mathcal{I}) \neq \emptyset.$$

# Interactions as Reflective Description

- In UML, reflective (temporal) descriptions are subsumed by **interactions**.
- A UML model  $\mathcal{M} = (\mathcal{CD}, \mathcal{SM}, \mathcal{OD}, \mathcal{I})$  has a set of interactions  $\mathcal{I}$ .
- An interaction  $\mathcal{I} \in \mathcal{I}$  can be (OMG claim: equivalently) **diagrammed** as
  - **sequence diagram**,      **timing diagram**, or
  - **communication diagram** (formerly known as collaboration diagram).

- 20 - 2015-02-03 – Sinteract

**Figure 14.26 - Sequence Diagram**



# Interactions as Reflective Description

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- 20 - 2015-02-03 – **Interaction**  
 Figure 14.26 - Sequence Diagram  
 Figure 14.28 - Interaction Overview Diagram representing a High Level Interaction diagram [OMG, 2007b, 518]

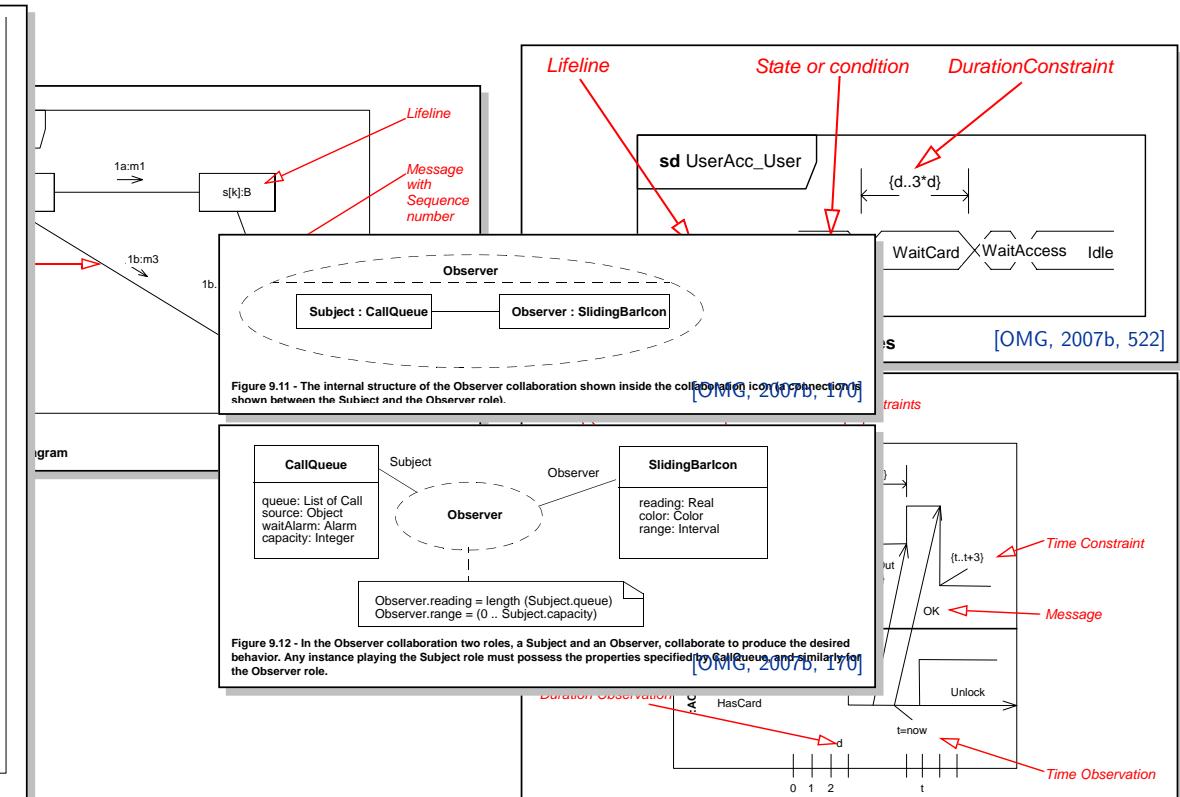
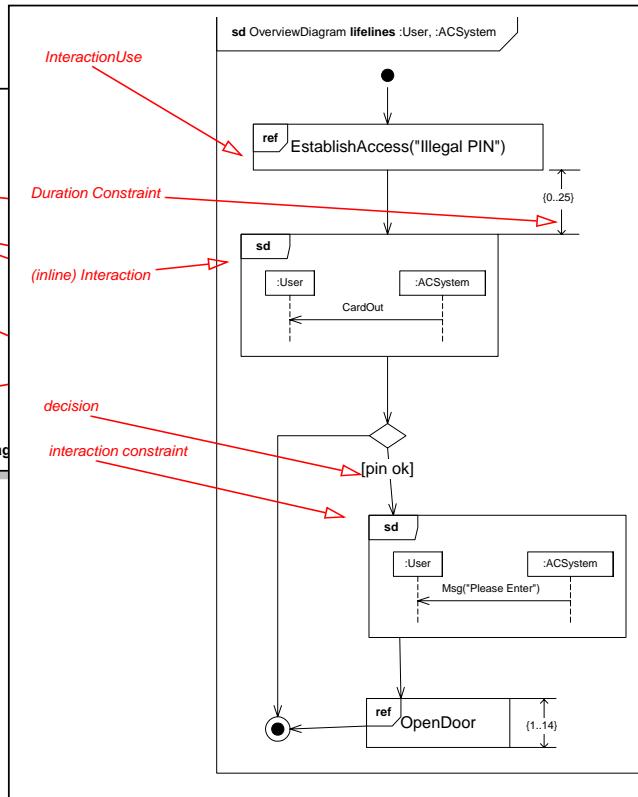


Figure 14.31 - Timing Diagram with more than one Lifeline and with Messages [OMG, 2007b, 522]

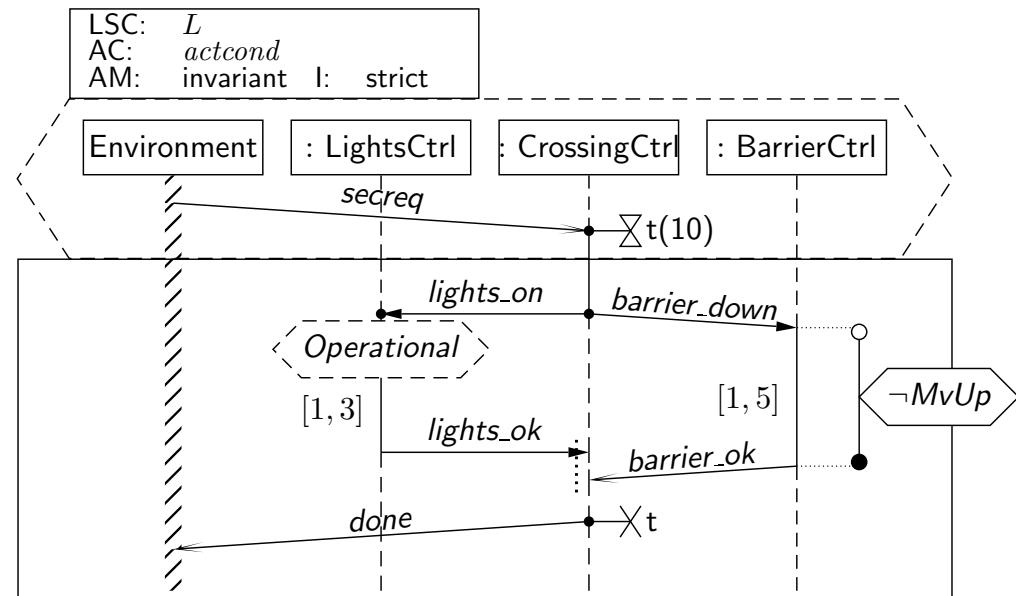
# Why Sequence Diagrams?

**Most Prominent:** Sequence Diagrams — with **long history**:

- **Message Sequence Charts**, standardized by the ITU in different versions, often accused to lack a formal semantics.
- **Sequence Diagrams** of UML 1.x

Most severe **drawbacks** of these formalisms:

- unclear **interpretation**:  
example scenario or invariant?
- unclear **activation**:  
what triggers the requirement?
- unclear **progress** requirement:  
must all messages be observed?
- **conditions** merely comments
- no means to express  
**forbidden scenarios**



# *Thus: Live Sequence Charts*

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- **SDs of UML 2.x** address **some** issues, yet the standard exhibits unclarities and even contradictions [Harel and Maoz, 2007, Störrle, 2003]
- For the lecture, we consider **Live Sequence Charts** (LSCs) [Damm and Harel, 2001, Klose, 2003, Harel and Marelly, 2003], who have a common fragment with UML 2.x SDs [Harel and Maoz, 2007]
- **Modelling guideline:** stick to that fragment.

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