Software Design, Modelling and Analysis in UML

Lecture 9: Class Diagrams IV

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Recall: Associations and OCL Syntax

Recall: OCL syntax as introduced in Lecture 3, interesting part:

```
 |r_1(expr_1) : \tau_C \to \tau_D 
 |r_2(expr_1) : \tau_C \to Set(\tau_D) 
\begin{aligned} r_1:D_{0,1}\in atr(C)\\ r_2:D_*\in atr(C) \end{aligned}
```

```
\langle r: \dots, \langle role: D, \mu, \dots, \dots \rangle \in V or \langle r: \dots, \langle role: C, \dots, \dots \rangle \in V, \langle role: D, \mu, \dots, \dots \rangle \in V, \langle role: \neq role'.
                                                                                                                                                                                                                                                                                                                       \begin{array}{ll} expr ::= \dots & | \ role(expr_1) &: \tau_C \to \tau_D & \mu = 0..1 \ \text{or} \ \mu = 1..1 \\ | \ role(expr_1) &: \tau_C \to Set(\tau_D) & \text{otherwise} \end{array}
```

Association name as such does not occur in OCL syntax, role names do. expr_1 has to denote an object of a class which "participates" in the association.

OCL and Associations: Semantics

$\bullet \ I[r_1(\alpha pr_1)][\sigma,\beta) \coloneqq \begin{cases} u & \text{. if } u_1 \in \text{dom}(\sigma) \text{ and } \sigma(u_1)(r_1) = \{u\} \\ \bot & \text{. otherwise} \end{cases}$ Assume $\exp r_1: \tau_C$ for some $C\in \mathscr{C}$. Set $u_1:=I[\exp r_1](\sigma,\beta)\in \mathscr{D}(T_C)$. $I[r_2(\exp r_1)](\sigma,\beta) \coloneqq \begin{cases} \sigma(u_1)(r_2) & \text{. if } u_1 \in \text{dom}(\sigma) \\ \bot & \text{. otherwise} \end{cases}$

Now needed:

```
I[\![mle(expr_1)]\!]((\sigma,\lambda),\beta)
```

```
But it yields a set of n-tuples, of which some relate u and some instances of D.

• role denotes the position of the D's in the tuples constituting the value of r.
                                                                                                                                                                                                                                                                              • What we have is \lambda(r) (with association name r, not with role name role1).
                                                                                                                                                                                                                                                                                                                                                            • We cannot simply write \sigma(u)(role).
Recall: role is (for the moment) not an attribute of object u (not in atr(C)).
                                                                                                                                                                          \langle r:\dots,\langle role:D,\mu,\_,\_,\_\rangle,\dots,\langle role':C,\_,\_,\_,\_\rangle,\dots\rangle
```

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Contents & Goals

Last Lecture:

- Associations syntax and semantics.
 Associations in OCL syntax.

- This Lecture:

Educational Objectives: Capabilities for following tasks/questions.

- Compute the value of a given OCL constraint in a system state with links.
 How did we treat "multiplicity" semantically? What does "navigability", "ownership", ... mean?

- Associations and OCL: semantics.Associations: the rest.

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Associations and OCL Cont'd

OCL and Associations: Semantics Cont'd $\textbf{Assume } expr_1: \tau_C \text{ for some } C \in \mathscr{C}. \text{ Set } u_1 := I[\![expr_1]\!]((\sigma,\lambda),\beta) \in \mathscr{D}(T_C).$

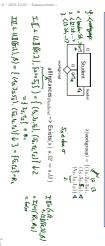
 $\bullet \ I [\operatorname{Pole}(expr_1)] [(\sigma, \lambda), \beta) := \begin{cases} u & \text{. if } u_1 \in \operatorname{dom}(\sigma) \text{ and } L(\underline{\operatorname{vole})}(\underline{u_1, \lambda}) = \{u\} \\ & \text{. otherwise} \end{cases}$

 $\bullet \ I[[role(expr_1)]]((\sigma,\lambda),\beta) := \begin{cases} L(role)(u_1,\lambda) & \text{, if } u_1 \in \text{dom}(\sigma) \\ \bot & \text{, otherwise} \end{cases}$

$$\begin{split} &L(\underline{role})(u,\lambda) = \{(u_1,\dots,u_n) \in \lambda(r) \mid u \in \{u_1,\dots,u_n\} \} \downarrow i \\ &\text{if} & \langle r : \langle role_1 : \dots , \dots \rangle, \dots \langle role_n : \dots , \dots \rangle \rangle, \quad \underline{role} = \underline{role_i}. \\ &\text{Given a set of n-tuples A}. \\ &A \downarrow i \text{ denotes the element-wise projection onto the i-th component.} \end{split}$$

OCL and Associations Semantics: Example





Associations: The Rest

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Navigability

Navigability is treated similar to visibility: Using names of non-navigable association ends ($\nu=\times$) are forbidden.

Example: Given

the following OCL expression is not well-typed wrt. navigability,

 $\mathsf{context}\ D\ \mathsf{inv}: role.x > 0$

The standard says: navigation is...

'--': ...possible 'x': ...not possible

'>': ...efficient

So: In general, UML associations are different from pointers / references in general But: Pointers / references can faithfully be modelled by UML associations.

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 $x:Int \xrightarrow{C} role \xrightarrow{ik\mathfrak{D}} D$

Multiplicities as Constraints

$$\begin{split} & \textbf{Recall: Multiplicity is a term of the form } N_1..N_2, \ \dots, \ N_{2k-1}..N_{2k} \\ & \textbf{where } N_i \leq N_{i+1} \text{ for } 1 \leq i \leq 2k, \quad N_1, \dots, N_{2k-1} \in \mathbb{N}, \quad N_{2k} \in \mathbb{N} \cup \{s\}. \end{split}$$

for each $\langle r:\dots,\langle role:D,\mu,\dots,\neg,\neg\rangle,\dots,\langle role':C,\neg\neg\neg,\dots,\neg\rangle,\dots\rangle\in V$ or

with $role \neq role'$, if $\mu \neq 0..1$, $\mu \neq 1..1$, and $\mu_{\mathsf{OCL}}^C(role) := \mathsf{context}\ C\ \mathsf{inv} : \mathsf{not}(\mathsf{ocllsUndefined}(role))$

 $\text{context } C \text{ inv}: (N_1 \leq role \Rightarrow \text{size}() \leq N_2) \text{ or } \dots \text{ or } (N_{2k-1} \leq role \Rightarrow \text{size}() \underbrace{\leq N_{2k}}_{\text{ordel}}) \underbrace{\leq N_{2k}}_{\text{ordel}})$

 $\langle r: \dots, \langle role': C, \neg, \neg, \neg, \neg \rangle, \dots, \langle role: D, \mu, \neg, \neg, \neg, \neg, \rangle, \dots \rangle \in V$,

Note: in n-ary associations with n>2, there is redundancy.

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The Rest

Recapitulation: Consider the following association:

 $\langle r:\langle role_1:C_1,\mu_1,P_1,\xi_1,\nu_1,o_1\rangle,\ldots,\langle role_n:C_n,\mu_n,P_n,\xi_n,\nu_n,o_n\rangle\rangle$

- Association name r and role names / types $role_i$ / C_i induce extended system states (σ, λ) .
- Multiplicity μ is considered in OCL syntax.
- Visibility ξ / Navigability ν : well-typedness (in a minute).

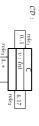
Now the rest:

- Multiplicity \(\mu\): we propose to view them as constraints.
- Properties P_i: even more typing.
- Ownership o: getting closer to pointers/references.
- Diamonds: exercise.

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Multiplicities as Constraints Example

$$\begin{split} \rho_{\mathrm{CL}}^{C}(nk) &= \mathrm{context}\ C \text{ in } r: \\ (N_1 \leq rale \Rightarrow \mathrm{size}() \leq N_2) \ \text{ or } \dots \text{ or } (N_{2k-1} \leq rale \Rightarrow \mathrm{size}() \leq N_{2k}) \end{split}$$



· Mac (role) = contact C inv: 4 = role, > size = 4 or 17 = role, > size = 17

· $\mu_{\alpha c}^{c}(\sigma l_{13}) = context Cinv: 3 \leq role_{3} + size$

We don't want to cover association properties in detail, only some observations (assume binary associations):

	ordered, sequence	bag •	unique •	Property
1774 get conto	an r-link is a sequence of object identi- ties (possibly including duplicates)	one object may have multiple r -links to have $\lambda(r)$ yield a single other object multi-sets	one object has at most one r -link to a single other object	Intuition
Tongial	have $\lambda(r)$ yield sequences	have $\lambda(r)$ yield multi-sets	current setting	Semantical Effect

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Properties

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have $\lambda(r)$ yield sequences	have $\lambda(r)$ yield multi-sets	current setting	Semantical Effect

ordered, sequence	bag	unique	Property
$T_D \rightarrow Seq(T_C)$	$T_D \rightarrow Bag(T_C)$	$T_D \rightarrow Set(T_C)$	OCL Typing of expression $role(expr)$

For subsets, redefines, union, etc. see (?, 127).

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Back to the main track:

Recall: on some earlier slides we said, the extension of the signature is only to study associations in "full beauty".

For the remainder of the course, we should look for something simpler...

Back to the Main Track

 from now on, we only use associations of the form (ii) C *

• Form (i) introduces $role: C_{0,1}$, and form (ii) introduces $role: C_*$ in V.

(And we may omit the non-navigability and ownership symbols.)

• In both cases, $role \in atr(C)$.

• We drop λ and go back to our nice σ with $\sigma(u)(\varpi le) \subseteq \mathscr{D}(D)$.

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Ownership

Intuitively it says:

Association r is not a "thing on its own" (i.e. provided by λ), but association end 'role' is owned by C (1). (That is, it's stored inside C object and provided by σ).

So: if multiplicity of role is 0..1 or 1..1, then the picture above is very close to concepts of pointers/pictences.

Actually, conversible is eddom seen in JML diagrams. Again: if target platform is clear, one may well live without (cf. (OMS, 2011b, 42) for more details).

Not clear to me:

OCL Constraints in (Class) Diagrams

Where Shall We Put OCL Constraints?

Two options:

(i) Notes.(ii) Particular dedicated places.

A UML note is a picture of the form



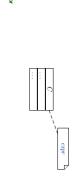
text can principally be everything, in particular comments and constraints.

Sometimes, content is explicitly classified for clarity:



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OCL in Notes: Conventions



stands for



context C inv: expr

Semantics of a Class Diagram

Invariants of a Class Diagram

As usual: consider all invariants in all notes in any class diagram — plus implicit multiplicity-induced invariants.

as the set $\{\varphi_1,\dots,\varphi_n\}$ of OCL constraints occurring in notes in \mathcal{CD} — after unfolding all graphical abbreviations (cf. previous slides).

Definition. Let $\mathscr{C}\mathscr{D}$ be a set of class diagrams. We say, the semantics of $\mathscr{C}\mathscr{D}$ is the signature it induces and the set of OCL constraints occurring in $\mathscr{C}\mathscr{D}$, denoted

 $[\![\mathscr{C}\mathscr{D}]\!] := \langle \mathscr{S}(\mathscr{C}\mathscr{D}), \mathit{Inv}(\mathscr{C}\mathscr{D}) \rangle.$

Given a structure $\mathscr D$ of $\mathscr F$ (and thus of $\mathscr F$ $\mathscr D$), the class diagrams describe the system states $\Sigma_\mathscr F^s$, of which some may satisfy $Inv(\mathscr C\mathscr D)$.



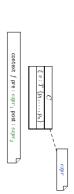
ullet Analogously: $\mathit{Inv}(\,\cdot\,)$ for any kind of diagram (like state machine diagrams).

Where Shall We Put OCL Constraints?

(ii) Particular dedicated places in class diagrams: (behavioural features: later)



For simplicity, we view the above as an abbreviation for



Pragmatics

Recall: a UML model is an image or pre-image of a software system.

- A set of class diagrams \mathscr{CD} describes the structure of system states.
- Together with the invariants $\mathit{Inv}(\mathscr{C}\mathscr{D})$ it can be used to state:
- Pre-image: Dear programmer, please provide an implementation which uses only system states that satisfy $Inv(\mathscr{CD})$.
- Post-image: Dear user/maintainer, in the existing system, only system states which satisfy $Im(\mathscr{CD})$ are used.

(The exact meaning of 'use' will become clear when we study behaviour — intuitively; the system states that are reachable from the initial system states (b) to calling methods or firing transitions in state-machines.)

Example: highly abstract model of traffic lights controller.



Design Guidelines for (Class) Diagram (partly following Ambler (2005))

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Some Example Class Diagrams

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Popus Landerine

Main and General Modelling Guideline

Be good to your audience.

"Imagine you're given your diagram ${\mathcal D}$ and asked to conduct task ${\mathcal T}_\cdot$

So: what makes a class diagram a good class diagram?

 Can you do T with D? (semantics sufficiently clear? all necessary information available? ...)

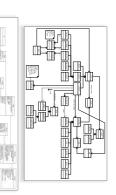
Does doing T with D cost you more nerves/time/money/...than it should?" (syntactical well-formedness? readability? intention of deviations from standard syntax clear? reasonable selection of information? layout? ...)

• the things most relevant for task \mathcal{T} , do they stand out in \mathcal{D} ?
• the things less relevant for task \mathcal{T} , do they disturb in \mathcal{D} ?

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Some More Example Class Diagrams



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Main and General Quality Criterion

- Q: When is a (class) diagram a good diagram?
- A: If it serves its purpose/makes its point.
- Examples for purposes and points and rules-of-thumb:
- Analysis/Design
- realizable, no contradictions
 abstract, focused, admitting degrees of freedom for (more detailed) design
 platform independent as far as possible but not (artificially) farer
- Implementation/A
- * close to target platform $(C_{0,1}$ is easy for Java, C_* comes at a cost other way round for RDB)
- Implementation/B
 complete, executable
- Documentation
- Right level of abstraction: "If you've only one diagram to spend, illustrate the concepts, the architecture, the difficult part"

 The more detailed the documentation, the higher the probability for regression "outdated/wrong documentation is worse than none"

General Diagramming Guidelines Ambler (2005)

(Note: "Exceptions prove the rule.")

• 2.1 Readability

• 1.-3. Support Readability of Lines 30/40

References

References

Ambier, S. W. (2005). The Benents of UNL 2.0 Style. Cambridge University Press.

OMG (2011a). Unified modeling language. Infrastructure, version 2.4.1. Technical Report formal/2011-08-05.

OMG (2011b). Unified modeling language: Superstructure, version 2.4.1. Technical Report formal/2011-08-06.

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