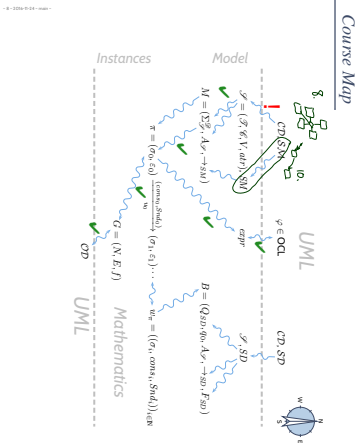


Software Design, Modelling and Analysis in UML

Lecture 8: Class Diagrams III

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Course Map

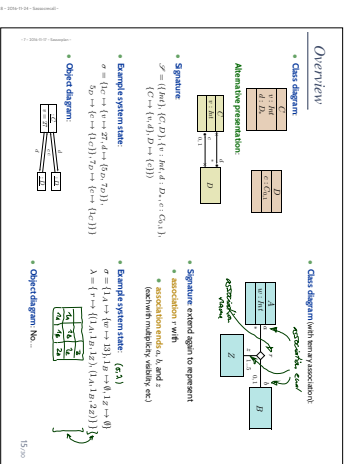
Content

- Recall: Associations
 - Overview & Plan
 - (Temporary) Extended Signature
- From Class Diagrams to Signatures
 - What if things are missing?
 - Association Semantics
 - Links in System States
 - Associations and OCL
- The Rest
 - Visibility Notation
 - Multiplicity Properties
 - Overship: "Diamonds"
- Back to the Main Track

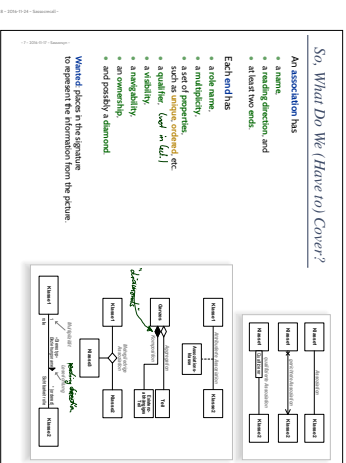
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Recall: Plain & Extended Signature

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Wait, If Omitting Things...

- ...is causing so much trouble (e.g. leading to misunderstanding) why does the standard say "In practice, it is often convenient...?"
- Is it a good idea to make **convenience** for precision/ambiguity?
- It depends:
 - Convenience as such is a legitimate goal
 - In UML-As-Sketch mode, precision **Researcher's** so convenient (for writer) can even be a **primary goal**
 - In UML-As-Blueprint mode, **precision** is the **primary goal**
- And misunderstandings are in most cases annoying
- But, (even in UML-As-Blueprint mode)
 - If all associations in your model have multiplicity "1", then it's probably a good idea not to write all these "1's."
 - So tell the reader about your convention and leave out the "1's."

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Links in System States

$$\langle r : (vok_1 : C_1, \dots, P_1, \dots, vok_n : C_n, \dots, P_n, \dots, vok_m : C_m, \dots, P_m, \dots) \rangle$$

Only for the course of lecture 7 / ? we change the definition of system states:

Definition. Let \mathcal{D} be a structure of the (extended) signature with associations $\mathcal{D} = (\mathcal{D}, \delta, V, \text{obj})$.

System state of \mathcal{D} w.r.t. \mathcal{D} is a pair (α, λ) consisting of

- a type-consistent mapping (as before)
- a mapping λ which maps each association $r : (vok_1 : C_1, \dots, vok_n : C_n) \in V$ to a relation $\lambda(r) \subseteq \mathcal{D}(C_1) \times \dots \times \mathcal{D}(C_n)$ (i.e. a set of type-consistent n -tuples of identities)

$\sigma : \mathcal{D}(C) \rightarrow (\text{obj}(C) \rightarrow \mathcal{D}(C))$

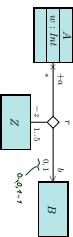
obj. Assoc. type
obj. Assoc. type

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Associations: Semantics

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Association / Link Example



Signature

$$\mathcal{Y} = \{ \{A\}, \{B, Z\} \} \text{ with } \delta$$

$\delta = \{ \langle A, A, x, r, \text{formal } x, 0? \rangle, \langle A, B, x, r, \text{formal } x, 0? \rangle, \langle B, Z, y, r, \text{formal } y, 0? \rangle, \langle A, B, z, r, \text{formal } z, 0? \rangle \}$

$\lambda = \{ r \mapsto \{ \langle a_1, a_2, z_1 \rangle, \langle a_1, a_2, z_2 \rangle, \langle a_1, a_2, z_3 \rangle, \langle a_1, a_2, z_4 \rangle \} \}$

System state

$$\sigma = \{ \langle a_1, a_2, z_1 \rangle, \langle a_1, a_2, z_2 \rangle, \langle a_1, a_2, z_3 \rangle, \langle a_1, a_2, z_4 \rangle \}$$

$\lambda(r) = \{ \langle a_1, a_2, z_1 \rangle, \langle a_1, a_2, z_2 \rangle, \langle a_1, a_2, z_3 \rangle, \langle a_1, a_2, z_4 \rangle \}$

$\lambda(r) = \{ \langle a_1, a_2, z_1 \rangle, \langle a_1, a_2, z_2 \rangle, \langle a_1, a_2, z_3 \rangle, \langle a_1, a_2, z_4 \rangle \}$

a	z
a	z
a	z
a	z
a	z

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Associations in General

- Recall: We consider associations of the following form:
- $$\langle r : (vok_1 : C_1, vok_2 : P_1, S_1, v_1, o_1), \dots, (vok_n : C_n, vok_{n+1} : P_n, S_n, v_n, o_n) \rangle$$
- Only these parts are relevant for extended system states
- $$\langle r : (vok_1 : C_1, \dots, P_1, \dots, vok_n : C_n, \dots, P_n, \dots) \rangle$$
- (recall we assume $P_i = R_i = \{\text{unique}\}$)
- The UML standard thinks of associations as **many relations** which "live on their own" in a system state:
- do not belong (in general) to certain objects (in contrast to pointers, e.g.)
 - are "first-class citizens" next to objects.
 - are (in general) **not directed** (in contrast to pointers).

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Associations and OCL

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Navigability

Navigability is treated similar to visibility.

Using names of non-navigable association ends ($v = x$) are **forbidden**.

Example: Given



the following OCL expression is **not well-typed** wrt. navigability.

context D inv: $mlc.a > 0$

The standard says: navigability is:

- $-$: possible
- X^+ : not possible



• $-$: efficient

See in general: UML associations are different from pointers / references in general. But: pointers / references can faithfully be modeled by UML associations.

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Multiplicities as Constraints

Recall: Multiplicity is a term of the form $N_1..N_2$, $N_1 \dots N_2$, $N_1..N_2$, N_2

where $N_i \leq N_{i+1}$ for $1 \leq i \leq 2k$, $N_1, \dots, N_{k-1} \in \mathbb{N}$, $N_k \in \mathbb{N} \cup \{*\}$

Define: $f_{CD}(mlc) :=$

context C inv: $(N_1 \leq mlc \rightarrow \text{size}(l) \leq N_1)$ or \dots or $(N_{k-1} \leq mlc \rightarrow \text{size}(l) \leq N_{k-1})$

until $N_k = *$

for each i : $\{ \dots (mlc : D, mlc := \dots) \dots (mlc' : C, \dots := \dots) \dots \} \in V$ or

$\{ i : \dots (mlc' : C, \dots := \dots) \dots (mlc : D, mlc := \dots) \dots \} \in V$

with $mlc \neq mlc'$, if $i \neq 0, 1, i \neq 1, 1$, and

$f_{CD}(mlc) := \text{context } C$ inv: $\text{not}(\text{undefined}(mlc))$

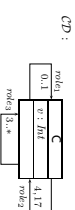
if $i = 1, 1$.

Note: in n -ary associations with $n > 2$, there is redundancy.

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Multiplicities as Constraints Example

$f_{CD}(mlc) = \text{context } C$ inv: $(N_1 \leq mlc \rightarrow \text{size}(l) \leq N_1)$ or \dots or $(N_{k-1} \leq mlc \rightarrow \text{size}(l) \leq N_{k-1})$



CD:

- context C inv: $1 \leq mlc \rightarrow \text{size}(l) \leq 4$ or $17 \leq mlc \rightarrow \text{size}(l) \leq 17$
- context C inv: $\text{not}(\text{undefined}(mlc))$ or $1 \leq mlc \rightarrow \text{size}(l) = 17$
- context C inv: $3 \leq mlc \rightarrow \text{size}(l)$

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Properties

We don't want to cover association properties in detail, only some observations (assume binary associations):

Property	Intuition	Semantical Effect
unique	one object has at most one r -link to a single one object	current setting
bag	one object may have multiple r -links to a single other object	have $X(r)$ yield multiple sets
ordered	an r -link is a sequence of object identities (possibly including duplicates)	have $X(r)$ yield set-sequences

Property	OCL Typing of expression mlc ($capr$)
unique	$!m \rightarrow \text{Set}(C)$
bag	$!m \rightarrow \text{Bag}(C)$
ordered sequence	$!m \rightarrow \text{Seq}(C)$

For subsets, redefines, union, etc. see (1.17)

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Ownership

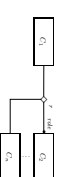
Intuitively it says:

Association r is not a "thing on its own" (ie. provided by A), but association end mlc is owned by C (B). (That is, its source node C object and provided by A .)

So: if multiplicity of mlc is 0, 1, or 1..1, then the picture above is **very close** to concepts of pointers/references.

Actually, ownership is seldom seen in UML diagrams. Again: if target platform is clear, one may well live without it (OMG, 2011b, 4.3) for more details).

Not clear to me:



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Back to the Main Track

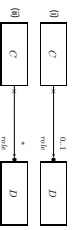
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Back to the main track:

Recall on some earlier slides we said the extension of the signature is **only** to study the semantics of the model. For the remainder of the course, we should look for something simpler...

Proposal:

- from now on, we only use associations of the form



(And we may omit the non-navigability and ownership symbols)

- Form (i) introduces *role* : C_1, λ and form (ii) introduces *role* : C_1 in λ .
- In both cases, *role* $\in \text{dir}(C)$
- We drop λ and go back to our nice σ with $\sigma(C) = \text{role} \in \mathcal{A}(D)$.

Tell Them What You've Told Them...

- From class diagrams with (general) associations, we obtain extended signatures ✓
- Links (instances of associations) "live on their own" in the λ in extended system states (σ, λ) ✓
- OCL considers role names, the semantics is (more or less) **straightforward** ✓
- **The Rest**
 - navigability is treated like visibility ✓
 - view multiplicities as shorthand for constraints ✓
 - properties ownership "diamonds" exist ✓

Back to the main track

For simplicity, lets restrict the following discussion to C_1, λ and C_2 as before (now viewed as abbreviations for particular associational)



References

References
 OMG (2011a). Unified modeling language Infrastructure, version 2.4.1. Technical Report formal/2011-08-05.
 OMG (2011b). Unified modeling language Superstructure, version 2.4.1. Technical Report formal/2011-08-06.