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- Hierarchical State Machines
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 - Abstract Syntax States
 - pseudo-states, regions, ...
- Legal System Configurations
- Abstract Syntax Transitions
- Embeddness of Fork/Join Transitions
 - scope, priority, maximality, ...

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Putting It All Together

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Initial States

Recall: a labelled transition system is (S, A, \rightarrow, S_0)

We have

- S system configurations (α, ε)
- \rightarrow labelled transition relation $(\alpha, \varepsilon) \xrightarrow{(\text{trans}, S_{\text{init}})} (\alpha', \varepsilon')$

Wanted: initial states S_0

Proposal:

Require a (finite) set of object diagrams $\mathcal{O}(\mathcal{G})$ as part of a UML model

And set $S_0 = \{(\alpha, \varepsilon) \mid \sigma \in \mathcal{O}^{-1}(\text{OD}), \text{OD} \in \mathcal{O}(\mathcal{G}), \varepsilon \text{ empty}\}$



Other Approach: (used by Rippey) tool multiplicity of classes (plus initialisation code)
We can read that as an abbreviation for an object diagram

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Semantics of UML Model (So Far)

The semantics of the UML model

$$\mathcal{M} = (\mathcal{G}, \mathcal{M}, \mathcal{O}(\mathcal{G}))$$

where

- some classes in \mathcal{G} are stereotyped as signal (standard)
- some signals and attributes are stereotyped as external (non-standard)
- there is a 1-to-1 relation between classes and state machines
- $\mathcal{O}(\mathcal{G})$ is a set of object diagrams over \mathcal{G}

is the transition system (S, A, \rightarrow, S_0) constructed on the previous slides!

The computations of \mathcal{M} are the computations of (S, A, \rightarrow, S_0)

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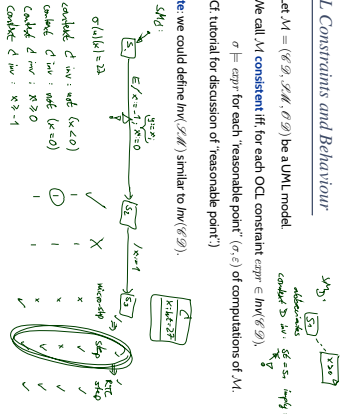
OCL Constraints and Behaviour

Let $\mathcal{M} = (\mathcal{G}, \mathcal{M}, \mathcal{O}(\mathcal{G}))$ be a UML model

- We call \mathcal{M} consistent iff, for each OCL constraint $\text{expr} \in \text{Inv}(\mathcal{G}(\mathcal{G}))$, $\sigma = \text{expr}$ for each "reasonable point" (α, ε) of computations of \mathcal{M} .

(cf. tutorial for discussion of "reasonable point")

Note: we could define $\text{Inv}(\mathcal{G}(\mathcal{M}))$ similar to $\text{Inv}(\mathcal{G}(\mathcal{G}))$.



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Last Missing Piece: Create and Destroy Transformer

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abstract syntax	concrete syntax
$create(C, expr, v)$ Infixe semantics Create an object of class C and assign it to attribute v of the object denoted by expression $expr$.	$op_{C,v} \rightarrow new C$
well-typedness $expr : T, v \in attr(D)$, $attr(C) = \{(a_i : T_i, expr_i^0) \mid 1 \leq i \leq n\}$	
semantics $attr(C) = \{(a_i : T_i, expr_i^0) \mid 1 \leq i \leq n\}$	
observables ...	
(error) conditions $\llbracket expr \rrbracket[\alpha, \beta]$ not defined.	

$x = new C \{ y = new D \};$
 can be written as
 $new C \{$
 $y = new D;$
 $\}$
 $x = new C \{ new D \};$

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Transformer: Create

abstract syntax	concrete syntax
$create(C, expr, v)$ Infixe semantics Create an object of class C and assign it to attribute v of the object denoted by expression $expr$.	
well-typedness $expr : T, v \in attr(D)$, $attr(C) = \{(a_i : T_i, expr_i^0) \mid 1 \leq i \leq n\}$	
semantics $attr(C) = \{(a_i : T_i, expr_i^0) \mid 1 \leq i \leq n\}$ $\llbracket create(C, expr, v) \rrbracket[\alpha, \beta] = \{v \mapsto \llbracket expr \rrbracket[\alpha, \beta]\}$	
observables $Obs_{create}[\alpha, \beta] = \{v \mapsto \llbracket expr \rrbracket[\alpha, \beta]\}$	
(error) conditions $\llbracket create \rrbracket[\alpha, \beta]$ not defined.	

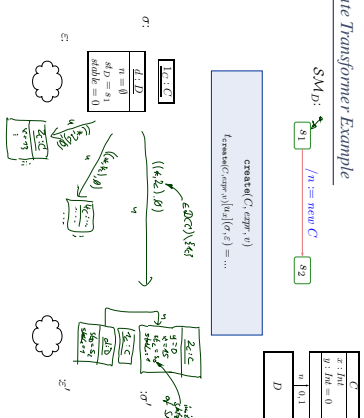
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Transformer: Create

- Re-use, choose any identity that is not alive now! (i.e. not in dom(σ))
 - Doesn't depend on history
 - May "undangle" dangling references - may happen on some platforms.
- Fresh: choose any identity that has not been alive ever, i.e. not in dom(σ) and any predecessor in current run.
- Depends on history.
- Dangling references remain dangling - could mask "dirty" effects of platform.

Create Transformer Example



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Transformer: Create

abstract syntax	concrete syntax
$create(C, expr, v)$ Infixe semantics Create an object of class C and assign it to attribute v of the object denoted by expression $expr$.	$op_{C,v} \rightarrow new C$
well-typedness $expr : T, v \in attr(D)$, $attr(C) = \{(a_i : T_i, expr_i^0) \mid 1 \leq i \leq n\}$	
semantics $attr(C) = \{(a_i : T_i, expr_i^0) \mid 1 \leq i \leq n\}$	
observables ...	
(error) conditions $\llbracket create \rrbracket[\alpha, \beta]$ not defined.	

• We use an "and assign" action for simplicity - it doesn't add or remove expressive power, but it makes the concrete syntax more readable.
 • Also for simplicity, no parameters to constructor! (= parameters of constructor). Adding them is straightforward but somewhat tedious.

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How To Choose New Identities?

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abstract syntax	concrete syntax
destroy(<i>exp</i>)	
infixive semantics Destroy the object denoted by expression <i>exp</i> .	
well-typedness	$exp : T, C \in \mathcal{C}$
semantics	...
observables	$Obs_{destroy}(u_2) = \{(u_2, \perp, (+, 0), u)\}$
(error) conditions	$I[[exp]](\sigma, \beta)$ not defined.

What to Do With the Remaining Objects?

- Assume object u_0 is destroyed...
- object u_1 may still refer to it via association r .
 - allow dangling references?
 - or remove u_0 from $r(u_1)(r)$?
 - object u_0 may have been the last one linking to object u_2 .
 - leave u_2 alone?
 - or remove u_2 also? (garbage collection)
 - Plus: (temporal extensions of OCL may have dangling references.

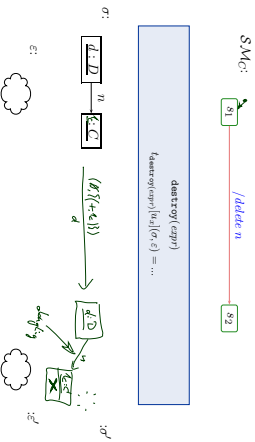
Our choice: Dangling references and no garbage collection!
 This is in line with "expect the worst", because there are target platforms which don't provide garbage collection - and models shall (in general) be correct without assumptions on target platform.

But the more "dirty" effects we see in the model, the more expensive it often is to analyse.
 Valid proposal for simple analysis: monotone frame semantics, no destruction at all.

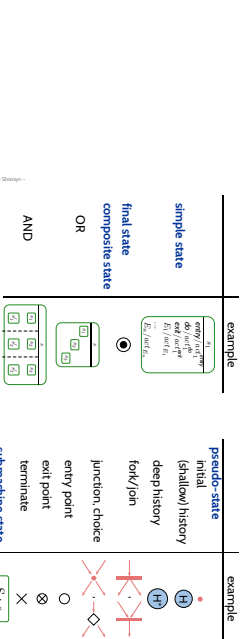
Transformer: Destroy

abstract syntax	concrete syntax
destroy(<i>exp</i>)	
infixive semantics Destroy the object denoted by expression <i>exp</i> .	
well-typedness	$exp : T, C \in \mathcal{C}$
semantics	$_{destroy}(exp)_{u_2}(\sigma, \varepsilon) = \{(\sigma', \delta' \} \} \mathcal{E} \cdot \mathcal{L} \cdot \mathcal{L}(\mathcal{E})$ where $\sigma' = \sigma \setminus \text{dom}(\sigma)(u_0)$ with $u = I[[exp]](\sigma, u_2)$.
observables	$Obs_{destroy}(exp)(u_2) = \{(+, u)\}$
(error) conditions	$I[[exp]](\sigma, u_2)$ not defined.

Destroy Transformer Example

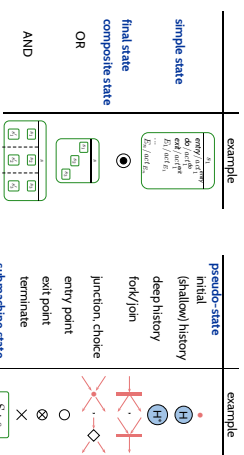


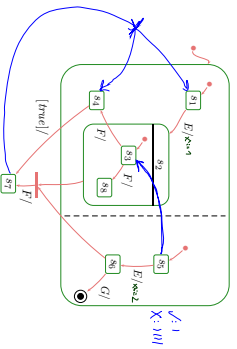
Hierarchical State-Machines



The Full Story

UML distinguishes the following kinds of states:





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Plan:

- States / Syntax:
 - What's the abstract syntax of a diagram?
 - States / Semantics:
 - what is the type of the implicit $\#$ attribute?
 - what are **legal** system configurations?
- Transitions / Syntax:
 - what are legal / well-formed transitions?
- Transitions / Semantics:
 - when is a legal transition enabled?
 - which effects do transitions have?

For example: From s_1, s_5, s_6 what may happen on E_7 ? what may happen on E_8 ? E_7 can $\Delta \subseteq C$ kill the object!

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So far:

$$(S, s_0 \rightarrow), s_0 \in S, \rightarrow \subseteq S \times (\mathcal{P} \cup \{\perp\}) \times Expr_{\mathcal{L}} \times Act_{\mathcal{L}} \times S$$

Labels: $s_1, s_2, s_3, s_4, s_5, s_6, s_7, s_8, s_9, s_{10}, s_{11}, s_{12}, s_{13}, s_{14}, s_{15}, s_{16}, s_{17}, s_{18}, s_{19}, s_{20}, s_{21}, s_{22}, s_{23}, s_{24}, s_{25}, s_{26}, s_{27}, s_{28}, s_{29}, s_{30}, s_{31}, s_{32}, s_{33}, s_{34}, s_{35}, s_{36}, s_{37}, s_{38}, s_{39}, s_{40}, s_{41}, s_{42}, s_{43}, s_{44}, s_{45}, s_{46}, s_{47}, s_{48}, s_{49}, s_{50}, s_{51}, s_{52}, s_{53}, s_{54}, s_{55}, s_{56}, s_{57}, s_{58}, s_{59}, s_{60}, s_{61}, s_{62}, s_{63}, s_{64}, s_{65}, s_{66}, s_{67}, s_{68}, s_{69}, s_{70}, s_{71}, s_{72}, s_{73}, s_{74}, s_{75}, s_{76}, s_{77}, s_{78}, s_{79}, s_{80}, s_{81}, s_{82}, s_{83}, s_{84}, s_{85}, s_{86}, s_{87}, s_{88}, s_{89}, s_{90}, s_{91}, s_{92}, s_{93}, s_{94}, s_{95}, s_{96}, s_{97}, s_{98}, s_{99}, s_{100}$

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Representing All Kinds of States

- So far:**

$$(S, s_0 \rightarrow), s_0 \in S, \rightarrow \subseteq S \times (\mathcal{P} \cup \{\perp\}) \times Expr_{\mathcal{L}} \times Act_{\mathcal{L}} \times S$$
 - From now on: (hierarchical) state machines**

$$(S, kind, region, \rightarrow, \psi, annot)$$
- where
- $S \supseteq \{top\}$ is a finite set of states
 - $kind: S \rightarrow \{st, int, fn, shdr, dist, for, join, par, chr, ent, ext, tem\}$ is a function which labels states with their kind.
 - $region: S \rightarrow 2^{2^S}$ is a function which characterizes the regions of a state.
 - 2^S : Big set of transitions.
 - 2^{2^S} : Big set of transitions.
 - $\psi: (s, t) \rightarrow 2^S \times 2^S$ is an incidence function, and
 - $annot: (s, t) \rightarrow (\mathcal{P} \cup \{\perp\}) \times Expr_{\mathcal{L}} \times Act_{\mathcal{L}}$ provides an annotation for each transition.
 - s_0 is then redundant – replaced by proper state \emptyset of kind *int*

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Well-Formedness: Regions

	$\in S$	$kind$	$region \subseteq 2^{2^S}, S_i \subseteq S$	$child \subseteq S$
final state	s	fn	\emptyset	\emptyset
pseudo-state	s	int, \dots	\emptyset	\emptyset
simple state	s	st	$\{S_1, \dots, S_n\}, n \geq 1$	$S_1 \cup \dots \cup S_n$
composite state	s	st	$\{S_1, \dots, S_n\}, n \geq 1$	$S_1 \cup \dots \cup S_n$
implicit top state	top	st	$\{S\}$	S

- Final and pseudo states must not comprise regions.
- States $s \in S$ with $kind(s) = st$ may comprise regions. Naming conventions can be defined based on regions:
 - No region: simple state.
 - One region: OR-state.
 - Two or more regions: AND-state.
- Each state (except for *top*) must lie in exactly one region.
- Note: The region function induces a child function.
- Note: Diagramming tools (like Khapsody) can ensure well-formedness.

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From UML to Hierarchical State Machine: By Example

$(S, kind, region, \rightarrow, \psi, annot)$

	example	$\in S$	$kind$	region
simple state	s	s	st	\emptyset
final state	s_1	s_1	fn	\emptyset
composite state	s_2	s_2	st	$\{s_3, s_4, s_5\}$
OR	s_3	s_3	st	$\{s_3, s_4, s_5\}$
AND	s_4	s_4	st	$\{s_3, s_4, s_5\}$
submachine state	s_5	s_5	st	$\{s_6, s_7, s_8, s_9, s_{10}\}$
pseudo-state	s_6	s_6	st	$\{s_6, s_7, s_8, s_9, s_{10}\}$

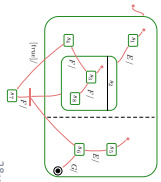
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A hierarchical state-machine (S final, region, \rightarrow h , $initial$) is called **well-formed** if and only if for all transitions $t \in \rightarrow$,

- source kind destination) states are pairwise orthogonal, i.e.
 - $\forall s, s' \in source(t) (\in target(t)) \bullet s \perp s'$
- the top state is neither source nor destination, i.e.
 - $top \notin source(t) \cup source(t)$.

Recall: final states are not sources of transitions.

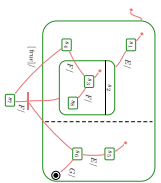
Example:



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- Transitions involving non-pseudo states.
- Initial pseudostate, final state
- Entry/exit actions, internal transitions
- History and other pseudostates, the rest.

	example	example	example
simple state			
final state			
composition state			
AND			
OR			
alternative state			
region state			
initial history			
deep history			
fork/join			
junction choice			
entry point			
exit point			
terminate			
alternative state			



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- For the **Create Action**, we have two main choices:
 - **re-use** identifies ("nasty semantics")
 - use **fresh** identifies ("clean semantics" (depends on history))

Similar for **Destroy**:

- Hierarchical State Machines introduce **Regions**
 - Thereby, states can lie within states as children.
 - The implicit variable it becomes set-valued.

- Transitions may now have
 - multiple source states, multiple destination states,
 - but need to adhere to **well-formedness conditions**.
- **Enabledness** of a set (I) of transitions
 - is a **bitstring** **to define** (\rightarrow scope, priority, maximality)
- Steps are a proper generalisation of core state machines.

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OMG (2011a). Unified modeling language: Infrastructure, version 2.41. Technical Report formal/2011-08-05.

OMG (2011b). Unified modeling language: Superstructure, version 2.41. Technical Report formal/2011-08-06.