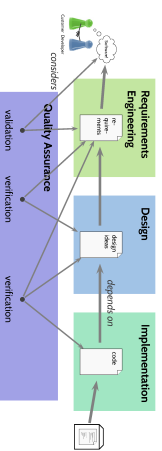


Content

- Introduction
 - ↳ a software engineering perspective
 - ↳ a theoretical computer science perspective
- Real-Time Systems
 - ↳ vs. reactive systems
 - ↳ vs. hybrid systems
 - ↳ safety-critical systems
 - ↳ examples
- Lecture Content Overview
 - ↳ and/or content
- Formalia
 - ↳ time/dates, procedures, exam
- A Formal Model of Real-Time Behaviour
 - ↳ state variables / observables
 - ↳ evolution / behaviour

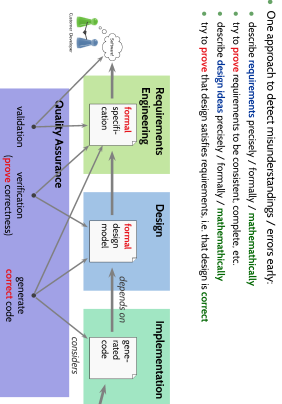
Introduction: Software Engineering Perspective

Recall: Software Engineering



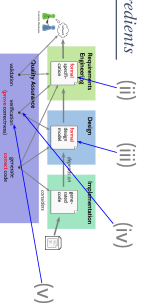
- misunderstandings / errors detected late in development can be expensive
- design and implementation may need to be re-done
- misunderstandings / errors detected only during use can be fatal
- software malfunction may harm business goals, or even lead to people being hurt.

Recall: Formal Methods



- One approach to detect misunderstandings / errors early
- describe requirements precisely / formally / mathematically
- try to prove requirements to be consistent, complete, etc.
- describe design ideas precisely / formally / mathematically
- try to prove that design satisfies requirements, i.e. that design is correct

Necessary Ingredients



- To develop software that is provably correct wrt. its requirements, we need:
- (i) a formal model of software behaviour
 - (ii) a language* to specify requirements on behaviour, (to distinguish desired from undesired behaviour),
 - (iii) a language* to specify behaviour of design ideas.
 - (iv) a notion of correctness (a relation between requirements and design specifications),
 - (v) and a method to verify (or prove) correctness (that a given pair of requirements and design specifications are in correctness relation)
 - * at best concisely and conveniently, with adequate expressive power.

Example (Un-timed): Traffic Lights



- Choose observables:
 - R : red light on, R : red light off, Y : yellow light on, \bar{Y} : yellow light off,
 - G : green light on, \bar{G} : green light off.
- Model of (final) behaviour: $\Sigma^* = ((R, R) \times (Y, Y) \times (G, G))$.
- We write, e.g. $R \bar{G}$ as shorthand for (R, Y, G) .

Example behaviours:

- $R \bar{G}, R \bar{G}, R \bar{G}$
- $R \bar{G}, R \bar{G}, R \bar{G}$

Requirements:

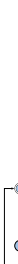
- Desired lights sequence: red, red-yellow, green, yellow, ...

Formalisation: Req₁ := (R G, R G, R G, R G) }

Undesired configuration: red-green

Formalisation: Req₂ := $\Sigma^* \bar{R} \bar{G} \bar{G} \Sigma^*$

Design:



Define notion of correctness:

A design, Des is correct wrt. requirement Req₁ and only if $\Delta(Des) \subseteq \Delta(Req_1)$.

Example (Un-timed): Traffic Lights



- Choose observables:
 - R : red light on, R : red light off, Y : yellow light on, \bar{Y} : yellow light off,
 - G : green light on, \bar{G} : green light off.
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Example behaviours:

- $R \bar{G}, R \bar{G}, R \bar{G}$
- $R \bar{G}, R \bar{G}, R \bar{G}$

Requirements:

- Desired lights sequence: red, red-yellow, green, yellow, ...

Formalisation: Req₁ := (R G, R G, R G, R G) }

Undesired configuration: red-green

Formalisation: Req₂ := $\Sigma^* \bar{R} \bar{G} \bar{G} \Sigma^*$

Design:



Define notion of correctness:

A design Des is correct wrt. requirements Req₁ and Req₂ (proof method: automata theory).

Example (Timed): Traffic Lights



- Requirement: yellow phase (R, G) should have a duration of 3 seconds on streets with speed limit 50 km/h.
- How do we formally model traffic lights behaviour with time?

For example (informal):

- red for 10s
- red-yellow for 2s
- green for 10s
- yellow for 3s

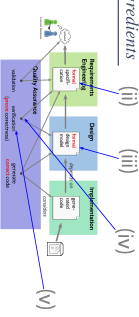
- How do we formalise the timed requirement of 3s?
- How do we formally model a controller design with time?
- What does it mean for a timed design to be correct wrt. a timed requirement?
- How do we prove timed designs correct wrt. timed requirements?

→ Lecture "Real-Time Systems"

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 - ↳ andron-content
 - ↳ Formali
 - ↳ formalises procedure, exam
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Necessary Ingredients



To develop software that is (provably) correct wrt. its requirements, we need:

- a formal model of software behaviour
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- a language to specify behaviour of design ideas. (a relation between requirements and design specifications).
- a notion of correctness (that a given pair of requirements and design specifications are in correctness relation).
- a method to verify (or prove) correctness * at best concisely and conveniently, with adequate expressive power.

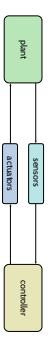
Introduction: Theoretical Computer Science Perspective

Lectures like **Introduction to Theoretical Computer Science** ("Informatik 3") cover content such as

- **propositional logic**
 - syntax, semantics, decision problems (e.g. satisfiability is decidable)
 - **finite automata**
 - syntax, language of an automaton
 - decision problems (e.g. language emptiness is decidable)
 - properties, e.g. finite automata are closed under intersection
 - **Questions: Are there logics whose models are timed behaviour?**
 - Is satisfiability still decidable?
 - If not for the full logic, then for which fragment?
 - **Questions: If we equip finite automata with real-time clocks**
 - Is language emptiness still decidable?
 - Are the set of such timed automata still closed under intersection?
 - Is it decidable whether a timed automaton satisfies a timed property?
- Lecture "Real-Time Systems"

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- A reactive system interacts with its environment by reacting to inputs from the environment with certain outputs.
- Reactive systems usually **do not terminate**.
For example, the traffic lights controller continues to run, unless there is a power outage or a scheduled maintenance.
- Contrast: terminating, transformational systems.
For example: a sorting or searching function.
- Reactive systems can be partitioned into:



- "In constructing a real-time system the aim is to control a physically existing environment, the plant, in such a way that the controlled plant satisfies all desired (timing) requirements."

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- A **Real-Time System** is a **reactive system** which, for certain inputs, has to compute the corresponding outputs **within given time bounds**.
- A **Hybrid System** is a **real-time system** consisting of continuous and discrete components. The continuous components are time-dependent (!) physical variables ranging over a continuous value set.



- A system is called **Safety Critical** if and only if a malfunction can cause loss of goods, money, or even life.

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- **Introduction**
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- **Controller requirement:** "When a crash is detected, fire the airbag."
 - When firing **too early**: airbag ineffective.
 - When firing **too late**: additional threat.

Say: 300ms plus/minus small (ε) after a crash is the right time to fire. Then the precise requirement is "When a crash is detected at time t, fire the airbag at t + 300ms ± ε."

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- "A real-time system is one that has **performance deadlines** on its computations and actions."
- Sometimes distinguished:
 - **Hard deadlines:** performance requirements that **absolutely must** be met each and every event or time mark. (Early / late data can be bad data.)
 - **Soft deadlines:** for instance about **average** response times. (Early / late data is still good data.)
- **Design Goal:** A **timely system**, i.e. one which is meeting its performance requirements.
- **Note:** performance can in general be measured by any unit of quantities: (discrete) number of steps or processor instructions, (discrete or continuous) number of seconds, etc. (→ **this lecture**)

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Example: Airbag Controller



Controller requirement: "When a crash is detected, fire the airbag."

- When firing too early, airbag ineffective.
- When firing too late, additional threat.

Say, 300ms (plus/minus small δ) after a crash is the right^{*} time to fire.

Then the precise requirement is:

"When a crash is detected at time t , fire the airbag at $t + 300\text{ms} \pm \epsilon$."

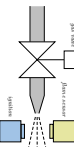
What is the plant, what is the controller?



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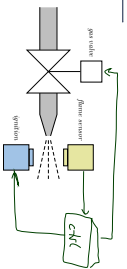
Sketch of the Methodology: Gas Burner Example

- Requirements**
 - At most 5% of any at least 60s long interval amounts to leakage.
- Reflective Design**
 - Time intervals with leakage last at most 1s.
 - After each leak, wait 30s before opening valve again.
- Constructive Design**
 - PLC Automation: open valve for 0.5s; ignite; if no flame after 0.1s close valve!
- Implementation**
 - IEC 61131-3 program



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Example: Gas Burner



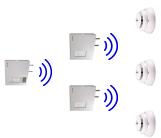
Where is the plant, where is the controller?



18/46

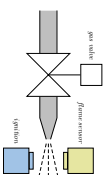
Example: Wireless Fire Alarm System

- Wireless fire alarm systems are regulated by European Norm EN 54, Part 25.
- EN 54-25 states the following requirements:
 - The loss of the ability of the system to transmit a signal from a component to the central unit is detected in less than 300 seconds and displayed at the central unit within 100 seconds thereafter.
 - Out of exactly ten alarms occurring simultaneously, the first should be displayed at the central unit within 10 seconds and all others within 100 seconds.
 - There must be no spurious displays of events at the central unit.
 - The above requirements must hold as well in the presence of radio interference by other users of the frequency band in which the system operates. Such radio interference is simulated by a jamming device specified in the standard.



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Example: Gas Burner



A situation where the gas valve is open but there is no flame is called leakage. Leakage is practically unavoidable.

- For ignition, first open valve.
- then ignite the available gas;
- ignition may fail...

Leakage is safety critical:

- Igniting large amounts of leaked gas may lead to a dangerous explosion.
- Requirement: Leakage phases should have a limited duration.

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Content Overview

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- **Worst Case Execution Time**
- Over-simplified airbag controller program:


```

while (true) do
  poll_sensors();
  if (crash) tmr_start(300ms);
  if (tmr_expired()) fire := 1;
  update_actuators();
      
```
- The execution of `poll_sensors()` and `update_actuators()` also takes time! (And we have to consider it!)
- **Not in lecture:** How to determine the WCET of for instance, C code. (A science of its own)

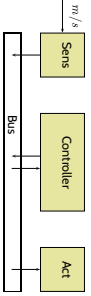
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Content

- Introduction**
- Observables and Evolutions
- Duration Calculus (DC)
- Semantical Correctness Proofs
- DC Decidability
- DC Implementables
- PLC Automata
- **Automatic Verification**...
 - ...whether a TA satisfies a DC formula, observer-based
 - Recent Results:
 - Timed Sequence Diagrams, or Quasi-equal Clocks
 - of Automatic Code Generation or ...
- **Timed Automata (TA), Uppaal**
 - Networks of Timed Automata
 - Region/Zone-Abstraction
 - TA model-checking
 - Extended Timed Automata
 - Undecidability Results

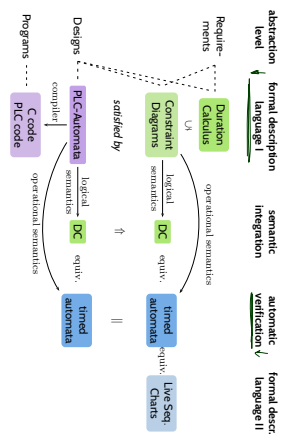
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Non-Content

- **Scheduling**
- A bit less over-simplified airbag controller:
 
- **Not in lecture:** Specialised methods to determine...
 - ...whether the bus provides sufficient bandwidth
 - ...whether the Real-Time OS controlling CPU Controller schedules the airbag control code in time
 - ...how to distribute tasks over multiple CPUs.
- etc.
- (Also a science of its own)

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Tying It All Together



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Content

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 - timed/dates, procedures, exam
 - statevariables / observables
 - evolution / behaviour
- **A Formal Model of Real-Time Behaviour**

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Formalia

- Course language **English** (slides/ writing/ presentation/ questions/discussions)
- **Presentation:** half slides/half on-screen **hand-writing** – for reasons
- **Script/Media:**
 - slides without annotations on **homepage**
 - **trying** to put them there **before** the lecture
 - slides with annotations on **homepage**, 2-up for printing typically **soon after** the lecture
 - recordings in **ILIAS** course with max. 1 week delay.
- **Interaction:**
 - absence often moaned but it takes two, so please ask/comment immediately

28.00

Formalia: Event

- **Lecturer:** Dr. Bernd Westphal
- **Support:** Liridon Mustiu
- **Homepage:** <http://srv1.inf.comatik.uni-freiburg.de/teaching/MS2017-18/teigs>
- **ILIAS course:** see homepage
- **Location:**
 - Tuesday, Thursday: here

29.00

Formalia: Exercises and Tutorials

- **Schedule/Submission:**
 - **Recall:** exercises online on Thursday before (or soon after) lecture, regular turn in on corresponding tutorial day until 14:00 local time
 - **!** should work in groups of max. 3, clearly give names on submission
 - please submit electronically, **paper submissions are tolerated** some ITEX styles on homepage; paper submissions are tolerated
- **Didactical aim:**
 - deal more extensively with notions from lecture (easy)
 - explore corner cases or alternatives (medium)
 - evaluate/appreciate approaches (difficult)
 - additional **difficulty:** instructor/arc4car talks – by intention
- **True aim: most complicated rating system ever, namely two ratings** (reasonable solution with knowledge **before** tutorial!) (reasonable solution with knowledge **after** tutorial!)
 - Good will
 - Exam/Earn
- **10% bonus for early submission.**

30.00

Formalia: Dates/Times, Break

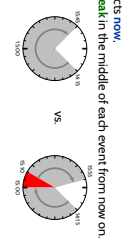
- **Schedule:**
 - Thursday, week N: 14:00-16:00 **lecture** (exercises M **online**)
 - Tuesday, week N + 1: 14:00-16:00 **lecture** (exercises M **online**)
 - Thursday, week N + 1: 14:00-16:00 **lecture** (exercises M **online**)
 - Monday, week N + 2: 14:00 ? — 70% (exercises M **early turn-in**)
 - Tuesday, week N + 2: 14:00 ? — 70% (exercises M **late turn-in**)
 - Thursday, week N + 2: 14:00-16:00 **lecture** (exercises M **late turn-in**)
 - Monday, week N + 2: 14:00-16:00 **lecture** (exercises M **late turn-in**)
 - Thursday, week N + 2: 14:00-16:00 **lecture** (exercises M **late turn-in**)
- With a prefix of lectures, with public holidays; see homepage for details.

31.00

Formalia: Exam

- **Exam Admission:**
 - 50% of the maximum possible non-bonus **good-will points** in total are **sufficient** for admission to exam
- **Exam Form:** (oral or written) not yet decided

32.00



33.00

33.00

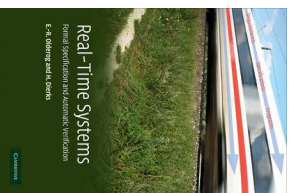
Formalia: Evaluation

Speaking of grading and examination...

- **Mid-term Evaluation:** We will have a mid-term evaluation¹, but we're always interested in comments/hints/proposals concerning form or content.

¹That is, students are asked to evaluate lecture, lecture, and tutor...

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Real-Time Systems
Formal Specification and Analysis of Real-time Systems
Lecture 4: Off-line and On-line

Cambridge

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Formalia: Questions

• **Questions:**

- **"online":**
 - (i) ask immediately or in the break
- **"offline":**
 - (i) try to solve yourself
 - (ii) discuss with colleagues
 - (iii) Exercises contact tutor via ILIAS forum or by mail
- **Rest:** contact lecturer by mail (cf. homepage) or just drop by: Building 52, Room OO-020

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Formalia

Speaking of questions

Any questions so far...?

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Formalia: Literature offered as book by UB

Tell Them What You've Told Them...

- **Real-Time Systems...**
 - ... have to compute outputs for certain inputs within **(quantitative) time bounds**.
 - ... are often **safety critical**, then computation requires high degrees of precision.
 - (discrete) **reactive system**, without time (other lecture), other continuous components than clocks (other lecture)
- **hybrid system:** other continuous components than clocks (other lecture)
- The lecture presents approaches for the precise development of real-time systems.
 - logic-based **Duration Calculus**
 - automata-based **Timed Automata**
- **Non-content:** (other lectures)
 - Real-time operating systems,
 - Scheduling,
 - Worst-case execution time, etc.

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References

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References

- Arenas, S. F., Wehrhahn, B., Dreyer, D., Müller, M., Andersen, K. S., and Podelski, A. (2010). Reach for nothing: proving safety invariants of heap-manipulating programs. In *Formal Verification*. Springer, 459–478–527.
- Douglas, B. P. (1993). *Doing Hard Time*. Addison-Wesley.
- Ohlberg, E.-R. and Dinkels, H. (2008). *Real-Time Systems - Formal Specification and Automatic Verification*. Cambridge University Press.