

Real-Time Systems

Lecture 9: DC Implementables II

2017-11-28

Dr. Bernd Westphal

Albert-Ludwigs-Universität Freiburg, Germany

- 9 - 2017-11-28 - main -

Content

- **Correctness Proof**
for the Gas Burner Implementables
- **Now where's the implementation?**
- **Programmable Logic Controllers (PLC)**
 - How do they **look like**?
 - What's **special** about them?
 - The **read/compute/write** cycle of PLC
- **Example: Stutter Filter**
 - **Structured Text** example
 - Other IEC 61131-3 programming languages
- **PLC Automata**
 - **Example: Stutter Filter**
 - **PLCA Semantics** by example
 - **Cycle time**

- 9 - 2017-11-28 - Content -

Recall: Specification of a Gas Burner Controller

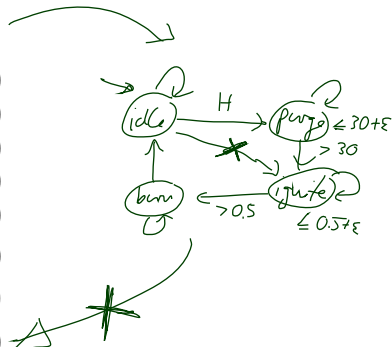
- 9 - 2017-11-28 - main -

Gas Burner Controller: The Complete Specification

$C: \{ \text{idle, purge, ignite, burn} \}$

Controller: (local)

- $\square \vee [\text{idle}] ; \text{true},$ (Init-1)
- $[\text{idle}] \longrightarrow [\text{idle} \vee \text{purge}]$ (Seq-1)
- $[\text{purge}] \longrightarrow [\text{purge} \vee \text{ignite}]$ (Seq-2)
- $[\text{ignite}] \longrightarrow [\text{ignite} \vee \text{burn}]$ (Seq-3)
- $[\text{burn}] \longrightarrow [\text{burn} \vee \text{idle}]$ (Seq-4)
- $[\text{purge}] \xrightarrow{30+\epsilon} [\neg \text{purge}]$ (Prog-1)
- $[\text{ignite}] \xrightarrow{0.5+\epsilon} [\neg \text{ignite}]$ (Prog-2)
- $[\neg \text{purge}] ; [\text{purge}] \xrightarrow{\leq 30} [\text{purge}]$ (Stab-2)
- $[\neg \text{ignite}] ; [\text{ignite}] \xrightarrow{\leq 0.5} [\text{ignite}]$ (Stab-3)
- $[\text{idle} \wedge H] \xrightarrow{\epsilon} [\neg \text{idle}]$ (Syn-1)
- $[\text{burn} \wedge (\neg H \vee \neg F)] \xrightarrow{\epsilon} [\neg \text{burn}]$ (Syn-2)
- $[\neg \text{idle}] ; [\text{idle} \wedge \neg H] \longrightarrow [\text{idle}]$ (Stab-1)
- $[\text{idle} \wedge \neg H] \longrightarrow_0 [\text{idle}]$ (Stab-1-init)
- $[\neg \text{burn}] ; [\text{burn} \wedge H \wedge F] \longrightarrow [\text{burn}]$ (Stab-4)



- 9 - 2017-11-28 - slides -

Controller: (local)

$$\begin{aligned}
 & \square \vee [\text{idle}] ; \text{true}, & (\text{Init-1}) \\
 & [\text{idle}] \longrightarrow [\text{idle} \vee \text{purge}] & (\text{Seq-1}) \\
 & [\text{purge}] \longrightarrow [\text{purge} \vee \text{ignite}] & (\text{Seq-2}) \\
 & [\text{ignite}] \longrightarrow [\text{ignite} \vee \text{burn}] & (\text{Seq-3}) \\
 & [\text{burn}] \longrightarrow [\text{burn} \vee \text{idle}] & (\text{Seq-4}) \\
 & [\text{purge}] \xrightarrow{30+\varepsilon} [\neg \text{purge}] & (\text{Prog-1}) \\
 & [\text{ignite}] \xrightarrow{0.5+\varepsilon} [\neg \text{ignite}] & (\text{Prog-2}) \\
 & [\neg \text{purge}] ; [\text{purge}] \xrightarrow{\leq 30} [\text{purge}] & (\text{Stab-2}) \\
 & [\neg \text{ignite}] ; [\text{ignite}] \xrightarrow{\leq 0.5} [\text{ignite}] & (\text{Stab-3}) \\
 & [\text{idle} \wedge H] \xrightarrow{\varepsilon} [\neg \text{idle}] & (\text{Syn-1}) \\
 & [\text{burn} \wedge (\neg H \vee \neg F)] \xrightarrow{\varepsilon} [\neg \text{burn}] & (\text{Syn-2}) \\
 & [\neg \text{idle}] ; [\text{idle} \wedge \neg H] \longrightarrow [\text{idle}] & (\text{Stab-1}) \\
 & [\text{idle} \wedge \neg H] \longrightarrow_0 [\text{idle}] & (\text{Stab-1-init}) \\
 & [\neg \text{burn}] ; [\text{burn} \wedge H \wedge F] \longrightarrow [\text{burn}] & (\text{Stab-4})
 \end{aligned}$$

Gas Valve: (output)

$$\begin{aligned}
 & \square \vee [\neg G] ; \text{true} & (\text{Init-4}) \\
 & [G \wedge (\text{idle} \vee \text{purge})] \xrightarrow{\varepsilon} [\neg G] & (\text{Syn-3}) \\
 & [\neg G \wedge (\text{ignite} \vee \text{burn})] \xrightarrow{\varepsilon} [G] & (\text{Syn-4}) \\
 & [G] ; [\neg G \wedge (\text{idle} \vee \text{purge})] \longrightarrow [\neg G] & (\text{Stab-6}) \\
 & [\neg G \wedge (\text{idle} \vee \text{purge})] \longrightarrow_0 [\neg G] & (\text{Stab-6-init}) \\
 & [\neg G] ; [G \wedge (\text{ignite} \vee \text{burn})] \longrightarrow [G] & (\text{Stab-7})
 \end{aligned}$$

Heating Request: (input)

$$\square \vee [\neg H] ; \text{true}, \quad (\text{Init-2})$$

Flame: (input)

$$\begin{aligned}
 & \square \vee [\neg F] ; \text{true}, & (\text{Init-3}) \\
 & [F] ; [\neg F \wedge \neg \text{ignite}] \longrightarrow [\neg F] & (\text{Stab-5}) \\
 & [\neg F \wedge \neg \text{ignite}] \longrightarrow_0 [\neg F] & (\text{Stab-5-init})
 \end{aligned}$$

Implementable Gas Burner Controller: Correctness Proof

Gas Burner Controller *Correctness Proof*

Set $\text{GB-Ctrl} := \text{Init-1} \wedge \dots \wedge \text{Stab-7} \wedge \varepsilon > 0$.

In the following, we show

$$\models \text{GB-Ctrl} \wedge A(\varepsilon) \implies \text{Req-1.}$$

where $A(\varepsilon)$ constrains the **reaction time** of computers executing the control program.

Read: if a program behaving like 'GB-Ctrl' is executed on a computer with reaction time ε such that $A(\varepsilon)$ holds, then 'Req' is **satisfied** in the system.

Recall:

$$\text{Req} : \iff \Box(\ell \geq 60 \implies 20 \cdot \int L \leq \ell)$$

and (cf. Olderog and Dierks (2008))

$$\models \text{Req-1} \implies \text{Req}$$

for the **simplified** requirement

$$\text{Req-1} := \Box(\ell \leq 30 \implies \int L \leq 1).$$

- 9 - 2017-11-28 - Sigheproof -

6/42

Lemma 3.15

$$\models \text{GB-Ctrl} \implies \Box \left(\begin{array}{l} ([\text{idle}] \implies \int G \leq \varepsilon) \\ \wedge ([\text{purge}] \implies \int G \leq \varepsilon) \\ \wedge ([\text{ignite}] \implies \ell \leq 0.5 + \varepsilon) \\ \wedge ([\text{burn}] \implies \int \neg F \leq 2\varepsilon) \end{array} \right)$$

Proof: Let \mathcal{I} be an interpretation, \mathcal{V} a valuation, and $[c, d]$ an interval with $\mathcal{I}, \mathcal{V}, [c, d] \models \text{GB-Ctrl}$.

Let $[b, e] \subseteq [c, d]$.

- **Case 1:** $\mathcal{I}, \mathcal{V}, [b, e] \models [\text{idle}]$
From

$$[G \wedge (\text{idle} \vee \text{purge})] \xrightarrow{\varepsilon} [\neg G] \quad (\text{Syn-3})$$

$$[G] ; [\neg G \wedge (\text{idle} \vee \text{purge})] \longrightarrow [\neg G] \quad (\text{Stab-6})$$

we can conclude

$$\mathcal{I}, \mathcal{V}, [b, e] \models \underbrace{\Box([G] \implies \ell \leq \varepsilon)}_{\text{by (Syn-3), the valve is closed within } \varepsilon \text{ time units when in 'idle'}} \wedge \underbrace{\neg \Diamond([G] ; [\neg G] ; [G])}_{\text{by (Stab-6), the valve doesn't open again when in 'idle'}}$$

Thus $\mathcal{I}, \mathcal{V}, [b, e] \models \int G \leq \varepsilon$.

- **Case 2:** $\mathcal{I}, \mathcal{V}, [b, e] \models [\text{purge}]$ Analogously to case 1.

- 9 - 2017-11-28 - Sigheproof -

7/42

Lemma 3.15 Cont'd

$$\text{GB-Ctrl} \Rightarrow \square \left(\begin{array}{l} ([\text{idle}] \Rightarrow fG \leq \varepsilon) \\ \wedge ([\text{purge}] \Rightarrow fG \leq \varepsilon) \\ \wedge ([\text{ignite}] \Rightarrow \ell \leq 0.5 + \varepsilon) \\ \wedge ([\text{burn}] \Rightarrow f\neg F \leq 2\varepsilon) \end{array} \right)$$

- **Case 3:** $\mathcal{I}, \mathcal{V}, [b, e] \models [\text{ignite}]$

From

$$[\text{ignite}] \xrightarrow{0.5+\varepsilon} [\neg\text{ignite}] \quad (\text{Prog-2})$$

we can directly conclude $\mathcal{I}, \mathcal{V}, [b, e] \models \ell \leq 0.5 + \varepsilon$.

- **Case 4:** $\mathcal{I}, \mathcal{V}, [b, e] \models [\text{burn}]$

From

$$[\text{burn} \wedge (\neg H \vee \neg F)] \xrightarrow{\varepsilon} [\neg\text{burn}] \quad (\text{Syn-2})$$

$$[F]; [\neg F \wedge \neg\text{ignite}] \rightarrow [\neg F] \quad (\text{Stab-5})$$

we can conclude

$$\mathcal{I}, \mathcal{V}, [b, e] \models \square \underbrace{([\neg F] \Rightarrow \ell \leq \varepsilon)}_{\text{by (Syn-2)}} \wedge \underbrace{\neg\Diamond([F]; [\neg F]; [F])}_{\text{by (Stab-5)}}$$

Thus $\mathcal{I}, \mathcal{V}, [b, e] \models f\neg F \leq 2\varepsilon$.

- 9 - 2017-11-28 - Sigheproof -

8/42

Lemma 3.16

$$\models \exists \varepsilon \bullet \text{GB-Ctrl} \Rightarrow \underbrace{\square(\ell \leq 30 \Rightarrow fL \leq 1)}_{\text{Req-1}}$$

Proof: Let \mathcal{I}, \mathcal{V} , and $[b, e]$ such that $\mathcal{I}, \mathcal{V}, [b, e] \models \text{GB-Ctrl} \wedge \ell \leq 30$.

Distinguish 5 cases:

- (i) $\mathcal{I}, \mathcal{V}, [b, e] \models \square$ ✓
- (ii) $\mathcal{I}, \mathcal{V}, [b, e] \models ([\text{idle}]; \text{true} \wedge \ell \leq 30)$
- (iii) $\mathcal{I}, \mathcal{V}, [b, e] \models ([\text{purge}]; \text{true} \wedge \ell \leq 30)$
- (iv) $\mathcal{I}, \mathcal{V}, [b, e] \models ([\text{ignite}]; \text{true} \wedge \ell \leq 30)$
- (v) $\mathcal{I}, \mathcal{V}, [b, e] \models ([\text{burn}]; \text{true} \wedge \ell \leq 30)$

- 9 - 2017-11-28 - Sigheproof -

9/42

Lemma 3.16 Cont'd

$$3.15: \text{GB-Ctrl} \Rightarrow \square \left(\begin{array}{l} ([\text{idle}] \Rightarrow fG \leq \varepsilon) \\ \wedge ([\text{purge}] \Rightarrow fG \leq \varepsilon) \\ \wedge ([\text{ignite}] \Rightarrow \ell \leq 0.5 + \varepsilon) \\ \wedge ([\text{burn}] \Rightarrow f\neg F \leq 2\varepsilon) \end{array} \right)$$

- **Case (i):** $\mathcal{I}, \mathcal{V}, [b, e] \models \top$
- **Case (ii):** $\mathcal{I}, \mathcal{V}, [b, e] \models [\text{idle}] ; \text{true} \wedge \ell \leq 30$
From

$$[\text{idle}] \longrightarrow [\text{idle} \vee \text{purge}] \quad (\text{Seq-1})$$

$$[\neg \text{purge}] ; [\text{purge}] \xrightarrow{\leq 30} [\text{purge}] \quad (\text{Stab-2})$$

we can conclude

$$\mathcal{I}, \mathcal{V}, [b, e] \models [\text{idle}] \vee [\text{idle}] ; [\text{purge}]$$

By 3.15,

$$\mathcal{I}, \mathcal{V}, [b, e] \models (fL \leq \varepsilon) \vee (fL \leq \varepsilon ; fL \leq \varepsilon)$$

hence

$$\mathcal{I}, \mathcal{V}, [b, e] \models fL \leq 2\varepsilon$$

Thus $\boxed{\varepsilon \leq 0.5}$ is sufficient for Req-1 ($fL \leq 1$) **in this case.**

- 9 - 2017-11-28 - Sighepost -

10/42

Lemma 3.16 Cont'd

$$3.15: \text{GB-Ctrl} \Rightarrow \square \left(\begin{array}{l} ([\text{idle}] \Rightarrow fG \leq \varepsilon) \\ \wedge ([\text{purge}] \Rightarrow fG \leq \varepsilon) \\ \wedge ([\text{ignite}] \Rightarrow \ell \leq 0.5 + \varepsilon) \\ \wedge ([\text{burn}] \Rightarrow f\neg F \leq 2\varepsilon) \end{array} \right)$$

- **Case (iii):** $\mathcal{I}, \mathcal{V}, [b, e] \models [\text{burn}] ; \text{true} \wedge \ell \leq 30$
From

$$[\text{burn}] \longrightarrow [\text{burn} \vee \text{idle}] \quad (\text{Seq-4})$$

we can conclude

$$\mathcal{I}, \mathcal{V}, [b, e] \models ([\text{burn}] \vee [\text{burn}] ; \underbrace{[\text{idle}] ; \text{true}}_{\text{Case (ii)}}) \wedge \ell \leq 30.$$

By 3.15 and Case (ii),

$$\mathcal{I}, \mathcal{V}, [b, e] \models ((fL \leq 2\varepsilon) \vee (fL \leq 2\varepsilon) ; (fL \leq 2\varepsilon)) \wedge \ell \leq 30.$$

hence

$$\mathcal{I}, \mathcal{V}, [b, e] \models fL \leq 4\varepsilon.$$

Thus $\boxed{\varepsilon \leq 0.25}$ is sufficient for Req-1 ($fL \leq 1$) **in this case.**

- 9 - 2017-11-28 - Sighepost -

11/42

Lemma 3.16 Cont'd

$$3.15: \text{GB-Ctrl} \Rightarrow \square \left(\begin{array}{l} ([\text{idle}] \Rightarrow fG \leq \varepsilon) \\ \wedge ([\text{purge}] \Rightarrow fG \leq \varepsilon) \\ \wedge ([\text{ignite}] \Rightarrow \ell \leq 0.5 + \varepsilon) \\ \wedge ([\text{burn}] \Rightarrow f\neg F \leq 2\varepsilon) \end{array} \right)$$

- **Case (iv):** $\mathcal{I}, \mathcal{V}, [b, e] \models [\text{ignite}]; \text{true} \wedge \ell \leq 30$
From

$$[\text{ignite}] \longrightarrow [\text{ignite} \vee \text{burn}] \quad (\text{Seq-3})$$

we can conclude

$$\mathcal{I}, \mathcal{V}, [b, e] \models ([\text{ignite}] \vee [\text{ignite}]; \underbrace{[\text{burn}]; \text{true}}_{\text{Case (iii)}}) \wedge \ell \leq 30.$$

By 3.15 and Case (iii),

$$\mathcal{I}, \mathcal{V}, [b, e] \models ((fL \leq 0.5 + \varepsilon) \vee (fL \leq 0.5 + \varepsilon); (fL \leq 4\varepsilon)) \wedge \ell \leq 30$$

hence

$$\mathcal{I}, \mathcal{V}, [b, e] \models fL \leq 0.5 + 5\varepsilon.$$

Thus $\boxed{\varepsilon \leq 0.1}$ is sufficient for Req-1 ($fL \leq 1$) **in this case.**

- 9 - 2017-11-28 - Sighepost -

12/42

Lemma 3.16 Cont'd

$$3.15: \text{GB-Ctrl} \Rightarrow \square \left(\begin{array}{l} ([\text{idle}] \Rightarrow fG \leq \varepsilon) \\ \wedge ([\text{purge}] \Rightarrow fG \leq \varepsilon) \\ \wedge ([\text{ignite}] \Rightarrow \ell \leq 0.5 + \varepsilon) \\ \wedge ([\text{burn}] \Rightarrow f\neg F \leq 2\varepsilon) \end{array} \right)$$

- **Case (v):** $\mathcal{I}, \mathcal{V}, [b, e] \models [\text{purge}]; \text{true} \wedge \ell \leq 30$
From

$$[\text{purge}] \longrightarrow [\text{purge} \vee \text{ignite}] \quad (\text{Seq-2})$$

and 3.15 and Case (iv) we can conclude

$$\mathcal{I}, \mathcal{V}, [b, e] \models fL \leq 0.5 + 6\varepsilon.$$

Thus $\boxed{\varepsilon \leq \frac{1}{12}}$ is sufficient for Req-1 ($fL \leq 1$) **in this case.** \square

Lemma 3.16.

$$\models \exists \varepsilon \bullet \text{GB-Ctrl} \Rightarrow \underbrace{\square(\ell \leq 30 \Rightarrow fL \leq 1)}_{\text{Req-1}}$$

- 9 - 2017-11-28 - Sighepost -

13/42

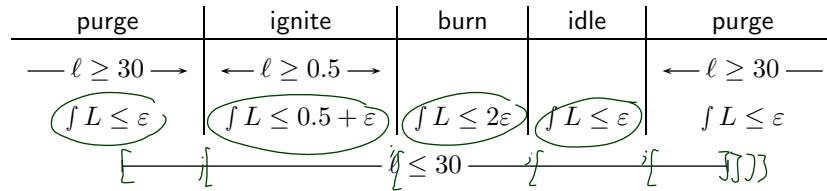
Correctness Result

Theorem 3.17.

$$\models \left(\text{GB-Ctrl} \wedge \varepsilon \leq \frac{1}{12} \right) \implies \text{Req}$$

Recall:

- Req-1 = $\square(\ell \leq 30 \implies fL \leq 1)$ implies Req.
- 3.15: $\lceil \text{purge} \rceil \implies fL \leq \varepsilon$, $\lceil \text{ignite} \rceil \implies fL \leq 0.5 + \varepsilon$, $\lceil \text{burn} \rceil \implies fL \leq 2\varepsilon$, $\lceil \text{idle} \rceil \implies fL \leq \varepsilon$.



- Thus $fL \leq 0.5 + 6\varepsilon$, so a sufficient reaction time constraint is $A(\varepsilon) := \varepsilon \leq \frac{1}{12}$.

- 9 - 2017-11-28 - Sighepost -

Discussion

- We used only

'Seq-1', 'Seq-2', 'Seq-3', 'Seq-4',
 'Prog-2', 'Syn-2', 'Syn-3',
 'Stab-2', 'Stab-5', 'Stab-6'.

What about

$$\text{Prog-1} = \lceil \text{purge} \rceil \xrightarrow{30+\varepsilon} \lceil \neg \text{purge} \rceil$$

for instance?

```

Gas Burner Controller: The Complete Specification

Controller: (local)
  [] v [idle] : true,      (Init-1)
  [idle] -> [idle v purge] (Seq-1)
  [purge] -> [purge v ignite] (Seq-2)
  [ignite] -> [ignite v burn] (Seq-3)
  [burn] -> [burn v idle] (Seq-4)
  [purge] -> [purge] (Prog-1)
  [ignite] -> [ignite] (Prog-2)
  [-purge] : [purge] -> [purge] (Stab-2)
  [-ignite] : [ignite] -> [ignite] (Stab-3)
  [idle v H] -> [-idle] (Syn-1)
  [burn v (-H v -F)] -> [-burn] (Syn-2)
  [-idle] : [idle v -H] -> [idle] (Stab-5)
  [idle v -H] -> [idle] (Stab-1-init)
  [-burn] : [burn v H v F] -> [burn] (Stab-4)

Gas Valve: (output)
  [] v [-G] : true,      (Init-4)
  [G v (-G v purge)] -> [-G] (Syn-3)
  [-G v (ignite v burn)] -> [G] (Syn-4)
  [G] : [-G v (idle v purge)] -> [-G] (Stab-6)
  [-G v (idle v purge)] -> [-G] (Stab-6-init)
  [-G] : [G v (ignite v burn)] -> [G] (Stab-7)

Heating Request: (input)
  [] v [-H] : true,      (Init-2)

Flame: (input)
  [] v [-F] : true,      (Init-3)
  [F] : [-F v -ignite] -> [-F] (Stab-5)
  [-F v -ignite] -> [-F] (Stab-5-init)
  
```

- 9 - 2017-11-28 - Sighepost -

Discussion

- We used only

'Seq-1,' 'Seq-2,' 'Seq-3,' 'Seq-4,'
'Prog-2,' 'Syn-2,' 'Syn-3,'
'Stab-2,' 'Stab-5,' 'Stab-6.'

What about

$$\text{Prog-1} = [\text{purge}] \xrightarrow{30+\epsilon} [\neg\text{purge}]$$

for instance?

We only proved the **safety** property on leakage,
we did not consider the (not formalised) **liveness** requirement:
the controller **should do something** finally,
e.g. heating requests should be served finally by trying an ignition.

Content

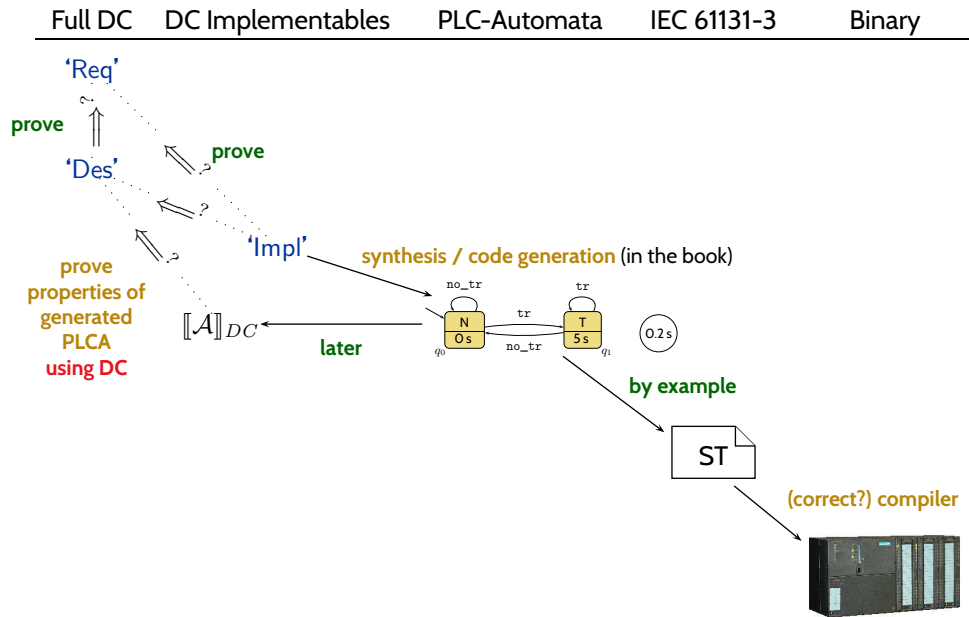
- **Correctness Proof**
for the Gas Burner Implementables

- **Now where's the implementation?**
- **Programmable Logic Controllers (PLC)**
 - How do they **look like**?
 - What's **special** about them?
 - The **read/compute/write** cycle of PLC
- **Example: Stutter Filter**
 - **Structured Text** example
 - Other IEC 61131-3 programming languages
- **PLC Automata**
 - **Example: Stutter Filter**
 - **PLCA Semantics** by example
 - **Cycle time**

Now Where's the Implementation?

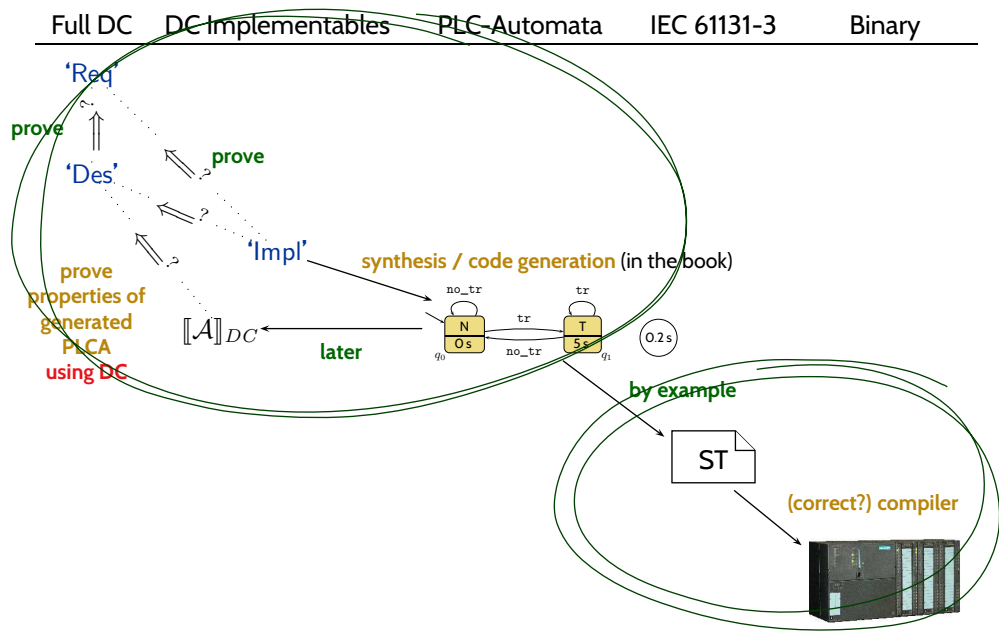
- 9 - 2017-11-28 - main -

The Plan



- 9 - 2017-11-28 - main -

The Plan



- 9 - 2017-11-28 - main -

Content

- **Correctness Proof**
for the Gas Burner Implementables
- **Now where's the implementation?**
- **Programmable Logic Controllers (PLC)**
 - How do they **look like**?
 - What's **special** about them?
 - The **read/compute/write** cycle of PLC
- **Example: Stutter Filter**
 - **Structured Text** example
 - Other IEC 61131-3 programming languages
- **PLC Automata**
 - **Example: Stutter Filter**
 - **PLCA Semantics** by example
 - **Cycle time**

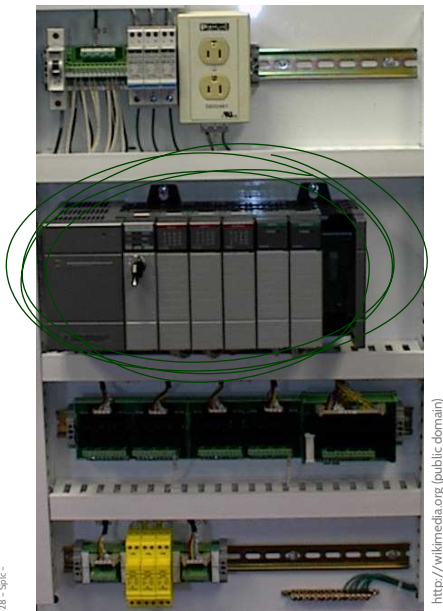
- 9 - 2017-11-28 - Content -

What is a PLC?

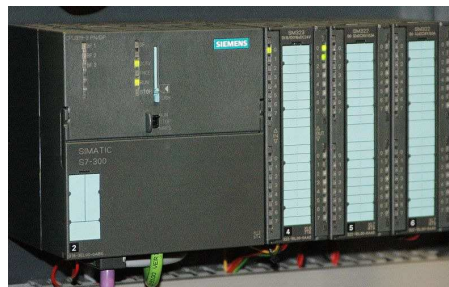
- 9 - 2017/11/28 - main -

21/42

How do PLC look like?



- 9 - 2017/11/28 - 5/6 -



22/42

What's special about PLC?



- 9 - 2017/11/28 - 5pk -

- microprocessor, memory, **timers**
- digital (or analog) I/O ports
- possibly RS 232, fieldbuses, networking
- robust hardware
- reprogrammable
- **standardised programming model** (IEC 61131-3)

23/42

Where are PLC employed?



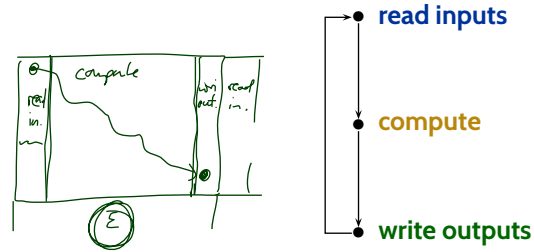
- 9 - 2017/11/28 - 5pk -

- mostly **process automation**
 - production lines
 - packaging lines
 - chemical plants
 - power plants
 - electric motors, pneumatic or hydraulic cylinders
 - ...
- not so much: **product automation**, there
 - tailored or OTS controller boards
 - embedded controllers
 - ...

24/42

How are PLC programmed?

- PLC have in common that they operate in a cyclic manner:



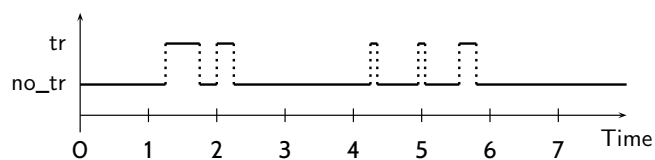
- Cyclic operation is repeated until external interruption (such as shutdown or reset).
- Cycle time: typically a few milliseconds (Lukoschus, 2004).
- Programming for PLC means providing the “compute” part.
- Input/output values are available via designated local variables.

- 9 - 2017-11-28 - 5:46 -

25/42

How are PLC programmed, practically?

- **Example:** reliable, stutter-free train sensor.
 - Assume a track-side sensor which outputs:
 - no_tr – iff “no passing train”
 - tr – iff “a train is passing”
 - Assume that a change from “no_tr” to “tr” signals arrival of a train. (No spurious sensor values.)
- **Problem:** the sensor may **stutter**, i.e. oscillate between “no_tr” and “tr” multiple times.

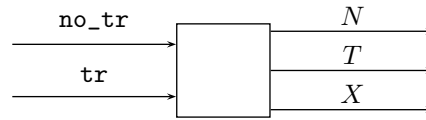


- 9 - 2017-11-28 - 5:46 -

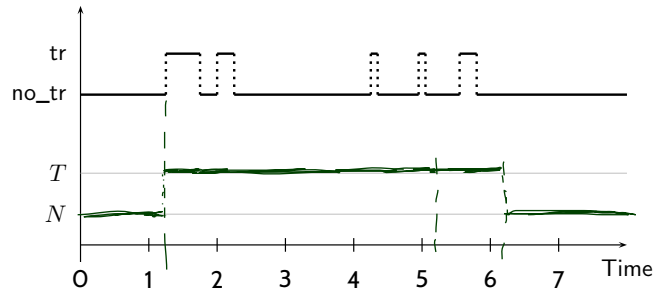
26/42

Example: Stutter Filter

- **Idea:** a stutter filter with outputs N and T , for “no train” and “train passing” (and possibly X , for error).



After arrival of a train, it should ignore “no_tr” for 5 seconds.



- 9 - 2017/11/28 - 5%k -

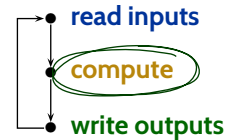
27/42

How are PLC programmed, practically?

```

1 PROGRAM PLC_PRG_FILTER
2 VAR
3   state : INT := 0; (* 0:=N, 1:=T, 2:=X *)
4   tmr : TP;
5 ENDVAR
6
7 IF state = 0 THEN
8   %output := N;
9   IF %input = tr THEN
10    state := 1;
11    %output := T;
12   ELSIF %input = Error THEN
13    state := 2;
14    %output := X;
15   ENDIF
16 ELSIF state = 1 THEN
17
18   tmr( IN := TRUE, PT := t#5.0s );
19   IF (%input = no_tr AND NOT tmr.Q) THEN
20    state := 0;
21    %output := N;
22    tmr( IN := FALSE, PT := t#0.0s );
23   ELSIF %input = Error THEN
24    state := 2;
25    %output := X;
26    tmr( IN := FALSE, PT := t#0.0s );
27   ENDIF
28 ENDIF

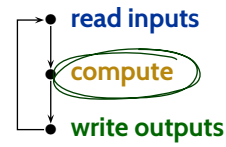
```



- 9 - 2017/11/28 - 5%k -

28/42

How are PLC programmed, practically?



```

1 PROGRAM PLC_PRG_FILTER
2 VAR
3   state : INT := 0; (* 0:=N, 1:=T, 2:=X *)
4   tmr   : TP;
5 ENDVAR
6
7 IF state = 0 THEN
8   %output := N;
9   IF %input = tr THEN
10    state := 1;
11    %output := T;
12   ELSIF %input = Error THEN
13    state := 2;
14    %output := X;
15   ENDIF
16 ELSIF state = 1 THEN
17   tmr( IN := TRUE, PT := t#5.0s );
18   IF (%input = no_tr AND NOT tmr.Q) THEN
19    state := 0;
20    %output := N;
21    tmr( IN := FALSE, PT := t#0.0s );
22   ELSIF %input = Error THEN
23    state := 2;
24    %output := X;
25    tmr( IN := FALSE, PT := t#0.0s );
26   ENDIF
27 ENDIF
28

```

declare timer *tmr*

intuitive semantics:

- do the assignment
- if assignment changed *IN* from FALSE to TRUE ("rising edge on *IN*") then set *tmr* to given duration (initially, *IN* is FALSE)

duration

TRUE: iff *tmr* is still running (here: if 5s not yet elapsed)

- 9 - 2007-11-28 - 5gk -

Alternative Programming Languages by IEC 61131-3

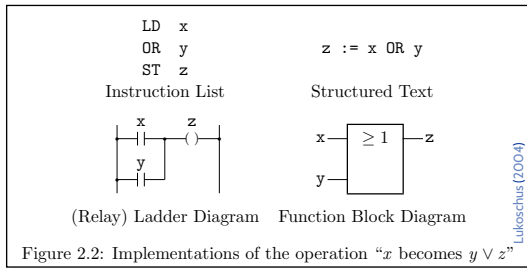


Figure 2.2: Implementations of the operation "x becomes y v z"

Lukoschus (2004)

- Tied together by
- Sequential Function Charts (SFC)
- Unfortunate: deviations in semantics... Bauer (2003)

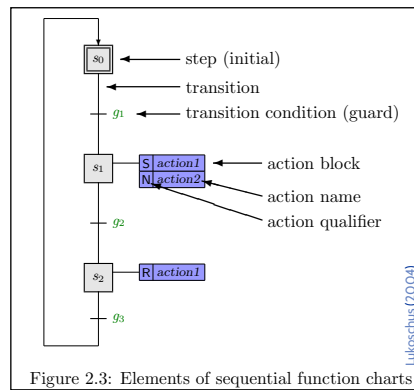


Figure 2.3: Elements of sequential function charts

Lukoschus (2004)

- 9 - 2007-11-28 - 5gk -

- **Correctness Proof**
for the Gas Burner Implementables
- **Now where's the implementation?**
- **Programmable Logic Controllers (PLC)**
 - How do they **look like**?
 - What's **special** about them?
 - The **read/compute/write** cycle of PLC
- **Example: Stutter Filter**
 - **Structured Text** example
 - Other IEC 61131-3 programming languages
- **PLC Automata**
 - **Example: Stutter Filter**
 - **PLCA Semantics** by example
 - **Cycle time**

Tell Them What You've Told Them...

- We can **prove** the Gas Burner implementables **correct** by carefully considering its phases. ✓
- A **crucial aspect** is **reaction time**: ✓
 - Controller programs executed on some hardware platform do not react in **0-time**,
 - some platforms may be **too slow** to satisfy requirements.
- **Programmable Logic Controllers (PLC)** are epitomic for real-time controller platforms:
 - have a **real-time clock** device,
 - can **read inputs** and **write outputs**,
 - can manage **local state**. ✓
- **PLC programs**
 - are executed in **read/compute/write** cycles,
 - have a **cycle-time** (possibly a watchdog).
- **PLC Automata** are a more abstract (than IEC 61131-3) way of describing and studying PLC programs.

References

References

Bauer, N. (2003). *Formale Analyse von Sequential Function Charts*. PhD thesis, Universität Dortmund.

Lukoschus, B. (2004). *Compositional Verification of Industrial Control Systems*. PhD thesis, Christian-Albrechts-Universität zu Kiel.

Olderog, E.-R. and Dierks, H. (2008). *Real-Time Systems - Formal Specification and Automatic Verification*. Cambridge University Press.