

Contents & Goals



- Last Lecture:
- OCL Syntax and Semantics

This Lecture:

- Educational Objectives:** Capabilities for following tasks/questions:
 - What is an object diagram? What are object diagrams good for?
 - When is an object diagram called partial? What are partial ones good for?
 - When is an object diagram an object diagram (wrt. what)?
 - Is this an object diagram wrt. to that other thing?
 - How are system states and object diagrams related?
 - What does it mean that an OCL expression is satisfiable?
 - When is a set of OCL constraints said to be consistent?
 - Can you think of an object diagram which violates this OCL constraint?
- Content:**
 - Object Diagrams
 - Example: Object Diagrams for Documentation
 - OCL: consistency, satisfiability

Where Are We?

Object Diagrams

Graph

Definition. A node labelled graph is a triple

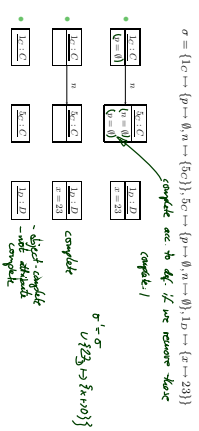
$$G = (N, E, f)$$

consisting of

- vertices N ,
- edges E ,
- node labelling $f : N \rightarrow X$, where X is some label domain,

- $N = \text{dom}(\sigma)$, if $u_2 \in \sigma(a_1)(r)$ then $(u_1, r, u_2) \in E$.
- $f(u) = \sigma(a_1)(r) \cup \{r\} \cup (\sigma(a_1)(r) \setminus N) \cup \sigma(a)(r) \setminus N$

Complete or partial? (not system state σ)

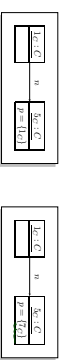


- Claim:
 - Each finite system state has **exactly one** complete object diagram.
 - A finite system state can have **many** partial object diagrams.
- Each object diagram G represents a set of system states, namely $G^{-1} := \{\sigma \in \Sigma_{\mathcal{O}} \mid G \text{ is an object diagram of } \sigma\}$ (possibly)
- **Observation:** If somebody tells us that a given object diagram G is **complete**, we can uniquely reconstruct the corresponding system state. In other words: G^{-1} is then a singleton.

Corner Cases

Closed Object Diagrams vs. Dangling References

Find the 10 differences! (Both diagrams shall be **complete**.)

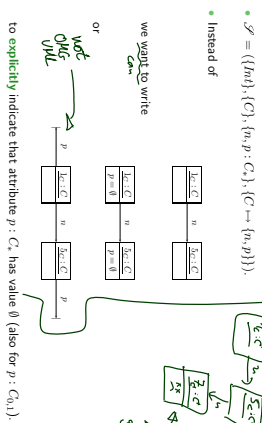


Definition. Let σ be a system state. We say attribute $r \in K_{A_1}$ has a **dangling reference** in object $u \in \text{dom}(\sigma)$ if and only if the attribute's value comprises an object which is not alive in σ , i.e. if $\sigma(a)(r) \not\subseteq \text{dom}(\sigma)$ *active, spec*

We call σ **closed** if and only if no attribute has a dangling reference in any object alive in σ .

Observation: Let G be the () complete object diagram of a closed system state σ . Then the nodes in G are labeled with σ -typed attribute/value pairs only.

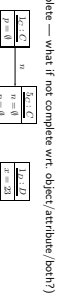
Special Notation



Aftermath

- We slightly deviate from the standard (for reasons):
 - In the course, $C_{0,1}$ and C -typed attributes **only** have **sets as values**. UML also considers multisets, that is, they can have (This is not an object diagram in the sense of our definition because of the requirement on the edges E . Extension is straightforward but tedious.)
 - We **allow** to give the valuation of $C_{0,1}$ - or C -typed attributes in the **values compartment**.
 - Allows us to indicate that a certain r is not referring to another object.
 - Allows us to represent 'dangling references', i.e. references to objects which are not alive in the current system state.
 - We introduce a graphical representation of \emptyset values.

- Let G be an object diagram of signature \mathcal{S} wrt. structure \mathcal{D} . Let $expr$ be an OCL expression over \mathcal{S} . We say G satisfies $expr$, denoted by $G \models expr$, if and only if $\forall \sigma \in \mathcal{S}^G : \sigma \models expr$.
- If G is complete, we can also talk about " $G \models expr$ ". (Otherwise better not to avoid confusion: G^{-1} could comprise different system states in which $expr$ evaluates to true, false, and \perp .)



Definition (Consistency). A set $Inv = \{i_1, \dots, i_n\}$ of OCL constraints over \mathcal{S} is called consistent (or satisfiable) if and only if there exists a system state of \mathcal{S} wrt. \mathcal{D} which satisfies all of them, i.e. if $\exists \sigma \in \Sigma_{\mathcal{S}}^{\mathcal{D}} : \sigma \models i_1 \wedge \dots \wedge \sigma \models i_n$ and inconsistent (or unrealizable) otherwise.

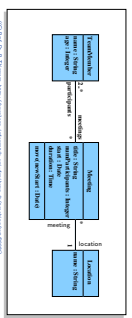
- Whether a set of OCL constraints is satisfiable or not is in general not as obvious as in the made-up example.
- Wanted:** A procedure which decides the OCL satisfiability problem.
- Unfortunately:** in general undecidable. Otherwise we could, for instance, solve diophantine equations

$$c_1 x_1^{a_1} + \dots + c_n x_n^{a_n} = d$$

Diophantine

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- context Lobby: inv: name implies meeting -> isLobby()
- context Meeting: inv: title == "Reception" implies location.name == "Lobby"
- allInstancesReception -> exist! w: Meeting | w.title == "Reception"

- Expressive Power:**
 - "Pure OCL expressions only compute primitive recursive functions, but not recursive functions in general." [Cengie and Knapp, 2001]
 - Evolution over Time: "Finally set/∪ > ∪"
 - Proposal for fixes e.g. [Fiske and Müller, 2003]. (Or: sequence diagrams)
 - Real-Time: "Objects respond within 10s"
 - Proposal for fixes e.g. [Cengie and Knapp, 2002]
 - Reachability: "After insert operation, node shall be reachable."
 - Fix: add transitive closure

Concrete Syntax
 "The syntax of OCL has been criticized – e.g. by the authors of Galaxys [...] – for being hard to read and write."
 "OCL's expressions are stacked in the style of Smalltalk, which makes it hard to see the scope of quantified variables."
 "Navigations are applied to atoms and not sets of atoms, although there is a collect operation that maps a function over a set."
 "Attributes [...] are partial functions in OCL, and result in expressions with undefined value." [Jackson, 2002]

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