

# Software Design, Modelling and Analysis in UML

## Lecture 02: Semantical Model

2011-10-26

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### Contents & Goals

#### Last Lecture:

- Motivation: model-based development of things (houses, software) to cope with complexity, detect errors early
- Model-based (or -driven) Software Engineering
- UML Mode of the Lecture: Blueprint.

#### This Lecture:

- **Educational Objectives:** Capabilities for these tasks/questions:
  - Why is UML of the form it is?
  - Shall one feel bad if not using all diagrams during software development?
  - What is a signature, an object, a system state, etc.?
  - What's the purpose of signature, object, etc. in the course?
  - How do Basic Object System Signatures relate to UML class diagrams?
- **Content:**
  - Brief history of UML
  - Course map revisited
  - Basic Object System Signature, Structure, and System State

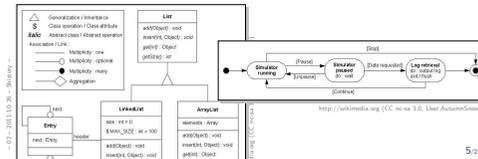
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- Note: being a **modelling** languages doesn't mean being graphical (or: being a visual formalism [Harel]).
- For instance, [Kastens and Büning, 2008] also name:
  - Sets, Relations, Functions
  - Terms and Algebras
  - Propositional and Predicate Logic
  - Graphs
  - XML Schema, Entity Relation Diagrams, UML Class Diagrams
  - Finite Automata, Petri Nets, UML State Machines
- **Pro:** visual formalisms are found appealing and easier to **grasp**. Yet they are not necessarily easier to **write**!
- **Beware:** you may meet people who dislike visual formalisms just for being graphical — maybe because it is easier to "trick" people with a meaningless picture than with a meaningless formula.  
More serious: it's maybe easier to misunderstand a picture than a formula.

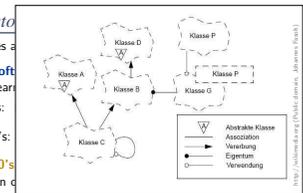
### A Brief History of UML

- Boxes/lines and finite automata are used to visualise software for ages.
- **1970's, Software Crisis**<sup>TM</sup>
  - Idea: learn from engineering disciplines to handle growing complexity.
  - Languages: **Flowcharts, Nassi-Shneiderman, Entity-Relation Diagrams**
- **Mid 1980's: Statecharts** [Harel, 1987], **StateMate**<sup>TM</sup> [Harel et al., 1990]
- **Early 1990's, advent of Object-Oriented-Analysis/Design/Programming**
  - Inflation of notations and methods, most prominent:
    - **Object-Modeling Technique (OMT)** [Rumbaugh et al., 1990]



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      - Booch Method and Notation [Booch, 1993]
      - Object-Oriented Software Engineering (OOSE) [Jacobson et al., 1992]
- Each "persuasion" selling books, tools, seminars...
- Late 1990's: joint effort **UML 0.x, 1.x**
    - Standards published by **Object Management Group (OMG)**, "international, open membership, not-for-profit computer industry consortium".
  - Since 2005: **UML 2.x**

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## UML Overview [OMG, 2007b, 684]

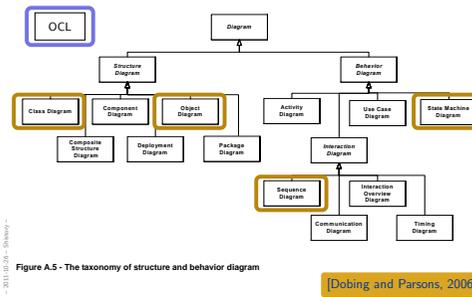


Figure A.5 - The taxonomy of structure and behavior diagram

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## Common Expectations on UML

- Easily writeable, readable even by customers
- Powerful enough to bridge the gap between idea and implementation
- Means to tame complexity by separation of concerns ("views")
- Unambiguous
- Standardised, exchangeable between modelling tools
- UML standard says how to develop software
- Using UML leads to better software
- ...

## We will see...

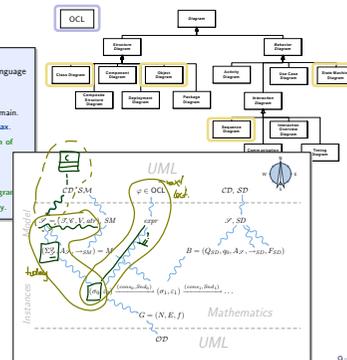
Seriously: After the course, you should have an own opinion on each of these claims. In how far/in what sense does it hold? Why? Why not? How can it be achieved? Which ones are really only hopes and expectations? ...?

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## Course Map Revisited

### The Plan

- Recall:
- Overall aim: a formal language for software blueprints.
  - Approach:
    - Common semantical domain.
    - UML fragments as syntax.
    - Abstract representation of diagrams.
    - Informal semantics: UML standard
    - assign meaning to diagram
    - Define, e.g., consistency.



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## UML: Semantic Areas

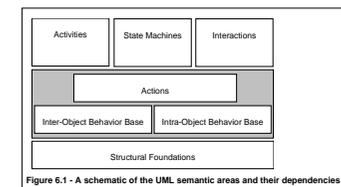


Figure 6.1 - A schematic of the UML semantic areas and their dependencies

[OMG, 2007b, 11]

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### System State

all object identities  
partial function  
yields  
domain of non-class types

**Definition.** Let  $\mathcal{A}$  be a structure of  $\mathcal{S} = (\mathcal{C}, \mathcal{V}, V, \text{atr})$ .  
A system state of  $\mathcal{A}$  wrt  $\mathcal{S}$  is a **type-consistent** mapping  
 $\sigma : \mathcal{D}(\mathcal{C}) \rightarrow (V \rightarrow (\mathcal{D}(\mathcal{S}) \cup \mathcal{D}(\mathcal{C}_*))$

That is, for each  $u \in \mathcal{D}(C)$ ,  $C \in \mathcal{C}$ , if  $u \in \text{dom}(\sigma)$

- $\text{dom}(\sigma(u)) = \text{atr}(C)$   
:  $V \rightarrow (\mathcal{D}(\mathcal{S}) \cup \mathcal{D}(\mathcal{C}_*))$
- $(\sigma(u))v \in \mathcal{D}(\tau)$  if  $v : \tau, \tau \in \mathcal{S}$
- $(\sigma(u))v \in \mathcal{D}(D_*)$  if  $v : D_{0,1}$  or  $v : D_*$  with  $D \in \mathcal{C}$

We call  $u \in \mathcal{D}(\mathcal{C})$  **alive** in  $\sigma$  if and only if  $u \in \text{dom}(\sigma)$ .

We use  $\Sigma_{\mathcal{S}}^{\mathcal{A}}$  to denote the set of all system states of  $\mathcal{A}$  wrt  $\mathcal{S}$ .

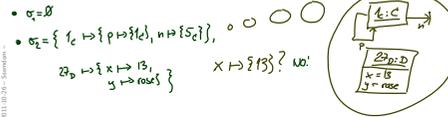
### System State Example

**Signature, Structure:**

$\mathcal{S}_0 = (\{Int\}, \{C, D\}, \{x : Int, p : C_{0,1}, n : C_*\}, \{C \mapsto \{p, n\}, D \mapsto \{x\}\})$   
 $\mathcal{D}(Int) = \mathbb{Z}$ ,  $\mathcal{D}(C) = \{1c, 2c, 3c, \dots\}$ ,  $\mathcal{D}(D) = \{1d, 2d, 3d, \dots\}$   
 $\mathcal{D}(\mathcal{C}_*) = \{rose, 4c\}$   $\mathcal{D}(C_{0,1}) = \mathcal{D}(C)$

**Wanted:**  $\sigma : \mathcal{D}(\mathcal{C}) \rightarrow (V \rightarrow (\mathcal{D}(\mathcal{S}) \cup \mathcal{D}(\mathcal{C}_*)))$  such that

- $\text{dom}(\sigma(u)) = \text{atr}(C)$ ,
- $\sigma(u)(v) \in \mathcal{D}(\tau)$  if  $v : \tau, \tau \in \mathcal{S}$ ,
- $\sigma(u)(v) \in \mathcal{D}(C_*)$  if  $v : D_*$  with  $D \in \mathcal{C}$ .



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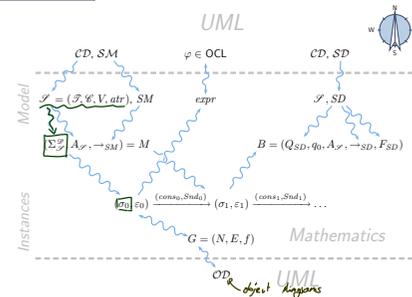
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- **Concrete, explicit:**  
 $\sigma = \{1c \mapsto \{p \mapsto \emptyset, n \mapsto \{5c\}\}, 5c \mapsto \{p \mapsto \emptyset, n \mapsto \emptyset\}, 1d \mapsto \{x \mapsto 23\}\}$
- **Alternative: symbolic system state**  
 $\sigma = \{c_1 \mapsto \{p \mapsto \emptyset, n \mapsto \{c_2\}\}, c_2 \mapsto \{p \mapsto \emptyset, n \mapsto \emptyset\}, d \mapsto \{x \mapsto 23\}\}$   
 assuming  $c_1, c_2 \in \mathcal{D}(C)$ ,  $d \in \mathcal{D}(D)$ ,  $c_1 \neq c_2$ .

You Are Here.

### Course Map



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