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## Tutorials for Decision Procedures Exercise sheet 11

**Exercise 1: Nelson-Oppen** 8 Points Apply the deterministic version of Nelson-Oppen to the following  $T_{\mathsf{E}} \cup T_{\mathbb{Q}}$ -formulae:

(a) 
$$x + y = z \land f(z) = x + y \land f(f(x + y)) \neq z$$
.

(b) 
$$g(x+y,z) = f(g(x,y)) \land x+z = y \land z \ge 0 \land x \ge y \land g(x,x) = z \land f(z) \ne g(2x,0)$$

## Exercise 2: DPLL(T)

Consider the following formula

$$\begin{aligned} f_b(i) &\neq f_c(i) \land \\ f_b(j) &= v \land (i \neq j \to f_b(i) = f_a(i)) \land \\ f_c(j) &= v \land (i \neq j \to f_c(i) = f_a(i)) \end{aligned}$$

- (a) Compute the propositional core in CNF.
- (b) Run the DPLL(T) algorithm by repeatedly applying the rules from the lecture. Is the formula satisfiable?