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Tutorials for Decision Procedures Exercise sheet 6

Exercise 1: Quantifier Elimination for $T_{\mathbb{Q}}$

Apply quantifier elimination to the following $\Sigma_{\mathbb{Q}}$ -formulae:

- (a) $\exists y. (x = 2y \land y < x)$
- (b) $\forall y. (25 < x + 2y \lor x + 2y < 25)$

(c)
$$\forall x. \exists y. (y > x \land -y < x)$$

(d) $\forall x. (x > 0 \leftrightarrow \exists y. (x > y \land -x < y))$

Exercise 2: Sufficient Set

For $T_{\mathbb{Q}}$ the algorithm in the lecture examines terms $\frac{s+t}{2}$ for all $s, t \in S$. Suppose we split up S in S_A , S_B , S_C depending on whether the term t comes from an (A) x < t, (B) t < x, or (C) x = t literal. Based on this distinction, give a smaller set of terms that still is sufficient.

Exercise 3: Quantifier Elimination for $T_{\mathbb{Z}}$

Apply quantifier elimination to the following $\Sigma_{\mathbb{Z}}$ -formulae:

- (a) $\exists y. (x = 2y \land y < x)$
- (b) $\forall y. (25 < x + 2y \lor x + 2y < 25)$
- (c) $\forall y. (x + y < 8 \rightarrow x + 2y < 8)$