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3. Presence Exercise Sheet for the Lecture Computer Science Theory

WITH PROPOSALS FOR SOLUTIONS

Exercise 1: Pushdown automata

Consider the following PDA \mathcal{A} over $\Sigma = \{a, b\}$.

$$(Z_0, a, AZ_0),$$

$$(A, a, AA)$$

$$(A, a, \varepsilon)$$

$$(Z_0, b, Z_0)$$

$$(A, a, \varepsilon)$$

$$(Z_0, \varepsilon, Z_0)$$

$$(Z_0, \varepsilon, Z_0)$$

$$(Z_0, \varepsilon, Z_0)$$

- (a) What is L(A), i.e., the language accepted by A with final states? Hint: Decompose the problem:
 - What happens in q_0 (q_1, q_2) ?
 - When can we go from q_0 to q_1 (from q_1 to q_2)?
- (b) Construct a PDA which accepts the same language, but with the empty stack.

......Sketch of solution

(a)
$$L = \{a^n b a^n \mid n \in \mathbb{N}\}$$

(b)

$$(Z_0, a, AZ_0),$$

$$(A, a, AA)$$

$$(A, a, \varepsilon)$$

$$(Z_0, \varepsilon, \varepsilon)$$

$$(Z_0, \varepsilon, Z_0)$$

$$(Z_0, \varepsilon, Z_0)$$

$$(Z_0, \varepsilon, Z_0)$$

$$(Z_0, \varepsilon, Z_0)$$

$$(Z_0, \varepsilon, Z_0)$$