

Softwaretechnik / Software-Engineering

Lecture 14: Behavioural Software Modelling

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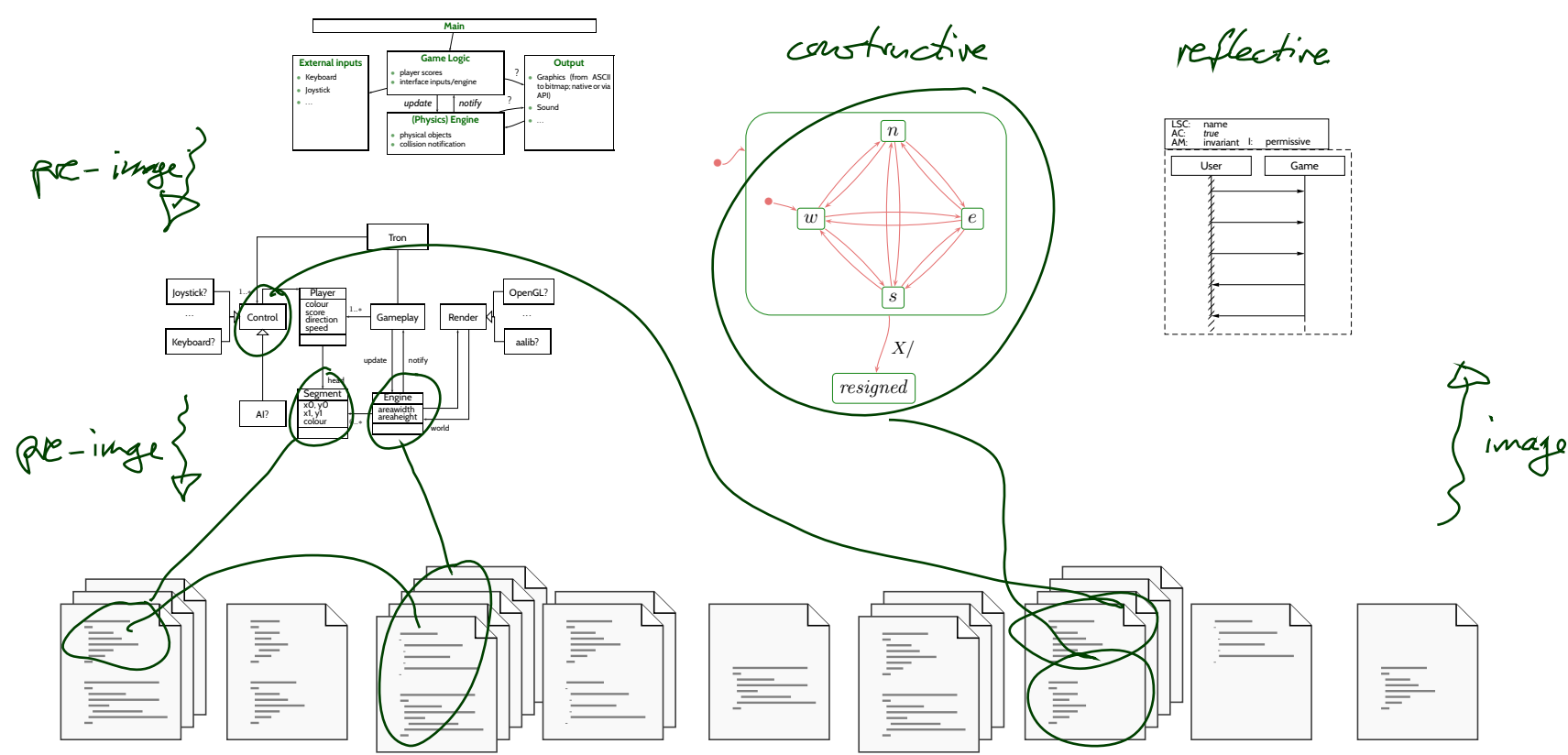
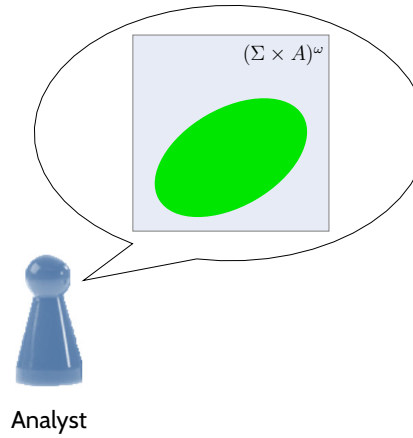
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Topic Area Architecture & Design: Content

- VL 11
 - **Introduction and Vocabulary**
 - **Software Modelling**
 - model; views / viewpoints; 4+1 view
- ⋮
- VL 12
 - **Modelling structure**
 - (simplified) class & object diagrams
 - (simplified) object constraint logic (OCL)
- ⋮
- VL 13
 - **Principles of Design**
 - modularity, separation of concerns
 - information hiding and data encapsulation
 - abstract data types, object orientation
- ⋮
- VL 14
 - **Design Patterns**
 - **Modelling behaviour**
 - communicating finite automata (CFA)
 - Uppaal query language
- ⋮
- VL 15
 - CFA vs. Software
 - **Unified Modelling Language (UML)**
 - basic state-machines
 - an outlook on hierarchical state-machines
- ⋮
- **Model-driven/-based Software Engineering**

- **Communicating Finite Automata (CFA)**
 - concrete and abstract syntax,
 - networks of CFA,
 - operational semantics.
- **Transition Sequences**
- **Deadlock, Reachability**
- **Uppaal**
 - tool demo (simulator),
 - query language,
 - CFA model-checking.
- **CFA at Work**
 - drive to configuration, scenarios, invariants
 - tool demo (verifier).
- **Uppaal Architecture**

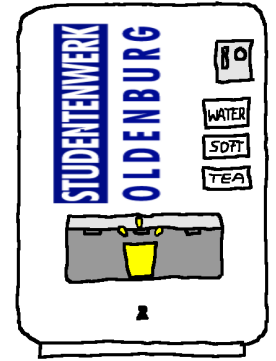
Software Modelling



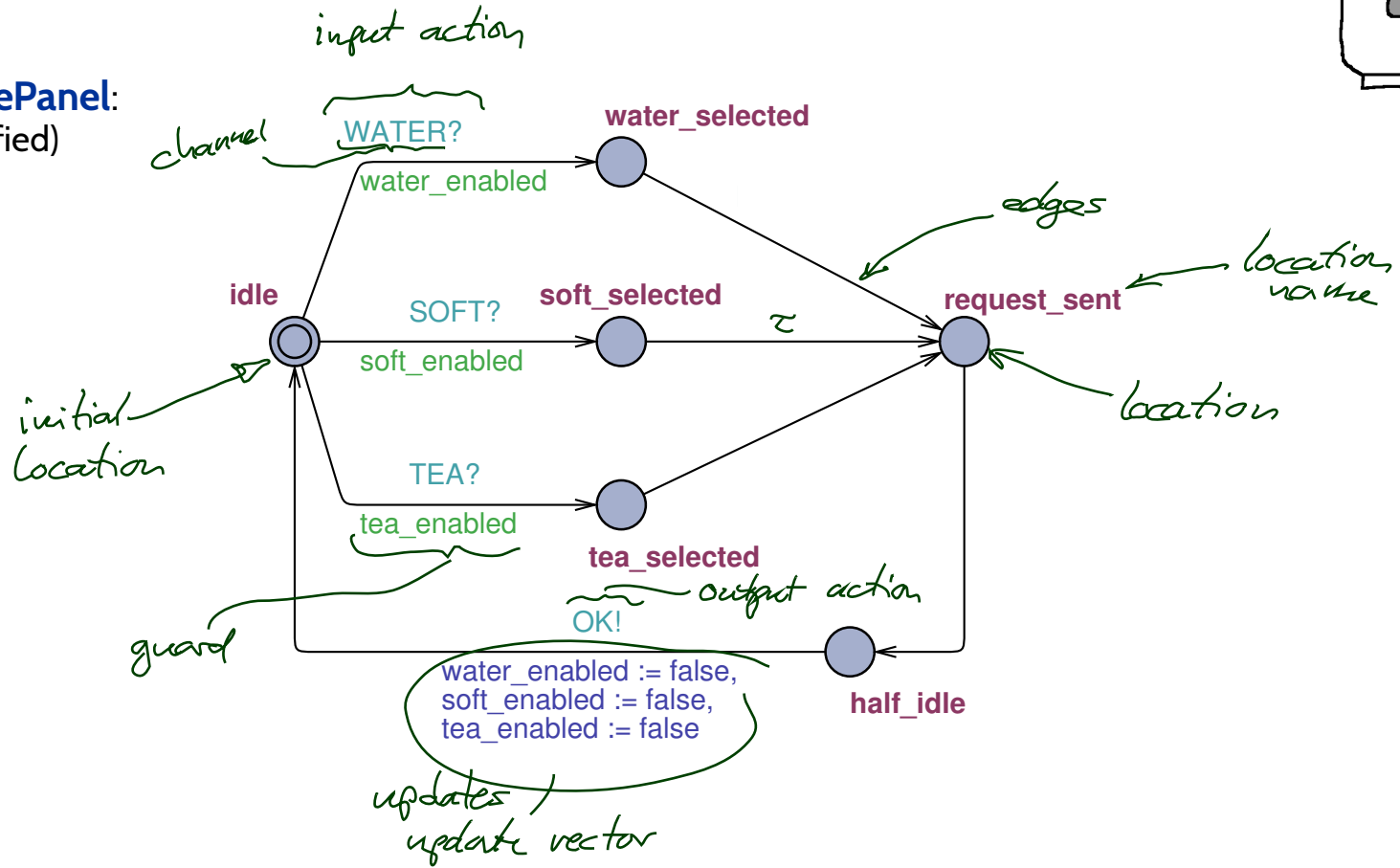
Communicating Finite Automata

presentation follows (Olderog and Dierks, 2008)

Example



ChoicePanel:
(simplified)



Channel Names and Actions

To define communicating finite automata, we need the following sets of symbols:

- A set $(a, b \in) \text{Chan}$ of **channel names** or **channels**.
- For each channel $a \in \text{Chan}$, two **visible actions**:
 $a?$ and $a!$ denote **input** and **output** on the **channel** ($a?, a! \notin \text{Chan}$).
- $\tau \notin \text{Chan}$ represents an **internal action**, not visible from outside.
- $(\alpha, \beta \in) \text{Act} := \{a? \mid a \in \text{Chan}\} \cup \{a! \mid a \in \text{Chan}\} \cup \{\tau\}$ is the set of **actions**.
- An **alphabet** B is a set of **channels**, i.e. $B \subseteq \text{Chan}$.
- For each alphabet B , we define the corresponding **action set**

$$B_{?!} := \{a? \mid a \in B\} \cup \{a! \mid a \in B\} \cup \{\tau\}.$$

Note: $\text{Chan}_{?!} = \text{Act}$.

Integer Variables and Expressions, Resets

- Let $(v, w \in) V$ be a set of ((**finite domain**) integer) variables. *including 0.*

By $(\varphi \in) \Psi(V)$ we denote the set of **integer expressions** over V using function symbols $+$, $-$, \dots and relation symbols $<$, \leq , \dots

$v < w$

- A **modification** on $v \in V$ is of the form

or update

$$v ::= \varphi, \quad v \in V, \quad \varphi \in \Psi(V).$$

By $R(V)$ we denote the set of all modifications.

- By \vec{r} we denote a finite list $\langle r_1, \dots, r_n \rangle$, $n \in \mathbb{N}_0$, of modifications $r_i \in R(V)$. \vec{r} is called **reset vector** (or **update vector**).

$\langle \rangle$ is the empty list ($n = 0$).

- By $R(V)^*$ we denote the set of all such finite lists of modifications.

Communicating Finite Automata

Definition. A **communicating finite automaton** is a structure

$$\mathcal{A} = (L, B, V, E, \ell_{ini})$$

where

- $(\ell \in) L$ is a finite set of **locations** (or **control states**),
- $B \subseteq \text{Chan}$,
- V : a set of data variables,
- $E \subseteq L \times B_{!?} \times \Phi(V) \times R(V)^* \times L$: a finite set of **directed edges** such that

$$(\ell, \alpha, \varphi, \vec{r}, \ell') \in E \wedge \text{chan}(\alpha) \in U \implies \varphi = \text{true}.$$

Edges $(\ell, \alpha, \varphi, \vec{r}, \ell')$ from location ℓ to ℓ' are labelled with an **action** α , a **guard** φ , and a list \vec{r} of **modifications**.

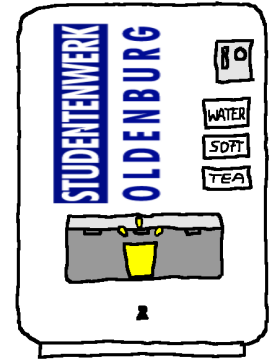
- $\ell_{ini} \in L$ is the **initial location**.

Example

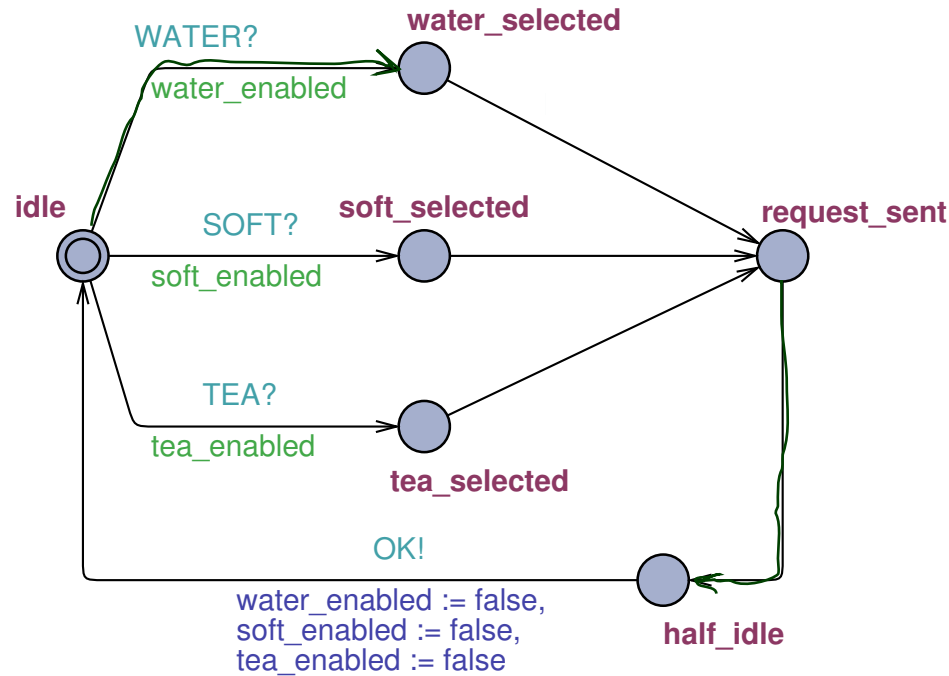
$$L = \{idle, water_selected, \dots\}$$

$$B = \{WATER, OK, \dots\}$$

$$V = \{water_enabled, \dots\}$$



ChoicePanel:
(simplified)



$$E = \{ (idle, WATER?, water_enabled, \langle \rangle, water_selected), \\ (request_sent, \tau, true, \langle \rangle, half_idle), \dots \}$$

$$\begin{matrix} \uparrow & \uparrow & \uparrow & \uparrow & \uparrow \\ L & B_{?} & \psi(V) & R(V)^* & L \end{matrix}$$

$$l_{ini} = idle$$

Operational Semantics of Networks of CFA

Definition.

Let $\mathcal{A}_i = (L_i, B_i, V_i, E_i, \ell_{ini,i})$, $1 \leq i \leq n$, be communicating finite automata.

The **operational semantics** of the network of CFA $\mathcal{C}(\mathcal{A}_1, \dots, \mathcal{A}_n)$ is the labelled transition system

$$\mathcal{T}(\mathcal{C}(\mathcal{A}_1, \dots, \mathcal{A}_n)) = (\text{Conf}, \underbrace{\text{Chan} \cup \{\tau\}}_{\text{Labels}}, \{\xrightarrow{\lambda} \mid \lambda \in \text{Chan} \cup \{\tau\}\}, C_{ini})$$

where

- $V = \bigcup_{i=1}^n V_i$, $\nu \in \mathcal{L}_1 \times \mathcal{L}_2 \times \dots \times \mathcal{L}_n$
- $\text{Conf} = \{ \langle \vec{\ell}, \nu \rangle \mid \ell_i \in L_i, \nu : V \rightarrow \mathcal{D}(V) \}$, *valuation of ν*
- $C_{ini} = \langle \vec{\ell}_{ini}, \nu_{ini} \rangle$ with $\nu_{ini}(v) = 0$ for all $v \in V$.

The transition relation consists of transitions of the following two types.

Helpers: Extended Valuations and Effect of Resets

- $\nu : V \rightarrow \mathcal{D}(V)$ is a **valuation** of the variables,
- A valuation ν of the variables canonically assigns an integer value $\nu(\varphi)$ to each integer expression $\varphi \in \Phi(V)$.
 $\nu(v), \nu(w) \rightsquigarrow \nu(v+w)$
- $\models \subseteq (V \rightarrow \mathcal{D}(V)) \times \Phi(V)$ is the canonical **satisfaction relation** between valuations and integer expressions from $\Phi(V)$.
 $\nu \models v > w$

- **Effect of modification** $r \in R(V)$ on ν , denoted by $\nu[r]$:

$$\left(\nu[v := \varphi] \right)(a) := \begin{cases} \nu(\varphi), & \text{if } a = v, \\ \nu(a), & \text{otherwise} \end{cases}$$

- We set $\nu[\langle r_1, \dots, r_n \rangle] := \nu[r_1] \dots [r_n] = (((\nu[r_1])[r_2]) \dots)[r_n]$.

That is, modifications are executed sequentially from left to right.

$$\begin{array}{c} \xrightarrow{\quad} \\ \vec{r} \quad w := w + 1, w := 0 \quad \nu(w) = 27 \quad \nu[\vec{r}] := 0 \\ \xleftarrow{\quad} \end{array}$$

Operational Semantics of Networks of CFA

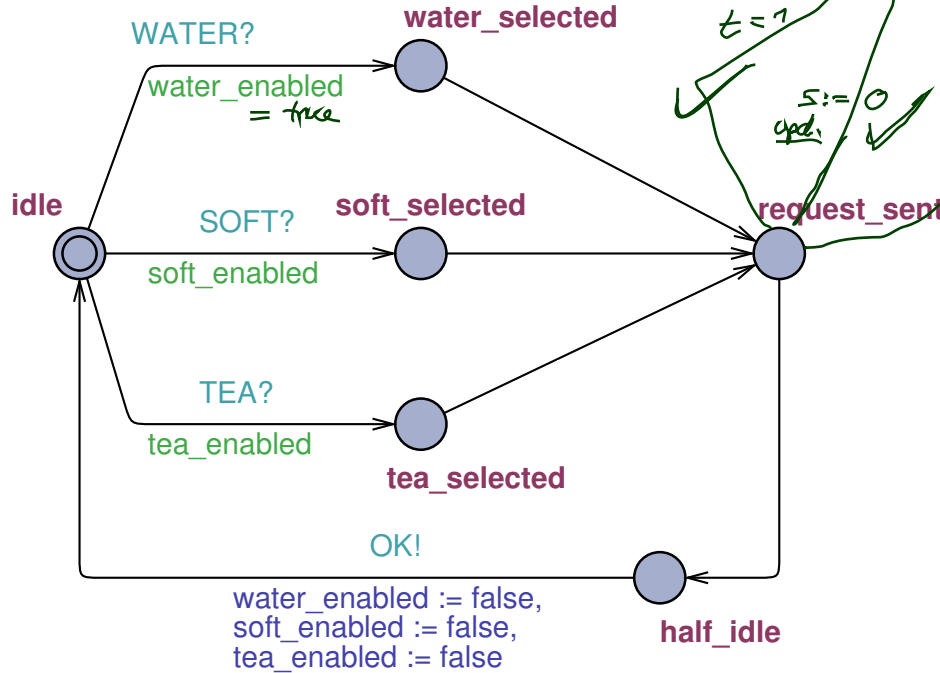
$$(\langle \vec{e}, \nu \rangle, \langle \vec{e}', \nu' \rangle) \in \xrightarrow{\tau} \left(\in \{ \xrightarrow{\lambda} \mid \lambda \text{ label} \} \right)$$

- An **internal transition** $\langle \vec{l}, \nu \rangle \xrightarrow{\tau} \langle \vec{l}', \nu' \rangle$ occurs if there is $i \in \{1, \dots, n\}$ and
 - there is a τ -edge $(l_i, \tau, \varphi, \vec{r}, l'_i) \in E_i$ such that
 - $\nu \models \varphi$, “source valuation satisfies guard”
 - $\vec{l}' = \vec{l}[l_i := l'_i]$, “automaton i changes location”
 - $\nu' = \nu[\vec{r}]$, “ ν' is the result of applying \vec{r} on ν ”
- A **synchronisation transition** $\langle \vec{l}, \nu \rangle \xrightarrow{b} \langle \vec{l}', \nu' \rangle$ occurs if there are $i, j \in \{1, \dots, n\}$ with $i \neq j$ and
 - there are edges $(l_i, b!, \varphi_i, \vec{r}_i, l'_i) \in E_i$ and $(l_j, b?, \varphi_j, \vec{r}_j, l'_j) \in E_j$ such that
 - $\nu \models \varphi_i \wedge \varphi_j$, “source valuation satisfies guards (!)”
 - $\vec{l}' = \vec{l}[l_i := l'_i][l_j := l'_j]$, “automaton i and j change location”
 - $\nu' = (\nu[\vec{r}_i])[\vec{r}_j]$, “ ν' is the result of applying first \vec{r}_i and then \vec{r}_j on ν ”

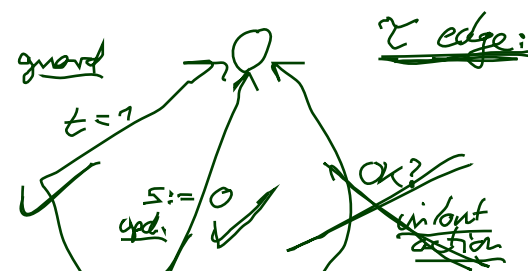
This style of communication is known under the names “rendezvous”, “synchronous”, “blocking” communication (and possibly many others).

Example

ChoicePanel:
(simplified)



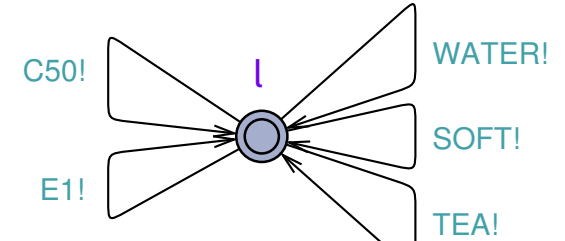
water_enabled := false,
soft_enabled := false,
tea_enabled := false



z edge:

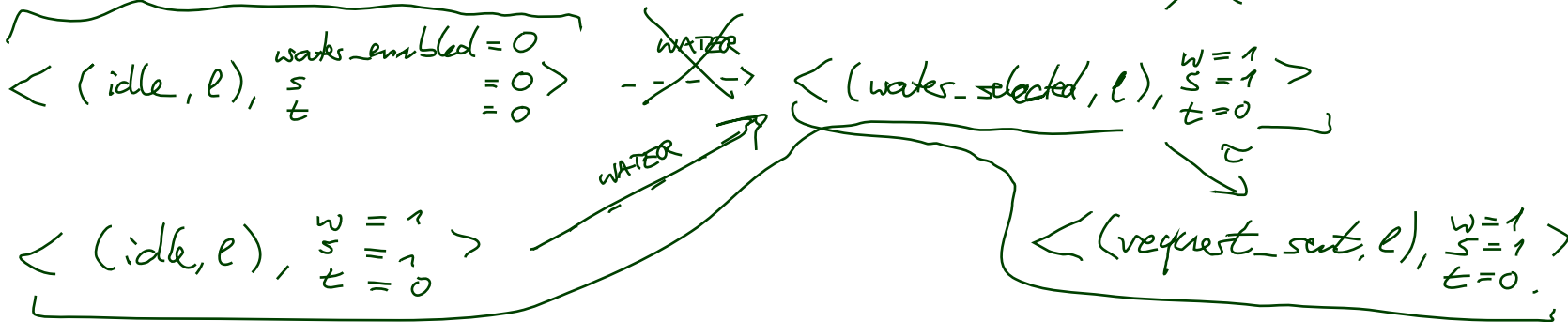


User:



$\langle (water_selected, l), w=2, s=0, t=1 \rangle$

Ciri



Transition Sequences

(starting at / from $\langle \vec{l}_0, \nu_0 \rangle$)

- A **transition sequence** of $C(\mathcal{A}_1, \dots, \mathcal{A}_n)$ is any (in)finite sequence of the form

$$\langle \vec{l}_0, \nu_0 \rangle \xrightarrow{\lambda_1} \langle \vec{l}_1, \nu_1 \rangle \xrightarrow{\lambda_2} \langle \vec{l}_2, \nu_2 \rangle \xrightarrow{\lambda_3} \dots$$

with

- $\langle \vec{l}_0, \nu_0 \rangle = C_{ini}$. (without "start / from")
- for all $i \in \mathbb{N}$, there is $\xrightarrow{\lambda_{i+1}}$ in $\mathcal{T}(C(\mathcal{A}_1, \dots, \mathcal{A}_n))$ with $\langle \vec{l}_i, \nu_i \rangle \xrightarrow{\lambda_{i+1}} \langle \vec{l}_{i+1}, \nu_{i+1} \rangle$.

Deadlock

- A **configuration** $\langle \ell, \nu \rangle$ of $\mathcal{C}(\mathcal{A}_1, \dots, \mathcal{A}_n)$ is called **deadlock** if and only if there are no transitions from $\langle \ell, \nu \rangle$, i.e. if

$$\neg(\exists \lambda \in \Lambda \overset{\text{labels}}{\exists} \langle \ell', \nu' \rangle \in \text{Conf} \bullet \langle \ell, \nu \rangle \xrightarrow{\lambda} \langle \ell', \nu' \rangle).$$

The **network** $\mathcal{C}(\mathcal{A}_1, \dots, \mathcal{A}_n)$ is said to **have a deadlock** if and only if there is a reachable configuration $\langle \ell, \nu \rangle$ which is a deadlock.

Reachability

- A **configuration** $\langle \vec{\ell}, \nu \rangle$ is called **reachable** (in $\mathcal{C}(\mathcal{A}_1, \dots, \mathcal{A}_n)$) **from** $\langle \vec{\ell}_0, \nu_0 \rangle$ if and only if there is a transition sequence of the form

$$\langle \vec{\ell}_0, \nu_0 \rangle \xrightarrow{\lambda_1} \langle \vec{\ell}_1, \nu_1 \rangle \xrightarrow{\lambda_2} \langle \vec{\ell}_2, \nu_2 \rangle \xrightarrow{\lambda_3} \dots \xrightarrow{\lambda_n} \langle \vec{\ell}_n, \nu_n \rangle = \underline{\underline{\langle \vec{\ell}, \nu \rangle}}.$$

- A **configuration** $\langle \vec{\ell}, \nu \rangle$ is called **reachable** (without “from”!) if and only if it is reachable from C_{ini} .
- A **location** $\ell \in L_i$ is called **reachable** if and only if **any** configuration $\underline{\underline{\langle \vec{\ell}, \nu \rangle}}$ with $\underline{\underline{\ell_i = \ell}}$ is reachable, i.e. there exist $\vec{\ell}$ and ν such that $\ell_i = \ell$ and $\langle \vec{\ell}, \nu \rangle$ is reachable.

Uppaal

(Larsen et al., 1997; Behrmann et al., 2004)

Tool Demo

The Uppaal Query Language

Consider $\mathcal{N} = \mathcal{C}(\mathcal{A}_1, \dots, \mathcal{A}_n)$ over data variables V .

- **basic formula:**

$$atom ::= \mathcal{A}_i.l \mid \varphi \mid \text{deadlock}$$

where $l \in L_i$ is a location and φ an expression over V .

- **configuration formulae:**

$$term ::= atom \mid \text{not } term \mid term_1 \text{ and } term_2$$

- **existential path formulae:**

$$\begin{aligned} e\text{-formula} ::= & \exists \diamond term && \text{(exists finally)} \\ & \mid \exists \square term && \text{(exists globally)} \end{aligned}$$

- **universal path formulae:**

$$\begin{aligned} a\text{-formula} ::= & \forall \diamond term && \text{(always finally)} \\ & \mid \forall \square term && \text{(always globally)} \\ & \mid term_1 \rightarrow term_2 && \text{(leads to)} \end{aligned}$$

- **formulae (or queries):**

$$F ::= e\text{-formula} \mid a\text{-formula}$$

Satisfaction of Uppaal Queries by Configurations

- The **satisfaction relation**

$$\langle \vec{l}, \nu \rangle \models F$$

between **configurations**

$$\langle \vec{l}, \nu \rangle = \langle (l_1, \dots, l_n), \nu \rangle$$

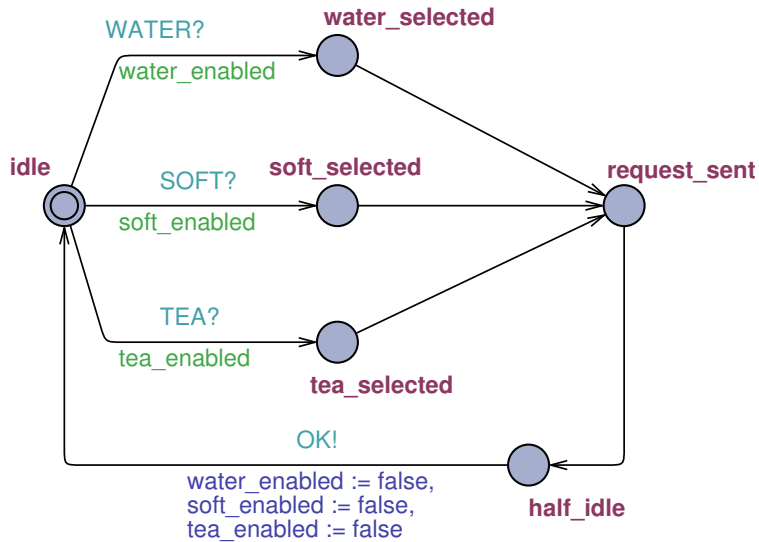
of a network $\mathcal{C}(\mathcal{A}_1, \dots, \mathcal{A}_n)$ and **formulae** F of the Uppaal logic is defined **inductively** as follows:

- $\langle \vec{l}, \nu \rangle \models \text{deadlock}$ iff $\langle \vec{l}, \nu \rangle$ is a *deadlock configuration*
- $\langle \vec{l}, \nu \rangle \models \mathcal{A}_i.l$ iff $l_0.l_i = l$
- $\langle \vec{l}, \nu \rangle \models \varphi$ iff $\nu \models \varphi$
- $\langle \vec{l}, \nu \rangle \models \text{not term}$ iff $\langle \vec{l}, \nu \rangle \not\models \text{term}$
- $\langle \vec{l}, \nu \rangle \models \text{term}_1 \text{ and } \text{term}_2$ iff $\langle \vec{l}, \nu \rangle \models \text{term}_i, \quad i = 1, 2$

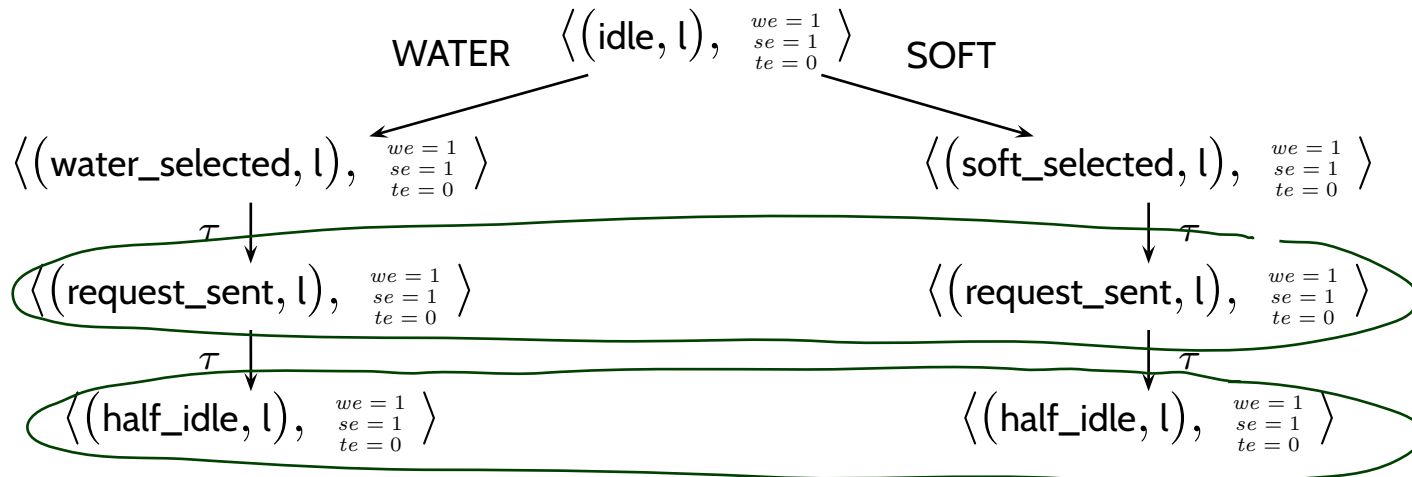
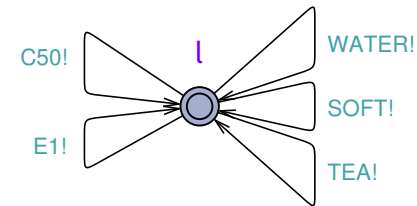
Example: Computation Paths vs. Computation Tree



ChoicePanel:



User:

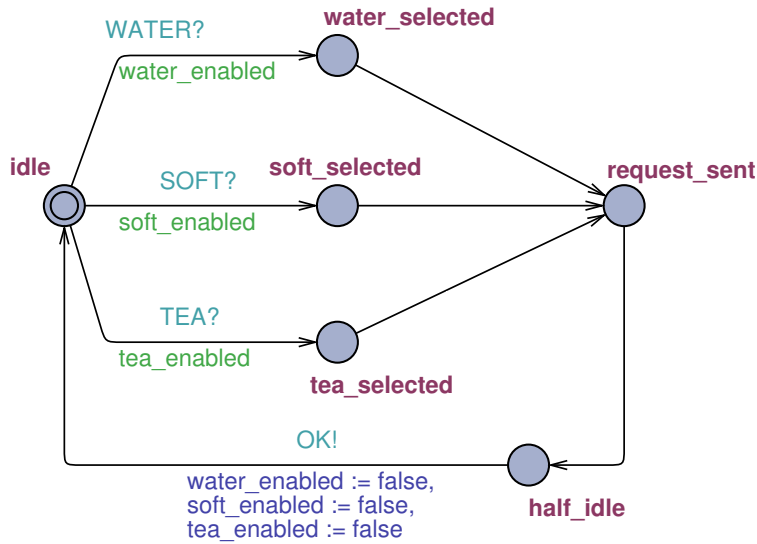


Example: Computation Paths vs. Computation Graph

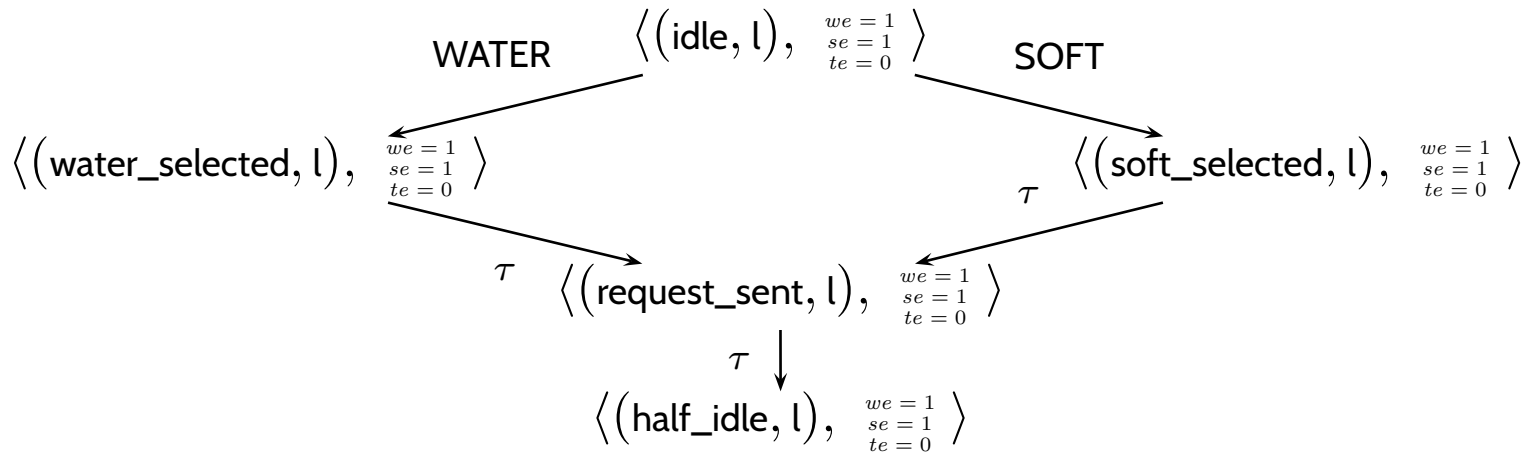
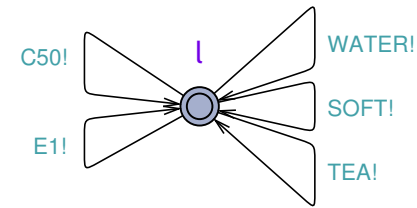
(or: Transition Graph)



ChoicePanel:



User:



Satisfaction of Uppaal Queries by Configurations

Exists finally:

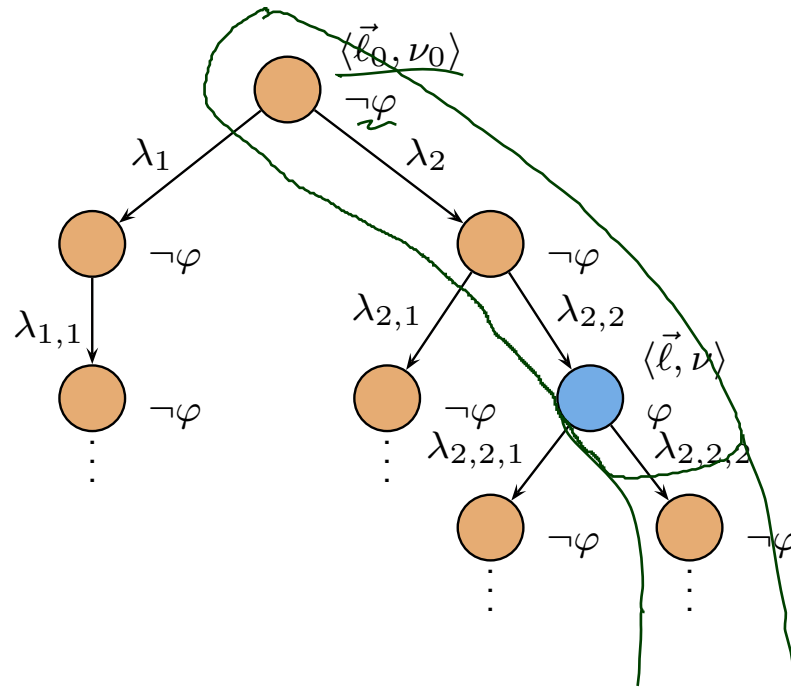
• $\langle \vec{l}_0, \nu_0 \rangle \models \exists \diamond term$

iff $\exists \text{ path } \xi \text{ of } \mathcal{N} \text{ starting in } \langle \vec{l}_0, \nu_0 \rangle$
 $\exists i \in \mathbb{N}_0 \bullet \xi^i \models term$

i-th config. in ξ

“some configuration satisfying *term* is reachable”

Example: $\langle \vec{l}_0, \nu_0 \rangle \models \exists \diamond \varphi$



Satisfaction of Uppaal Queries by Configurations

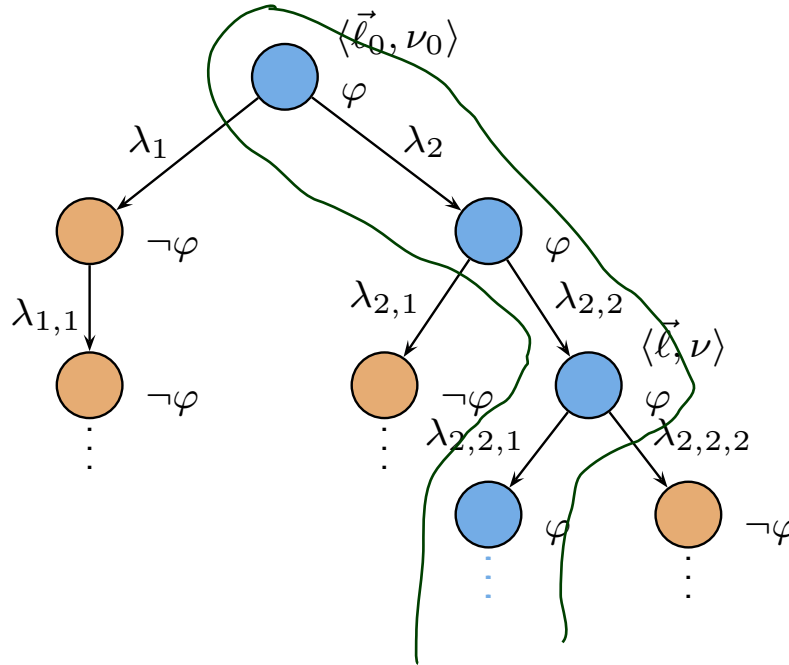
Exists globally:

- $\langle \vec{\ell}_0, \nu_0 \rangle \models \exists \square term$
iff \exists path ξ of \mathcal{N} starting in $\langle \vec{\ell}_0, \nu_0 \rangle$

 $\forall i \in \mathbb{N}_0 \bullet \xi^i \models term$

“on some computation path, all configurations satisfy *term*”

Example: $\langle \vec{\ell}_0, \nu_0 \rangle \models \exists \square \varphi$



Satisfaction of Uppaal Queries by Configurations

- **Always globally:**

- $\langle \vec{\ell}_0, \nu_0 \rangle \models \forall \square term$ iff $\langle \vec{\ell}_0, \nu_0 \rangle \not\models \exists \diamond \neg term$

“not (some configuration satisfying $\neg term$ is reachable)”
or: “all reachable configurations satisfy $term$ ”

- **Always finally:**

- $\langle \vec{\ell}_0, \nu_0 \rangle \models \forall \diamond term$ iff $\langle \vec{\ell}_0, \nu_0 \rangle \not\models \exists \square \neg term$

“not (on some computation path, all configurations satisfy $\neg term$)”
or: “on all computation paths, there is a configuration satisfying $term$ ”

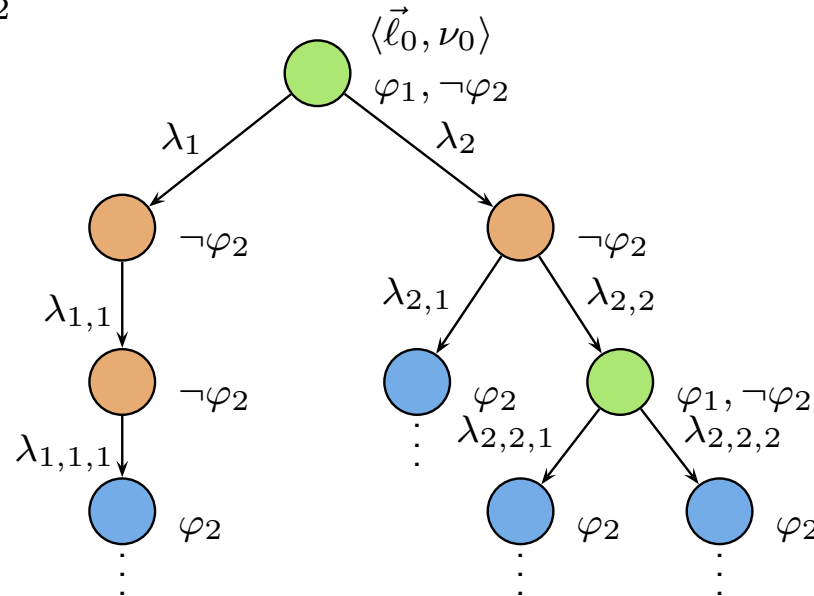
Satisfaction of Uppaal Queries by Configurations

Leads to:

- $\langle \vec{\ell}_0, \nu_0 \rangle \models term_1 \longrightarrow term_2$
iff
 $\forall \text{ path } \xi \text{ of } \mathcal{N} \text{ starting in } \langle \vec{\ell}_0, \nu_0 \rangle \forall i \in \mathbb{N}_0 \bullet$
 $\xi^i \models term_1 \implies \xi^i \models \forall \Diamond term_2$

“on all paths, from each configuration satisfying $term_1$,
 a configuration satisfying $term_2$ is reachable” (**response pattern**)

Example: $\langle \vec{\ell}_0, \nu_0 \rangle \models \varphi_1 \longrightarrow \varphi_2$



CFA Model-Checking

Definition. Let $\mathcal{N} = \mathcal{C}(\mathcal{A}_1, \dots, \mathcal{A}_n)$ be a network and F a query.

- (i) We say \mathcal{N} **satisfies** F , denoted by $\mathcal{N} \models F$, if and only if $C_{ini} \models F$.
- (ii) The **model-checking problem** for \mathcal{N} and F is to decide whether $(\mathcal{N}, F) \in \models$.

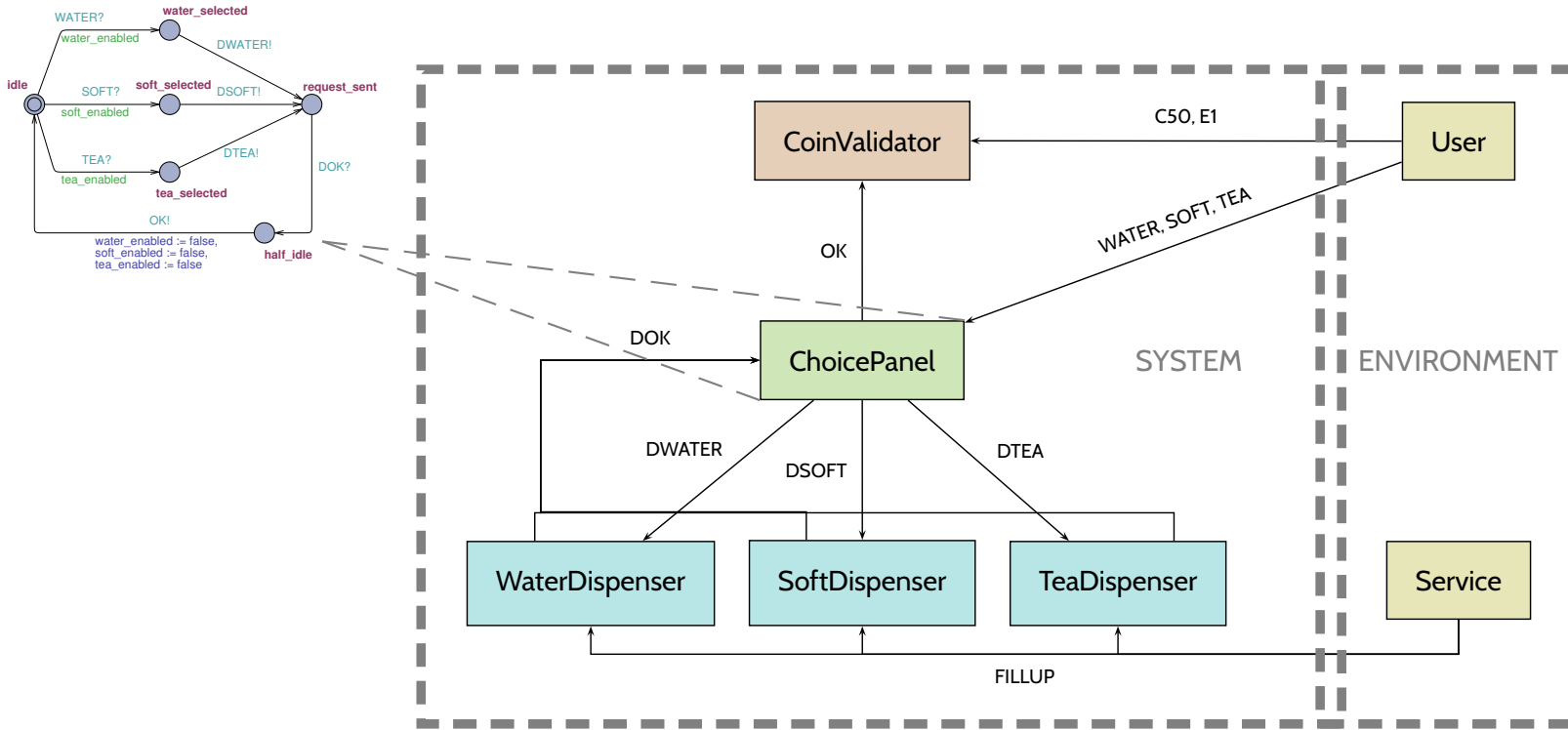
Proposition.

The model-checking problem for communicating finite automata is **decidable**.

- **Communicating Finite Automata (CFA)**
 - concrete and abstract syntax,
 - networks of CFA,
 - operational semantics.
- **Transition Sequences**
- **Deadlock, Reachability**
- **Uppaal**
 - tool demo (simulator),
 - query language,
 - CFA model-checking.
- **CFA at Work**
 - drive to configuration, scenarios, invariants
 - tool demo (verifier).
- **Uppaal Architecture**

CFA and Queries at Work

Model Architecture — Who Talks What to Whom



- **Shared variables:**

- `bool water_enabled, soft_enabled, tea_enabled;`
- `int w = 3, s = 3, t = 3;`

- **Note:** Our model does not use scopes (“information hiding”) for channels. That is, ‘Service’ could send ‘WATER’ if the modeler wanted to.

Design Sanity Check: Drive to Configuration

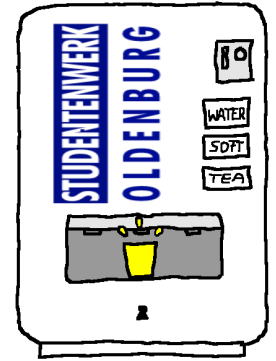
- **Question:** Is it (at all) possible to have no water in the vending machine model?
(Otherwise, the design is definitely broken.)
- **Approach:** Check whether a configuration satisfying

$$w = 0$$

is reachable, i.e. check

$$\mathcal{N}_{\text{VM}} \models \exists \diamond w = 0.$$

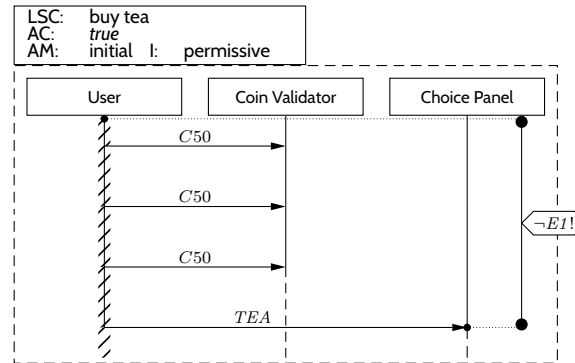
for the vending machine model \mathcal{N}_{VM} .



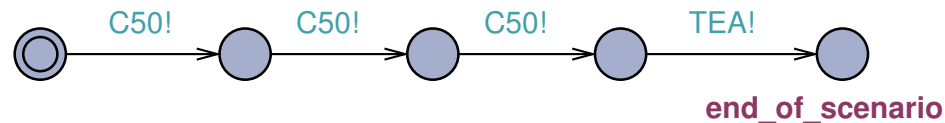
Design Check: Scenarios



- **Question:** Is the following existential LSC satisfied by the model?
(Otherwise, the design is definitely broken.)



- **Approach:** Use the following newly created CFA 'Scenario'



instead of **User** and check whether location `end_of_scenario` is reachable, i.e. check

$$\mathcal{N}'_{VM} \models \exists \diamond \text{Scenario.end_of_scenario.}$$

for the modified vending machine model \mathcal{N}'_{VM} .

Design Verification: Invariants



- **Question:** Is it the case that the “tea” button is **only** enabled if there is € 1.50 in the machine?
(Otherwise, the design is broken.)

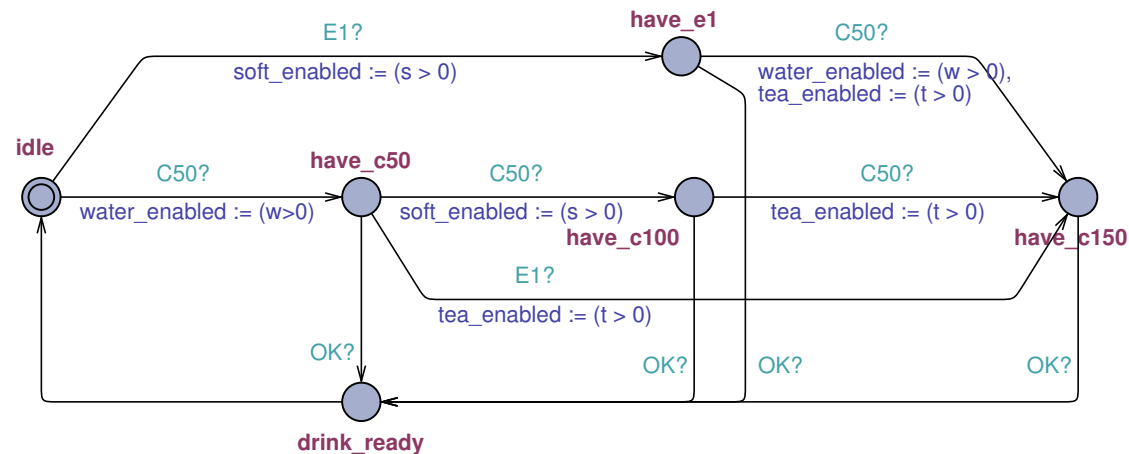
- **Approach:** Check whether the implication

$$\text{tea_enabled} \implies \text{CoinValidator.have_c150}$$

holds in all reachable configurations, i.e. check

$$\mathcal{N}_{\text{VM}} \models \forall \square \text{tea_enabled} \text{ imply } \text{CoinValidator.have_c150}$$

for the vending machine model \mathcal{N}_{VM} .



Design Verification: Sanity Check

- **Question:** Is the “tea” button **ever** enabled?
(Otherwise, the considered invariant

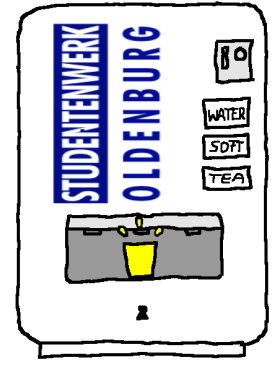
$\text{tea_enabled} \implies \text{CoinValidator.have_c150}$

holds vacuously.)

- **Approach:** Check whether a configuration satisfying $\text{water_enabled} = 1$ is reachable.
Exactly like we did with $w = 0$ earlier.



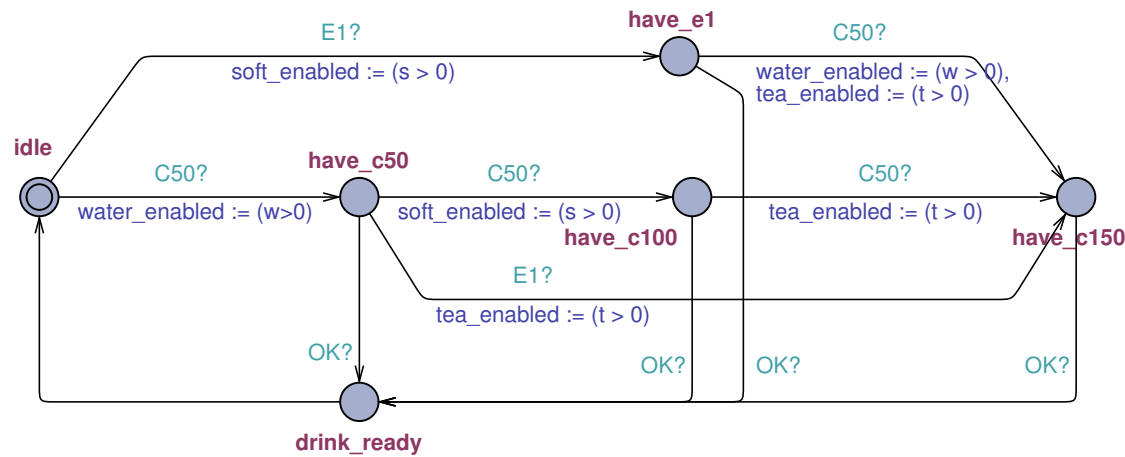
Design Verification: Another Invariant



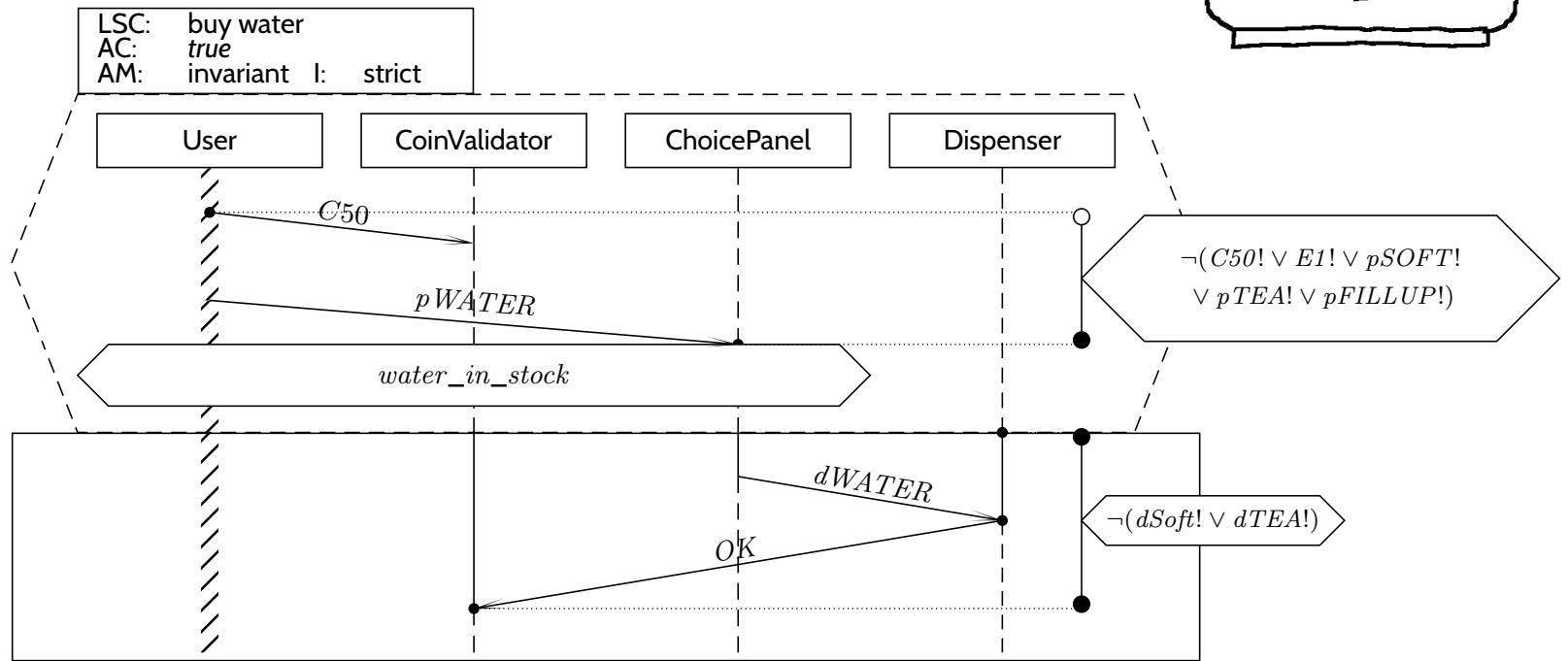
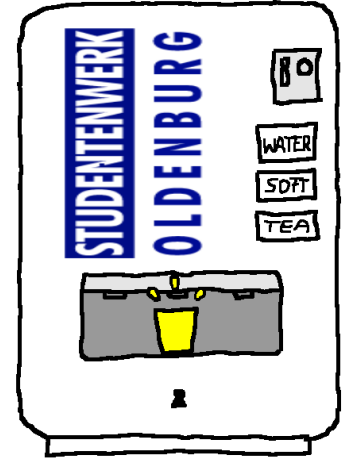
- **Question:** Is it the case that, if there is money in the machine and water in stock, that the “water” button is enabled?

- **Approach:** Check

$$\mathcal{N}_{VM} \models \forall \square (\text{CoinValidator.have_c50 or CoinValidator.have_c100 or CoinValidator.have_c150}) \text{ imply water_enabled.}$$



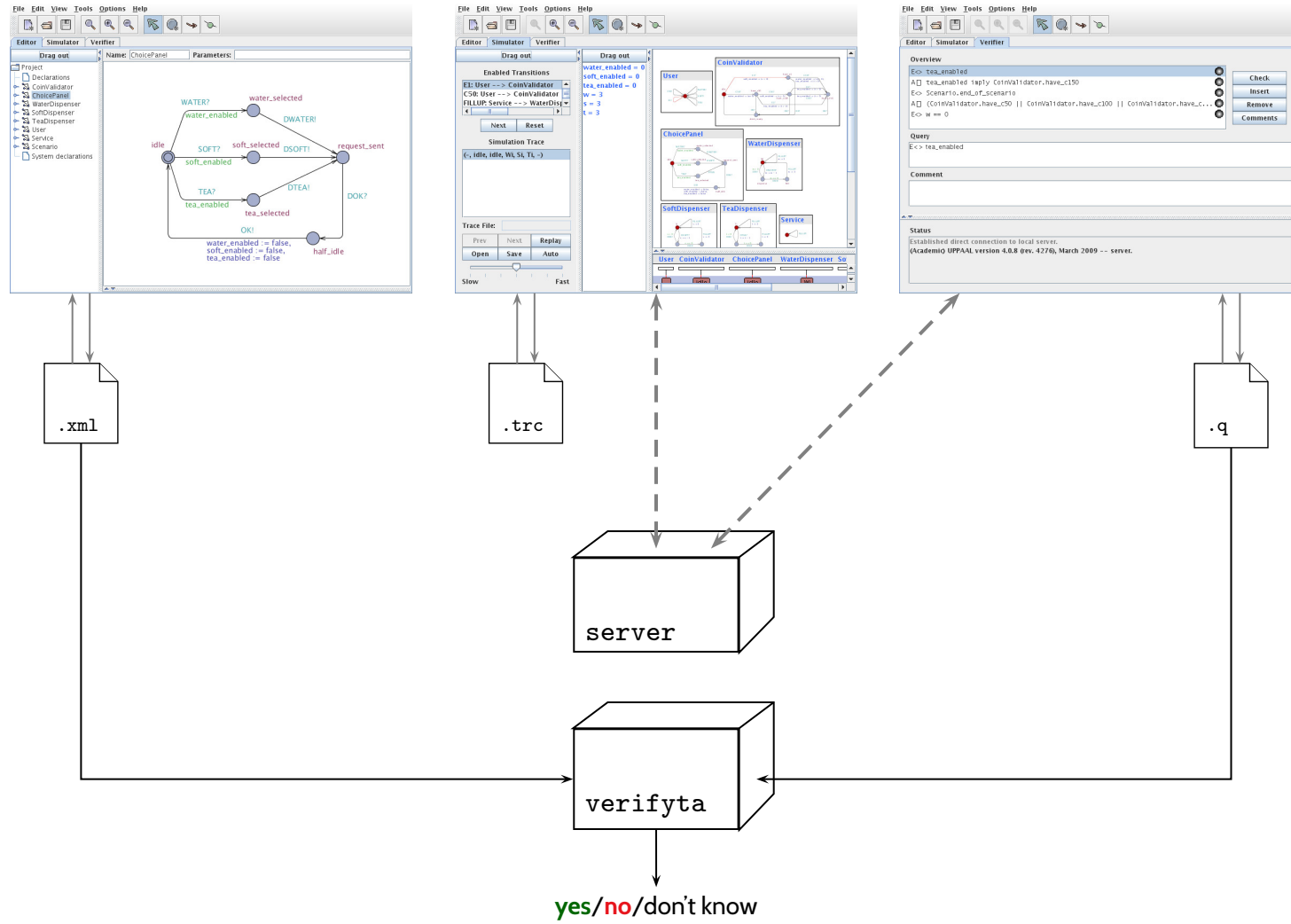
Recall: Universal LSC Example



- **Communicating Finite Automata (CFA)**
 - concrete and abstract syntax,
 - networks of CFA,
 - operational semantics.
- **Transition Sequences**
- **Deadlock, Reachability**
- **Uppaal**
 - tool demo (simulator),
 - query language,
 - CFA model-checking.
- **CFA at Work**
 - drive to configuration, scenarios, invariants
 - tool demo (verifier).
- **Uppaal Architecture**

Uppaal Architecture

Uppaal Architecture



Java

C++

Tell Them What You've Told Them. . .

- A **network of communicating finite automata**
 - describes a **labelled transition system**,
 - can be used to **model** software behaviour.
- The **Uppaal Query Language** can be used to
 - formalize **reachability** ($\exists\Diamond CF, \forall\Box CF, \dots$) and
 - **leadsto** ($CF_1 \longrightarrow CF_2$) properties.
- Since the **model-checking problem** of CFA is **decidable**,
 - there are tools which **automatically check** whether a network of CFA satisfies a given query.
- Use model-checking, e.g., to
 - **obtain a computation path** to a certain configuration (**drive-to-configuration**),
 - check whether a **scenario** is possible,
 - check whether an **invariant** is satisfied.
(If not, analyse the design further using the obtained **counter-example**).

References

References

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