

Softwaretechnik / Software-Engineering
Lecture 6: Formal Methods for
Requirements Engineering

2019-05-16

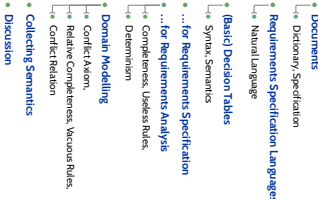
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Topic Area Requirements Engineering: Content



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Content



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Requirements Documents

Requirements Specification

specification – A document that specifies:
• in a complete, precise, verifiable manner,
the
• requirements, design behavior
or other characteristics of a system or component,
and often, the procedures for determining whether these provisions have
been satisfied. **(IEEE 60321:1990)**

software requirements specification (SRS) – Documentation of the ex-
ternal and internal requirements of a software system and its external interfaces. **(IEEE 60321:1990)**

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A hand-drawn mind map of the seven layers of the OSI model. The central node is '7 LAYERS' with a large '7' written next to it. A green line connects this central node to a green oval containing the list of layer numbers and names. From this oval, seven lines radiate outwards to seven numbered nodes, each containing a layer name. The nodes are arranged in a circular pattern around the central oval.

```

graph TD
    Center((7 LAYERS)) --- Oval([7  
1. Physical  
2. Data Link  
3. Network  
4. Transport  
5. Session  
6. Presentation  
7. Application])
    Oval --- 1[1. Physical]
    Oval --- 2[2. Data Link]
    Oval --- 3[3. Network]
    Oval --- 4[4. Transport]
    Oval --- 5[5. Session]
    Oval --- 6[6. Presentation]
    Oval --- 7[7. Application]
  
```

7 LAYERS

7
1. Physical
2. Data Link
3. Network
4. Transport
5. Session
6. Presentation
7. Application

1. Physical

2. Data Link

3. Network

4. Transport

5. Session

6. Presentation

7. Application

(Ludewig and Lichter, 2013) based on (IEEE, 1998)

Dictionary

- Requirements analysis should be based on a **dictionary**.
 - A **dictionary** comprises definitions and clarifications of **terms** that are relevant to the project. It may have different understandings before agreeing on the dictionary.
 - Each entry in the dictionary should provide the following information:
 - term and synonyms (in the world of the requirements specification),
 - meaning (definition, explanation),
 - definition (where not to use the terms),
 - attributes (in time, in space...),
 - denotation, unique identifier, ...
 - open questions not yet resolved,
 - related terms, cross references.
- Note:** entries for terms that **seemed** "crystal clear" at first sight are **not uncommon**.
- All work on requirements should, as far as possible, be done using terms from the dictionary consistently and consequently. The dictionary should be negotiated with the customer and the responsibility for it is possible, at least developers should be back to dictionary terms.
 - Note: do not mix up each world/domain term with ones of "living" in the software.

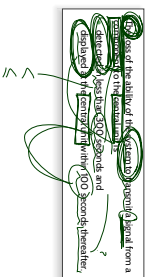
Note: entries for terms that seemed “crystal clear” at first sight are not uncommon.

- All work on requirements should, as far as possible, be done **using terms from the dictionary** consistently and consequently

and used in communication (if not possible, at least developers should stick to dictionary terms)

- **Note:** do not mix up **real-world/domain** terms with ones only “living” in the software

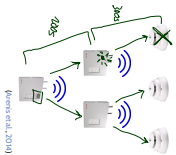
Example: Wireless Fire Alarm System



Dictionary Example

Example: Wireless Fire Alarm System

- During a project on designing a highly reliable, EN-54-75 conforming fire alarm communication protocol, we had to learn that the relevant components of a fire alarm system are:
 - terminal products (field-installed sensors and manual indications),
 - repeaters (a non-terminal product),
 - and a central unit (not a participant).
- Repeaters and central unit are technically very similar, but need to be distinguished to understand requirements. The dictionary explains these terms.



(Aueris et al., 2014)

Except from the dictionary (ca. 50 entries in total):

Part A part of a fire alarm system is either a participant or a central unit.

Repeater A repeater is a participant which accepts messages for the central unit from other participants, or messages from the central unit to other participants.

Central Unit: A central unit is a **part** which receives messages from different assigned participants, assesses the messages, and reacts, e.g. by forwarding to persons or optical/acoustic signalling devices.

Terminal Participant: A terminal participant is a **participant** which is not a **repeater**. Each terminal participant consists of **exactly one** wireless communication module and devices which provide sensor and/or signalling functionality.

Content

- Documents
 - Dictionary, Specification
- Requirements Specification Language
 - Natural Language
- (Basic) Decision Tables
 - Syntax, Semantics
- ... for Requirements Specification
- ... for Requirements Analysis
 - Completeness, Useful Rules
 - Determinism
- Domain Modelling
 - Conflict Mgmt.
 - Resolve Completeness, Vacuous Rules, Conflict Reduction
- Collecting Semantics
- Discussion



Requirements Specification Languages

Natural Language Specification (Lewin and Leherer, 2013) based

on (Rupp and the SOPHISTs, 2009)

[illegible]

Natural Language Patterns

Natural language requirements can be (tried to be) written as an instance of the pattern " $\langle A \rangle \langle B \rangle \langle C \rangle \langle D \rangle \langle E \rangle \langle F \rangle$," (German grammar) where

A	defines when and under what conditions the activity takes place
B	is WMS (obligation, SHOULD), or WILL (intention), or MAY (likelihood)
C	states the statistical or the concrete nature of a task system
D	one of a description of a system activity <ul style="list-style-type: none"> • use of description of a system activity • other: description of a function offered by the system to somebody, i.e. a task
E	usage of a function offered by a third party, under certain conditions
F	extension, in particular an object
G	the actual process word (what happens)

(Rupp and die SOPHISTen, 2009)

Example:

After office hours ($= A$), the system ($= C$) should ($= B$) offer to the operator ($= D$) a backup ($= F$) of all new registrations to an external medium ($= E$).

Other Pattern Example: RFC 2119

[illegible]

Content

- Documents
 - Dictionary Specification
- Requirements Specification Language
 - Natural language
 - (Basic) Decision Tables
 - Syntax, Semantics
 - ... for Requirements Specification
 - ... for Requirements Analysis
 - Completeness, Unused Rules, Determinism
- Domain Modelling
 - Conflict Atom
 - Relative completeness, Various Rules, Conflict Reduction
- Collecting Semantics

Discussion



Formal Methods in the Software Development Domain

Definition, Formal and Verified Proof
A method is called formal method if and only if its techniques and tools can be explained in mathematics.

Example:

If a method includes a specification language (as a tool), then that language has

- a formal syntax,
- a formal semantics, and
- a formal proof system.

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Formal, Rigorous, or Systematic Development

The techniques of a formal method help

- construct a specification, and/or
- analyse a specification, and/or
- transform (refine) one (or more) specification(s) into a program.

The techniques of a formal method, (besides the specification languages) are typically software packages that help developers use the techniques and other tools.

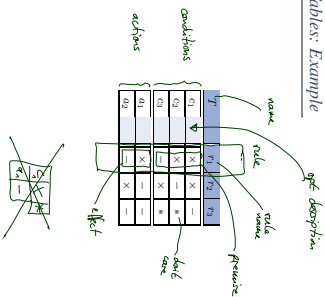
The aim of developing software, either

- formally (all arguments are formal) or
- rigorously (some arguments are made and they are formal) or
- systematically (some arguments are made on a form that can be made formal) is to (be able to) reason in a precise manner about properties of what is being developed. (Bierman and Havelund, 2014)

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Decision Tables

Decision Tables: Example



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Decision Table Syntax

- Let C be a set of conditions and A be a set of actions s.t. $C \cap A = \emptyset$.
- A decision table T over C and A is labelled $(m + k) \times n$ matrix

T: decision table		A			
		$a_1, 1$	$a_2, 1$	$a_3, 1$	$a_4, 1$
c_1	description of condition c_1	\vdots	\vdots	\vdots	\vdots
\vdots	\vdots	\vdots	\vdots	\vdots	\vdots
c_m	description of condition c_m	\vdots	\vdots	\vdots	\vdots
a_1	description of action a_1	$a_1, 1$	$a_1, 2$	$a_1, 3$	$a_1, 4$
\vdots	\vdots	\vdots	\vdots	\vdots	\vdots
a_k	description of action a_k	$a_k, 1$	$a_k, 2$	$a_k, 3$	$a_k, 4$

- where
 - $c_1, \dots, c_m \in C$, • $a_1, \dots, a_n \in A$
 - $a_1, \dots, a_n \in A$, • $a_1, \dots, a_n \in \{-, X, +\}$ and
- Columns $(c_1, \dots, c_m, c_1, w_1, \dots, w_m, a_1, 1 \leq i \leq n)$ are called rules.
- r_1, \dots, r_m are rule names.
- (c_1, \dots, c_m, a_1) is called premise of rule r_i .
- (a_1, \dots, a_n, a_1) is called effect of r_i .

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Decision Table Semantics

Each rule $r \in \{r_1, \dots, r_n\}$ of table T

T: decision table		A			
		$a_1, 1$	$a_2, 1$	$a_3, 1$	$a_4, 1$
c_1	description of condition c_1	\vdots	\vdots	\vdots	\vdots
\vdots	\vdots	\vdots	\vdots	\vdots	\vdots
c_m	description of condition c_m	\vdots	\vdots	\vdots	\vdots
a_1	description of action a_1	$a_1, 1$	$a_1, 2$	$a_1, 3$	$a_1, 4$
\vdots	\vdots	\vdots	\vdots	\vdots	\vdots
a_k	description of action a_k	$a_k, 1$	$a_k, 2$	$a_k, 3$	$a_k, 4$

is assigned to a propositional logical formula, $F(r)$ over signature $C \cup A$ as follows:

- Let (c_1, \dots, c_m) and (a_1, \dots, a_n) be premise and effect of r .
- Then

$$F(r) := \underbrace{F(c_1 \wedge \dots \wedge c_m)}_{\text{premise}} \wedge \underbrace{F(a_1 \vee \dots \vee a_n)}_{\text{effect}}$$

where

$$F(v, x) = \begin{cases} x & \text{if } v = X \\ \neg x & \text{if } v = - \\ \text{true} & \text{if } v = * \end{cases}$$

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Decision Table Semantics: Example

$$F(r) := F(r_1, r_2) \wedge \dots \wedge F(r_{n_1}, r_{n_2})$$

$$F(r, r_1) := \begin{cases} \text{true} & \text{if } r = r_1 \\ \text{false} & \text{if } r \neq r_1 \end{cases}$$

r	r_1	r_2	r_3
r_1	X	X	X
r_2	X	X	X
r_3	X	X	X
r_4	X	X	X

$$F(r) = F(r_1, r_2) \wedge F(r_3, r_4) \wedge F(r_5, r_6)$$

$$F(r_2) = \underbrace{r_1 \wedge r_2}_{\text{true}} \wedge \underbrace{r_3 \wedge r_4}_{\text{true}} \wedge \underbrace{r_5 \wedge r_6}_{\text{true}}$$

$$F(r_3) = \neg r_1 \wedge \text{true} \wedge \text{true} \wedge r_2 \wedge r_3$$

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Decision Tables as Requirements Specification

7 room ventilation				
r_1	r_2	r_3	r_4	r_5
0	0	0	0	0
1	0	0	0	0
0	1	0	0	0
1	1	0	0	0
0	0	1	0	0
1	0	1	0	0
0	0	0	1	0
1	0	0	1	0
0	0	0	0	1
1	0	0	0	1
0	1	0	0	1
1	1	0	0	1
0	1	1	0	0
1	1	1	0	0
0	1	1	1	0
1	1	1	1	0
0	0	1	1	1
1	0	1	1	1
0	1	0	1	1
1	1	0	1	1
0	1	1	1	1
1	1	1	1	1

$$F(r_1) = b \wedge \text{off} \wedge \neg \text{on} \wedge \text{gap} \wedge \neg \text{stop}$$

$$F(r_2) = b \wedge \neg \text{off} \wedge \text{on} \wedge \neg \text{gap} \wedge \text{stop}$$

$$F(r_3) = \neg b \wedge \text{true} \wedge \text{true} \wedge \neg \text{gap} \wedge \neg \text{stop}$$

- (i) Assume button pressed, ventilation off, we (only) plan to start the ventilation.
 - Corresponding valuation: $r_1 = (b \rightarrow \text{true}, \text{off} \rightarrow \text{true}, \text{on} \rightarrow \text{false}, \text{start} \rightarrow \text{true}, \text{stop} \rightarrow \text{false})$.
 - Is our intention (to start the ventilation now) **allowed** by T7? Yes! (Because $r_1 \models F(r_1)$)
- (ii) Assume button pressed, ventilation on, we (only) plan to stop the ventilation.
 - Corresponding valuation: $r_2 = (b \rightarrow \text{true}, \text{off} \rightarrow \text{false}, \text{on} \rightarrow \text{true}, \text{start} \rightarrow \text{false}, \text{stop} \rightarrow \text{true})$.
 - Is our intention (to stop the ventilation now) **allowed** by T7? Yes! (Because $r_2 \models F(r_2)$)
- (iii) Assume button not pressed, ventilation on, we (only) plan to stop the ventilation.
 - Corresponding valuation:
 - Is our intention (to stop the ventilation now) **allowed** by T7? **No**

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Yes, And?

We can use decision tables to model (describe or prescribe) the behaviour of software

Example: Ventilation system of lecture hall IOT-O-026.

7 room ventilation				
r_1	r_2	r_3	r_4	r_5
0	0	0	0	0
1	0	0	0	0
0	1	0	0	0
1	1	0	0	0
0	0	1	0	0
1	0	1	0	0
0	0	0	1	0
1	0	0	1	0
0	0	0	0	1
1	0	0	0	1
0	1	0	0	1
1	1	0	0	1
0	1	1	0	0
1	1	1	0	0
0	1	1	1	0
1	1	1	1	0
0	0	1	1	1
1	0	1	1	1
0	1	0	1	1
1	1	0	1	1
0	1	1	1	1
1	1	1	1	1

- We can observe whether button is pressed and whether room ventilation is on or off, and whether we intend to start ventilation of stop ventilation.
- We can model our observation by a boolean valuation $r : C \cup A \rightarrow B$, e.g. set

$$r(r_1) := \text{true}$$
 if button pressed now and $r(r_2) := \text{false}$, if button not pressed now.
- A valuation $r : C \cup A \rightarrow B$ can be used to assign a truth value to a propositional formula φ over $C \cup A$. As usual, we write $r \models \varphi$ if φ evaluates to true under r and $r \not\models \varphi$ otherwise.
- Rule formulae $F(r)$ are propositional formulae over $C \cup A$. Thus, given r , we have either $r \models F(r)$ or $r \not\models F(r)$.

$$\begin{matrix} 0 & 1 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 1 & 0 & 0 \end{matrix} \models F(r_1)$$

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Example

7 room ventilation				
r_1	r_2	r_3	r_4	r_5
0	0	0	0	0
1	0	0	0	0
0	1	0	0	0
1	1	0	0	0
0	0	1	0	0
1	0	1	0	0
0	0	0	1	0
1	0	0	1	0
0	0	0	0	1
1	0	0	0	1
0	1	0	0	1
1	1	0	0	1
0	1	1	0	0
1	1	1	0	0
0	1	1	1	0
1	1	1	1	0
0	0	1	1	1
1	0	1	1	1
0	1	0	1	1
1	1	0	1	1
0	1	1	1	1
1	1	1	1	1

$$F(r_1) = b \wedge \text{off} \wedge \neg \text{on} \wedge \text{gap} \wedge \neg \text{stop}$$

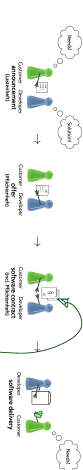
$$F(r_2) = b \wedge \neg \text{off} \wedge \text{on} \wedge \neg \text{gap} \wedge \text{stop}$$

$$F(r_3) = \neg b \wedge \text{true} \wedge \text{true} \wedge \neg \text{gap} \wedge \neg \text{stop}$$

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- (iii) Assume button not pressed, ventilation on, we (only) plan to stop the ventilation.
 - Corresponding valuation:
 - Is our intention (to stop the ventilation now) **allowed** by T7? **No**

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Decision Tables as Specification Language

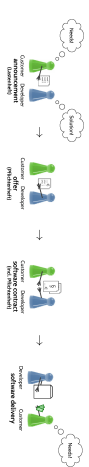


- Decision Tables can be used to **objectively** describe desired software behaviour.
- Example:** Dear developer, please provide a program such that
 - In each situation (button pressed, ventilation on/off),
 - whenever the software does (action start/stop)
 - is **allowed** by decision table T .

7 room ventilation				
r_1	r_2	r_3	r_4	r_5
0	0	0	0	0
1	0	0	0	0
0	1	0	0	0
1	1	0	0	0
0	0	1	0	0
1	0	1	0	0
0	0	0	1	0
1	0	0	1	0
0	0	0	0	1
1	0	0	0	1
0	1	0	0	1
1	1	0	0	1
0	1	1	0	0
1	1	1	0	0
0	1	1	1	0
1	1	1	1	0
0	0	1	1	1
1	0	1	1	1
0	1	0	1	1
1	1	0	1	1
0	1	1	1	1
1	1	1	1	1

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Decision Tables as Specification Language



- Decision Tables can be used to **objectively** describe desired software behaviour

- Another Example: Customer session at the bank:

T1: cash a cheque	P1	P2	else
c1 credit limit exceeded?	X	X	
c2 payment history ok?	X	—	
c3 $overdraft < \$500$ ok?	—	*	
a1 cash cheque	X	—	X
a2 do not cash cheque	—	X	—
a3 offer new conditions	X	—	—

- clerk checks database state (yields σ for c_1, \dots, c_5).
- database says: credit limit exceeded over 500 €, but payment history ok
- clerk cashes cheque but offers new conditions (according to T_1).

Decision Tables as Specification Language

Requirements on Requirements Specifications

- 1. **requirements specification** should be
 - **correct** ✓
 - correctly represents the nature/needs of the customer
 - **complete** ✓
 - all requirements (existing in context) listed as documents or ... should be present
 - **relevant** ✓
 - those are not relevant to the project should not be contained
 - **consistent** ✓
 - free of contradictions
 - **feasible** ✓
 - can be implemented with all other requirements; otherwise the requirements are **not realisable**
- 2. **Conciseness and completeness** are defined **relative**
 - to something which is usually **not** a **contract** and **completeness**
 - is a **difficult** if at all possible to be sure of **conciseness** and **completeness**
- 3. **measurable** ✓
 - a requirements specification does not contain the resolution more than necessary
- 4. **traceable** ✓
 - all requirements are well documented
- 5. **uniquely identifiable** ✓
 - requirements are uniquely identifiable
- 6. **stable** ✓
 - **stability objective**
 - **stability** ✓
 - should be checked for every 2nd requirement

Recall Once Again

Requirements on Requirements Specifications

- **Argument specification** should be
 - **concrete**
 - directly against the author/needs of the customer
 - **specific**
 - requirements leading to knowledge, belief or a document or... should be present, e.g. "the system shall be able to..."
 - things which are not relevant to the project should not be contained
 - **consider the use cases**
 - requirements which, with all other requirements, address the requirements for the system
 - **not reusable**
- **Contexts and complements** are defined **relation**
 - to something which is usually only a **contextual link**
 - **if critical** (if it is not possible to use a **context** and **complement**)
- **Relevant abstract**
 - requirements specification that not consider a relation from that necessary
- **Reusable, nonreusable**
 - **reusable**: requirements are documented requirements are implicitly derivable
 - **nonreusable**: requirements are not derivable
- **Reusable, objective**
 - **reusable, objectively** by checked for satisfying a requirement

Completeness

Definition. [completeness] A decision table T is called **complete** if and only if the disjunction of all rules' premises is a **tautology**, i.e. if

$$\models \bigvee_{r \in T} \mathcal{F}_{pre}(r).$$

Decision Tables for Requirements Analysis

- Decision tables are a formal requirements specification language for a formal language ✓
- formal syntax ✓
- formal semantics ✓
- Requirements analysts can use DTs to formally (objectively, precisely) describe their understanding of requirements. Customers may find natural or declarational DT properties like:
 - infinite completeness determination, ✓
 - inconsistency ✓
- can be used to analyse requirements, but they are not DT properties *themselves*, there can be no formal analysis tool.
- Domain modelling** formalises assumptions on the content of formal reqs. for DTs.
 - conflict situations, conflict relation.
 - Not every assumption can have serious consequences

Tell Them What You've Told Them...

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References

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