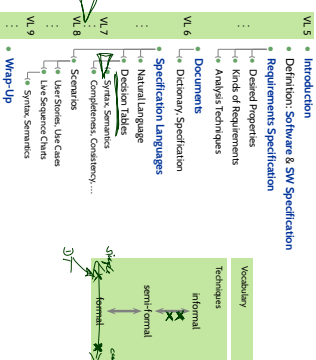
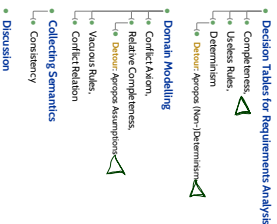


Topic Area Requirements Engineering: Content



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Content



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Recall: Decision Tables

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Decision Table Syntax

- Let C be a set of conditions and A be a set of actions s.t. $C \cap A = \emptyset$.
- A decision table T over C and A is a table of the form (C, A, n) where n is a natural number.
- where
 - $C = \{c_1, \dots, c_m\}$ is a set of conditions
 - $A = \{a_1, \dots, a_k\}$ is a set of actions
 - n is a natural number
- Columns $(c_1, \dots, c_m, a_1, \dots, a_k, 1 \leq i \leq m, 1 \leq j \leq k)$ are called cells.
- $(c_1, \dots, c_m, a_1, \dots, a_k)$ is called a rule.
- $(c_1, \dots, c_m, a_1, \dots, a_k)$ is called a rule.

T: decision table		F1		F2	
a_1	description of condition a_1	$w_{1,1}$...	$w_{1,n}$	
\vdots	\vdots	\vdots		\vdots	
a_m	description of condition a_m	$w_{m,1}$...	$w_{m,n}$	
a_1	description of action a_1	$w_{1,1}$...	$w_{1,n}$	
\vdots	\vdots	\vdots		\vdots	
a_k	description of action a_k	$w_{k,1}$...	$w_{k,n}$	
\vdots	\vdots	\vdots		\vdots	
a_l	description of action a_l	$w_{l,1}$...	$w_{l,n}$	
\vdots	\vdots	\vdots		\vdots	
a_m	description of action a_m	$w_{m,1}$...	$w_{m,n}$	

Decision Table Semantics: Example

$$F(v) := F'(v_1, c_1) \wedge \cdots \wedge F'(v_m, c_m) \\ \wedge F'(v_1, a_1) \wedge \cdots \wedge F'(v_k, a_k)$$

$$F'(v_i, x) = \begin{cases} x & \text{if } v = x \\ \neg x & \text{if } v = -x \\ \text{true} & \text{if } v = * \end{cases}$$

T	P_1	P_2	P_3
c_1	\times	\times	$-$
c_2	\times	$-$	$*$
c_3	$-$	\times	$*$
a_1	\times	$-$	$-$
a_2	$-$	\times	$-$

$$\bullet \mathcal{F}(n) = \overbrace{\bar{f}(x_1, c_1), \bar{f}(x_1, c_2), \bar{f}(-c_3), \bar{f}(y_{k+1}), \bar{f}(-d_2)}^{c_1 \wedge c_2 \wedge y_{k_3} \wedge a_1 \wedge d_2}$$

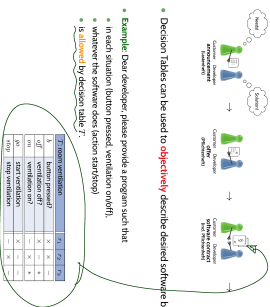
- $F(\tau_2) = c_1 \wedge \tau_2 \wedge c_3 \wedge \tau_4 \wedge a_2$

- $\mathcal{F}(\tau_3) = \neg \tau_1 \wedge \neg \tau_2 \wedge \tau_3 \wedge \neg \tau_4 \wedge \neg \tau_5$

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Decision Tables as Specification Language



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Decision Tables for Requirements Analysis

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Once Again...

Requirements on Requirements Specifications

- [illegible]

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Completeness

Definition. [Completeness] A decision table \mathcal{T} is called **complete** if and only if the disjunction of all rules' premises is a **tautology**, i.e. if

$$\models \bigvee_{r \in T} \mathcal{F}_{pm}(r).$$



Completeness: Example

T : room ventilation		r_1	r_2	r_3
b	button pressed?	x	x	x
off	ventilation off?	x	x	x
on	ventilation on?	x	x	x
$stop$	start ventilation	x	x	x
$stop$	stop ventilation	x	x	x

Is T complete?
 No! $b \wedge r_1, off \wedge r_2, on \wedge r_3$

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Completeness: Example

T : room ventilation		r_1	r_2	r_3
b	button pressed?	x	x	x
off	ventilation off?	x	x	x
on	ventilation on?	x	x	x
$stop$	start ventilation	x	x	x
$stop$	stop ventilation	x	x	x

Is T complete?
 No. Because there is no rule for, e.g. the case $\sigma(b) = \text{true}, \sigma(r_1) = \text{false}, \sigma(off) = \text{false}$.

Recall:

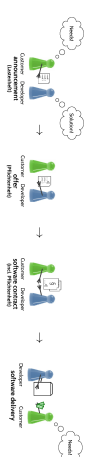
$$\begin{aligned} \mathcal{F}_T(r_1) &= e_1 \wedge e_2 \wedge \neg e_3 \wedge e_4 \wedge \neg e_5 \\ \mathcal{F}_T(r_2) &= e_1 \wedge \neg e_2 \wedge e_3 \wedge \neg e_4 \wedge e_5 \\ \mathcal{F}_T(r_3) &= \neg e_1 \wedge \text{true} \wedge \neg e_3 \wedge \neg e_4 \end{aligned}$$

$$\mathcal{F}_{\text{pre}}(r_1) \vee \mathcal{F}_{\text{pre}}(r_2) \vee \mathcal{F}_{\text{pre}}(r_3)$$

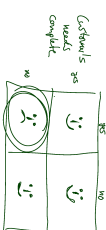
is not a tautology.
 $= (e_1 \wedge e_2 \wedge \neg e_3) \vee (e_1 \wedge \neg e_2 \wedge e_3) \vee (\neg e_1 \wedge \text{true} \wedge \text{true})$

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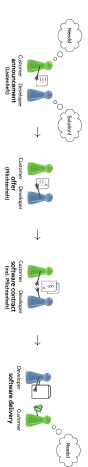
Requirements Analysis with Decision Tables



Assume we have formalised requirements as decision table T .



Requirements Analysis with Decision Tables



- Assume we have formalised requirements as decision table T .
- If T is (formally) incomplete,
 - then there is probably a case not yet discussed with the customer, or some misunderstanding.
- If T is (formally) complete,
 - then there still may be misunderstandings.
 - if there are no misunderstandings, then we did discuss all cases.
- Note:
 - Whether T is (formally) complete is **decidable**.
 - Deciding whether T is complete reduces to plain SAT.
 - There are efficient tools which decide SAT.
 - In addition, decision tables are often much easier to understand than natural language text.

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For Convenience: The 'else' Rule

Syntax:

T : Decision table		r_1	r_2	r_3	else
e_1	description of condition e_1	$True$	$True$	$True$	
\vdots	\vdots	\vdots	\vdots	\vdots	
e_n	description of condition e_n	$True$	$True$	$True$	
$else$	description of action e_{n+1}	$True$	$True$	$True$	

Semantics:

$$\mathcal{F}_T(\text{else}) := \neg \left(\bigvee_{e \in T} (\text{true}) \mathcal{F}_{\text{pre}}(e) \right) \wedge \mathcal{F}(e_{n+1}, e_{n+1}) \wedge \dots \wedge \mathcal{F}(e_{n+1}, e_{n+1})$$

Proposition: If decision table T has an 'else'-rule, then T is complete.

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Uselessness

Definition. (Uselessness) Let T be a decision table.
 A rule $r \in T$ is called **useless** (or **redundant**) if and only if there is another (different) rule $r' \in T$

- whose premises is implied by the one of r and
- whose effects is the same as r 's.

 i.e. if

$$\exists r' \neq r \in T \bullet \models (\mathcal{F}_{\text{pre}}(r) \implies \mathcal{F}_{\text{pre}}(r')) \wedge (\mathcal{F}_{\text{eff}}(r) \iff \mathcal{F}_{\text{eff}}(r')).$$
 r is called **subsumed** by r' .

Again, uselessness is **decidable**, reduces to SAT.

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Uselessness: Example

T: room ventilation		r ₁	r ₂	r ₃	r ₄
b ₁	button pressed?	x	x	x	—
off	ventilation off?	x	—	x	—
on	ventilation on?	—	x	—	—
stop	start ventilation	x	—	—	—
stop	stop ventilation	—	x	—	—

- Rule r₁ is **subsumed** by r₃.
- Rule r₂ is **not** subsumed by r₄.

- Useless rules "do not hurt" as such.
- Yet useless rules should be removed to make the table more readable, yielding an **easier usable** specification.

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Useless

Requirements on Requirements Specification Documents

The **representation** and **form** of a requirements specification should be:

- **clearly understandable**: Requirements should be stated in a way that is understandable by all affected parties. Should be able to read and interpret the requirements specification.
- **easily maintainable**: Requirements should be stated in a way that allows for easy modification and deletion of requirements.
- **testable**: Requirements should be stated in a way that allows for the requirements to be tested.

Note: Once again, to avoid over-engineering, a very precise **definition** requirements specification may not be easily understandable by every affected person.

- **Rule r₁**:
It is not enough to state that a requirement affects and how access effect, a requirements specification document is much more often **read** than **checked** or **written** (and thus the get requirements table is **handwritten**).

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- Useless rules "do not hurt" as such.
- Yet useless rules should be removed to make the table more readable, yielding an **easier usable** specification.

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Determinism: Example

T: room ventilation		r ₁	r ₂	r ₃	r ₄
b ₁	button pressed?	x	x	—	—
off	ventilation off?	x	—	x	—
on	ventilation on?	—	x	—	—
stop	start ventilation	x	—	—	—
stop	stop ventilation	—	x	—	—

- Is T **deterministic**? Yes.
- $\exists r \in R$ s.t. $r \wedge \neg r$ (s.t.)

1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36	37	38	39	40	41	42	43	44	45	46	47	48	49	50	51	52	53	54	55	56	57	58	59	60	61	62	63	64	65	66	67	68	69	70	71	72	73	74	75	76	77	78	79	80	81	82	83	84	85	86	87	88	89	90	91	92	93	94	95	96	97	98	99	100
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Determinism: Another Example

T _{door} : door ventilation		r ₁	r ₂	r ₃	r ₄
b ₁	button pressed?	x	x	—	—
off	start ventilation	—	x	—	—
stop	stop ventilation	x	—	—	—

- Is T_{door} **deterministic**? No. $b \rightarrow \neg b$.
- By the way...
- Is non-determinism a **bad thing** in general?
- **Just the opposite**: non-determinism is a very, very powerful **modelling tool**.
- Read table T_{door} as:
 - the button may switch the ventilation on
 - under certain conditions (which will specify later) and
 - under certain conditions (which will specify later)
- We in particular state that we do not (under any condition) want to see on and off executed together, and that we do not (under any condition) see go or stop without button pressed.
- On the other hand: non-determinism may not be intended by the customer.

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Determinism

Definition (Determinism)
A decision table T is called **deterministic** if and only if the premises of all rules are **pairwise disjoint**. I.e. if

$$\forall r_1 \neq r_2 \in T \bullet \neg (r_{pre}(r_1) \wedge r_{pre}(r_2)).$$

Otherwise, T is called **non-deterministic**.

- And again: determinism is **decidable**: reduces to SAT

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Content

- Decision Tables for Requirements Analysis
 - Completeness.
 - Useless Rules.
 - Determinism
 - **Domain Modelling**
 - Conflict-Avoidance.
 - Relative Completeness.
 - **Domain**: Assumptions
 - Vacuous Rules.
 - Conflict-Relation
 - Collecting Semantics
 - Consistency
 - Discussion

Logic

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Domain Modelling

Example:

Topon ventilation		on	off	on	off
on	on	+	+	+	+
off	on	+	+	+	+
on	off	+	+	+	+
off	off	+	+	+	+

- If *on* and *off* model opposite output values of one and the same sensor for "room ventilation on/off", then $\varphi \models \text{on} \wedge \text{off}$ and $\varphi \models \neg \text{on} \wedge \neg \text{off}$ never happen in reality for any observation σ .
- Decision table *T* is complete for exactly these cases.
- *T* does not know that *on* and *off* can be opposites in the real world.
- We should be able to tell *T* that *on* and *off* are opposites (if they are). Then *T* would be **relative complete** (relative to the domain knowledge that *on/off* are opposites).
- Bottom-line:**
 - Conditions and actions are **abstract entities** without inherent connection to the **real world**.
 - When modelling **real world aspects** by conditions and actions, we may also want to represent **relations between actions/conditions** in the real world (\rightarrow **domain model** (Bennett, 2008)).

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Domain Modelling for Decision Tables

Relative Completeness

Definition. [Completeness wrt. Conflict Axiom]
A decision table *T* is called **complete** wrt. **conflict axiom** φ_{conf} if and only if the disjunction of all rules' premises and the conflict axiom is a **tautology**, i.e. if

$$\models \varphi_{conf} \vee \bigvee_{r \in T} \mathcal{F}_{pre}(r).$$

- **Intuition:** a relative complete decision table explicitly cares for all cases which may happen.
- **Note:** with $\varphi_{conf} = \text{false}$, we obtain the previous definitions as a special case.
- **Its intuition:** $\varphi_{conf} = \text{false}$ means we don't exclude any states from consideration.

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Conflict Axioms for Domain Modelling

- A **conflict axiom** over conditions *C* is a propositional formula φ_{conf} over *C*.
- **Intuition:** a conflict axiom characterises all those cases, i.e. all those combinations of condition values which cannot happen – **according to our understanding of the domain**.
- **Note:** the decision table semantics remains unchanged!

Example:

- Let $\varphi_{conf} = (\text{on} \wedge \text{off}) \vee (\neg \text{on} \wedge \neg \text{off})$.
- φ_{conf} models an opposite of *off*, neither can both be satisfied nor both non-satisfied at a time!
- **Notation:**

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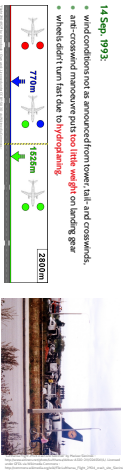
Topon ventilation		on	off	on	off
on	on	+	+	+	+
off	on	+	+	+	+
on	off	+	+	+	+
off	off	+	+	+	+

Pitfalls in Domain Modelling (Wikipedia, 2019)

- Airbus A320-300 overran runway at Warsaw Chopin Int. Airport on 14 Sep. 1993.
- To stop a plane after touchdown, there are spoilers and thrust reversers systems.
- Enabling one of those while in the act can have **fatal consequences**.
- Design decision: the software should block activation of spoilers or thrust req. **while in the act**.
- Simplified decision table of blocking procedure:

Spoilers requested		on	off	on	off
on	on	+	+	+	+
off	on	+	+	+	+
on	off	+	+	+	+
off	off	+	+	+	+

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Definition (Usably wrt Conflict Axiom)
A rule $r \in T$ is called **vacuous wrt. conflict axiom** φ_{conf} if and only if the premise of r implies the conflict axiom, i.e. if $\models \mathcal{F}_m(r) \rightarrow \varphi_{\text{conf}}$.

- Intuition: a vacuous rule would only be enabled in states which cannot happen

Example

Decision Table		$\mathcal{F}_m(r)$			
Requirements		a_1	a_2	a_3	a_4
$\neg \text{stop}$	enabled	-	-	-	-
$\neg \text{vacillation}$	g_1	-	-	-	-
$\neg \text{vacillation}$	g_2	-	-	-	-
$\neg \text{stop}$	stop	-	-	-	-
$\neg \text{stop}$	stop	-	-	-	-
$\neg (\text{vac} \wedge \neg \varphi_{\text{conf}}) \wedge (\text{vac} \wedge \varphi_{\text{conf}})$		-	-	-	-

- Vacuity wrt. φ_{conf} :** Like usefulness, vacuity doesn't hurt as such but
- May hint on inconsistencies on customer's side. (Misunderstanding with conflict axiom)
- Makes using the table less easy! (Due to more rules)
- Implementing vacuous rules is a waste of effort

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 - Detector: Always Non-Determinism
- Domain Modelling
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 - Relative Completeness.
 - Detector: Always Assumptions
 - Vacuous Rules.
 - Conflict Reduction
- Collecting Semantics
 - Consistency
- Discussion



Definition (Conflict Relation) A conflict relation on actions A is a **transitive and symmetric** relation $\subseteq (A \times A)$.



Definition (Consistency) Let r be a rule of decision table T over C and A .
(i) Rule r is called **consistent** with **conflict relation** \sharp if and only if there are no conflicting actions in its effect, i.e. if $\models \mathcal{F}_m(r) \rightarrow \bigwedge_{(a_1, a_2) \in \sharp} \neg (a_1 \wedge a_2)$.

(ii) T is called **consistent with \sharp** iff all rules $r \in T$ are consistent with \sharp .

- Again, consistency is **decidable** reduces to SAT

T over actions vacillation		$\mathcal{F}_m(r)$			
Requirements		a_1	a_2	a_3	a_4
$\neg \text{stop}$	enabled	-	-	-	-
$\neg \text{vacillation}$	g_1	-	-	-	-
$\neg \text{vacillation}$	g_2	-	-	-	-
$\neg \text{stop}$	stop	-	-	-	-
$\neg \text{stop}$	stop	-	-	-	-
$\neg (\text{vac} \wedge \neg \varphi_{\text{conf}}) \wedge (\text{vac} \wedge \varphi_{\text{conf}})$		-	-	-	-

Let \sharp be the transitive symmetric closure of $\{(stop, g_1)\}$.
Actions $stop$ and g_1 are not supposed to be executed at the same time.
Then rule r is inconsistent with \sharp .



- A decision table with **inconsistent rules** **may do harm to operation!**
- Detecting an inconsistency** only late during a project can incur significant cost
- Inconsistencies** – in particular in (multiple) decision tables, created and edited by multiple people, as well as in requirements in general – are **not always as obvious** as in the toy examples given here!
- And is even less obvious with the **collecting semantics** (\rightarrow in a minute).

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Collecting Semantics

- Let T be a decision table over C and A and σ be a model of an observation of C and A . Then
$$F_{col}(T) := \bigwedge_{a \in A} \bigvee_{c \in C} c(a) \Rightarrow \mathcal{F}_T(c)$$
is called the collecting semantics of T .
- We say σ is allowed by T in the collecting semantics if and only if $\sigma \models F_{col}(T)$. That is, if exactly all actions of all enabled rules are pairwise executed.

Example:

Action verification					Decision table				
button pressed?	no	yes	no	yes	button pressed?	no	yes	no	yes
wait 100ms	no	no	no	no	wait 100ms	no	no	no	no
wait 100ms	no	no	no	no	wait 100ms	no	no	no	no
wait 100ms	no	no	no	no	wait 100ms	no	no	no	no
wait 100ms	no	no	no	no	wait 100ms	no	no	no	no
wait 100ms	no	no	no	no	wait 100ms	no	no	no	no
wait 100ms	no	no	no	no	wait 100ms	no	no	no	no
wait 100ms	no	no	no	no	wait 100ms	no	no	no	no
wait 100ms	no	no	no	no	wait 100ms	no	no	no	no
wait 100ms	no	no	no	no	wait 100ms	no	no	no	no

- "Whenever the button is pressed, let it blink (in addition to go/stop action)"

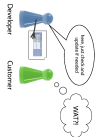
Consistency in the Collecting Semantics

Definition: (Consistency in the Collecting Semantics)
Decision table T is called **consistent with conflict relation \mathcal{I} in the collecting semantics** (under conflict axiom \mathcal{F}_{conf}) if and only if there are no conflicting actions in the effect of jointly enabled transitions, i.e. if
$$\models F_{col}(T) \wedge \neg \mathcal{F}_{conf} \rightarrow \bigwedge_{a_1, a_2 \in \mathcal{A}} \neg (a_1 \wedge a_2).$$

A Collecting Semantics for Decision Tables

Speaking of Formal Methods

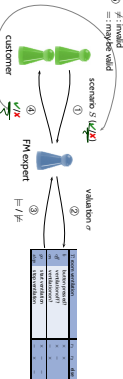
Es ist aussschlo, den Klienten mit formalen Darstellungen zu kommunizieren. [...] (It is futile to approach clients with formal representations) (Ludwig and Lehm, 2013)



- ... of course it is – the vast majority of customers is not trained in formal methods.
- A formalisation is (first of all) for developers – analysts have to translate for customers.
- A formalisation is the description of the analyst's understanding, in a most precise form. Precise/objective: whenever reads it whenever it whenever, the meaning will not change.

Formalisation Validation

- Two broad directions: • Option 1: teach formalism (usually not economic) • Option 2: serve as translator / mediator.



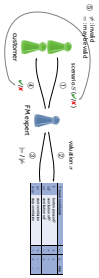
- domain experts tell system scenario S (maybe keep back, whether allowed / forbidden).
- FM expert translates system scenario to validation σ .
- FM expert evaluates DT on σ .
- FM expert translates outcome to "allowed" / "forbidden" by DT.
- compare expected outcome and real outcome

Discussion

Formalisation Validation

Two broad directions:

- Option 1: teach formalism (usually not economical)
- Option 2: serve as translator / mediator



- ① domain experts tell system scenario S (maybe keep track whether allowed / forbidden)
- ② PM expert translates system scenario to validation π .
- ③ PM expert evaluates DT on π .
- ④ PM expert translates outcome to "allowed / forbidden by DT".
- ⑤ compare expected outcome and real outcome.

Recommendation: (Corné's Method)

- use formal methods for the **most important** requirements (formalising all requirements is not always a good idea)
- use the **most appropriate** formalism for a given task.
- use formalisms you **can know** (really) well

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References

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