

J. Hoenicke J. Christ 05.02.2013 Hand in solutions via email to christj@informatik.uni-freiburg.de until 12.02.2013 (only Java sources, KeY proofs, and PDFs accepted). Paper submissions possible after the lecture.

## Tutorials for "Formal methods for Java" Exercise sheet 13

Note: The webstart version of KeY contains some GUI bugs when using Java 7. A working version can be downloaded from http://www.key-project.org/download/releases/key165rc/KeY-1.6.5\_cf8990d4ec6fef2d0a49662adb3ec509e023a0c3.tgz. A webstart for this version is available from http://www.key-project.org/download/releases/key165rc/webstart/KeY.jnlp. Please use this version for all exercises on this sheet.

## Exercise 1: Insertion Sort

On the webpage of the lecture you find a version of Insertion Sort that is fully annotated. Set the proof search strategy of KeY to

- Goal Chooser: "Default"
- Logical splitting: "Off"
- Loop treatment: "Invariant"
- Method treatment: "Expand"
- Quantifier treatment: "None"

This proof search strategy does not succeed to automatically prove total correctness even though the annotations are sufficient. Instead, this strategy leads to five goals.

- (a) Give a description of the different loop invariants in prose. Instead of i use "the outer iterator", and instead of j use "the inner iterator". For example, the invariant i >= 1 && i <= arr.length can be described as "The outer iterator is always between 1 and the length of the array."</li>
- (b) Explain the goals, i.e., what is to be proven in each case. Since KeY is deterministic at this part you may enumerate the remaining goals.
- (c) Use your knowledge from the previous exercise to prove the remaining goals.

## Exercise 2: Insertion Sort for Empty Arrays

In the previous exercise we forced to array to be non-empty by adding the pre-condition arr.length > 0. If we remove this pre-condition the proof gets slightly more complicated.

- (a) Identify the problems that might occur with empty arrays.
- (b) How can we elegantly fix these problems with KeY without modifying the code or the annotations of the class. Of course, we remove the pre-condition arr.length > 0.