

J. Hoenicke J. Christ 15.01.2013 Hand in solutions via email to christj@informatik.uni-freiburg.de until 22.01.2013 (only Java sources and PDFs accepted). Paper submissions possible after the lecture.

## Tutorials for "Formal methods for Java" Exercise sheet 10

## **Exercise 1: Jahob Integrated Proof Language** Consider the following class:<sup>1</sup> class Ex11 { /\*: public qhost specvar P :: "obj => bool"; public ghost specuar Q :: "obj => bool"; \*/ public static void test() /\*: requires "ALL x. $P x \longrightarrow Q x$ " ensures "ALL u v. P u $\mathcal{C}$ v=u --> Q v" \*/ { { //: pickAny u::obj, v::obj suchThat cond: "P u & v=u"; //: noteThat p1: "P v" from cond; //: noteThat p2: "Q v" from Precondition forSuch u, v; } } }

- (a) Which formula does this class try to prove?
- (b) Explain why the proof does not succeed.
- (c) Fix the proof.

<sup>&</sup>lt;sup>1</sup>This is a slightly modified version of a test class that comes with the Jahob distribution.

## **Exercise 2: Logical operators**

From the logical operators false,  $\rightarrow$  and  $\forall$ , all other logical operators are definable. For example  $\neg F$  can be defined as  $\neg F := F \rightarrow$  false. Find formulas defining

- (a)  $\neg F$
- (b) true,
- (c)  $F \lor G$
- (d)  $F \wedge G$
- (e)  $\exists x F$

in terms of false,  $\rightarrow$  and  $\forall$ . Prove the validity of these definitions in sequent calculus, e.g.  $\neg F \Longrightarrow F \rightarrow \mathsf{false}$  and  $F \rightarrow \mathsf{false} \Longrightarrow \neg F$ .