# Software Design, Modelling and Analysis in UML Lecture 12: Core State Machines III

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#### Contents & Goals

#### Last Lecture:

- The basic causality model
- Ether

#### **This Lecture:**

- Educational Objectives: Capabilities for following tasks/questions.
  - What does this State Machine mean? What happens if I inject this event?
  - Can you please model the following behaviour.
  - What is: Signal, Event, Ether, Transformer, Step, RTC.

#### • Content:

- System Configuration, Transformer
- Examples for transformer
- Run-to-completion Step
- Putting It All Together

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## Roadmap: Chronologically

- (i) What do we (have to) cover? UML State Machine Diagrams Syntax.
- (ii) Def.: Signature with signals.
- (iii) Def.: Core state machine.
- $\varphi \in \mathsf{OCL}$  $\mathcal{CD}, \mathcal{SD}$ CD, SM (iv) Map UML State Machine Diagrams /to core state machines.  $\mathcal{T}, \mathcal{C}, V, atr), SM$  $\mathcal{S}, SD$

 $(\Sigma^{\mathscr{D}})$ 

SM

UML

exp

 $(\sigma_1, \varepsilon_1)$ 

OD

 $(Snd_0)$ 

G= (N, E, f)

#### Semantics:

- The Basic Causality Model
- ✓ (v) Def.: Ether (aka. event pool)
- $\checkmark$ (vi) Def.: System configuration.
- (vii) Def.: Event.

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- (viii) Def.: Transformer.
- (ix) Def.: Transition system, computation.
- (x) Transition relation induced by core state machine.
- (xi) Def.: step, run-to-completion step.
- (xii) Later: Hierarchical state machines.

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 $_{SD}, F_{SD})$ 

 $((\sigma_i, cons_i, Snd_i))_{i \in \mathbb{N}}$ 

Mathematics

 $(Q_{SD}, q_0, A_s)$ 

UML

System Configuration, Ether, Transformer



### *Ether and [OMG, 2007b]*

The standard distinguishes (among others)

• SignalEvent [OMG, 2007b, 450] and Reception [OMG, 2007b, 447].

"receiption talks place", More caneptaul; for us: discard Ichisputch for us: even l On SignalEvents, it says A signal event represents the receipt of an asynchronous signal instance. A signal event may, for example, cause a state machine to trigger a transition. [OMG, 2007b, 449] = mersager [...]

Semantic Variation Points

The means by which requests are transported to their target depend on the type of requesting action, the target, the properties of the communication medium, and numerous other factors.

In some cases, this is instantaneous and completely reliable while in others it may involve  $\ensuremath{\mathsf{Transmission}}$  delays, of variable duration, loss of requests, reordering, or duplication.

(See also the discussion on page 421.) [OMG, 2007b, 450]

Our ether is a general representation of the possible choices.

Often seen minimal requirement: order of sending by one object is preserved. But: we'll later briefly discuss "discarding" of events. 8/60

#### System Configuration





- We start with some signature with signals  $\mathscr{S}_0 = (\mathscr{T}_0, \mathscr{C}_0, V_0, atr_0, \mathscr{E}).$
- A system configuration is a pair (σ, ε) which comprises a system state σ wrt. S (not wrt. S<sub>0</sub>).
- Such a system state  $\sigma$  wrt.  $\mathscr{S}$  provides, for each object  $u \in dom(\sigma)$ ,
  - values for the explicit attributes in  $V_0$ ,
  - values for a number of implicit attributes, namely
    - a stability flag, i.e.  $\sigma(u)(stable)$  is a boolean value,
    - a current (state machine) state, i.e.  $\sigma(u)(st)$  denotes one of the states of core state machine  $M_C$ ,
    - a temporary association to access event parameters for each class, i.e.  $\sigma(u)(params_E)$  is defined for each  $E \in \mathscr{E}$ .
- For convenience require: there is no link to an event except for  $params_E$ .

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#### Stability

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**Definition.** Let  $(\sigma, \varepsilon)$  be a system configuration over some  $\mathscr{S}_0$ ,  $\mathscr{D}_0$ , *Eth.* We call an object  $u \in \operatorname{dom}(\sigma) \cap \mathscr{D}(\mathscr{C}_0)$  stable in  $\sigma$  if and only if  $\sigma(u)(stable) = true.$  **Definition.** Let  $\mathscr{D}_0$  be a structure of the signature with signals  $\mathscr{S}_0 = (\mathscr{T}_0, \mathscr{C}_0, V_0, atr_0, \mathscr{E})$  and let  $E \in \mathscr{E}_0$  be a signal. Let  $atr(E) = \{v_1, \ldots, v_n\}$ . We call  $e = (E, \{v_1 \mapsto d_1, \ldots, v_n \mapsto d_n\}),$ or shorter (if mapping is clear from context)  $(E, (d_1, \ldots, d_n))$  or  $(E, \vec{d}),$ an event (or an instance) of signal E (if type-consistent). We use  $Evs(\mathscr{E}_0, \mathscr{D}_0)$  to denote the set of all events of all signals in  $\mathscr{S}_0$  wrt.  $\mathscr{D}_0$ .

As we always try to maximize confusion...:

- By our existing naming convention, u ∈ 𝔅(E) is also called instance of the (signal) class E in system configuration (σ, ε) if u ∈ dom(σ).
- The corresponding event is then  $(E, \sigma(u))$ .

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# Signals? Events...? Ether...?!

The idea is the following:

- Signals are types (classes).
- Instances of signals (in the standard sense) are kept in the system state component σ of system configurations (σ, ε).
- Identities of signal instances are kept in the ether.
- Each signal instance is in particular an **event** somehow "a recording that this signal occurred" (without caring for its identity)
- The main difference between signal instance and event: Events don't have an identity.
- Why is this useful? In particular for **reflective** descriptions of behaviour, we are typically not interested in the identity of a signal instance, but only whether it is an "*E*" or "*F*", and which parameters it carries.

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- (i) Introduce transformer as the semantics of action annotions. Intuitively,  $(\sigma', \varepsilon')$  is the effect of applying the transformer of the taken transition.
- (ii) Explain how to choose transitions depending on  $\varepsilon$  and when to stop taking transitions the **run-to-completion** "algorithm".

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# Transformer

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• In the following, we assume that each application of a transformer t to some system configuration  $(\sigma, \varepsilon)$  for object  $u_x$  is associated with a set of observations

$$Obs_t[u_x](\sigma,\varepsilon) \in 2^{\mathcal{D}(\mathscr{C}) \times \mathcal{D}(\mathscr{C}) \times Evs(\mathscr{C} \cup \{*,+\},\mathscr{D}) \times \mathscr{D}(\mathscr{C})} \xrightarrow{\operatorname{spectral}} \operatorname{ccelve} n \operatorname$$

 An observation (u<sub>src</sub>, u<sub>e</sub>, (E, d), u<sub>dst</sub>) ∈ Obs<sub>t</sub>[u<sub>x</sub>](σ, ε) represents the information that, as a "side effect" of u<sub>x</sub> executing t, an event (!) (E, d) has been sent from u<sub>src</sub> to u<sub>dst</sub>.

Special cases: creation/destruction.

• Recall the (simplified) syntax of transition annotations:

annot ::=  $\begin{bmatrix} \langle event \rangle & ['[' \langle guard \rangle ']' \end{bmatrix} & ['/' \langle action \rangle \end{bmatrix}$ 

- Clear:  $\langle event \rangle$  is from  $\mathscr E$  of the corresponding signature.
- But: What are  $\langle guard \rangle$  and  $\langle action \rangle$ ?
  - UML can be viewed as being parameterized in expression language (providing  $\langle guard \rangle$ ) and action language (providing  $\langle action \rangle$ ).
  - Examples:
    - Expression Language:
      - · OCL

· ...

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- $\cdot\,$  Java, C++,  $\ldots$  expressions
- Action Language:
  - · UML Action Semantics, "Executable UML"
  - · Java, C++, ... statements (plus some event send action)
  - · ...

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In the following, we consider

example OCL:

IlegerJ(o,v)=

In the following, we assume that we're given

- an expression language *Expr* for guards, and
- an action language Act for actions,

and that we're given

• a semantics for boolean expressions in form of a partial function ) modeling of the

$$I\llbracket \cdot \rrbracket(\cdot, \cdot) : Expr \to ((\Sigma_{\mathscr{S}}^{\mathscr{D}} \times (\operatorname{track}^{\mathscr{D}} \mathscr{D}(\mathscr{C}))) \to \mathbb{B})$$

which evaluates expressions in a given system configuration,

Assuming I to be partial is a way to treat "undefined" during runtime. If I is not defined (for instance because of dangling-reference navigation or division-by-zero), we want to go to a designated "error" system configuration.

• a transformer for each action: for each  $act \in Act$ , we assume to have

$$t_{act} \subseteq \mathscr{D}(\mathscr{C}) \times (\Sigma^{\mathscr{D}}_{\mathscr{S}} \times Eth) \times (\Sigma^{\mathscr{D}}_{\mathscr{S}} \times Eth)$$

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### Expression/Action Language Examples

We can make the assumptions from the previous slide because instances exist:

- for OCL, we have the OCL semantics from Lecture 03. Simply remove the pre-images which map to " $\perp$ ".
- for Java, the operational semantics of the SWT lecture uniquely defines transformers for sequences of Java statements.

We distinguish the following kinds of transformers:

- skip: do nothing recall: this is the default action
- send: modifies  $\varepsilon$  interesting, because state machines are built around sending/consuming events
- create/destroy: modify domain of  $\sigma$  not specific to state machines, but let's discuss them here as we're at it
- update: modify own or other objects' local state boring

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# Transformer Examples: Presentation



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# Transformer: Skip

abstract syntax skip	concrete syntax جائرہ
intuitive semantics	do nothing
well-typedness	"If ux exercites stip
semantics	$t[u_x](\sigma,\varepsilon) = \{(\sigma,\varepsilon)\} \qquad \qquad$
observables	$Obs_{\texttt{skip}}[u_x](\sigma,\varepsilon) = \emptyset$
(error) conditions	

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### Transformer: Update

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update $(expr_1, v, expr_2)$		
$\begin{split} t_{\texttt{update}(expr_1,v,expr_2)}[u_x](\sigma,\varepsilon) &= (\sigma[u\mapsto\sigma(u)[v\mapsto I[\![expr_2]\\ u &= I[\![expr_1]\!](\sigma,\beta) \end{split}$	$]\!](\sigma,\beta)]],\varepsilon),$	



# References

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### References

- [Harel and Gery, 1997] Harel, D. and Gery, E. (1997). Executable object modeling with statecharts. *IEEE Computer*, 30(7):31–42.
- [OMG, 2007a] OMG (2007a). Unified modeling language: Infrastructure, version 2.1.2. Technical Report formal/07-11-04.
- [OMG, 2007b] OMG (2007b). Unified modeling language: Superstructure, version 2.1.2. Technical Report formal/07-11-02.