# Software Design, Modelling and Analysis in UML 

Lecture 12: Core State Machines III

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## Contents \& Goals

Last Lecture:

- The basic causality model
- Ether


## This Lecture:

- Educational Objectives: Capabilities for following tasks/questions.
- What does this State Machine mean? What happens if I inject this event?
- Can you please model the following behaviour.
- What is: Signal, Event, Ether, Transformer, Step, RTC.
- Content:
- System Configuration, Transformer
- Examples for transformer
- Run-to-completion Step
- Putting It All Together



## Roadmap: Chronologically

(i) What do we (have to) cover? UML State Machine Diagrams Syntax.
(ii) Def.: Signature with signals.
(iii) Def.: Core state machine.
(iv) Map UML State Machine Diagrams $\sqrt{ }$ to core state machines.

## Semantics:

The Basic Causality Model
(v) Def.: Ether (aka. event pool)
$J$ (vi) Def.: System configuration.
(vii) Def.: Event.
(viii) Def.: Transformer.
(ix) Def.: Transition system, computation.

UML

(x) Transition relation induced by core state machine.
(xi) Def.: step, run-to-completion step.
(xii) Later: Hierarchical state machines.


## Ether and [OMG, 2007b]

The standard distinguishes (among others)

- SignalEvent [OMG, 2007b, 450] and Reception [OMG, 2007b, 447].

A signal event represents the receipt of an asynchronous signal instance. A signal event may, for example, cause a state machine to trigger a transition. [OMG, 2007b, 449]


## [...] $=$ mersager <br> Semantic Variation Points

The means by which requests are transported to their target depend on the type of requesting action, the target, the properties of the communication medium, and numerous other factors.
\} In some cases, this is instantaneous, and completely reliable while in others it may involve Transmission delays of variable duration, loss of requests, reordering, or duplication.
(See also the discussion on page 421.) [OMG, 2007b, 450]
Our ether is a general representation of the possible choices.
Often seen minimal requirement: order of sending by one object is preserved.
But: we'll later briefly discuss "discarding" of events.

## System Configuration





$D\left(m_{n}\right)=D_{0}\left(l_{n} t\right)$
$D\left(S_{n_{c}}\right)=\left\{s_{\left.O_{1}, S_{1}, S_{2}, Q_{1}, s_{2}\right\}}\right\}$

0 :



- We start with some signature with signals $\mathscr{S}_{0}=\left(\mathscr{T}_{0}, \mathscr{C}_{0}, V_{0}, a t r_{0}, \mathscr{E}\right)$.
- A system configuration is a pair $(\sigma, \varepsilon)$ which comprises a system state $\sigma$ wrt. $\mathscr{S}$ (not wrt. $\mathscr{S}_{0}$ ).
- Such a system state $\sigma$ wrt. $\mathscr{S}$ provides, for each object $u \in \operatorname{dom}(\sigma)$,
- values for the explicit attributes in $V_{0}$,
- values for a number of implicit attributes, namely - a stability flag, i.e. $\sigma(u)($ stable $)$ is a boolean value,
- a current (state machine) state, i.e. $\sigma(u)(s t)$ denotes one of the states of core state machine $M_{C}$,
- a temporary association to access event parameters for each class, i.e. $\sigma(u)\left(\right.$ params $\left._{E}\right)$ is defined for each $E \in \mathscr{E}$.
- For convenience require: there is no link to an event except for $\operatorname{params}_{E}$.


## Stability

## Definition.

Let $(\sigma, \varepsilon)$ be a system configuration over some $\mathscr{S}_{0}, \mathscr{D}_{0}$, Eth.
We call an object $u \in \operatorname{dom}(\sigma) \cap \mathscr{D}\left(\mathscr{C}_{0}\right)$ stable in $\sigma$ if and only if

$$
\sigma(u)(\text { stable })=\text { true }
$$

## Events Are Instances of Signals

Definition. Let $\mathscr{D}_{0}$ be a structure of the signature with signals $\mathscr{S}_{0}=\left(\mathscr{T}_{0}, \mathscr{C}_{0}, V_{0}, a t r_{0}, \mathscr{E}\right)$ and let $E \in \mathscr{E}_{0}$ be a signal.
Let $\operatorname{atr}(E)=\left\{v_{1}, \ldots, v_{n}\right\}$. We call

$$
e=\left(E,\left\{v_{1} \mapsto d_{1}, \ldots, v_{n} \mapsto d_{n}\right\}\right)
$$

or shorter (if mapping is clear from context)

$$
\left(E,\left(d_{1}, \ldots, d_{n}\right)\right) \text { or }(E, \vec{d})
$$

an event (or an instance) of signal $E$ (if type-consistent).
We use $\operatorname{Evs}\left(\mathscr{E}_{0}, \mathscr{D}_{0}\right)$ to denote the set of all events of all signals in $\mathscr{S}_{0}$ wrt. $\mathscr{D}_{0}$.

As we always try to maximize confusion...:

- By our existing naming convention, $u \in \mathscr{D}(E)$ is also called instance of the (signal) class $E$ in system configuration $(\sigma, \varepsilon)$ if $u \in \operatorname{dom}(\sigma)$.
- The corresponding event is then $(E, \sigma(u))$.


## Signals? Events...? Ether...?!

The idea is the following:

- Signals are types (classes).
- Instances of signals (in the standard sense) are kept in the system state component $\sigma$ of system configurations $(\sigma, \varepsilon)$.
- Identities of signal instances are kept in the ether.
- Each signal instance is in particular an event - somehow "a recording that this signal occurred" (without caring for its identity)
- The main difference between signal instance and event:

Events don't have an identity.

- Why is this useful? In particular for reflective descriptions of behaviour, we are typically not interested in the identity of a signal instance, but only whether it is an " $E$ " or " $F$ ", and which parameters it carries.

this. $x+1$
- Wanted: a labelled transition relation

$$
(\sigma, \varepsilon) \xrightarrow[U]{\left(\sigma^{\prime}, \varepsilon^{\prime}\right)}
$$

on system configuration, labelled with the consumed and sent events. ( $\sigma^{\prime}, \varepsilon^{\prime}$ ) being the result (or effect) of one object $u_{x}$ taking a transition of its state machine from the current state mach. state $\sigma\left(u_{x}\right)\left(s t_{C}\right)$.

- Have: system configuration $(\sigma, \varepsilon)$ comprising current state machine state and stability flag for each object, and the ether.


## - Plan:

(i) Introduce transformer as the semantics of action annotions. Intuitively, $\left(\sigma^{\prime}, \varepsilon^{\prime}\right)$ is the effect of applying the transformer of the taken transition.
(ii) Explain how to choose transitions depending on $\varepsilon$ and when to stop taking transitions - the run-to-completion "algorithm".

## Transformer

## becalar of ron-deterruindsm

Definition.
Let $\Sigma_{\mathscr{S}}^{\mathscr{g}}$ the set of system configurations over some $\mathscr{S}_{0}, \mathscr{D}_{0}$, Eth.


- In the following, we assume that each application of a transformer $t$ to some system configuration $(\sigma, \varepsilon)$ for object $u_{x}$ is associated with a set of observations

- An observation $\left(u_{s r c}, u_{e},(E, \vec{d}), u_{d s t}\right) \in O b s_{t}\left[u_{x}\right](\sigma, \varepsilon)$
represents the information that, as a "side effect" of $u_{x}$ executing $t$, an event (!) $(E, \vec{d})$ has been sent from $u_{\text {sc }}$ to $u_{d s t}$.

Special cases: creation/destruction.

- Recall the (simplified) syntax of transition annotations:

```
annot ::=[ \langleevent\rangle [ '['\langleguard\rangle']'] ['/'\langleaction\rangle] ]
```

- Clear: $\langle$ event $\rangle$ is from $\mathscr{E}$ of the corresponding signature.
- But: What are $\langle$ guard $\rangle$ and $\langle$ action $\rangle$ ?
- UML can be viewed as being parameterized in expression language (providing $\langle$ guard $\rangle$ ) and action language (providing $\langle$ action $\rangle$ ).
- Examples:
- Expression Language:
- OCL
- Java, C++, ... expressions
- Action Language:
- UML Action Semantics, "Executable UML"
- Java, C++, ...statements (plus some event send action)

In the furlouring, we consider

$$
\text { Expos: OCL expresoids over } \varphi
$$

$$
\begin{aligned}
& \text { Acth }:=\{\text { ship }\}
\end{aligned}
$$

$$
\begin{aligned}
& \left.u\{\text { crate }(C, \text { exon, } v)) \text { eco } \in \propto c e E_{\text {for }}, c \in C, v \in V\right\} \\
& u\{\text { destog (exam) } / \text { age } \in \text { Oclegac }\}
\end{aligned}
$$

## Transformers as Abstract Actions!

In the following, we assume that we're given

- an expression language Expr for guards, and
- an action language Act for actions,
and that we're given
a semantics for boolean expressions in form of a partial function

$$
I \llbracket \cdot \rrbracket(\cdot, \cdot): \operatorname{Expr} \rightarrow\left(\left(\Sigma_{\mathscr{S}}^{\mathscr{O}} \times(\underset{\sim}{\text { this }} \mathscr{D}(\mathscr{C}))\right) \xrightarrow{\rightarrow} \mathbb{B}\right)
$$

which evaluates expressions in a given system configuration
Assuming $I$ to be partial is a way to treat "undefined" during runtime. If $I$ is not defined (for instance because of dangling-reference navigation or division-by-zero), we want to go to a designated "error" system configuration.

- a transformer for each action: for each act $\in$ Act, we assume to have

$$
t_{a c t} \subseteq \mathscr{D}(\mathscr{C}) \times\left(\Sigma_{\mathscr{S}}^{\mathscr{D}} \times E t h\right) \times\left(\Sigma_{\mathscr{S}}^{\mathscr{D}} \times E t h\right)
$$

## Expression/Action Language Examples

We can make the assumptions from the previous slide because instances exist:

- for OCL, we have the OCL semantics from Lecture 03. Simply remove the pre-images which map to " $\perp$ ".
- for Java, the operational semantics of the SWT lecture uniquely defines transformers for sequences of Java statements.

We distinguish the following kinds of transformers:

- skip: do nothing - recall: this is the default action
- send: modifies $\varepsilon$ - interesting, because state machines are built around sending/consuming events
- create/destroy: modify domain of $\sigma$ - not specific to state machines, but let's discuss them here as we're at it
- update: modify own or other objects' local state - boring

| abstract syntax op | concrete syntax |
| :---: | :---: |
| intuitive semantics |  |
| well-typedness |  |
| semantics <br> object "exerstion" action of $\left((\sigma, \varepsilon),\left(\sigma^{\prime}, \varepsilon^{\prime}\right)\right) \in t_{\mathrm{op}}\left[u_{x}\right]$ iff $\ldots$ <br> or $t_{\mathrm{op}}\left[u_{x}\right](\sigma, \varepsilon)=\left\{\left(\sigma^{\prime}, \varepsilon^{\prime}\right)\right\}$ where $\ldots$ |  |
| observables $O b s_{\text {op }}\left[u_{x}\right]=\{\ldots\}$, not a relation, depends on choice |  |
| (error) conditions Not defined if |  |

## Transformer: Skip

| abstract syntax skip | concrete syntax skip |
| :---: | :---: |
| intuitive semantics | do nothing |
| well-typedness semantics |  |
| observables | $O b s_{\text {skip }}\left[u_{x}\right](\sigma, \varepsilon)=\emptyset$ |
| (error) conditions |  |

## Transformer: Update


i. $t_{\text {rupante }\left[. . f\left[u_{x}\right](\sigma, \varepsilon)=\varnothing\right.}$

## Update Transformer Example

$\mathcal{S} \mathcal{M}_{C}:$

this. $x$ : $=$ this. $x+1$

$$
\begin{gathered}
t_{\text {update }\left(\operatorname{expr}_{1}, v, \operatorname{expr}_{2}\right)}\left[u_{x}\right](\sigma, \varepsilon)=\left(\sigma\left[u \mapsto \sigma(u)\left[v \mapsto I \llbracket \operatorname{expr}_{2} \rrbracket(\sigma, \beta)\right]\right], \varepsilon\right), \\
u=I \llbracket \operatorname{expr}_{1} \rrbracket(\sigma, \beta)
\end{gathered}
$$

$\sigma:$

| $u_{1}: C$ | $\xrightarrow{v_{x}=v_{1}}$ | $u_{1}: C$ |
| :---: | :---: | :---: |
| $x=4$ | $t_{u p d}\left[u_{1}\right\}(\sigma, \Sigma)=$ | $x=5$ |
| $y=0$ |  | $y=0$ |

$\varepsilon$ :



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## References

## References

[Harel and Gery, 1997] Harel, D. and Gery, E. (1997). Executable object modeling with statecharts. IEEE Computer, 30(7):31-42.
[OMG, 2007a] OMG (2007a). Unified modeling language: Infrastructure, version 2.1.2. Technical Report formal/07-11-04.
[OMG, 2007b] OMG (2007b). Unified modeling language: Superstructure, version 2.1.2. Technical Report formal/07-11-02.

