

Software Design, Modelling and Analysis in UML

Lecture 13: Core State Machines V

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Contents & Goals

- Last Lecture:**
 - System configuration
 - Transformer
- This Lecture:**
 - Educational Objectives:** Capabilities for following tasks/questions:
 - What does this State Machine mean? What happens if I inject this event?
 - Can you please model the following behaviour?
 - What is: Signal, Event, Ether, Transformer, Step, RTIC
 - Content:**
 - Transformer cont'd
 - Examples for transformer
 - Run-to-completion Step
 - Putting It All Together

System Configuration, Ether, Transformer

System Configuration

Definition. Let $\mathcal{S}_0 = (S_0, \delta_0, V_0, \text{dir}, \delta^0)$ be a signature with signals, \mathcal{S}_0 a structure of \mathcal{S}_0 , $(E, H, \text{real}, \theta, \in, \cdot)$ an ether over \mathcal{S}_0 and \mathcal{S}_0 . Furthermore assume there is one core state machine M_C per class $C \in \mathcal{C}$.

A system configuration over $\mathcal{S}_0, \mathcal{S}_0, \delta_0$, and E, H is a pair (\mathcal{S}, δ) where \mathcal{S} is a set of state machines $(r, \delta) \in \mathcal{S}_0^2 \times \text{RM}$ where

- $\mathcal{S} = \{ \mathcal{S}_0 \cup \{ S_{MC} \mid C \in \mathcal{C} \}, \delta_0$
- $V_0 \cup \{ \text{state} : \text{Bool}, - \text{true} \} \cup \{ \text{state} : S_{MC} + s_{MC}, \theta \mid C \in \mathcal{C} \}$
- $\cup \{ \text{param} g : E_{0,1} + \theta \mid E \in \delta_0 \}$
- $\cup \{ \text{state}, s_{MC} \mid \text{param} g \mid E \in \delta_0 \mid C \in \mathcal{C} \}, \delta_0$
- $\cup \{ C \rightarrow \text{dir}(C) \}$

where $\delta = \delta_0 \cup \{ S_{MC} \rightarrow S(A_C) \mid C \in \mathcal{C} \}$, and $\delta^0(C) \cap \delta(A_C) = \emptyset$ for each $v \in \text{dom}(C)$ and $r \in V_{0,1}$.

Handwritten notes:
 - \mathcal{S} is a set of state machines
 - δ is a set of transitions
 - δ^0 is a set of transitions
 - $\delta^0(C)$ is a set of transitions
 - $\delta(A_C)$ is a set of transitions
 - $\delta^0(C) \cap \delta(A_C) = \emptyset$ for each $v \in \text{dom}(C)$ and $r \in V_{0,1}$



Where are we?

on system configuration, labelled with the consumed and sent events, (r, δ^0) being the result (or effect) of some object r , taking a transition of its state machine from the current state $\text{state } \delta^0(r, \delta^0)$.

- Wanted:** a labelled transition relation $(r, \delta) \xrightarrow{\text{consum. State}} (r', \delta')$
- Plan:**
 - Introduce transformer as the semantics of action annotations $(r, \delta^0) \xrightarrow{\text{action}} (r', \delta')$ in the effect of applying the transformer of the (r, δ^0) .
 - Explain how to choose transitions depending on r and when to stop taking transitions — the run-to-completion “algorithm”

Handwritten notes:
 - $(r, \delta) \xrightarrow{\text{consum. State}} (r', \delta')$
 - $r \xrightarrow{\text{action}} r'$
 - $\delta \xrightarrow{\text{action}} \delta'$
 - $\delta^0 \xrightarrow{\text{action}} \delta^0$
 - $\delta^0 \xrightarrow{\text{action}} \delta^0$
 - $\delta^0 \xrightarrow{\text{action}} \delta^0$

Transformer leave y non-abstract

Definition.
Let $\Sigma_{\mathcal{O}}$ the set of system configurations over some $\mathcal{O}_0, \mathcal{O}_1, E, H$.
We call a mapping σ the object receiving the action.
 $T \subseteq \mathcal{O}(C) \times (\Sigma_{\mathcal{O}}^0 \times E, H) \times (\Sigma_{\mathcal{O}}^0 \times E, H)$
a (system configuration) **Transformer** system configuration again

In the following, we assume that each application of a transformer T to some system configuration (σ, ε) for object u_0 is associated with a set of observations (σ', ε') same observation object as the config

$Obs_{\mathcal{O}}(u_0)(\sigma, \varepsilon) \in \mathcal{P}(Obs_{\mathcal{O}}(u_0) \times E, H) \cup \{ \perp \}$ no more a definition

An observation $(u_{act}, u_0, (E, \mathcal{D}), u_0, u_1) \in Obs_{\mathcal{O}}(u_0)(\sigma, \varepsilon)$ represents the information that, as a "side effect" of u_0 executing T , an event $(\perp) (E, \mathcal{D})$ has been sent from u_{act} to u_1 .

Special cases: creation/destruction

15/0

Transformer: Update

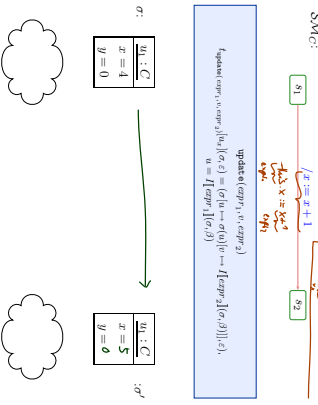
| | |
|--|--------------------------|
| abstract syntax | concrete syntax |
| update(exp_1, v, exp_2) | exp_1, v, \cdot, exp_2 |
| infixive semantics | |
| Update attribute v in the object denoted by exp_1 to the value denoted by exp_2 . | |
| well-typedness | |
| exp_1, v, exp_2 : τ and $v : \tau \in \text{attr}(C)$; $exp_2, v : \tau$ | |
| semantics | |
| $\tau \text{update}(exp_1, v, exp_2)(u_0)(\sigma, \varepsilon) = (u', \varepsilon')$ where $u' = \sigma(u) \rightarrow \sigma'(u) \rightarrow T[exp_2](u, \beta)$ with $u = T[exp_1](u, \beta)$; $\beta = [\text{this} \mapsto u_0]$ | |
| observables | |
| (err) conditions $Obs_{\text{update}(exp_1, v, exp_2)}(u_0) = \emptyset$ | |
| (err) Not defined if $T[exp_1](\sigma, \beta)$ or $T[exp_2](\sigma, \beta)$ not defined. | |

In the following, we consider:

$Act_{\mathcal{O}} := \{ \text{obj} \}$
 $u \} \text{update}(exp_1, v, exp_2) / exp_1, exp_2 \in \text{OZExp}, v \in V$
 $u \} \text{send}(l, exp_1, E, H) / exp_1, exp_2 \in \text{OZExp}, E \in \mathcal{E}$
 $u \} \text{create}(C, exp_1, v) / exp_1 \in \text{OZExp}, C \in C, v \in V$
 $u \} \text{destroy}(exp) / exp \in \text{OZExp}?$

Empty: OZ expressions are \emptyset

Update Transformer Example



Transformer: Skip

| | |
|--|------------------------|
| abstract syntax | concrete syntax |
| skip | $skip$ |
| infixive semantics | |
| do nothing | |
| well-typedness | |
| ./ | |
| semantics | |
| $T[skip](\sigma, \varepsilon) = \{(\sigma, \varepsilon)\}$ | |
| observables | |
| $Obs_{\text{skip}}(u_0)(\sigma, \varepsilon) = \emptyset$ | |
| (err) conditions | |

Transformer: Send

| | |
|---|-------------------------------------|
| abstract syntax | concrete syntax |
| send($E, exp_1, \dots, exp_n, exp_{act}$) | $exp_{act}, E, exp_1, \dots, exp_n$ |
| infixive semantics | |
| Object u_0 : C sends event E to object exp_{act} ; the create a fresh signal instance, fill in its attributes, and place it in the ether. | |
| well-typedness | |
| $exp_{act}, E, exp_1, \dots, exp_n, C, D \in \mathcal{P}, \forall \sigma', E \in \mathcal{E}$ | |
| $act(E) = (u_1, \tau_1, \dots, u_n, \tau_n); exp_1, \tau_1, \dots, exp_n, \tau_n \in \mathcal{C}$ | |
| semantics | |
| $\tau \text{send}(E, exp_1, \dots, exp_n, exp_{act})(u_0)(\sigma, \varepsilon) \ni (u', \varepsilon')$ where $u' = \sigma(u) \rightarrow (u_1 \rightarrow d_1, \dots, u_n \rightarrow d_n, 1 \leq i \leq n); \varepsilon' = \varepsilon \oplus (u_{act}, d);$ if $u_{act} = T[exp_{act}](u, \beta) \in \text{dom}(\sigma)$; $d_i = T[exp_i](u, \beta)$ for $u_i \in \text{attr}(C)$ a fresh identity, i.e. $u_i \notin \text{dom}(\sigma)$. | |
| observables | |
| $Obs_{\text{send}}(u_0) = \{(u_0, u_1, E, d_1, \dots, d_n, u_{act})\}$ | |
| (err) conditions | |
| $T[exp_i](\sigma, \beta)$ not defined for any $exp_i \in \{exp_{act}, exp_1, \dots, exp_n\}$ | |

Handwritten notes: $\tau \text{send}(E, \dots)$ can lead to err if u_{act} is not in $\text{dom}(\sigma)$.

Send Transformer Example

SMC:



send(f , $\text{copy}(x_1, \dots, \text{copy}(a_1), \text{copy}(a_2))$)
 $\text{fparam}(\text{copy}(x_1, \dots, \text{copy}(a_1), \text{copy}(a_2)))(\alpha, \beta) = \dots$



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Transformer: Create

abstract syntax
 create($C, \text{expr } v$)

concrete syntax
 $\text{copy } v \leftarrow \text{new } C$

$\text{copy } v \leftarrow \text{new } C$
 $x_i := \text{copy } v_i$
 $x_i := \text{copy } v_i$
 $x_i := \text{copy } v_i$

(4) as $\text{let } x; \text{ body } / \text{ let } (x_1, \dots, x_n) \text{ in } \text{body}$ if fresh :

intuitive semantics
 Create an object of class C and assign it to attribute v of the object

well-synopsisness
 $\text{expr} : \tau_D, v \in \text{dom}(D), \text{dom}(C) = \{(x_i : \tau_i, \text{copy } v_i) \mid 1 \leq i \leq n\}$

semantics
 ...

observables
 ...

(error) conditions
 $\llbracket \text{expr} \rrbracket(\alpha, \beta)$ not defined

We use an "and assign" action for simplicity — it doesn't add or remove expressive power, but moving creation to the expression language raises all kinds of other problems such as order of evaluation (and thus creation).

Also for simplicity: no parameters to construction (~ parameters of constructor). Adding them is straightforward (but somewhat tedious).

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Create Transformer Example

SMC:



create($C, \text{expr } v$)
 $\text{fparam}(\text{copy}(x_1, \dots, \text{copy}(a_1), \text{copy}(a_2)))(\alpha, \beta) = \dots$



15.4

How To Choose New Identities?

- **Re-use:** choose any identity that is not alive now, i.e. not in $\text{dom}(\sigma)$.
- Doesn't depend on history.
- May "undangle" dangling references — may happen on some platforms.
- **Fresh:** choose any identity that has not been alive ever, i.e. not in $\text{dom}(\sigma)$ and any predecessor in current run.
- Depends on history.
- Dangling references remain dangling — could mask "dirty" effects of platform.

Transformer: Create

abstract syntax
 create($C, \text{expr } v$)

concrete syntax
 $\text{copy } v \leftarrow \text{new } C$

intuitive semantics
 Create an object of class C and assign it to attribute v of the object

well-synopsisness
 $\text{expr} : \tau_D, v \in \text{dom}(D), \text{dom}(C) = \{(x_i : \tau_i, \text{copy } v_i) \mid 1 \leq i \leq n\}$

semantics
 $\llbracket \text{expr} \rrbracket(\alpha, \beta) = \dots$

observables
 $\text{Obs}_{\text{create}}[u_i] = \{(x_i, \perp, (\ast, \emptyset), u_i)\}$

(error) conditions
 $\llbracket \text{expr} \rrbracket(\alpha, \beta)$ not defined.

add new object to σ
 $\text{if } \sigma = \sigma' \cup \{(x_i, \perp, (\ast, \emptyset), u_i)\} \mid 1 \leq i \leq n$
 $\text{if } \sigma = \sigma' \cup \{(x_i, \perp, (\ast, \emptyset), u_i)\} \mid 1 \leq i \leq n$
 $\text{if } \sigma = \sigma' \cup \{(x_i, \perp, (\ast, \emptyset), u_i)\} \mid 1 \leq i \leq n$
 $u_i = \llbracket \text{copy } v_i \rrbracket(\alpha, \beta)$ if $\text{copy } v_i \neq \ast$ and arbitrary value from $\mathcal{V}(\tau_i)$ otherwise; $\beta = \text{this} \rightarrow u_i$.

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Transformer: Destroy

abstract syntax
 destroy(copy)

concrete syntax
 $\text{obj } \text{copy}$

intuitive semantics
 Destroy the object denoted by expression copy .

well-synopsisness
 $\text{copy} : \tau_C, C \in \mathcal{C}$

semantics
 $\llbracket \text{copy} \rrbracket(\alpha, \beta) = \dots$

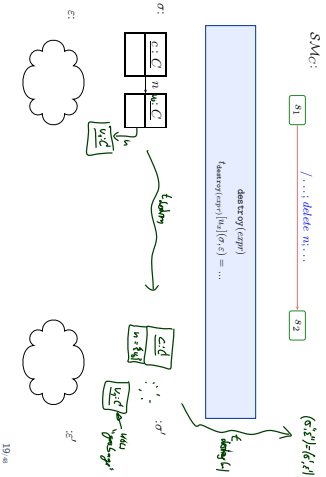
observables
 $\text{Obs}_{\text{destroy}}[u_i] = \{(x_i, \perp, (\ast, \emptyset), u_i)\}$

(error) conditions
 $\llbracket \text{copy} \rrbracket(\alpha, \beta)$ not defined.

$\text{if } \sigma = \sigma' \cup \{(x_i, \perp, (\ast, \emptyset), u_i)\} \mid 1 \leq i \leq n$
 $\text{if } \sigma = \sigma' \cup \{(x_i, \perp, (\ast, \emptyset), u_i)\} \mid 1 \leq i \leq n$
 $\text{if } \sigma = \sigma' \cup \{(x_i, \perp, (\ast, \emptyset), u_i)\} \mid 1 \leq i \leq n$
 $u_i = \llbracket \text{copy} \rrbracket(\alpha, \beta)$ if $\text{copy} \neq \ast$ and arbitrary value from $\mathcal{V}(\tau_i)$ otherwise; $\beta = \text{this} \rightarrow u_i$.

18.4

Destroy Transformer Example



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What to Do With the Remaining Objects?

- Assume object u_0 is destroyed ...
 - object u_1 may still refer to it via association r .
 - allow dangling references?
 - or remove u_0 from $\sigma(u_1)(r)$?
 - object u_0 may have been the last one linking to object u_2 :
 - leave u_2 alone?
 - or remove u_2 also?
 - Plus: (temporal extensions of) OCL may have dangling references.
- Our choice:** Dangling references and no garbage collection! This is in line with "expect the worst", because there are target platforms which don't provide garbage collection — and models shall (in general) be correct without assumptions on target platform.
- But:** the more "dirty" effects we see in the model, the more expensive it often is to analyse. Valid proposal for simple analysis: monotone frame semantics, no destruction at all.

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Transformer: Destroy

| | | |
|--------------------|--|--------------------|
| abstract syntax | destroy($expr$) | concrete syntax |
| infixive semantics | | |
| well-synthesized | Destroy the object denoted by expression $expr$. | |
| semantics | $\llbracket destroy(e) \rrbracket_{\sigma} = \{\langle \sigma', e \rangle\}$ | function notations |
| observables | where $\sigma' = \sigma \setminus_{\text{dom}(\sigma)}(u)$ with $u = \llbracket expr \rrbracket_{\sigma}(\beta)$. | |
| (error) conditions | $Obs_{destroy}[u_0] = \{(u_0, \perp, (+0), u)\}$ | |
| | $\llbracket expr \rrbracket_{\sigma}(\beta)$ not defined. | |

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Sequential Composition of Transformers

- Sequential composition** $t_1 \circ t_2$ of transformers t_1 and t_2 is canonically defined as

$$(t_2 \circ t_1)[u_0](\sigma, \varepsilon) = t_2[u_0](t_1[u_0](\sigma, \varepsilon))$$
 with observation

$$Obs_{(t_2 \circ t_1)}[u_0](\sigma, \varepsilon) = Obs_{t_1}[u_0](\sigma, \varepsilon) \cup Obs_{t_2}[u_0](t_1(\sigma, \varepsilon));$$
- Clear:** not defined if one the two intermediate "micro steps" is not defined.

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Transformers And Denotational Semantics

- Observation:** our transformers are in principle the **denotational semantics** of the actions/action sequences. The trivial case, to be precise.
- Note:** with the previous examples, we can capture
- empty statements, skips,
 - assignments,
 - conditionals (by normalisation and auxiliary variables),
 - create/destroy,
- but not possibly **diverging loops**.
- Our (Simple) Approach:** if the action language is, e.g., Java, then (syntactically) forbid loops and calls of recursive functions.
- Other Approach:** use full blown denotational semantics.
- No show-stopper, because loops in the action annotation can be converted into transition cycles in the state machine.

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Run-to-completion Step

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Definition. Let A be a set of actions and S a (not necessarily finite) set of states.
 We call $\xrightarrow{\alpha} \subseteq S \times A \times S$ a (labelled) transition relation.
 Let $S_0 \subseteq S$ be a set of initial states. A sequence $s_0 \xrightarrow{a_1} s_1 \xrightarrow{a_2} s_2 \xrightarrow{a_3} \dots$ with $s_i \in S, a_i \in A$ is called computation of the labelled transition system $(S, \xrightarrow{\cdot}, S_0)$ if and only if

- **initiation:** $s_0 \in S_0$
- **consistency:** $(s_i, a_i, s_{i+1}) \in \xrightarrow{\cdot}$ for $i \in \mathbb{N}_0$.

Note: for simplicity, we only consider infinite runs

- **Note:** From now on, assume that all classes are **active** for simplicity. We'll later briefly discuss the Rhapsody framework, which proposes a way how to integrate non-active objects.
- **Note:** The following RTC "algorithm" follows [Harel and Gery, 1997] (i.e. the one realised by the Rhapsody code generator) where the standard is ambiguous or leaves choices.

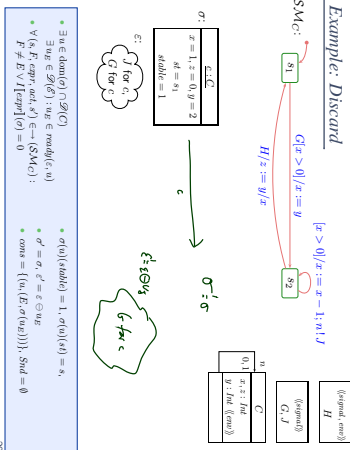
Definition. Let $\mathcal{SM} = (\mathcal{S}_0, \mathcal{S}_1, \mathcal{V}, \text{dom}, \mathcal{E})$ be a signature with signal (all classes active) \mathcal{S}_0 , a structure of \mathcal{S}_0 and $\mathcal{E}H$, $\text{ready} : \mathcal{S}_0 \rightarrow \{0, 1\}$ an ether over \mathcal{S}_0 and \mathcal{S}_1 . Assume there is one core state machine M_C per class $C \in \mathcal{C}$. We say, the state machines induce the following labelled transition relation on states $S := (\mathcal{S}_0 \times \mathcal{S}_1) \cup (\mathcal{E}H \times \mathcal{E}H)$ with actions $A := (\mathcal{S}_0 \times \mathcal{S}_1 \times \mathcal{S}_0 \cup \{1, 0\}) \times \text{Form}(\mathcal{E}, \mathcal{S}_0, \mathcal{S}_1)$:

- $(\sigma, \varepsilon) \xrightarrow{\text{consumption}} (\sigma', \varepsilon')$ if and only if:
 - (i) an event with destination v is discarded,
 - (ii) an event is dispatched to v , i.e. stable object processes an event, or run-to-completion processing by v commences,
 - (iii) i.e. object v is not stable and continues to process an event.
- $s \xrightarrow{\text{consumption}} \# \xrightarrow{\text{error}} s'$ if and only if
 - (iv) the environment interacts with object v ,
 - (v) $s \neq \#$ and $\text{cons} = \emptyset$ or an error condition occurs during consumption of cons .

(i) Discarding An Event

- if
- an E -event (instance of signal E) is ready in ε for object v of a class \mathcal{C} , i.e. if $v \in \text{dom}(\sigma) \cap \mathcal{D}(\mathcal{C}) \wedge \exists u \in \mathcal{D}(\mathcal{E}) : u \in \text{ready}(\varepsilon, v)$
 - v is stable and in state machine state s , i.e. $\sigma(v)(\text{stable}) = 1$ and $\sigma(v)(s) = s$, but there is no corresponding transition enabled (all transitions incident with current state of v either have other triggers or the guard is not satisfied)
- $\forall (s, F, \text{exp}, \text{act}, s') \in \xrightarrow{\cdot}(\text{SM}, \mathcal{C}) : F \neq E \vee \llbracket \text{exp} \rrbracket(\sigma) = 0$
- and
- the system configuration doesn't change, i.e. $\sigma' = \sigma$
 - the event $u \in E$ is removed from the ether, i.e. $\varepsilon' = \varepsilon \ominus u_E$
 - consumption of $u \in E$ is observed, i.e. $\text{cons} = \{(u, E, \sigma'(u_E))\}, \text{Stab} = \emptyset$

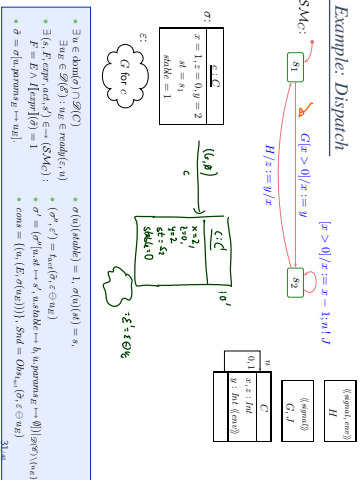
Example: Discard



(ii) Dispatch

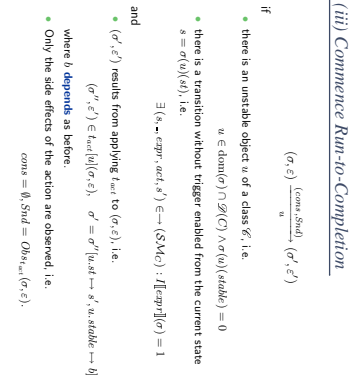
- $v \in \text{dom}(\sigma) \cap \mathcal{D}(\mathcal{C}) \wedge \exists u \in \mathcal{D}(\mathcal{E}) : u \in \text{ready}(\varepsilon, v)$
 - v is stable and in state machine state s , i.e. $\sigma(v)(\text{stable}) = 1$ and $\sigma(v)(s) = s$, a transition is enabled, i.e. $\exists (s', F, \text{exp}, \text{act}, s') \in \xrightarrow{\cdot}(\text{SM}, \mathcal{C}) : F = E \wedge \llbracket \text{exp} \rrbracket(\sigma) = 1$
- where $\sigma' = \sigma \upharpoonright_{\text{params}_E} \mapsto u_E$.
- and
- (σ', ε') results from applying Lact to (σ, ε) and removing $u \in E$ from the ether, i.e. $\sigma' = (\sigma \upharpoonright_{\text{params}_E} \mapsto s', u, \text{stable} \mapsto b, u, \text{params}_E \mapsto \emptyset) \upharpoonright_{\text{params}_E \cup \{v\}}$
 - $\varepsilon' = \varepsilon \upharpoonright_{\text{params}_E} \uplus u_E$
- where b depends:
- If v becomes stable in s' , then $b = 1$. It does become stable if and only if there is no transition without trigger enabled for v in (σ', ε') .
 - Otherwise $b = 0$.
 - Consumption of $u \in E$ and the side effects of the action are observed, i.e. $\text{cons} = \{(u, E, \sigma'(u_E))\}, \text{Stab} = \text{Obj}_{\text{st}, \text{act}}(\sigma', \varepsilon \ominus u_E)$.

Example: Dispatch



- $\exists u \in \text{dom}(C) \cap \mathcal{D}(C)$
- $\exists u \in \mathcal{D}(C) : u \in \text{inv}(c, u)$
- $\exists (s, s', \text{exp}, \text{act}, s') \in \rightarrow (SMC) : F = E \wedge \llbracket \text{exp} \rrbracket(s) = 1$
- $\theta = \sigma \wedge \text{promotes} \rightarrow \text{inv}$
- $\sigma'(u) \wedge \text{stable} = 1, \sigma'(u) = s$
- $(\sigma', \epsilon') = \text{keep}(s \in \text{inv})$
- $\sigma' = \sigma' \wedge \text{act} \rightarrow s', \text{stable} \rightarrow k, \text{update} \rightarrow k, \text{update} \rightarrow \emptyset \} \wedge \sigma' \setminus (s, s')$
- $\text{cons} = \{(u, (k, \sigma'(u)))\}, \text{Stnd} = \text{Obs}_{k, \text{inv}}(\sigma', \epsilon \in \text{inv})$

(iii) Commence Run-to-Completion



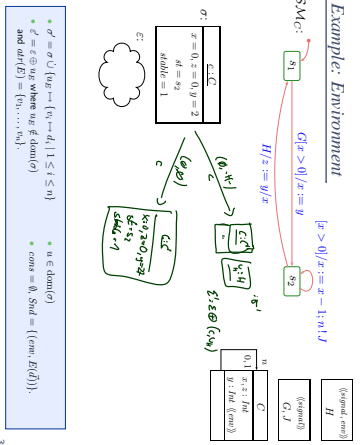
- $\sigma'(u) \wedge \text{stable} = 1, \sigma'(u) = s$
- $(\sigma', \epsilon') \in \text{keep}(\sigma', \epsilon)$
- $\sigma' = \sigma' \wedge \text{act} \rightarrow s', \text{update} \rightarrow b$
- where b depends as before.
- Only the side effects of the action are observed, i.e.
- $\text{cons} = \emptyset, \text{Stnd} = \text{Obs}_{k, \text{inv}}(\sigma', \epsilon)$

(iv) Environment Interaction

Assume that a set $\mathcal{E}_{\text{env}} \subseteq \mathcal{E}^e$ is designated as environment events and a set of attributes $\mathcal{V}_{\text{env}} \subseteq \mathcal{V}^e$ is designated as input attributes.

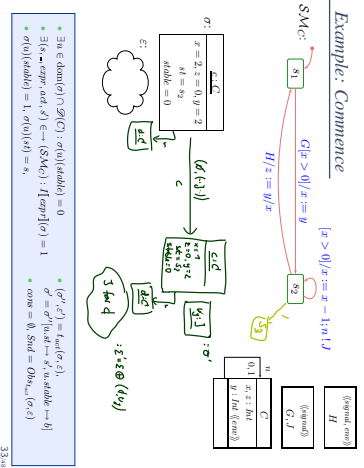
- Then
- $(\sigma', \epsilon) \xrightarrow{\text{cons, Stnd}}_{\text{env}} (\sigma', \epsilon')$
 - if
 - an environment event $E \in \mathcal{E}_{\text{env}}$ is spontaneously sent to an alive object $w \in \mathcal{D}(c)$, i.e.
 - $\sigma' = \sigma' \cup \{w \in \mathcal{D}(c) \mid 1 \leq i \leq n\}$, $\epsilon' = \epsilon \oplus w \oplus E$
 - where $w \in \mathcal{D}(c)$ and $\text{attr}(E) = (v_1, \dots, v_n)$.
 - Sending of the event is observed, i.e. $\text{cons} = \emptyset, \text{Stnd} = (\text{env}, E(\vec{v}))$.
 - or
 - Values of input attributes change freely in alive objects, i.e.
 - $\forall v \in \mathcal{V}^e \forall a \in \text{dom}(c) : \sigma'(a)(v) \neq \sigma'(a)(v) \implies v \in \mathcal{V}_{\text{env}}$
 - and no objects appear or disappear, i.e. $\text{dom}(\sigma') = \text{dom}(\sigma)$
 - $\epsilon' = \epsilon$.

Example: Environment



- $\sigma' = \sigma' \cup \{w \in \mathcal{D}(c) \mid 1 \leq i \leq n\}$
- $\ast \ast \ast u \in \text{dom}(c)$
- $\ast \ast \ast s \in \text{inv}$ where $w \in \mathcal{D}(c)$
- $\ast \ast \ast \text{attr}(E) = (v_1, \dots, v_n)$
- $\ast \ast \ast \text{cons} = \emptyset, \text{Stnd} = (\text{env}, E(\vec{v}))$

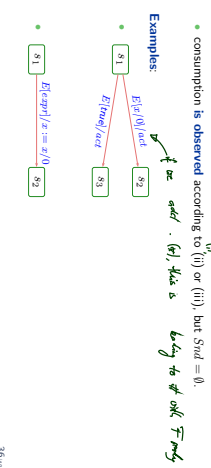
Example: Commence



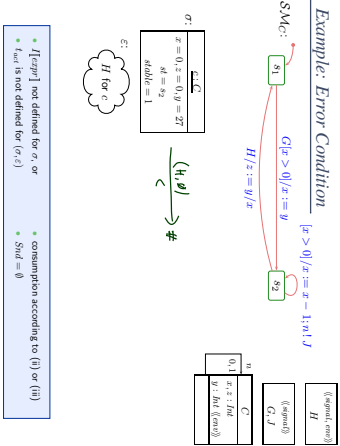
- $\exists u \in \text{dom}(C) \cap \mathcal{D}(C) : \sigma'(u) \wedge \text{stable} = 0$
- $\exists (s, s', \text{exp}, \text{act}, s') \in \rightarrow (SMC) : \llbracket \text{exp} \rrbracket(s) = 1$
- $\text{cons} = \emptyset, \text{Stnd} = \text{Obs}_{k, \text{inv}}(\sigma', \epsilon)$
- $(\sigma', \epsilon') = \text{keep}(\sigma', \epsilon)$
- $\sigma' = \sigma' \wedge \text{act} \rightarrow s', \text{update} \rightarrow b$
- $\text{cons} = \emptyset, \text{Stnd} = \text{Obs}_{k, \text{inv}}(\sigma', \epsilon)$

(v) Error Conditions

- if in (ii) or (iii).
- $\llbracket \text{exp} \rrbracket$ is not defined for σ or
 - act is not defined for (σ', ϵ) , i.e. $\text{act} \in \text{act}(c, \sigma')$
 - and
 - consumption is observed according to (ii) or (iii), but $\text{Stnd} = \emptyset$.



Example: Error Condition



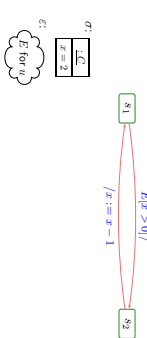
Notions of Steps: The Step

Note: we call one evolution $(\sigma, \varepsilon) \xrightarrow{\text{Cons, Stid}} \alpha \xrightarrow{(\sigma', \varepsilon')}$ a **step**.
 Thus in our setting, a **step directly corresponds** to **one object** (namely α) takes a **single transition** between regular states. (We have to extend the concept of 'single transition' for hierarchical state machines.)
That is: We're going for an interleaving semantics without true parallelism.
Remark: With only methods (later), the notion of step is not so clear.
 For example, consider
 • σ_1 calls $f()$ at σ_2 , which calls $g()$ at α , which in turn calls $h()$ for σ_2 .
 • Is the completion of $h()$ a step?
 • Or the completion of $f()$?
 • Or doesn't it play a role?
 It does play a role, because **constraints/invariants** are typically (= by convention) assumed to be evaluated at step boundaries, and sometimes the convention is meant to admit (temporary) violation in between steps.

Notions of Steps: The Run-to-Completion Step

What is a **run-to-completion** step...?
 • **Intuition:** a maximal sequence of steps, where the first step is a **dispatch** step and all later steps are **commence** steps.
 • **Note:** one step corresponds to one transition in the state machine.
 A run-to-completion step is in general not syntactically definable — one transition may be taken multiple times during an RT-C-step.

Example:



References

[Harel and Gery, 1997] Harel, D. and Gery, E. (1997). Executable object modeling with statecharts. *IEEE Computer*, 30(7):31–42.
 [OMG, 2007a] OMG (2007a). Unified modeling language: Infrastructure, version 2.1.2. Technical Report formal/07-11-04.
 [OMG, 2007b] OMG (2007b). Unified modeling language: Superstructure, version 2.1.2. Technical Report formal/07-11-02.