# *Software Design, Modelling and Analysis in UML*

## *Lecture 19: Live Sequence Charts III*

*2013-01-23*

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# *Contents & Goals*

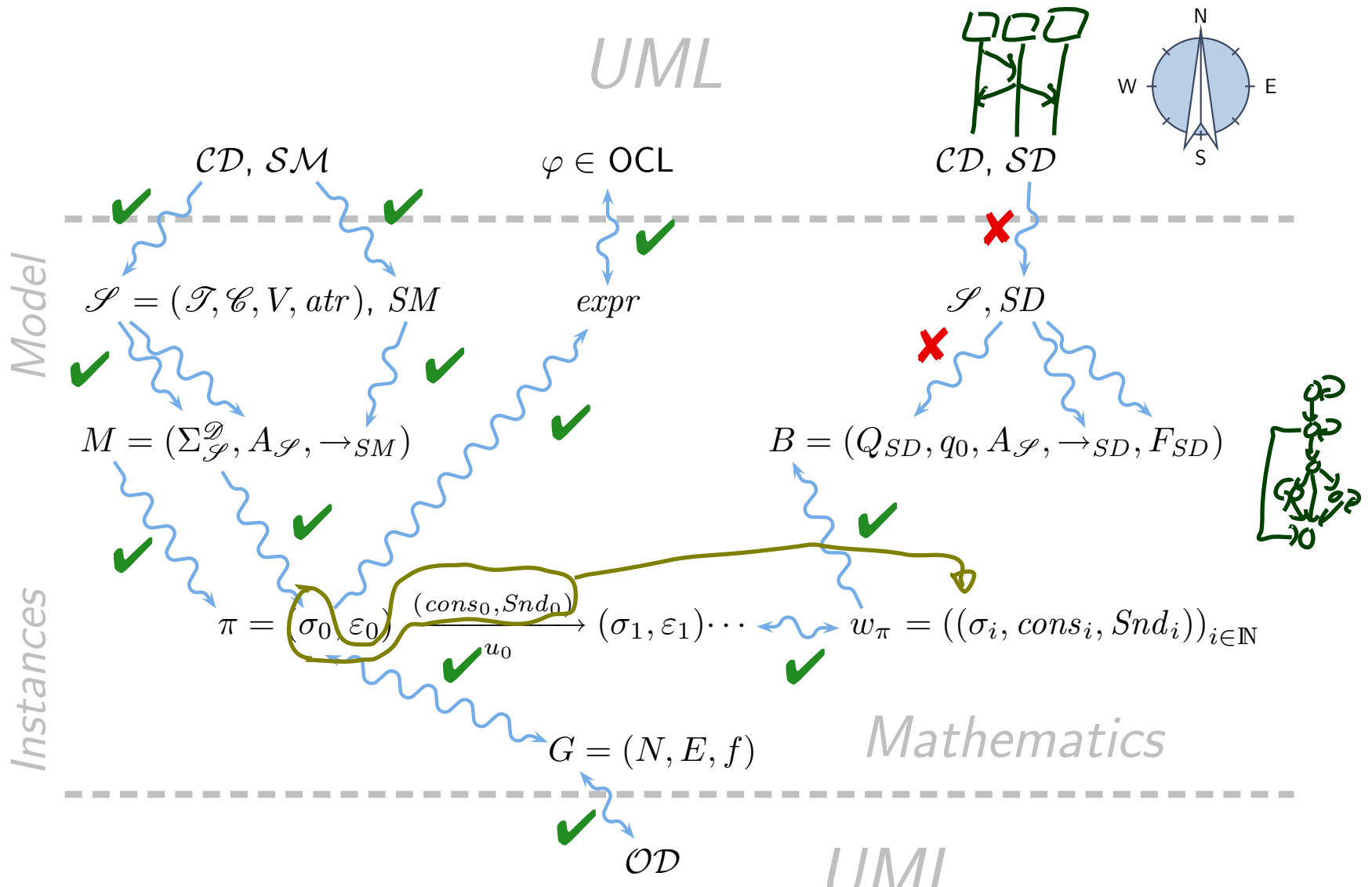
**Last Lecture:**

- Symbolic Büchi Automata (TBA) and its (accepted) language.
- Words of a model.

**This Lecture:**

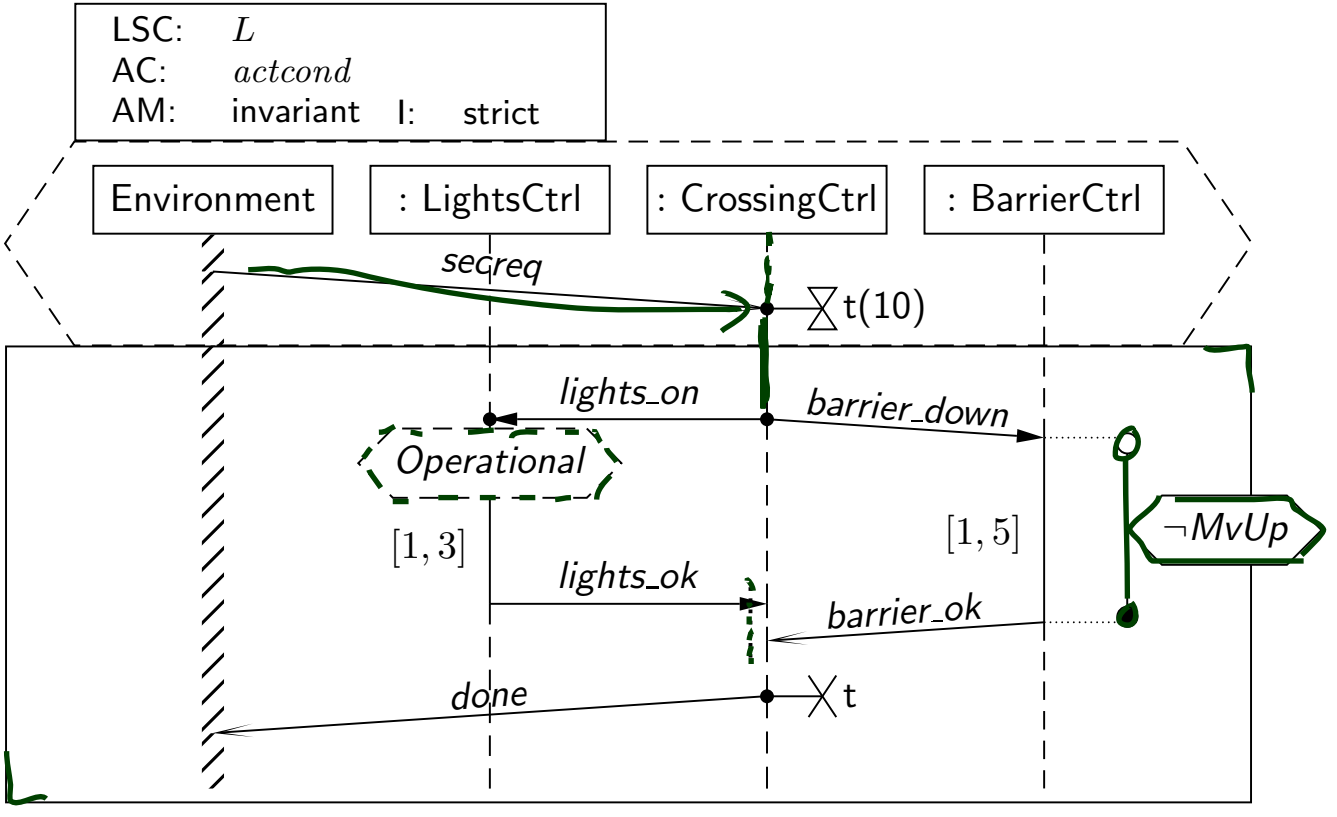
- **Educational Objectives:** Capabilities for following tasks/questions.
  - What does this LSC mean?
  - Are this UML model's state machines consistent with the interactions?
  - Please provide a UML model which is consistent with this LSC.
  - What is: activation, hot/cold condition, pre-chart, etc.?
- **Content:**
  - LSC abstract syntax.
  - LSC formal semantics.

# Course Map


UML
$\mathcal{CD}$, $\mathcal{SM}$
$\varphi \in$ OCL
$\mathcal{CD}$, $\mathcal{SD}$
N
W
E
S
Model
$\mathscr{S} = (\mathscr{T}, \mathscr{C}, V, atr)$, $SM$
$expr$
$\mathscr{S}$, $SD$
$M = (\Sigma^{\mathscr{D}}_{\mathscr{S}}, A_{\mathscr{S}}, \rightarrow_{SM})$
$B = (Q_{SD}, q_0, A_{\mathscr{S}}, \rightarrow_{SD}, F_{SD})$
Instances
$\pi = (\sigma_0, \varepsilon_0) \xrightarrow[u_0]{(cons_0, Snd_0)} (\sigma_1, \varepsilon_1) \cdots$
$w_\pi = ((\sigma_i, cons_i, Snd_i))_{i \in \mathbb{N}}$
$G = (N, E, f)$
Mathematics
$\mathcal{OD}$
UML

# *Live Sequence Charts Abstract Syntax*

# Example


LSC: $L$
AC: $actcond$
AM: invariant I: strict
Environment
: LightsCtrl
: CrossingCtrl
: BarrierCtrl
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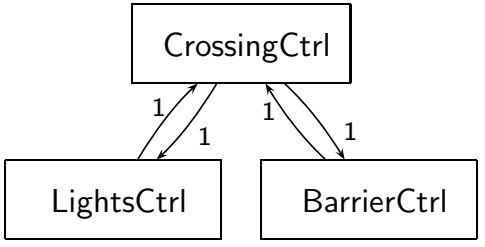
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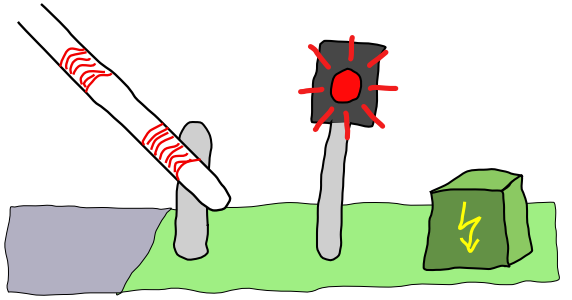
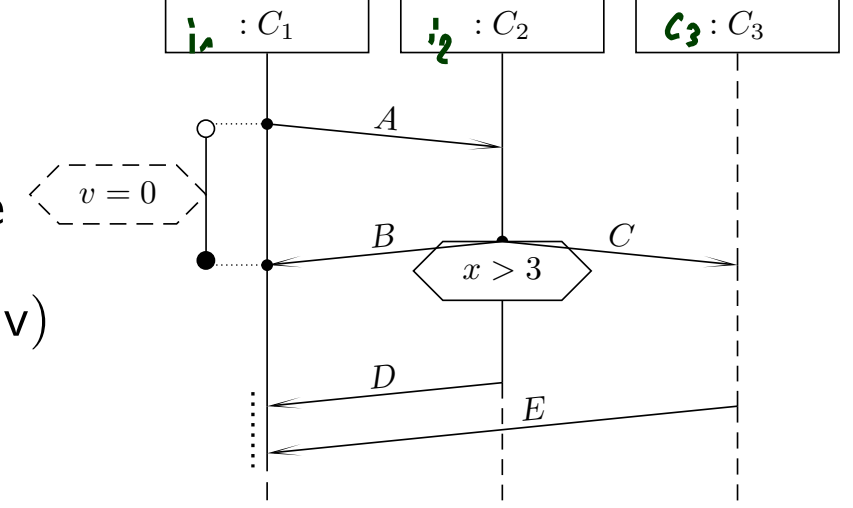


# LSC Body: Abstract Syntax

Let $\Theta = \{\text{hot}, \text{cold}\}$. An **LSC body** is a tuple

$$(I, (\mathscr{L}, \preceq), \sim, \mathscr{S}, \text{Msg}, \text{Cond}, \text{LocInv})$$

- $I$ is a finite set of **instance lines**,




$I = \{i_1, i_2, c_3\}$

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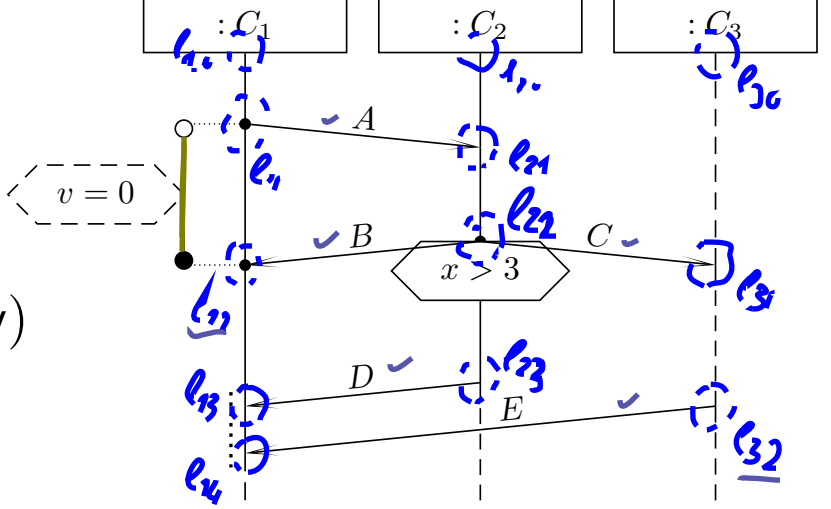
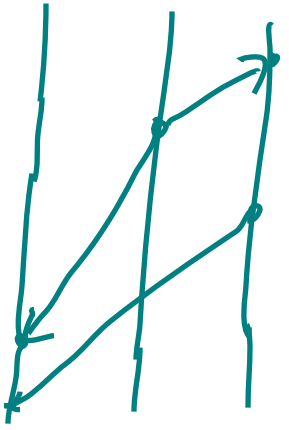
$\theta(\ell_{10}) = \text{hot}$
$\theta(\ell_{31}) = \text{cold}$
$\theta(\ell_{22}) = \text{hot}$
$\theta(\ell_{23}) = \text{cold}$
$\theta(\ell_{13}) = \text{cold}$ } one temp. for coregion
$\theta(\ell_{14}) = \text{cold}$ }

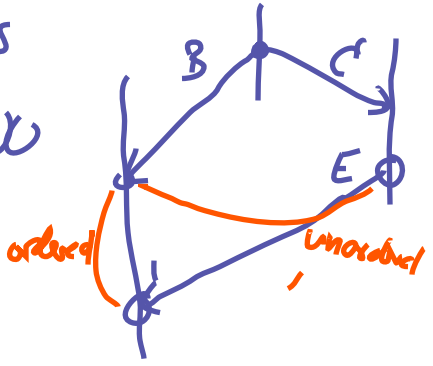



$\mathscr{L} = \{\ell_{10}, .., \ell_{14}, \ell_{20}, .., \ell_{23}, \ell_{30}, .., \ell_{32}\}$

$\preceq$: $\ell_{10} \prec \ell_{11}$, $\ell_{11} \prec \ell_{12}$, $\ell_{12} \prec \ell_{13}$, $\ell_{11} \prec \ell_{14}$
$\ell_{22} \prec \ell_{12}$, $\ell_{1} \prec \ell_{21}$, $\ell_{22} \prec \ell_{32}$,
$\ell_{20} \prec \ell_{21} \prec \ell_{22} \prec \ell_{23}$ $\quad$ $\ell_{23} \prec \ell_{31}$,
$\ell_{30} \prec \ell_{31} \prec \ell_{32}$ $\quad$ $\ell_{32} \prec \ell_{14}$

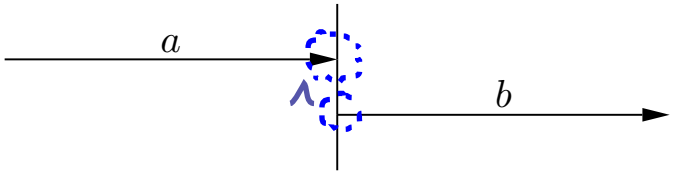


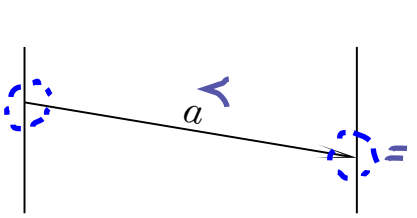
$\ell_{32} \succeq \ell_{11}$? YES
$\ell_{12} \preceq \ell_{32}$? NO

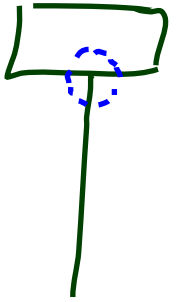


# *Recall: Intuitive Semantics*

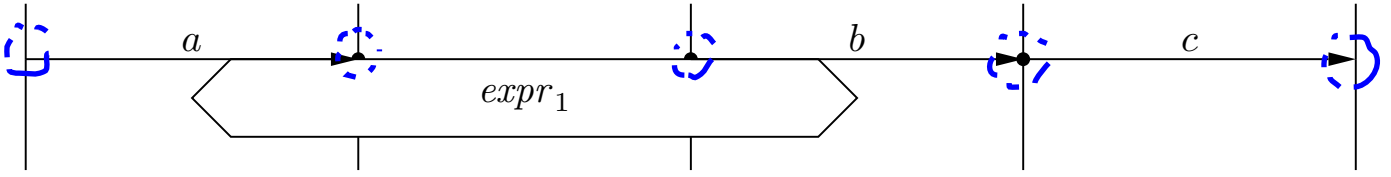
(i) **Strictly After:**



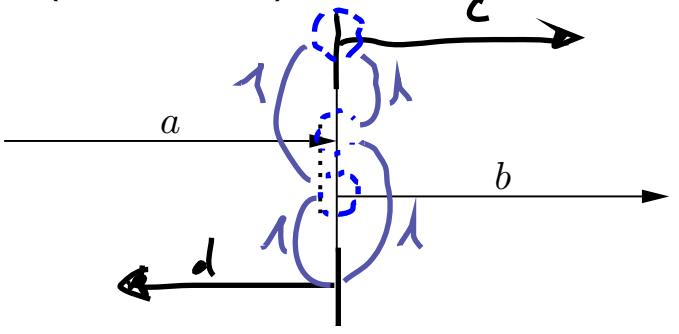



(ii) **Simultaneously:** (simultaneous region)




(iii) **Explicitly Unordered:** (co-region)




**Intuition:** A computation path **violates** an LSC if the occurrence of some events doesn't adhere to the partial order obtained as the **transitive closure** of (i) to (iii).

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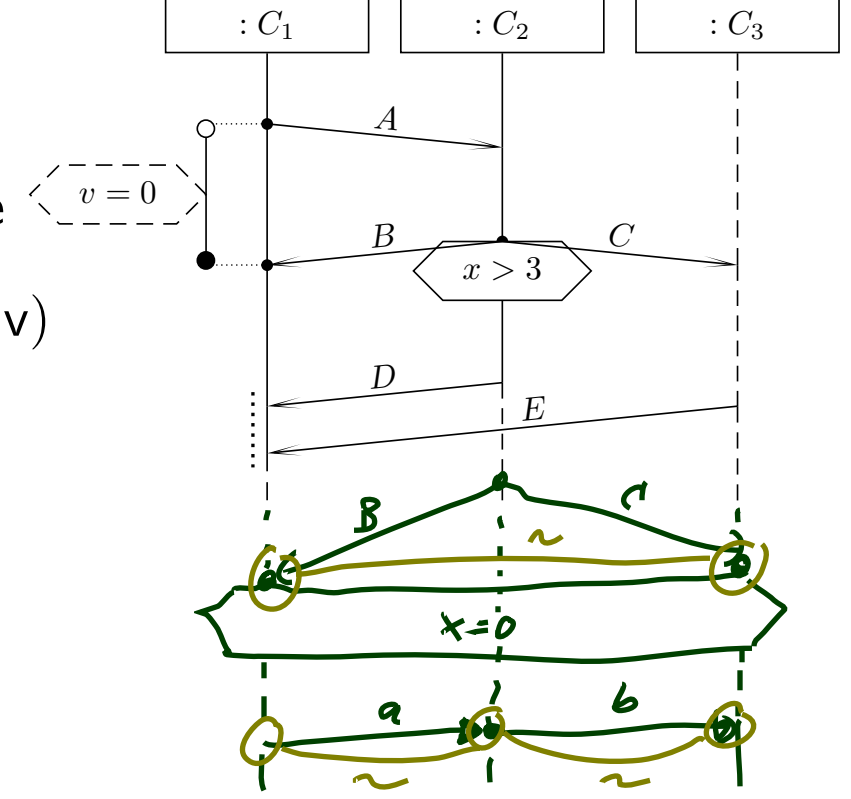

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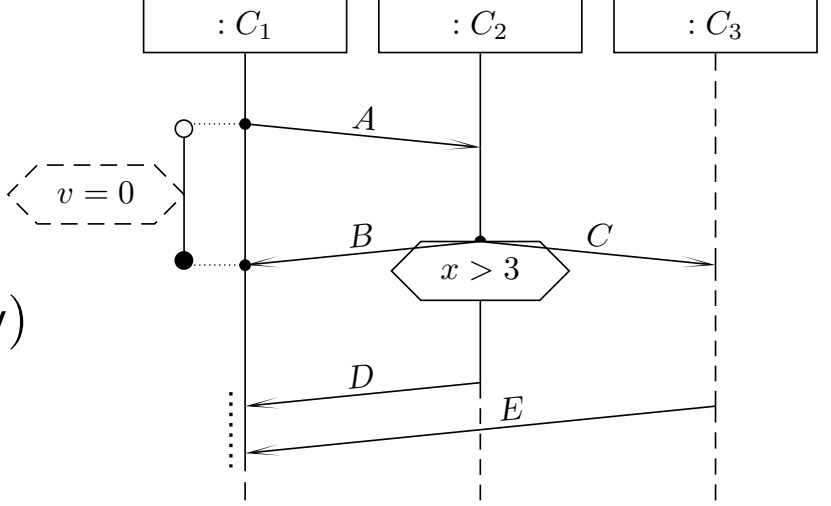


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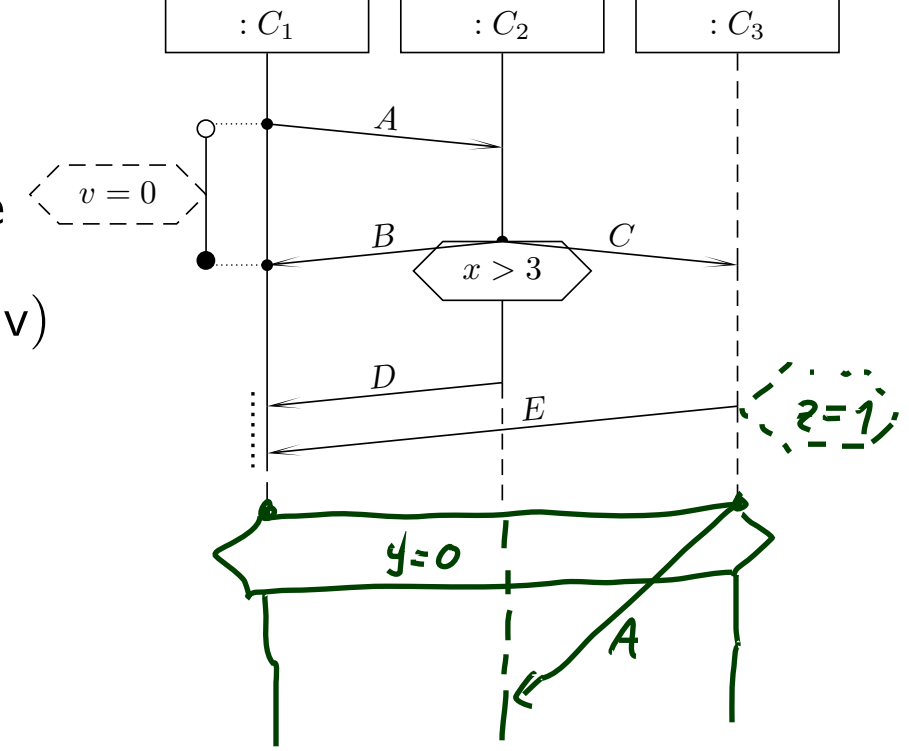
- $\mathscr{S} = (\mathscr{T}, \mathscr{C}, V, atr, \mathscr{E})$ is a signature,
- $\text{Msg} \subseteq \mathscr{L} \times \mathscr{E} \times \mathscr{L}$ is a set of **asynchronous messages** with $(l, b, l') \in \text{Msg}$ only if $l \preceq l'$, **Not**: **instantaneous messages** — could be linked to method/operation calls.

$\text{Msg} = \{ (\ell_{11}, A, \ell_{12}),$
$(\ell_{13}, B, \ell_{02}),$
$(\ell_{13}, C, \ell_{21}),$
$(\ell_{23}, D, \ell_{03}),$
$(\ell_{12}, E, \ell_{04}) \}$

# LSC Body: Abstract Syntax

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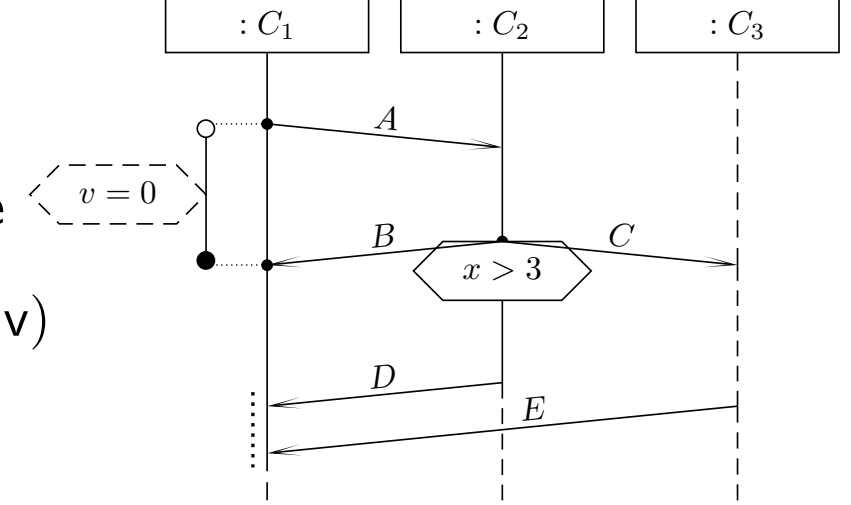
- $\text{Cond} \subseteq (2^{\mathscr{L}} \setminus \emptyset) \times Expr_{\mathscr{S}} \times \Theta$ is a set of **conditions** where $Expr_{\mathscr{S}}$ are OCL expressions over $W = I \cup \{self\}$ with $(L, expr, \theta) \in \text{Cond}$ only if $l \sim l'$ for all $l, l' \in L$,

Cond = { ({$l_{12}$}, x>3, hot),
({$l_{22}$}, z=1, cold),
({$l_{05}, l_{23}$}, y=0, hot) }

# LSC Body: Abstract Syntax

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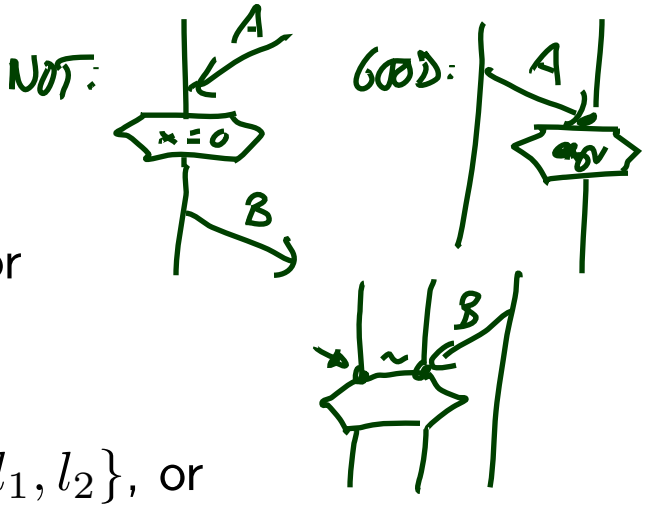
- $\text{LocInv} \subseteq \mathscr{L} \times \{\circ, \bullet\} \times Expr_{\mathscr{S}} \times \Theta \times \mathscr{L} \times \{\circ, \bullet\}$ is a set of **local invariants**,

$\text{LocInv} = \{(l_{01}, \circ, v=0, \text{cold}, l_{02}, \bullet)\}$

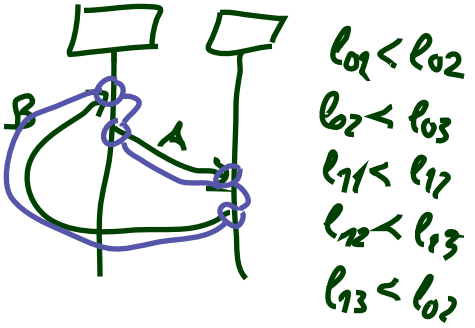
# *Well-Formedness*

**Bondedness/no floating conditions**: (could be relaxed a little if we wanted to)



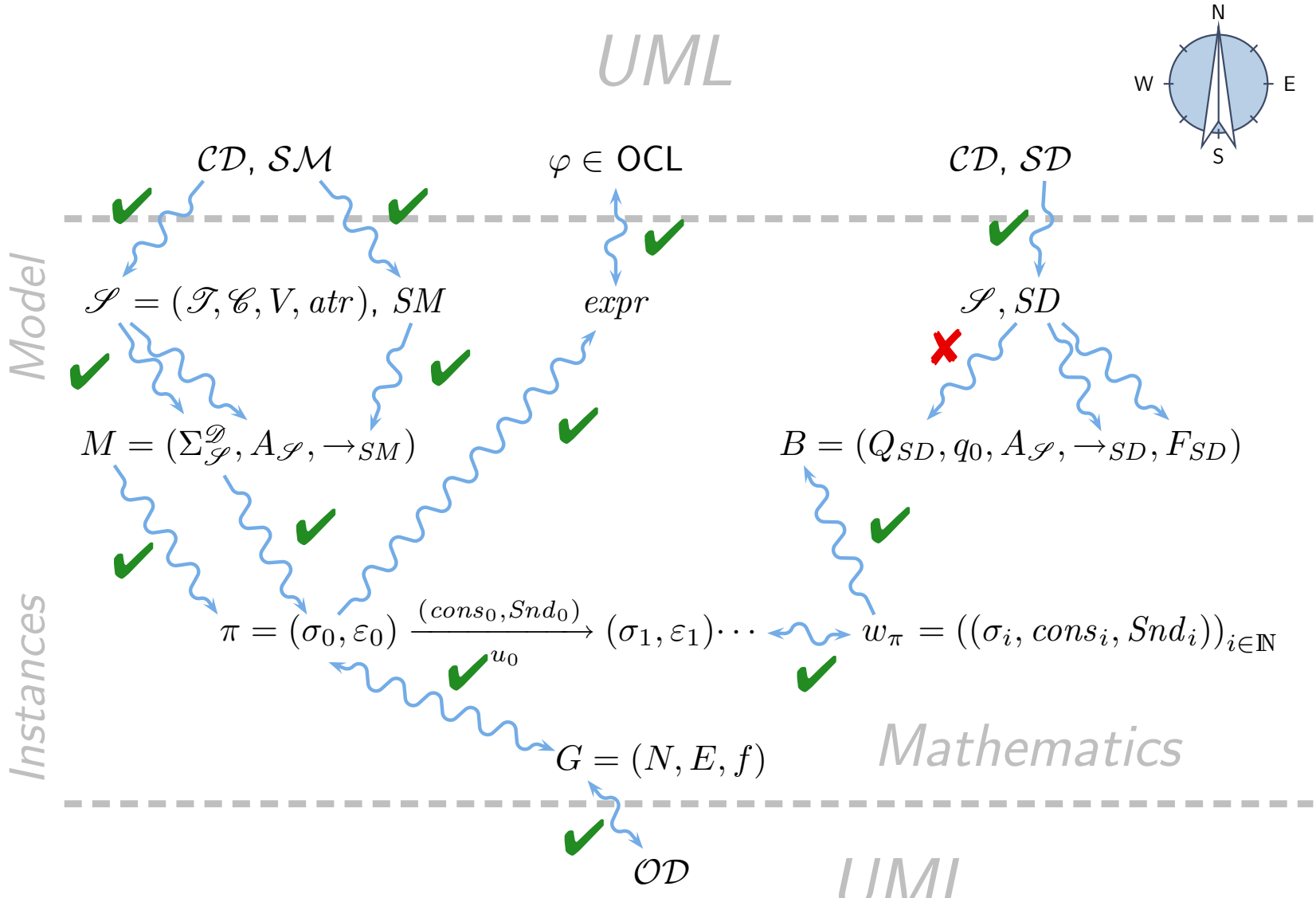

- For each location $l \in \mathscr{L}$, **if** $l$ is the location of
  - a **condition**, i.e.
    $$\exists\,(L, expr, \theta) \in \mathsf{Cond} : l \in L, \text{ or}$$
  - a **local invariant**, i.e.
    $$\exists\,(l_1, i_1, expr, \theta, l_2, i_2) \in \mathsf{LocInv} : l \in \{l_1, l_2\}, \text{ or}$$

  **then** there is a location $l'$ **equivalent** to $l$, i.e. $l \sim l'$, which is the location of
  - an **instance head**, i.e. $l'$ is minimal wrt. $\preceq$, or
  - a **message**, i.e.
    $$\exists\,(l_1, b, l_2) \in \mathsf{Msg} : l \in \{l_1, l_2\}.$$




**Note**: if messages in a chart are **cyclic**, then there doesn't exist a partial order (so such charts **don't even have** an abstract syntax).

# Course Map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UML

# *Live Sequence Charts Semantics*

# *TBA-based Semantics of LSCs*

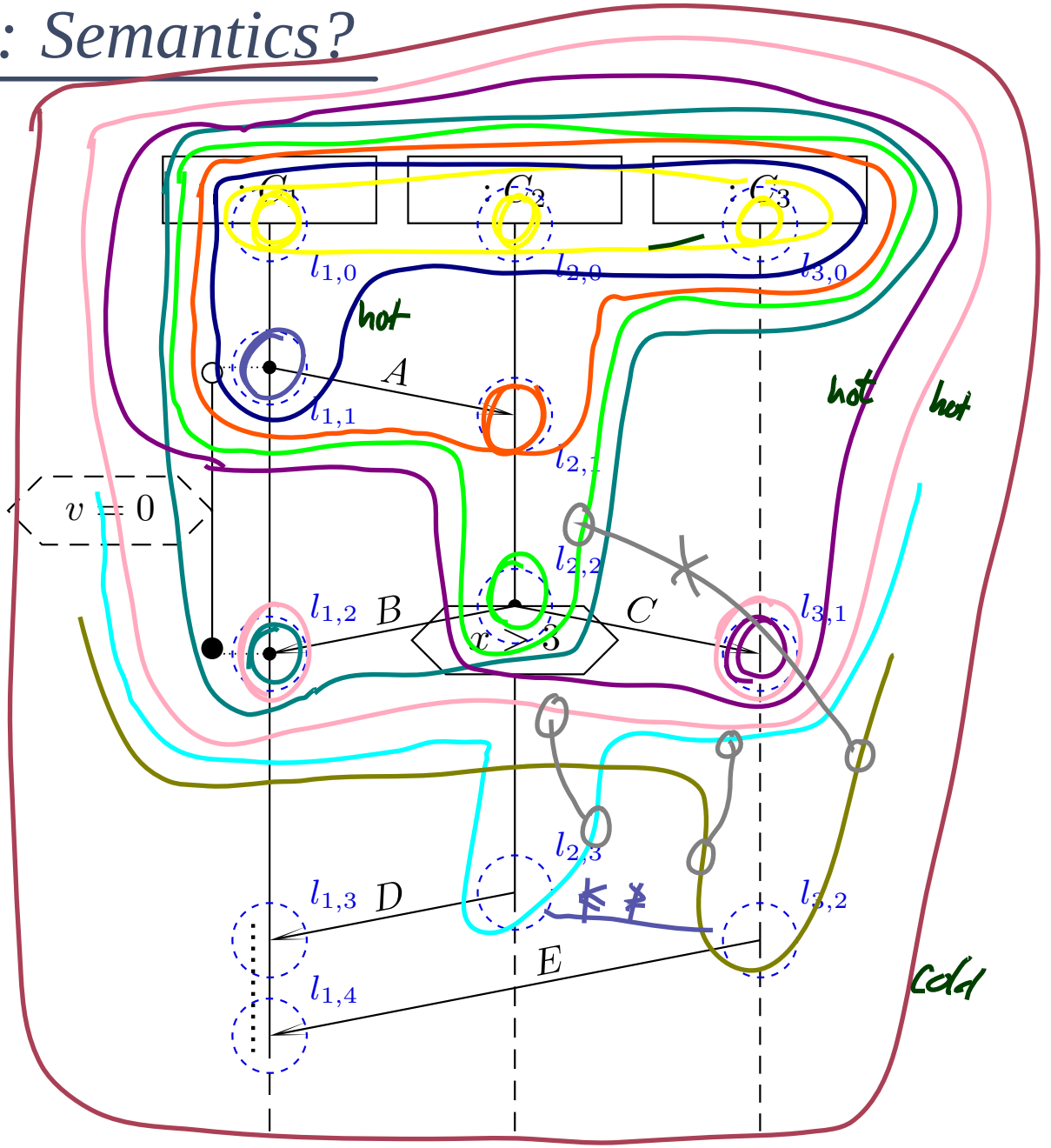
**Plan**:

- Given an LSC $L$ with body

$$(I, (\mathscr{L}, \preceq), \sim, \mathscr{S}, \mathsf{Msg}, \mathsf{Cond}, \mathsf{LocInv}),$$

- construct a TBA $\mathcal{B}_L$, and
- define $\mathcal{L}(L)$ **in terms of** $\mathcal{L}(\mathcal{B}_L)$,
  in particular taking activation condition and activation mode into account.
- Then $\mathcal{M} \models L$ (universal) if and only if $\mathcal{L}(\mathcal{M}) \subseteq \mathcal{L}(L)$.

# Examples: Semantics?



# *Formal LSC Semantics: It's in the Cuts!*

**Definition.**
Let $(I, (\mathscr{L}, \preceq), \sim, \mathscr{S}, \mathsf{Msg}, \mathsf{Cond}, \mathsf{LocInv})$ be an LSC body.

A non-empty set $\emptyset \neq C \subseteq \mathscr{L}$ is called a **cut** of the LSC body iff

- it is **downward closed**, i.e.

$$\forall\, l, l' : l' \in C \wedge l \preceq l' \implies l \in C,$$

- it is **closed** under **simultaneity**, i.e.

$$\forall\, l, l' : l' \in C \wedge l \sim l' \implies l \in C, \text{ and}$$

- it comprises at least **one location per instance line**, i.e.

$$\forall\, i \in I\ \exists\, l \in C : i_l = i.$$

A cut $C$ is called **hot**, denoted by $\theta(C) = \mathsf{hot}$, if and only if at least one of its maximal elements is hot, i.e. if

$$\exists\, l \in C : \theta(l) = \mathsf{hot} \wedge \nexists\, l' \in C : l \prec l'$$

Otherwise, $C$ is called **cold**, denoted by $\theta(C) = \mathsf{cold}$.

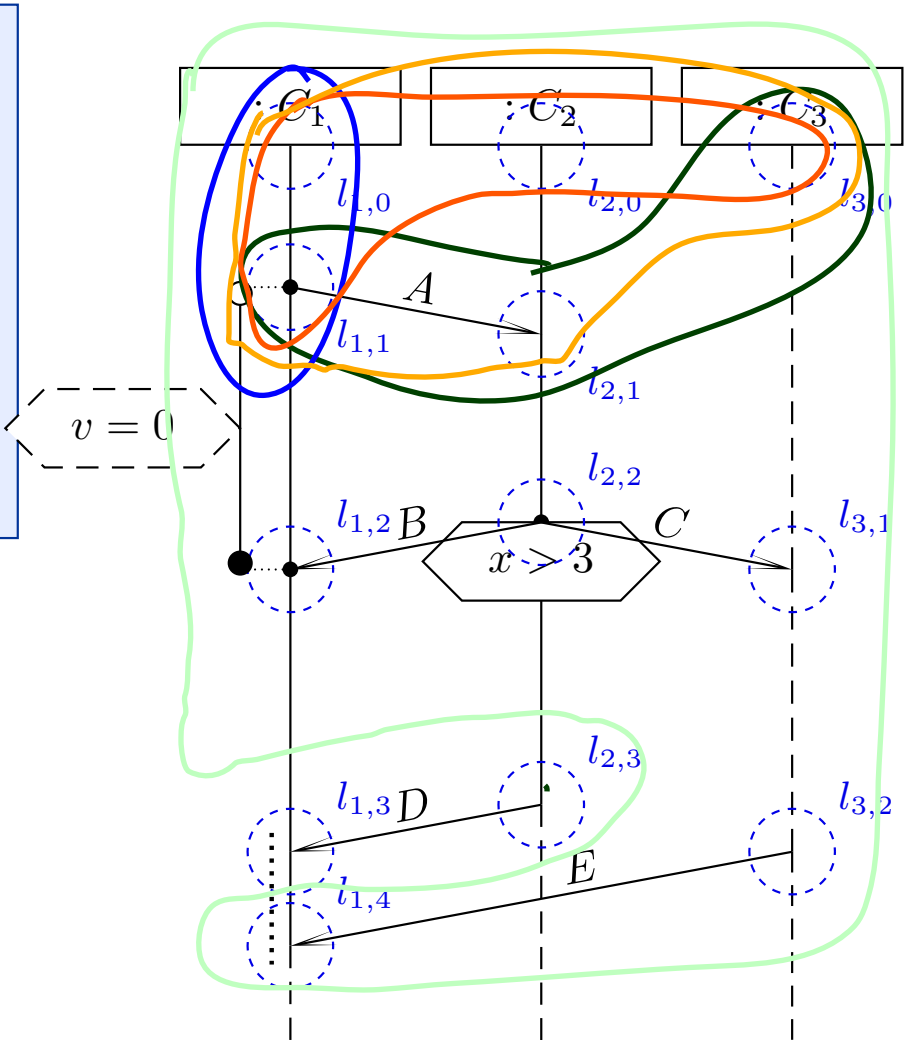
# *Examples: Cut or Not Cut? Hot/Cold?*

(i) **non-empty** set $\emptyset \neq C \subseteq \mathscr{L}$,

(ii) **downward closed**, i.e.
$\forall\, l, l' : l' \in C \wedge l \preceq l' \implies l \in C$

(iii) **closed** under **simultaneity**, i.e.
$\forall\, l, l' : l' \in C \wedge l \sim l' \implies l \in C$

(iv) at least **one location per instance line**, i.e.
$\forall\, i \in I\ \exists\, l \in C : i_l = i$,




- $C_0 = \emptyset$ NO
- $C_1 = \{l_{1,0}, l_{2,0}, l_{3,0}\}$ ✓
- $C_2 = \{l_{1,1}, l_{2,1}, l_{3,0}\}$ NO
- $C_3 = \{l_{1,0}, l_{1,1}\}$ NO
- $C_4 = \{l_{1,0}, l_{1,1}, l_{2,0}, l_{3,0}\}$ ✓
- $C_5 = \{l_{1,0}, l_{1,1}, l_{2,0}, l_{2,1}, l_{3,0}\}$ ✓
- $C_6 = \mathscr{L} \setminus \{l_{1,3}, l_{2,3}\}$ ✓
- $C_7 = \mathscr{L}$ ✓

# A Successor Relation on Cuts

The partial order of $(\mathscr{L}, \preceq)$ and the simultaneity relation "$\sim$" induce a **direct successor relation** on cuts of $\mathscr{L}$ as follows:

**Definition.** Let $C, C' \subseteq \mathscr{L}$ bet cuts of an LSC body with locations $(\mathscr{L}, \preceq)$ and messages Msg.
$C'$ is called **direct successor** of $C$ **via fired-set** $F$, denoted by $C \rightsquigarrow_F C'$, if and only if

- $F \neq \emptyset$,
- $C' \setminus C = F$,
- for each message reception in $F$, the corresponding sending is already in $C$,

$$\forall\, (l, E, l') \in \text{Msg} : l' \in F \implies l \in C, \text{ and}$$

- locations in $F$, that lie on the same instance line, are pairwise unordered, i.e.

$$\forall\, l, l' \in F : l \neq l' \wedge i_l = i_{l'} \implies l \not\preceq l' \wedge l' \not\preceq l$$

# *Properties of the Fired-set*

$C \rightsquigarrow_F C'$ if and only if

- $F \neq \emptyset$,
- $C' \setminus C = F$,
- $\forall\, (l, E, l') \in \text{Msg} : l' \in F \implies l \in C$, and
- $\forall\, l, l' \in F : l \neq l' \wedge i_l = i_{l'} \implies l \not\preceq l' \wedge l' \not\preceq l$

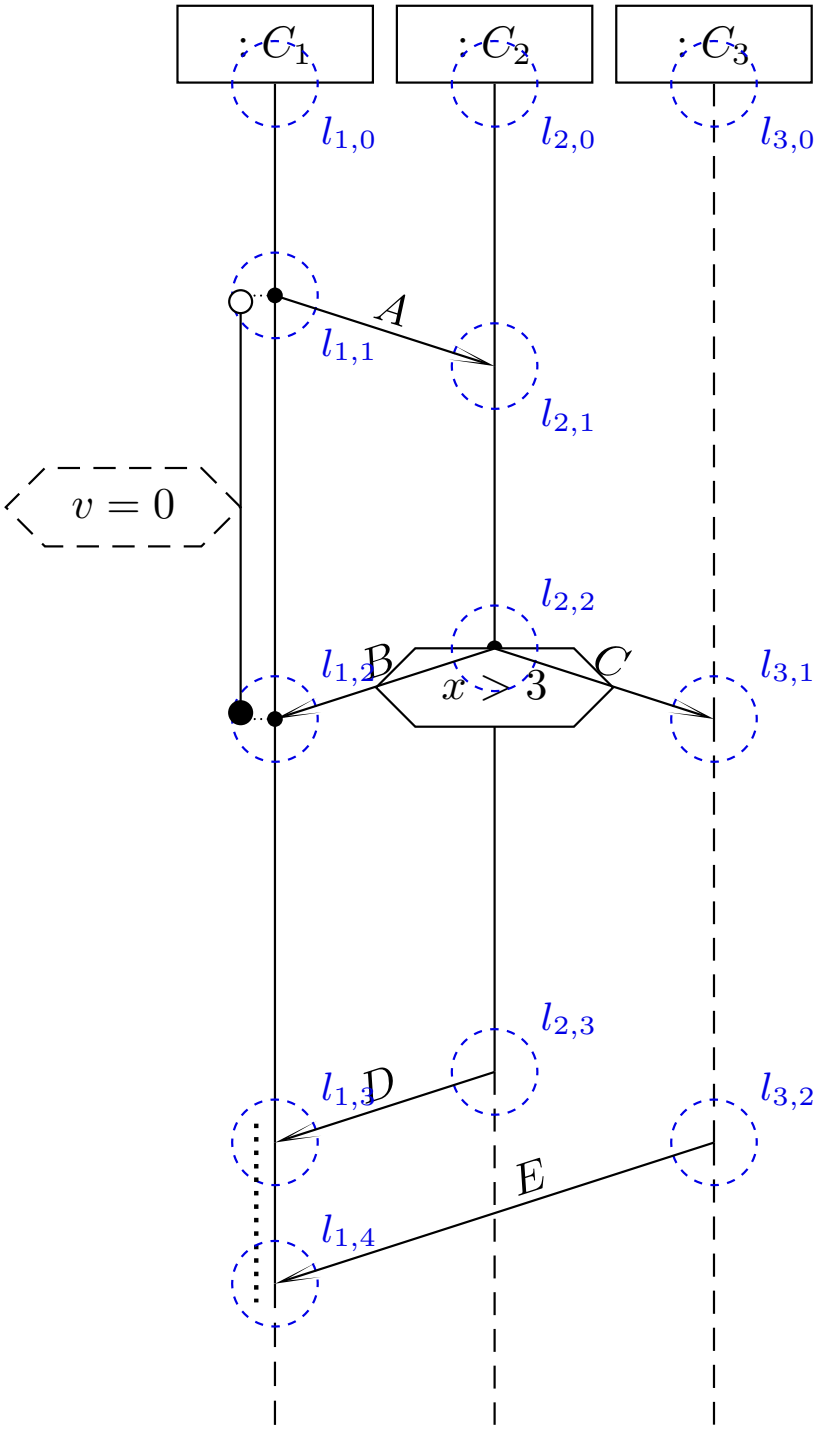
- **Note**: $F$ is closed under simultaneity.
- **Note**: locations in $F$ are direct $\preceq$-successors of locations in $C$, i.e.

$$\forall\, l' \in F\ \exists\, l \in C : l \prec l' \wedge \nexists\, l'' \in C : l' \prec l'' \prec l$$

# Successor Cut Examples

(i) $F \neq \emptyset$, (ii) $C' \setminus C = F$,
(iii) $\forall\,(l, E, l') \in \mathsf{Msg} : l' \in F \implies l \in C$, and
(iv) $\forall\, l, l' \in F : l \neq l' \wedge i_l = i_{l'} \implies l \not\preceq l' \wedge l' \not\preceq l$

see Slide 12



# *Idea: Accept Timed Words by Advancing the Cut*

- Let $w = (\sigma_0, cons_0, Snd_0), (\sigma_1, cons_1, Snd_1), (\sigma_2, cons_2, Snd_2), \ldots$ be a word of a UML model and $\beta$ a valuation of $I \cup \{self\}$.

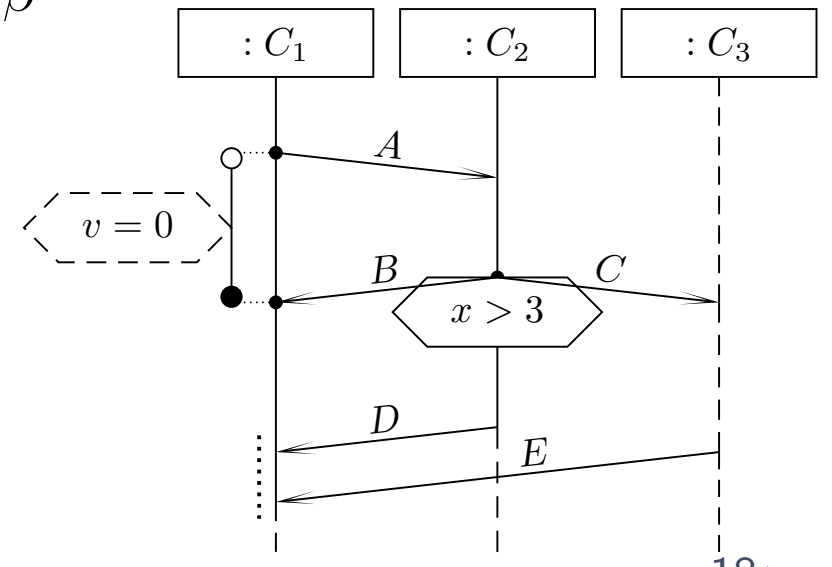
- **Intuitively** (and for now **disregarding** cold conditions),

  an LSC body $(I, (\mathscr{L}, \preceq), \sim, \mathscr{S}, \mathsf{Msg}, \mathsf{Cond}, \mathsf{LocInv})$
  is **supposed** to **accept** $w$ if and only if there exists a sequence

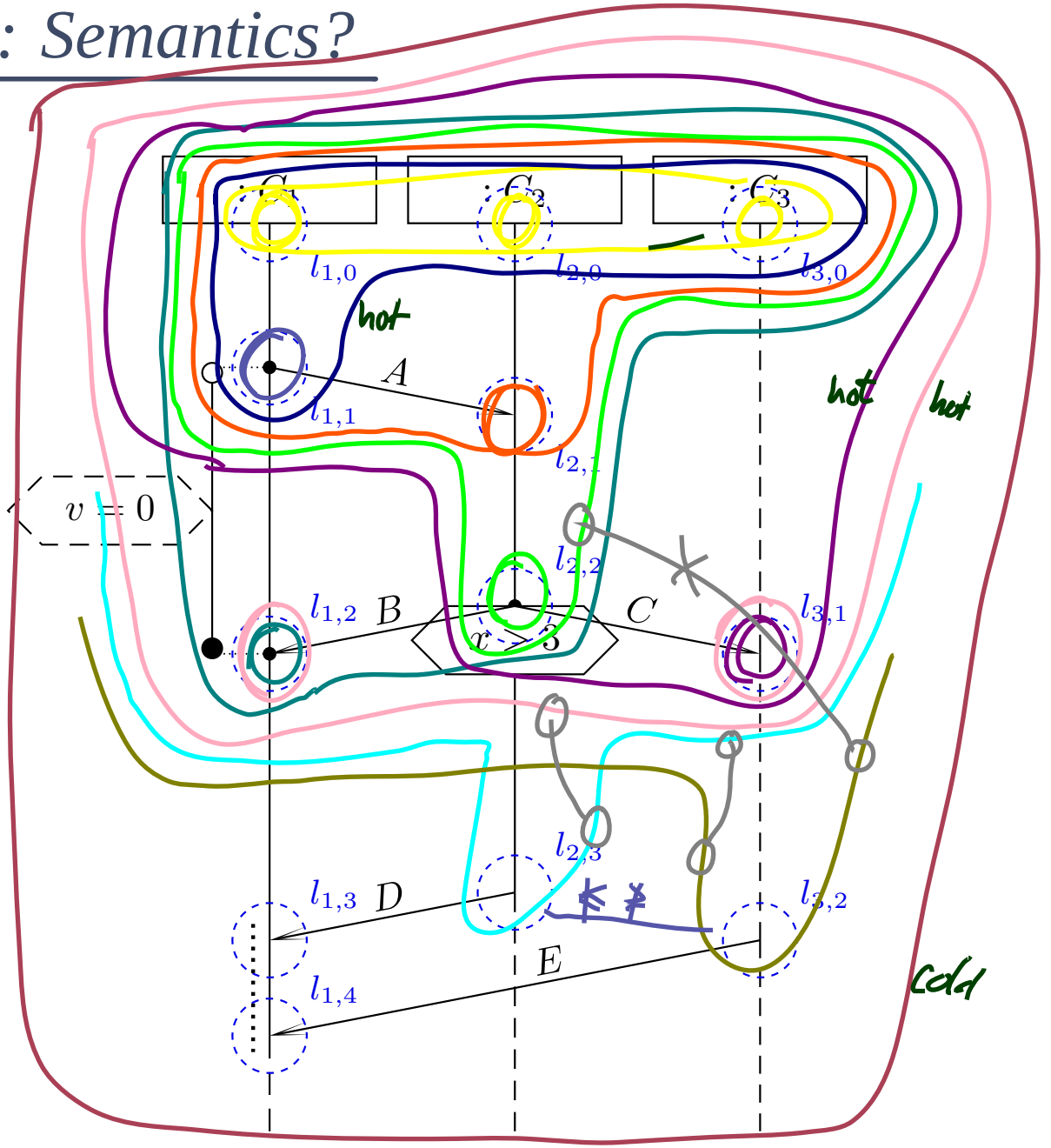
$$C_0 \rightsquigarrow_{F_1} C_1 \rightsquigarrow_{F_2} C_2 \cdots \rightsquigarrow_{F_n} C_n$$

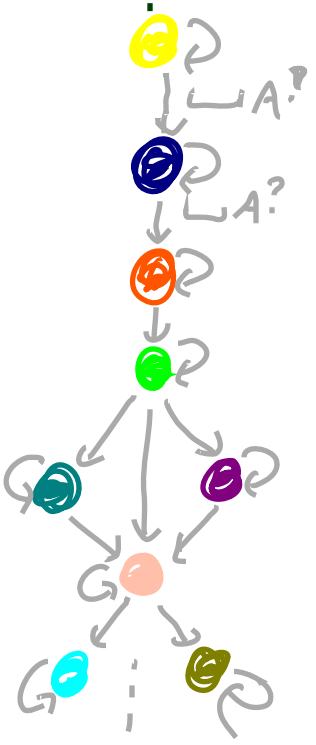
  and indices $0 = i_0 < i_1 < \cdots < i_n$ such that for all $0 \leq j < n$,

  - for all $i_j \leq k < i_{j+1}$, $(\sigma_k, cons_k, Snd_k)$, $\beta$ satisfies the **hold condition** of $C_j$,
  - $(\sigma_{i_j}, cons_{i_j}, Snd_{i_j})$, $\beta$ satisfies the **transition condition** of $F_j$,
  - $C_n$ is cold,
  - for all $i_n < k$, $(\sigma_k, cons_{i_j}, Snd_{i_j})$, $\beta$ satisfies the **hold condition** of $C_n$.



# Examples: Semantics?



# *Language of LSC Body*

The **language** of the body

$$(I, (\mathscr{L}, \preceq), \sim, \mathscr{S}, \text{Msg}, \text{Cond}, \text{LocInv})$$

of LSC $L$ is the language of the TBA

$$\mathcal{B}_L = (Expr_{\mathcal{B}}(X), X, Q, q_{ini}, \rightarrow, Q_F)$$

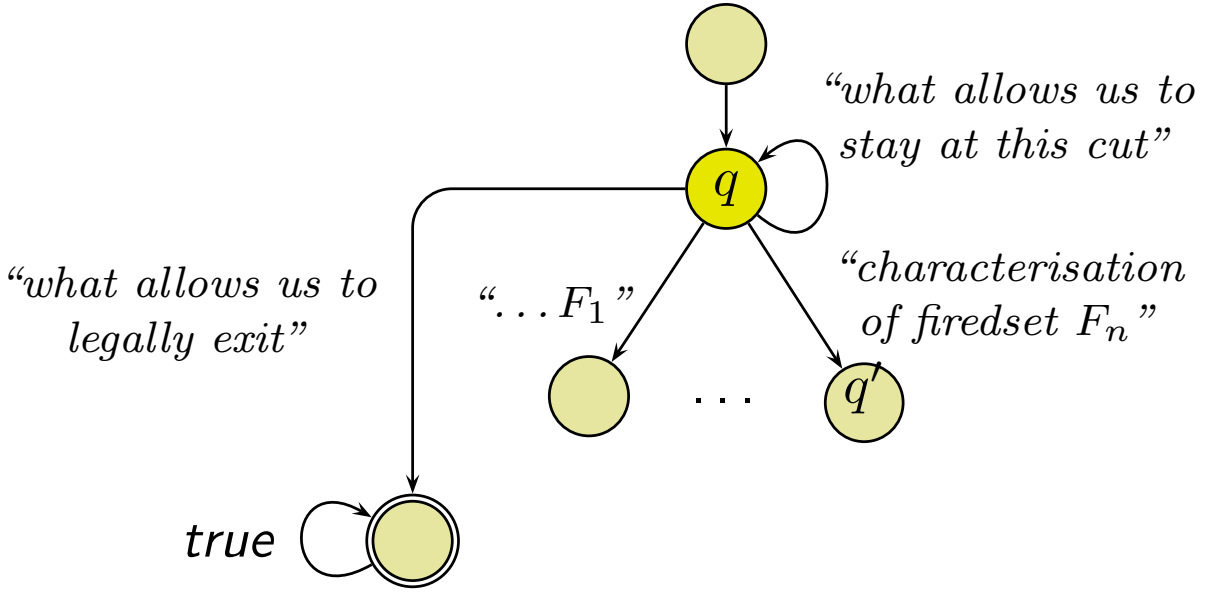
with

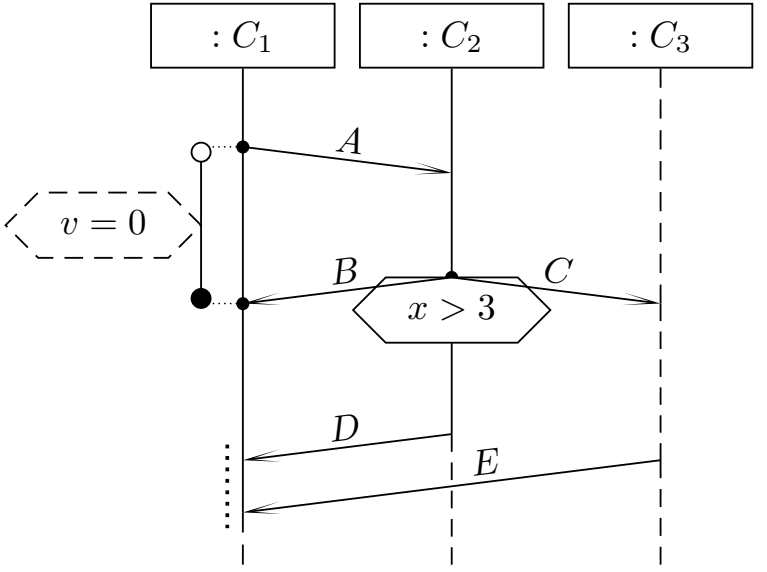
- $Expr_{\mathcal{B}}(X) = Expr_{\mathscr{S}}(\mathscr{S}, X)$
- $Q$ is the set of cuts of $(\mathscr{L}, \preceq)$, $q_{ini}$ is the **instance heads** cut,
- $F = \{C \in Q \mid \theta(C) = \text{cold}\}$ is the set of cold cuts of $(\mathscr{L}, \preceq)$,
- $\rightarrow$ as defined in the following, consisting of
  - **loops** $(q, \psi, q)$,
  - **progress transitions** $(q, \psi, q')$ corresponding to $q \rightsquigarrow_F q'$, and
  - **legal exits** $(q, \psi, \mathscr{L})$.

# *Language of LSC Body: Intuition*

$\mathcal{B}_L = (Expr_{\mathcal{B}}(X), X, Q, q_{ini}, \rightarrow, Q_F)$ with

- $Expr_{\mathcal{B}}(X) = Expr_{\mathscr{S}}(\mathscr{S}, X)$
- $Q$ is the set of cuts of $(\mathscr{L}, \preceq)$, $q_{ini}$ is the **instance heads** cut,
- $F = \{C \in Q \mid \theta(C) = \text{cold}\}$ is the set of cold cuts,
- $\rightarrow$ consists of
  - **loops** $(q, \psi, q)$,
  - **progress transitions** $(q, \psi, q')$ corresponding to $q \rightsquigarrow_F q'$, and
  - **legal exits** $(q, \psi, \mathscr{L})$.



# *Step I: Only Messages*

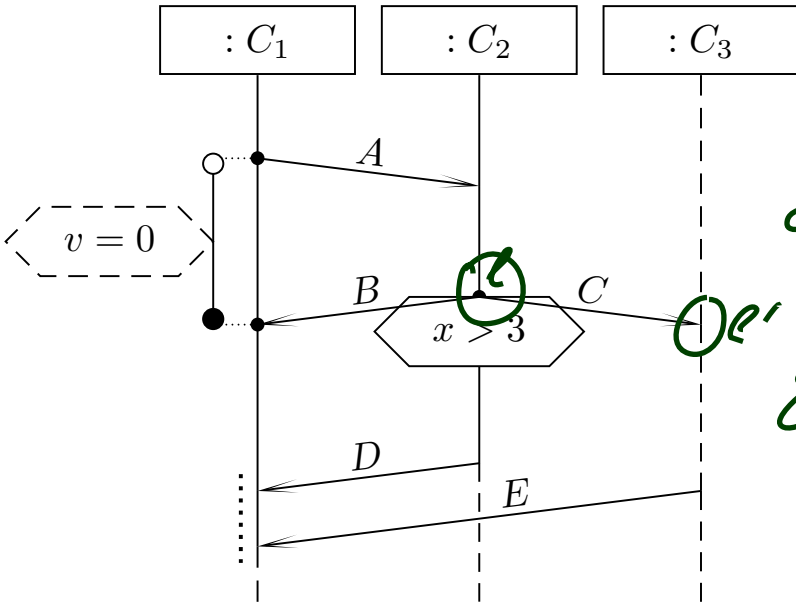
# Some Helper Functions

- **Message-expressions of a location**:

$$\mathscr{E}(l) := \{E^{!}_{i_l,i_{l'}} \mid (l, E, l') \in \mathsf{Msg}\} \cup \{E^{?}_{i_{l'},i_l} \mid (l', E, l) \in \mathsf{Msg}\},$$

$$\mathscr{E}(\{l_1, \ldots, l_n\}) := \mathscr{E}(l_1) \cup \cdots \cup \mathscr{E}(l_n).$$

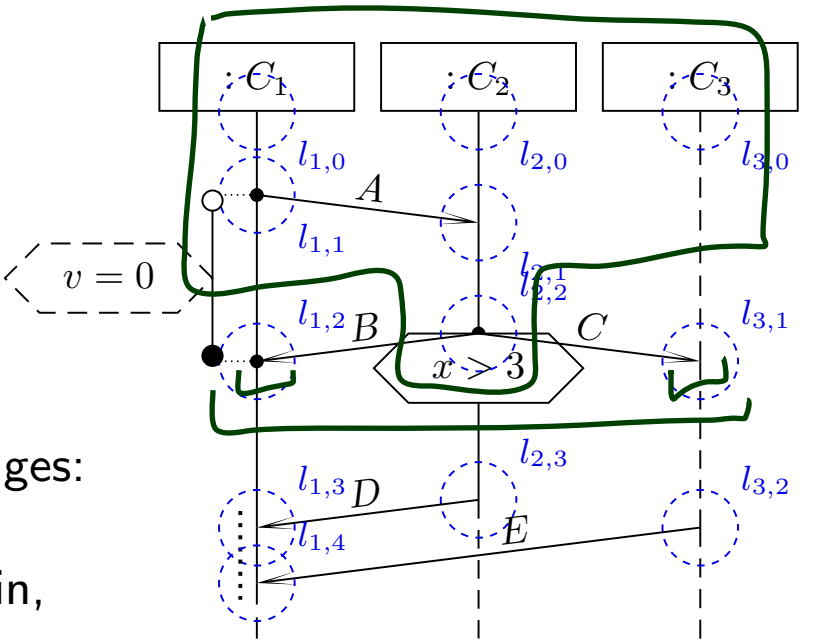
$$\bigvee \emptyset := \mathit{true}; \bigvee \{E_1{}^{!}_{i_{11},i_{12}}, \ldots F_k{}^{?}_{i_{k1},i_{k2}}, \ldots\} := \bigvee_{1 \le j < k} E_j{}^{!}_{i_{j1},i_{j2}} \vee \bigvee_{k \le j} F_j{}^{?}_{i_{j1},i_{j2}}$$




$\mathcal{E}(\ell) = \{ B^{!}_{i_2,i_1}, C^{!}_{i_2,i_3} \}$

$\mathcal{E}(\ell') = \{ C^{?}_{i_2,i_3} \}$

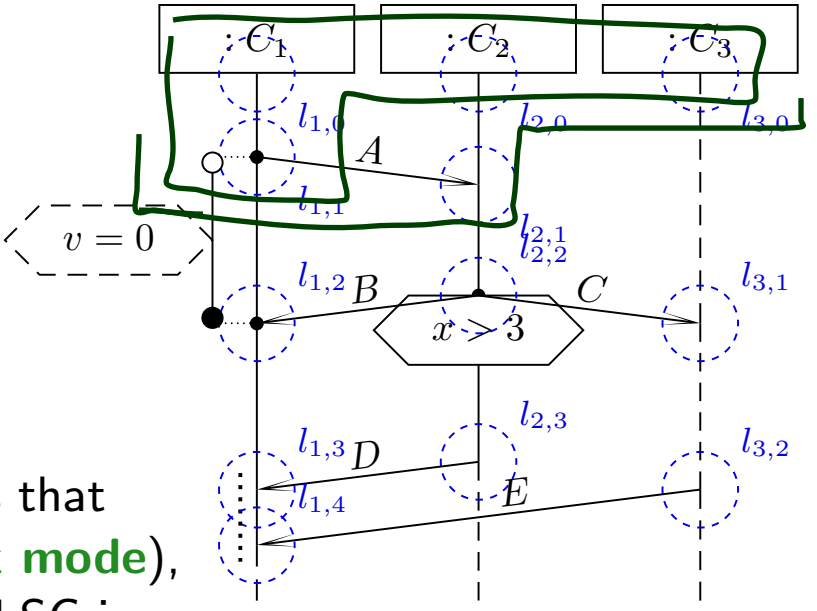
# Loops




- How long may we **legally** stay at a cut $q$?
- **Intuition**: those $(\sigma_i, cons_i, Snd_i)$ are allowed to fire the self-loop $(q, \psi, q)$ where
  - $cons_i \cup Snd_i$ comprises only irrelevant messages:
    - **weak mode**:
      no message from a direct successor cut is in,
    - **strict mode**:
      no message occurring in the LSC is in,
  - $\sigma_i$ satisfies the local invariants active at $q$

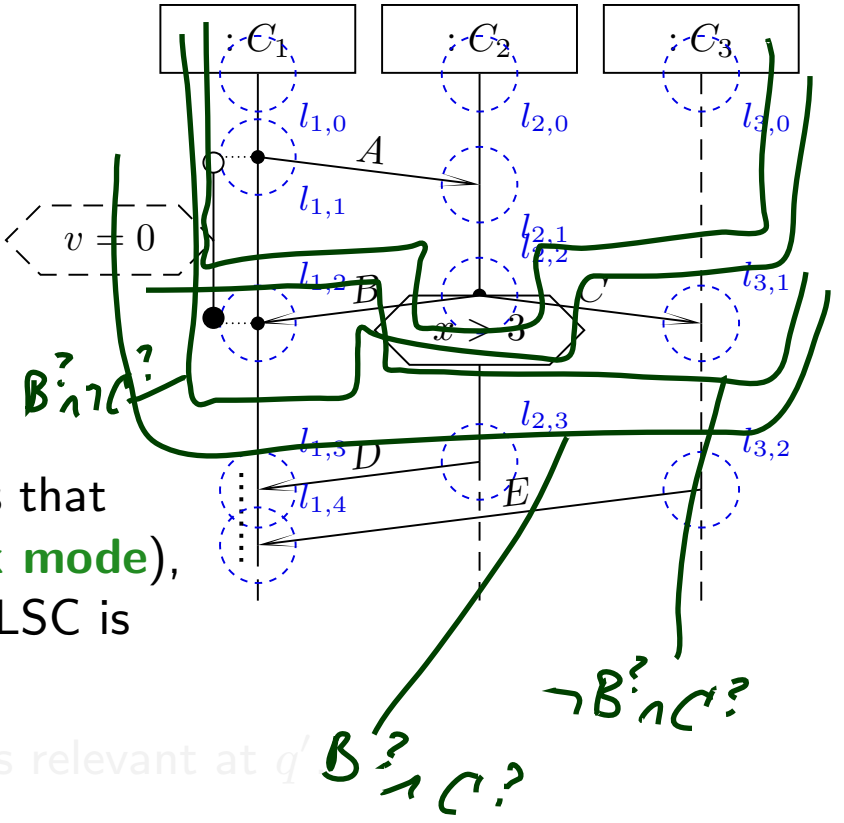
  And nothing else.
- **Formally**: Let $F := F_1 \cup \cdots \cup F_n$ be the union of the firedsets of $q$.
  - $\psi := \underbrace{\neg(\bigvee \mathscr{E}(F))}_{=\mathit{true}\text{ if }F=\emptyset} \wedge \bigwedge \psi(q).$

# Progress




- When do we move from $q$ to $q'$?
- **Intuition**: those $(\sigma_i, cons_i, Snd_i)$ fire the progress transition $(q, \psi, q')$ for which there exists a firedset $F$ such that $q \rightsquigarrow_F q'$ and
  - $cons_i \cup Snd_i$ comprises exactly the messages that distinguish $F$ from other firedsets of $q$ (**weak mode**), and in addition no message occurring in the LSC is in $cons_i \cup Snd_i$ (**strict mode**),
  - $\sigma_i$ satisfies the local invariants and conditions relevant at $q'$.

# Progress




- When do we move from $q$ to $q'$?
- **Intuition**: those $(\sigma_i, cons_i, Snd_i)$ fire the progress transition $(q, \psi, q')$ for which there exists a firedset $F$ such that $q \rightsquigarrow_F q'$ and
  - $cons_i \cup Snd_i$ comprises exactly the messages that distinguish $F$ from other firedsets of $q$ (**weak mode**), and in addition no message occurring in the LSC is in $cons_i \cup Snd_i$ (**strict mode**),
  - $\sigma_i$ satisfies the local invariants and conditions relevant at $q'$
- **Formally**: Let $F, F_1, \ldots, F_n$ be the firedsets of $q$ and let $q \rightsquigarrow_F q'$ (unique).
  - $\psi := \bigwedge \mathscr{E}(F) \wedge \neg\big(\bigvee\big(\mathscr{E}(F_1) \cup \cdots \cup \mathscr{E}(F_n)\big) \setminus \mathscr{E}(F)\big) \wedge \bigwedge \psi(q, q')$.

# *Step II: Conditions and Local Invariants*

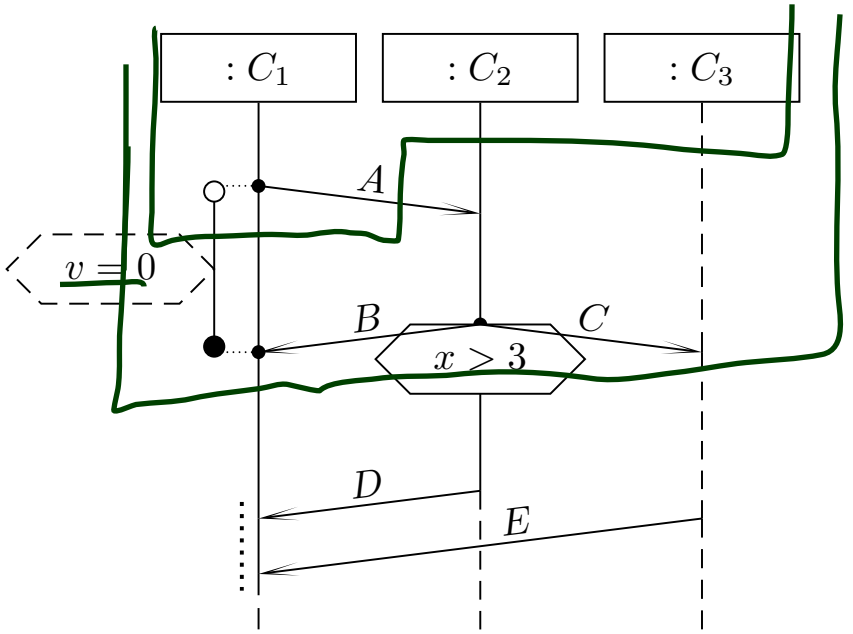
# *Some More Helper Functions*

- **Constraints** relevant **at** cut $q$:

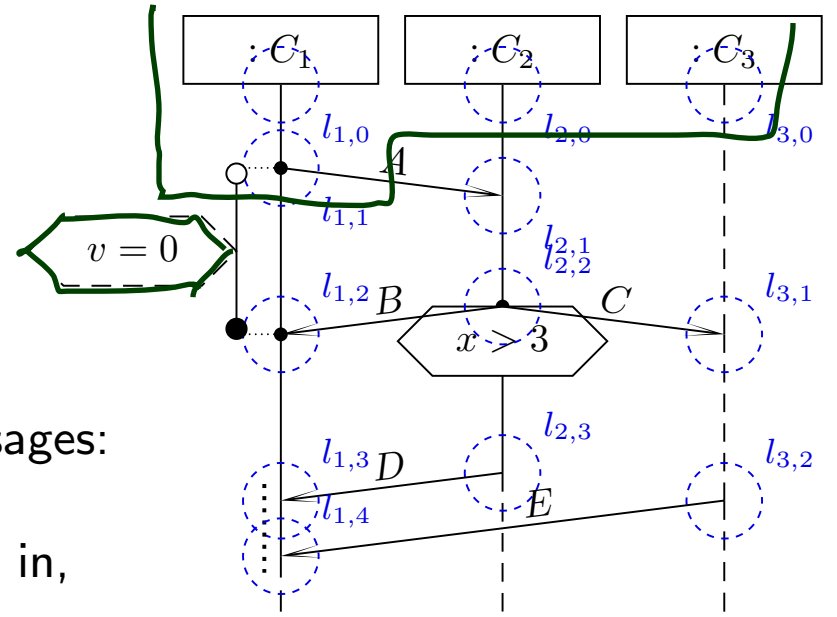
$$\psi_\theta(q) = \{\psi \mid \exists\, l \in q, l' \notin q \mid (l, \psi, \theta, l') \in \mathsf{LocInv} \vee (l', \psi, \theta, l) \in \mathsf{LocInv}\},$$

$$\psi(q) = \psi_{\mathsf{hot}}(q) \cup \psi_{\mathsf{cold}}(q)$$

$$\bigwedge \emptyset := \mathit{false}; \quad \bigwedge\{\psi_1, \ldots, \psi_n\} := \bigwedge_{1 \le i \le n} \psi_i$$



# Loops with Conditions




- How long may we **legally** stay at a cut $q$?
- **Intuition**: those $(\sigma_i, cons_i, Snd_i)$ are allowed to fire the self-loop $(q, \psi, q)$ where
  - $cons_i \cup Snd_i$ comprises only irrelevant messages:
    - **weak mode**:
      no message from a direct successor cut is in,
    - **strict mode**:
      no message occurring in the LSC is in,
  - $\sigma_i$ satisfies the local invariant relevant at $q$

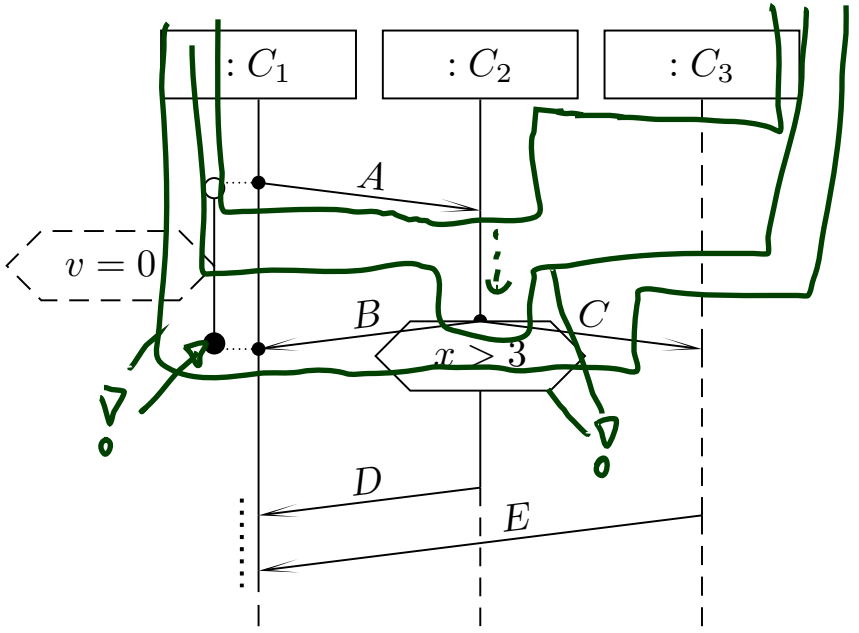
  And nothing else.
- **Formally**: Let $F := F_1 \cup \cdots \cup F_n$ be the union of the firedsets of $q$.
  - $\psi := \underbrace{\neg(\bigvee \mathscr{E}(F))}_{=\textit{true if } F=\emptyset} \wedge \bigwedge \psi(q)$

# *Even More Helper Functions*

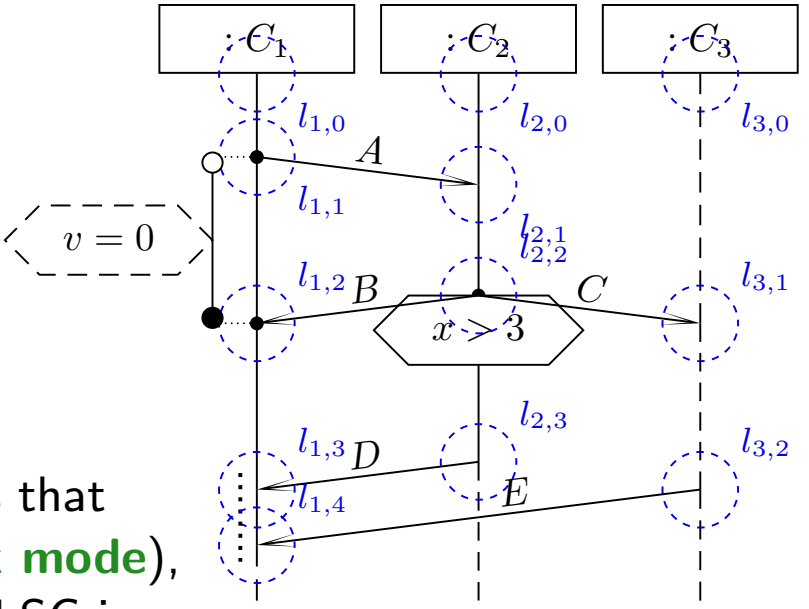
- **Constraints** relevant when moving from $q$ **to** cut $q'$:

$$\psi_\theta(q, q') = \{\psi \mid \exists\, L \subseteq \mathscr{L} \mid (L, \psi, \theta) \in \mathsf{Cond} \wedge L \cap (q' \setminus q) \neq \emptyset\}$$
$$\cup\, \psi_\theta(q')$$
$$\setminus \{\psi \mid \exists\, l \in q' \setminus q, l' \in \mathscr{L} \mid (l, \circ, expr, \theta, l') \in \mathsf{LocInv} \vee (l', expr, \theta, \circ, l) \in \mathsf{LocInv}\}$$
$$\cup \{\psi \mid \exists\, l \in q' \setminus q, l' \in \mathscr{L} \mid (l, \bullet, expr, \theta, l') \in \mathsf{LocInv} \vee (l', expr, \theta, \bullet, l) \in \mathsf{LocInv}\}$$

$$\psi(q, q') = \psi_{\mathsf{hot}}(q, q') \cup \psi_{\mathsf{cold}}(q, q')$$



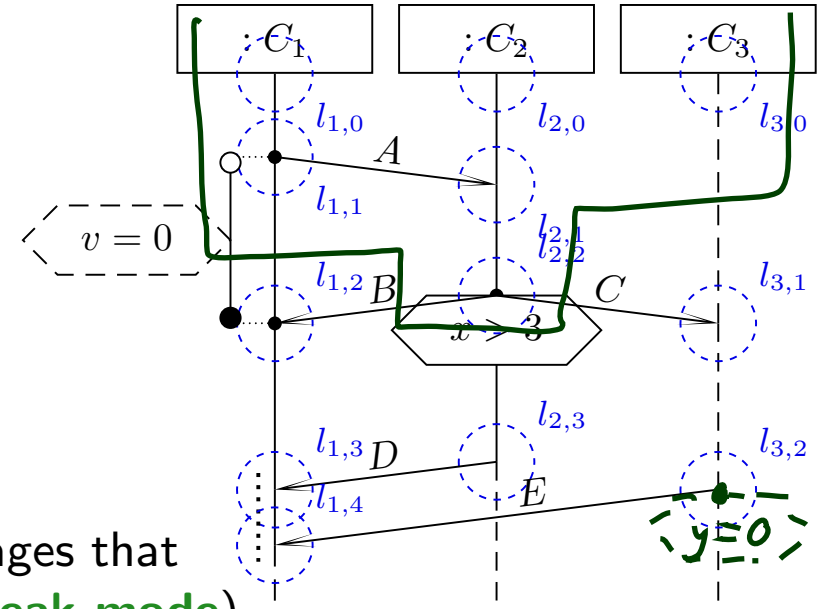
# Progress with Conditions




- When do we move from $q$ to $q'$?
- **Intuition**: those $(\sigma_i, cons_i, Snd_i)$ fire the progress transition $(q, \psi, q')$ for which there exists a firedset $F$ such that $q \rightsquigarrow_F q'$ and
  - $cons_i \cup Snd_i$ comprises exactly the messages that distinguish $F$ from other firedsets of $q$ (**weak mode**), and in addition no message occurring in the LSC is in $cons_i \cup Snd_i$ (**strict mode**),
  - $\sigma_i$ satisfies the local inv. and condition relevant at $q'$
- **Formally**: Let $F, F_1, \ldots, F_n$ be the firedsets of $q$ and let $q \rightsquigarrow_F q'$ (unique).
  - $\psi := \bigwedge \mathscr{E}(F) \wedge \neg\big(\bigvee\big(\mathscr{E}(F_1) \cup \cdots \cup \mathscr{E}(F_n)\big) \setminus \mathscr{E}(F)\big) \wedge \bigwedge \Psi(q, q')$

# *Step III: Cold Conditions and Cold Local Invariants*

# Legal Exits




- When do we take a legal exit from $q$?
- **Intuition**: those $(\sigma_i, cons_i, Snd_i)$ fire the legal exit transition $(q, \psi, \mathscr{L})$
  - for which there exists a firedset $F$ and some $q'$ such that $q \rightsquigarrow_F q'$ and
    - $cons_i \cup Snd_i$ comprises exactly the messages that distinguish $F$ from other firedsets of $q$ (**weak mode**), and in addition no message occurring in the LSC is in $cons_i \cup Snd_i$ (**strict mode**) and
    - at least one cold condition or local invariant relevant when moving to $q'$ is violated, or
  - for which there is no matching firedset and at least one cold local invariant relevant at $q$ is violated.
- **Formally**: Let $F_1, \ldots, F_n$ be the firedsets of $q$ with $q \rightsquigarrow_{F_i} q'_i$.
  - $\psi := \bigvee_{i=1}^{n} \bigwedge \mathscr{E}(F_i) \wedge \neg\big(\bigvee(\mathscr{E}(F_1) \cup \cdots \cup \mathscr{E}(F_n)) \setminus \mathscr{E}(F_i)\big) \wedge \bigvee \psi_{\text{cold}}(q, q'_i)$
    $\vee\ \neg(\bigvee \mathscr{E}(F_i)) \wedge \bigvee \psi_{\text{cold}}(q)$

# *Finally: The LSC Semantics*

A **full LSC** $L$ consist of

- a **body** $(I, (\mathscr{L}, \preceq), \sim, \mathscr{S}, \mathrm{Msg}, \mathrm{Cond}, \mathrm{LocInv})$,
- an **activation condition** (here: event) $ac = E^{?}_{i_1,i_2}$, $E \in \mathscr{E}$, $i_1, i_2 \in I$,
- an **activation mode**, either **initial** or **invariant**,
- a **chart mode**, either **existential** (cold) or **universal** (hot).

A set $W$ of words over $\mathscr{S}$ and $\mathscr{D}$ **satisfies** $L$, denoted $W \models L$, iff $L$

- **universal** ($=$ hot), **initial**, and

$$\forall\, w \in W\ \forall\, \beta : I \to \mathrm{dom}(\sigma(w^0)) \bullet w \text{ activates } L \implies w \in \mathcal{L}_\beta(\mathcal{B}_L).$$

- **existential** ($=$ cold), **initial**, and

$$\exists\, w \in W\ \exists\, \beta : I \to \mathrm{dom}(\sigma(w^0)) \bullet w \text{ activates } L \wedge w \in \mathcal{L}_\beta(\mathcal{B}_L).$$

- **universal** ($=$ hot), **invariant**, and

suffix starting at $k$

$$\forall\, w \in W\ \forall\, k \in \mathbb{N}_0\ \forall\, \beta : I \to \mathrm{dom}(\sigma(w^k)) \bullet w/k \text{ activates } L \implies w/k \in \mathcal{L}_\beta(\mathcal{B}_L).$$

- **existential** ($=$ cold), **invariant**, and

$$\exists\, w \in W\ \exists\, k \in \mathbb{N}_0\ \exists\, \beta : I \to \mathrm{dom}(\sigma(w^k)) \bullet w/k \text{ activates } L \wedge w/k \in \mathcal{L}_\beta(\mathcal{B}_L).$$

# *Back to UML: Interactions*

# *Model Consistency wrt. Interaction*

- We assume that the set of interactions $\mathscr{I}$ is partitioned into two (possibly empty) sets of **universal** and **existential** interactions, i.e.

$$\mathscr{I} = \mathscr{I}_\forall \dot\cup \mathscr{I}_\exists.$$

**Definition.** A model

$$\mathcal{M} = (\mathscr{CD}, \mathscr{SM}, \mathscr{OD}, \mathscr{I})$$

is called **consistent** (more precise: the constructive description of behaviour is consistent with the reflective one) if and only if

$$\forall \mathcal{I} \in \mathscr{I}_\forall : \mathcal{L}(\mathcal{M}) \subseteq \mathcal{L}(\mathcal{I})$$

and

$$\forall \mathcal{I} \in \mathscr{I}_\exists : \mathcal{L}(\mathcal{M}) \cap \mathcal{L}(\mathcal{I}) \neq \emptyset.$$

# *Interactions as Reflective Description*

- In UML, reflective (temporal) descriptions are subsumed by **interactions**.
- A UML model $\mathcal{M} = (\mathscr{CD}, \mathscr{SM}, \mathscr{OD}, \mathscr{I})$ has a set of interactions $\mathscr{I}$.
- An interaction $\mathcal{I} \in \mathscr{I}$ can be (OMG claim: equivalently) **diagrammed** as
  - **sequence diagram**, **timing diagram**, or
  - **communication diagram** (formerly known as collaboration diagram).

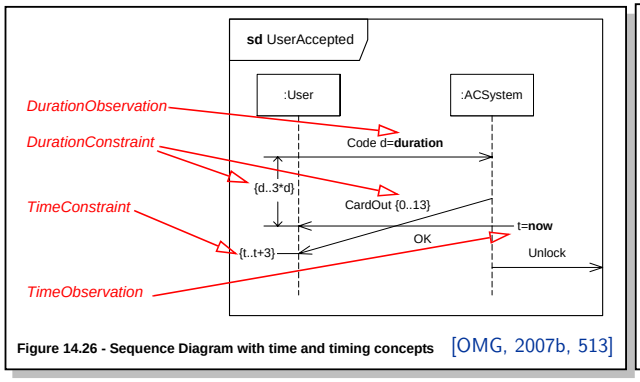



Figure 14.26 - Sequence Diagram with time and timing concepts [OMG, 2007b, 513]

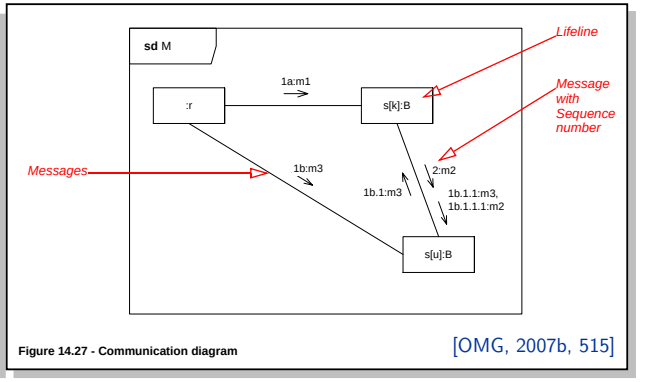



Figure 14.27 - Communication diagram [OMG, 2007b, 515]

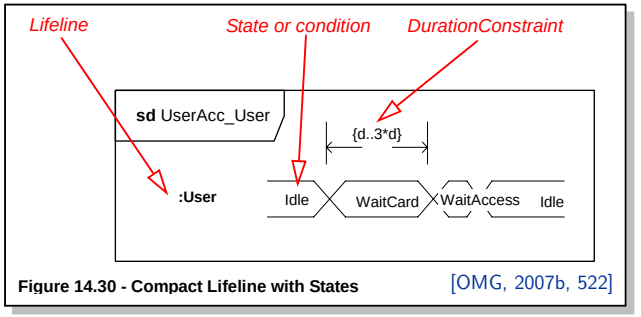



Figure 14.30 - Compact Lifeline with States [OMG, 2007b, 522]

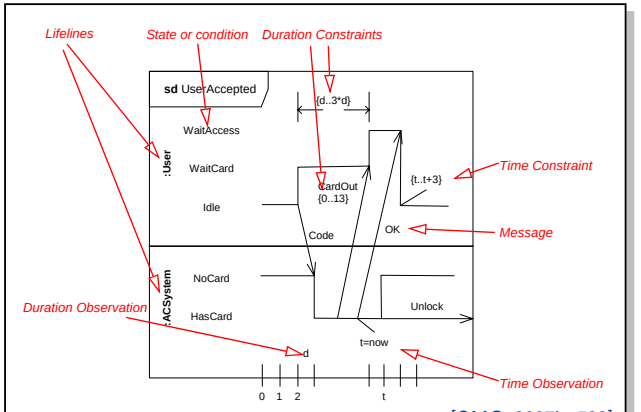
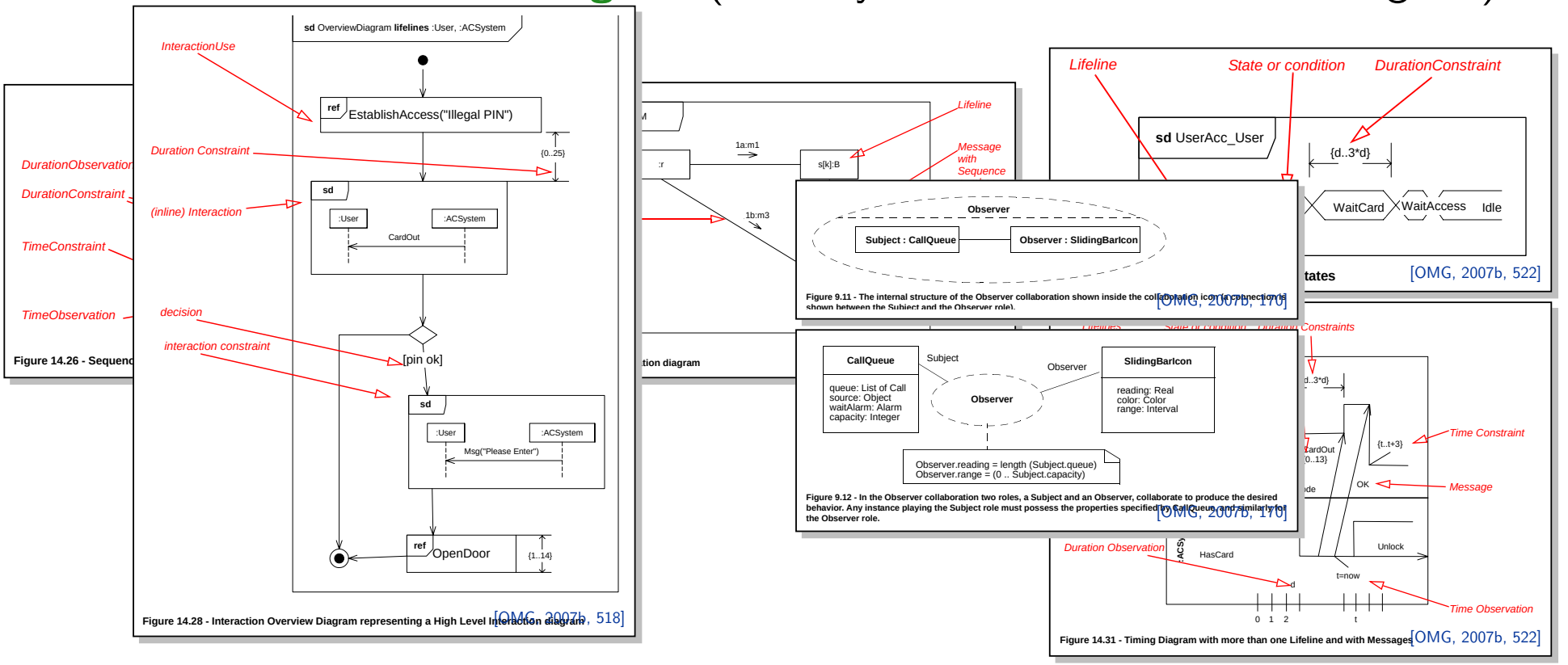



Figure 14.31 - Timing Diagram with more than one Lifeline and with Messages [OMG, 2007b, 522]

# *Interactions as Reflective Description*

- In UML, reflective (temporal) descriptions are subsumed by **interactions**.
- A UML model $\mathcal{M} = (\mathscr{CD}, \mathscr{SM}, \mathscr{OD}, \mathscr{I})$ has a set of interactions $\mathscr{I}$.
- An interaction $\mathcal{I} \in \mathscr{I}$ can be (OMG claim: equivalently) **diagrammed** as
  - **sequence diagram**, **timing diagram**, or
  - **communication diagram** (formerly known as collaboration diagram).



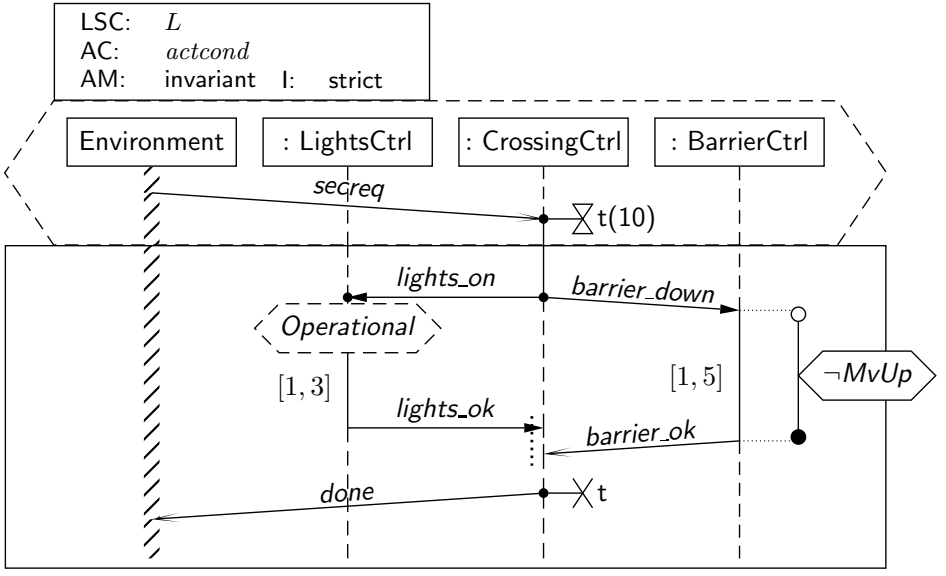
# *Why Sequence Diagrams?*

**Most Prominent**: Sequence Diagrams — with **long history**:

- **Message Sequence Charts**, standardized by the ITU in different versions, often accused to lack a formal semantics.
- **Sequence Diagrams** of UML 1.x

Most severe **drawbacks** of these formalisms:

- unclear **interpretation**:
  example scenario or invariant?
- unclear **activation**:
  what triggers the requirement?
- unclear **progress** requirement:
  must all messages be observed?
- **conditions** merely comments
- no means to express
  **forbidden scenarios**



# *Thus: Live Sequence Charts*

- **SDs of UML 2.x** address **some** issues, yet the standard exhibits unclarities and even contradictions [Harel and Maoz, 2007, Störrle, 2003]
- For the lecture, we consider **Live Sequence Charts** (LSCs) [Damm and Harel, 2001, Klose, 2003, Harel and Marelly, 2003], who have a common fragment with UML 2.x SDs [Harel and Maoz, 2007]
- **Modelling guideline**: stick to that fragment.

# *Side Note: Protocol Statemachines*

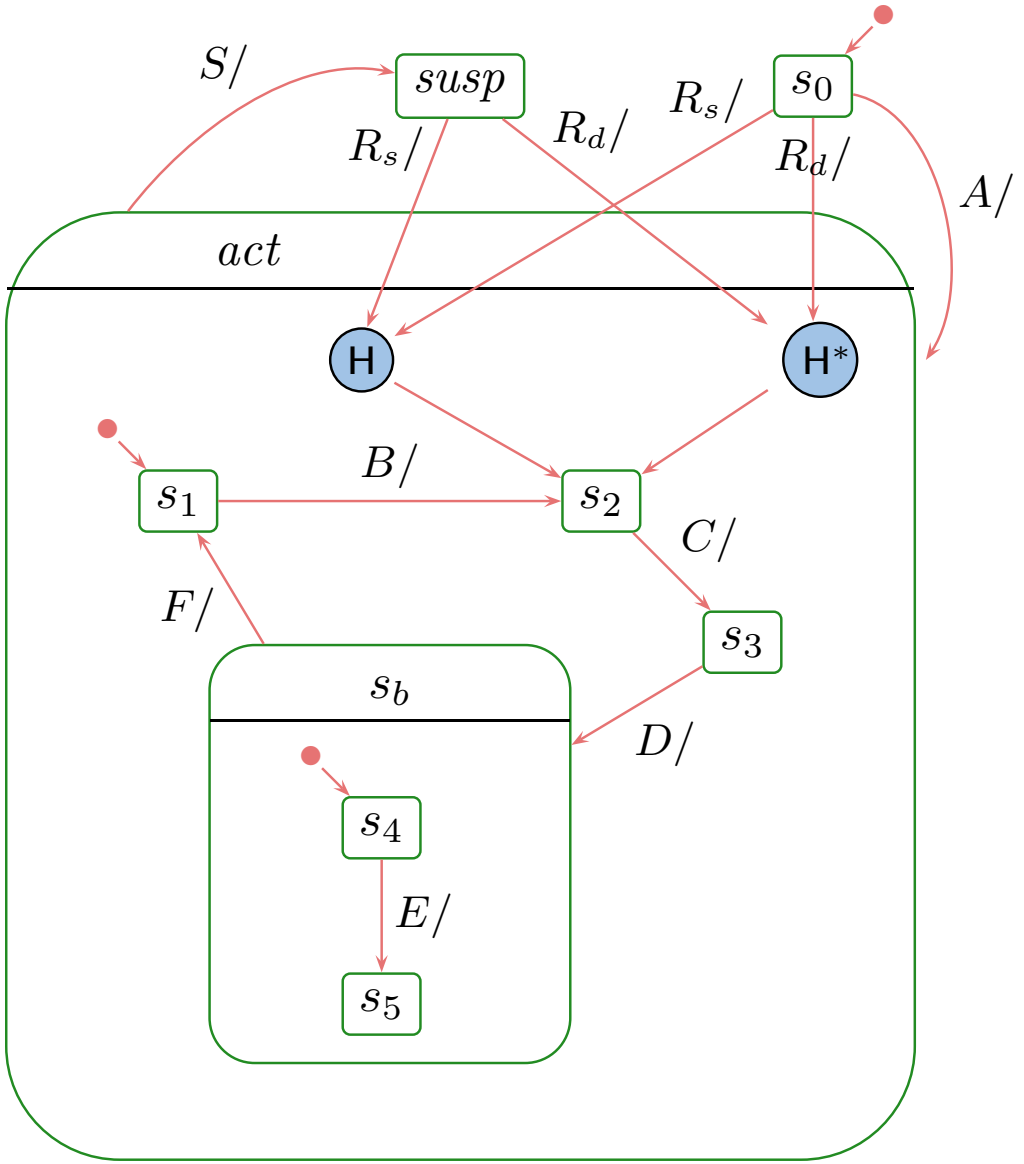
Same direction: **call orders** on operations

- **"for each $C$ instance, method $f()$ shall only be called after $g()$ but before $h()$"**

Can be formalised with protocol state machines.

# *The Concept of History, and Other Pseudo-States*

# History and Deep History: By Example

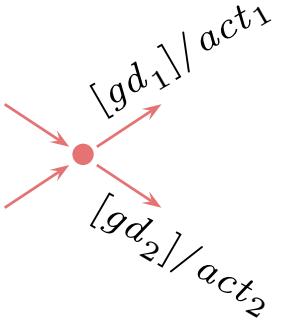



What happens on...

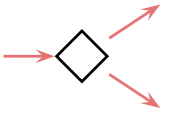
- $R_s$?
  $s_0, s_2$
- $R_d$?
  $s_0, s_2$
- $A, B, C, S, R_s$?
  $s_0, s_1, s_2, s_3, susp, s_3$
- $A, B, S, R_d$?
  $s_0, s_1, s_2, s_3, susp, s_3$
- $A, B, C, D, E, R_s$?
  $s_0, s_1, s_2, s_3, s_4, s_5, susp, s_3$
- $A, B, C, D, R_d$?
  $s_0, s_1, s_2, s_3, s_4, s_5, susp, s_5$

# *Junction and Choice*

- Junction (**"static conditional branch"**):



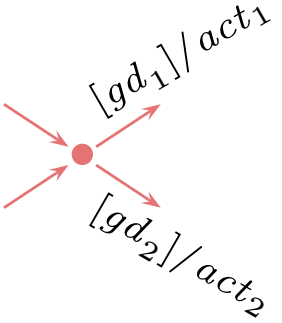

- Choice: (**"dynamic conditional branch"**)



Note: not so sure about naming and symbols, e.g.,
**I'd guessed** it was just the other way round...

# *Junction and Choice*

- Junction (**"static conditional branch"**):




  - **good**: abbreviation
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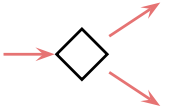

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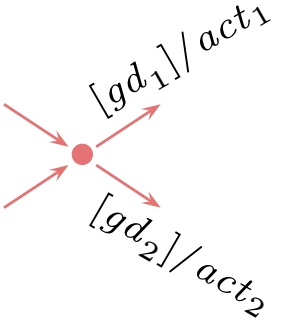


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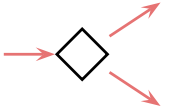

  - **evil**: may get stuck
  - enters the transition **without knowing** whether there's an enabled path
  - at best, use "else" and convince yourself that it cannot get stuck
  - maybe even better: **avoid**

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# *Entry and Exit Point, Submachine State, Terminate*

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  (but: this can also hinder readability.)
- Can even be taken from a different state-machine for re-use. $S : s$

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    - **First** the exit action of the exiting state,
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    - and **then** that internal state's entry action.
- **Terminate Pseudo-State** ×
  - When a terminate pseudo-state is reached, the object taking the transition is immediately killed.

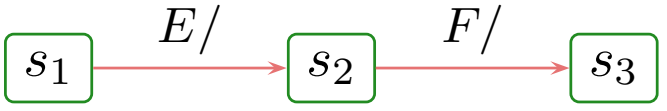
# *Deferred Events in State-Machines*

# *Deferred Events: Idea*

For ages, UML state machines comprises the feature of **deferred events**.

The idea is as follows:

- Consider the following state machine:

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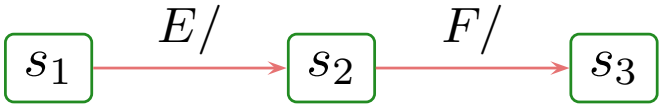


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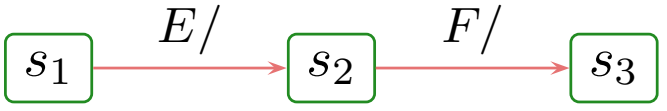


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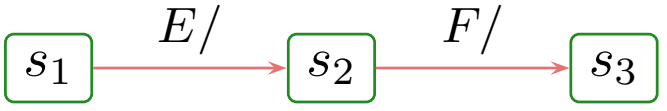


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General options to satisfy such needs:

- Provide a pattern how to "program" this (use self-loops and helper attributes).
- Turn it into an original language concept. **(← OMG's choice)**

# *Deferred Events: Syntax and Semantics*

- **Syntactically**,
  - Each state has (in addition to the name) a set of deferred events.
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  - if an event $E$ is dispatched,
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  - and turn attention to the next event.

- **Not so obvious**:
  - Is there a priority between deferred and regular events?
  - Is the order of deferred events preserved?
  - ...

  [Fecher and Schönborn, 2007], e.g., claim to provide semantics for the complete Hierarchical State Machine language, including deferred events.

# *Active and Passive Objects [Harel and Gery, 1997]*

# *What about non-Active Objects?*

**Recall**:

- We're **still** working under the assumption that all classes in the class diagram (and thus all objects) are **active**.
- That is, each object has its own thread of control and is (if stable) at any time ready to process an event from the ether.

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- That is, each object has its own thread of control and is (if stable) at any time ready to process an event from the ether.

But the world doesn't consist of only active objects.

For instance, in the crossing controller from the exercises we could wish to have the whole system live in one thread of control.

So we have to address questions like:

- Can we send events to a non-active object?
- And if so, when are these events processed?
- etc.

# *Active and Passive Objects: Nomenclature*

[Harel and Gery, 1997] propose the following (orthogonal!) notions:

- A class (and thus the instances of this class) is either **active** or **passive** as declared in the class diagram.
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Which combinations do we understand?

| | active | passive |
|---|---|---|
| reactive | ✔ | (*) |
| non-reactive | (✔) | (✔) |

# *Passive and Reactive*

- So why don't we understand passive/reactive?
- Assume passive objects $u_1$ and $u_2$, and active object $u$, and that there are events in the ether for all three.

  Which of them (can) start a run-to-completion step...?
  Do run-to-completion steps still interleave...?

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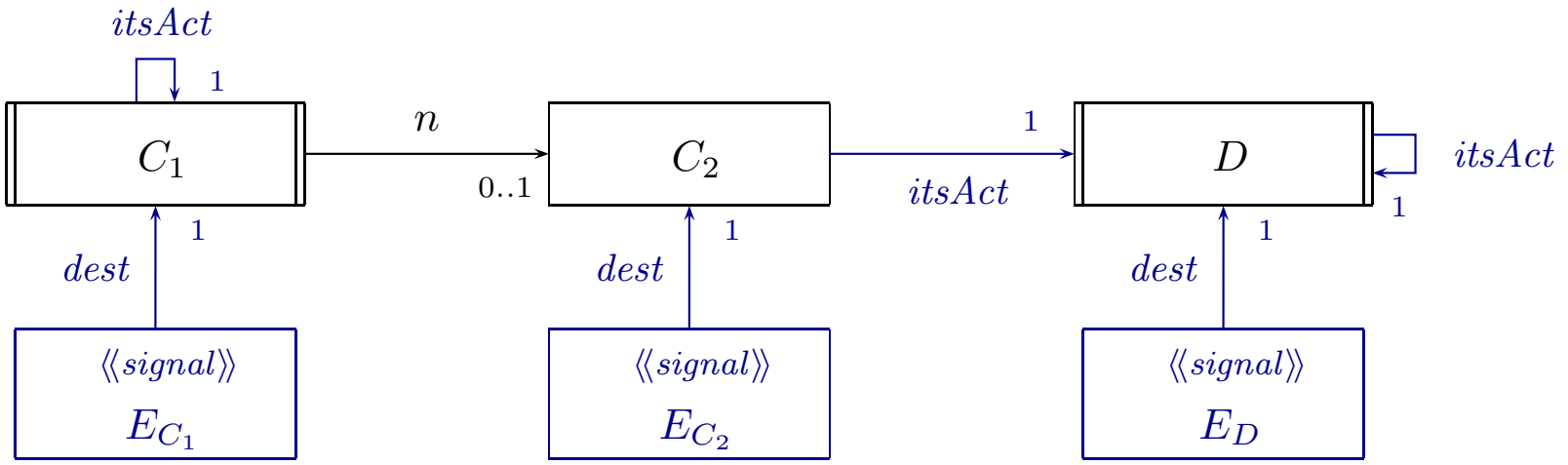
**Reasonable Approaches:**

- **Avoid** — for instance, by
  - require that **reactive implies active** for model well-formedness.
  - requiring for model well-formedness that events are **never sent** to instances of non-reactive classes.
- **Explain** — here: (following [Harel and Gery, 1997])
  - Delegate all dispatching of events to the active objects.

# *Passive Reactive Classes*

- Firstly, establish that each object $u$ knows, via (implicit) link $itsAct$, **the active object** $u_{act}$ which is responsible for dispatching events to $u$.
- If $u$ is an instance of an active class, then $u_a = u$.



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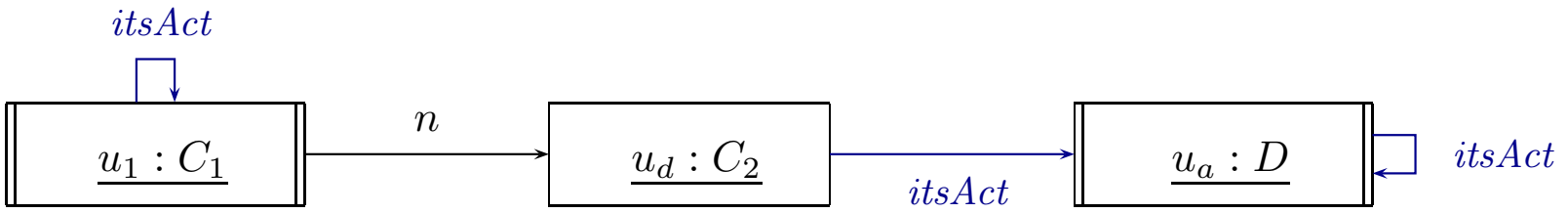


**Sending an event**:

- Establish that of each signal we have a version $E_C$ with an association $dest : C_{0,1}$, $C \in \mathscr{C}$.
- Then $n!E$ in $u_1 : C_1$ becomes:
- Create an instance $u_e$ of $E_{C_2}$ and set $u_e$'s $dest$ to $u_d := \sigma(u_1)(n)$.
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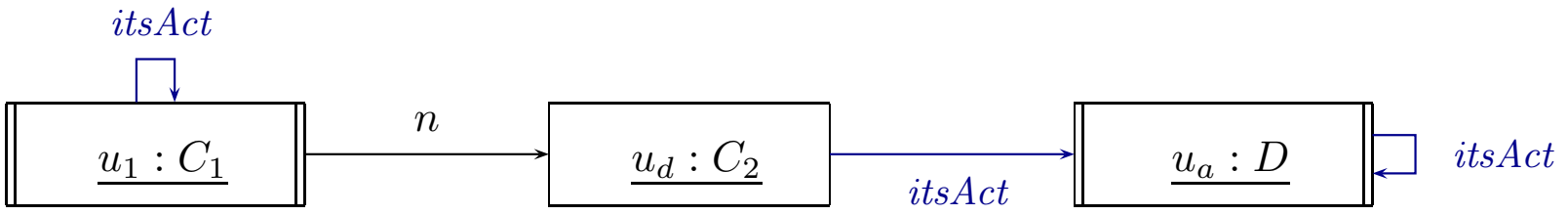


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## Dispatching an event:

- Observation: the ether only has events for active objects.
- Say $u_e$ is ready in the ether for $u_a$.
- Then $u_a$ asks $\sigma(u_e)(dest) = u_d$ to process $u_e$ — and waits until completion of corresponding RTC.
- $u_d$ may in particular discard event.

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- In the current setting, the (local) state of objects is only modified by actions of transitions, which we abstract to transformers.
- In general, there are also **methods**.
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  - the **interface declaration** from
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  In C++ lingo: distinguish **declaration** and **definition** of method.

- In UML, the former is called **behavioural feature** and can (roughly) be
  - a **call interface** $f(\tau_{1_1}, \ldots, \tau_{n_1}) : \tau_1$
  - a **signal name** $E$

| $C$ |
| --- |
| |
| $\xi_1\ f(\tau_{1,1}, \ldots, \tau_{1,n_1}) : \tau_1\ P_1$<br>$\xi_2\ F(\tau_{2,1}, \ldots, \tau_{2,n_2}) : \tau_2\ P_2$ |
| $\langle\langle signal \rangle\rangle\ E$ |

Note: The signal list can be seen as redundant (can be looked up in the state machine) of the class. But: certainly useful for documentation (or sanity check).

# *Behavioural Features*

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| --- |
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  - The class' **state-machine** ("triggered operation").
    - Calling $F$ with $n_2$ parameters for a stable instance of $C$ creates an auxiliary event $F$ and dispatches it (bypassing the ether).
    - Transition actions may fill in the return value.
    - On completion of the RTC step, the call returns.
    - For a non-stable instance, the caller blocks until stability is reached again.

# *Behavioural Features: Visibility and Properties*

| $C$ |
| --- |
| |
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- **Visibility**:
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- **Visibility**:
  - Extend typing rules to sequences of actions such that a well-typed action sequence only calls visible methods.
- **Useful properties**:
  - **concurrency**
    - **concurrent** — is thread safe
    - **guarded** — some mechanism ensures/should ensure mutual exclusion
    - **sequential** — is not thread safe, users have to ensure mutual exclusion
  - **isQuery** — doesn't modify the state space (thus thread safe)
- For simplicity, we leave the notion of steps untouched, we construct our semantics around state machines.
  Yet we could explain pre/post in OCL (if we wanted to).

# *References*

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