


Software Design, Modelling and Analysis in UML

Lecture 21: Inheritance II

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Contents & Goals

- Last Lecture:**
- State Machine semantics completed
 - Inheritance in UML: concrete syntax
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This Lecture:

- Educational Objectives:** Capabilities for following tasks/questions:
 - What is the Liskov Substitution Principle?
 - What is late/early binding?
 - What is the subject, what the uplink semantics of inheritance?
 - What is the effect of inheritance on LSCs, State Machines, System States?
 - What's the idea of Meta-Modeling?
- Content:**
 - Liskov Substitution Principle — derived semantics
 - Two approaches to obtain desired semantics

Inheritance: Syntax

Recall: Abstract Syntax

Recall: a signature (with signals) is a tuple $\mathcal{S} = (\mathcal{F}, \mathcal{E}, V, \text{atr}, \delta)$.

Now (finally): extend to

$$\mathcal{S} = (\mathcal{F}, \mathcal{E}, V, \text{atr}, \delta, F, \text{mth}, \triangleleft)$$

where F/mth are methods, analogously to attributes and

$$\triangleleft \subseteq (\mathcal{F} \times \mathcal{F}) \cup (\mathcal{E} \times \mathcal{E})$$

is a **generalisation** relation such that $C \triangleleft^+ C'$ for **no** $C \in \mathcal{F}$ ("acyclic").

$C \triangleleft D$ reads as

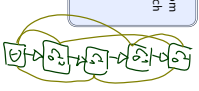
- C is a generalisation of D ,
- D is a specialisation of C ,
- D inherits from C ,
- D is a sub-class of C ,
- C is a super-class of D ,
- ...

Recall: Reflexive, Transitive Closure of Generalisation

Definition: Given classes $C_0, C_1, D \in \mathcal{F}$, we say D inherits from C_0 via C_1 if and only if there are $C_0^1, \dots, C_0^m, C_1^1, \dots, C_1^m \in \mathcal{F}$ such that

$$C_0 \triangleleft C_0^1 \triangleleft \dots \triangleleft C_0^m \triangleleft C_1 \triangleleft C_1^1 \triangleleft \dots \triangleleft C_1^m \triangleleft D.$$

We use " \triangleleft^* " to denote the reflexive, transitive closure of " \triangleleft ".



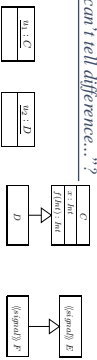
In the following, we assume

- that all attribute (method) names are of the form $C::x, C \in \mathcal{F} \cup \mathcal{E} \quad (C::f, C \in \mathcal{F})$,
- that we have $C::x \in \text{atr}(C)$ resp. $C::f \in \text{mth}(C)$ if and only if $x (f)$ appears in an attribute (method) component of C in a class diagram.

We still want to accept "context C inv: $v < 0$ ", which v is meant? Later!

Inheritance: Desired Semantics

“...can't tell difference...”



- Sequence Diagram: $\{f(x), g(y)\} \in L(B_1)$ implies $w \in L(B_1)$.



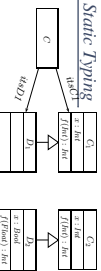
Motivations for Generalisation

- Re-use.
- Sharing.
- Avoiding Redundancy.
- Modularisation.
- Separation of Concerns.
- Abstraction.
- Extensibility.
- ...

→ See textbooks on object-oriented analysis, development, programming.

“...shall be usable...” for UML

Exers: Static Typing



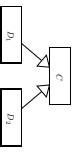
Given: $x > 0$ also well-typed for D_1 .
Wanted: assignment $\{kxCI := kxDI, kxCI\}$ being well-typed (and doing the right thing).
Approach: 1) Simply define it as being well-typed. 2) adjust system state definition to do the right thing.

Handwritten notes: "make by $x=20$ ", "make by $x=20$ ", "make by $x=20$ ", "make by $x=20$ ", "make by $x=20$ ", "make by $x=20$ ".

What Does [Fischer and Wehrheim, 2000] Mean for UML?

“An instance of the sub-type shall be usable whenever an instance of the supertype was expected, without a client being able to tell the difference.”

- Wanted: sub-typing for UML.
- With
- we don't even have usability.
- It would be nice, if the well-formedness rules and semantics of



- would ensure D_1 is a sub-type of C ;
- that D_1 objects can be used interchangeably by everyone who is using C 's;
- is not able to tell the difference (i.e. see unexpected behaviour).

Static Typing Cont'd



Notions (from category theory): $\{kxCI := kxDI, kxCI\}$ being well-typed (and doing the right thing).
 • invariance.
 • covariance.
 • contravariance.

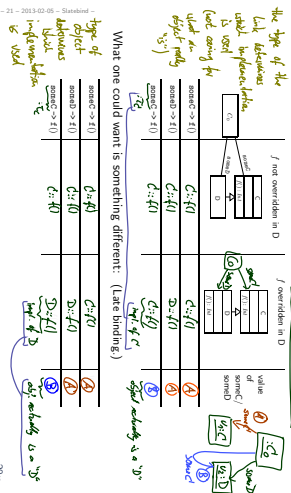
We could call, e.g. a method, sub-type preserving, if and only if it
 • accepts more general types as input (contravariant),
 • provides a more specialised type as output (covariant).

This is a notion used by many programming languages — and easily type-checked.

Excursus: Late Binding of Behavioural Features

Late Binding

What transformer applies in what situation? (Early (compile time) binding)



Back to the Main Track: "...tell the difference..." for UML

With Only Early Binding...

- ...we're done (if we realise it correctly in the framework).
 - Then
 - if we're calling method f of an object u ,
 - which is an instance of D with $C \leq D$
 - via a C-link,
 - then we (by definition) only see and change the C-part.
 - We cannot tell whether u is a C or an D instance.
- So we immediately also have behavioural/dynamic subtyping.

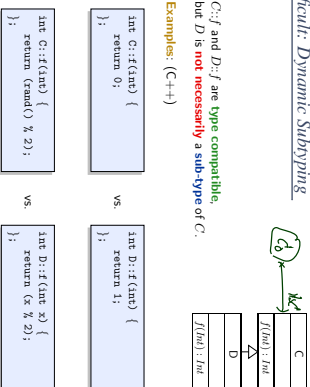
Late Binding in the Standard and Programming Lang.

- In the standard, Section 11.3.10 "CallOperatorAction":
 - "Semantic Violation Points"
 - The mechanism for determining the method to be invoked as a result of a call operation is unspecified" [OMG 2007b: 247]
 - In C++:
 - methods are by default "early" compile time binding",
 - can be declared to be "late binding" by keyword "virtual",
 - the declaration applies to all inheriting classes.
 - In Java:
 - methods are "late binding";
 - there are patterns to imitate the effect of "early binding"
- Exercise: What could have driven the designers of C++ to take that approach?
- Note: late binding typically applies only to methods, not to attributes. (But: getter/setter methods have been invented recently)

Difficult: Dynamic Subtyping

- C::f and D::f are type compatible,
- but D is not necessarily a sub-type of C.

• Example: (C++)



- In the standard, Section 7.3.96, "Operation":
 - "Semantic Variation Points"
 - [...] When operations are redefined in a specialization, rules regarding invariance, covariance, or contravariance of types and preconditions determine whether the specialized classifier is substitutable for its more general parent. Such rules constitute semantic variation points with respect to redefinition of operations." [OMG, 2007a, 109]
 - So, better: call a method **sub-type preserving**, if and only if it:
 - (i) accepts **more input values** (contravariant),
 - (ii) on the **old values**, has **fewer behaviour** (covariant).
 - Note: This (i) is no longer a matter of simple type-checking!
 - And not necessarily the end of the story:
 - One could, e.g. want to consider execution time.
 - Or, like [Fischer and Wehrhan, 2000](#), relax to "fewer observable behaviour", thus admitting the sub-type to do more work on inputs.
 - Note: "Testing" differences depends on the **granularity** of the semantics.
 - Related: "has a weaker pre-condition." (contravariant), "has a stronger post-condition." (covariant)." 28/11

Domain Inclusion Semantics

Ensuring Sub-Typing for State Machines

- In the CASE tool we consider, multiple classes in an inheritance hierarchy can have state machines.
 - But the state machine of a sub-class **cannot** be drawn from scratch.
 - Instead, the state machine of a sub-class can only be obtained by applying actions from a restricted set to a copy of the original one. Roughly (cf. User Guide, p. 760, for details),
 - add things into (hierarchical) states,
 - add more states,
 - attach a transition to a different target (limited).
- They **ensure**, that the sub-class is a **behavioural sub-type** of the super class. (But method implementations can still destroy that property.)
 - Technically, the idea is that (by late binding) only the state machine of the most specialised class are running.
 - By knowledge of the framework, the code for state machines of super-classes is still accessible — but using it is hardly a good idea... 28/11



Domain Inclusion Structure

- Let $\mathcal{S} = (\mathcal{S}, \mathcal{C}, V, attr, \delta, F, mod, \triangleleft)$ be a signature.
- Now a **structure** \mathcal{D}
- [as before] maps types, classes, associations to domains,
 - [for completeness] methods to transformers,
 - [as before] identities of instances of classes not (transitively) related by generalisation are disjoint.
 - [changed] the identities of a super-class comprise all identities of sub-classes, i.e.

$$\forall C \in \mathcal{C} : \mathcal{D}(C) \supseteq \bigcup_{C \triangleleft D} \mathcal{D}(D),$$

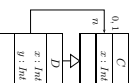
Note: the old setting coincides with the special case $\triangleleft = \emptyset$.

Towards System States

- Wanted: a formal representation of "if $C \leq D$ then D is a C^* ", that is:
- D has the same attributes and behavioural features as C , and
 - D objects (identities) can replace C objects.
- We'll discuss **two approaches** to semantics:
- Domain-Inclusion Semantics**
 - (more theoretical)
 - UML class diagram: C has attributes x, y, z and methods m1, m2, m3. D inherits from C and has attribute w and methods m4, m5, m6.
 - Handwritten diagram shows state machines for C and D. C's state machine has states {s1, s2, s3} and transitions r(a), r(b), r(c). D's state machine has states {s1, s2, s3, s4} and transitions r(a), r(b), r(c), r(d).
 - Uplink Semantics**
 - (more technical)
 - Handwritten diagram shows state machines for C and D. C's state machine has states {s1, s2, s3} and transitions r(a), r(b), r(c). D's state machine has states {s1, s2, s3, s4} and transitions r(a), r(b), r(c), r(d).

Domain Inclusion System States

- Now: a **system state** of \mathcal{S} wrt. \mathcal{D} is a **type-consistent mapping** $\sigma : \mathcal{D}(\mathcal{C}) \rightarrow (V \rightarrow (\mathcal{D}(\mathcal{C}) \cup \mathcal{D}(A_0, 1) \cup \mathcal{D}(R_0)))$ that is, for all $u \in \text{dom}(\sigma) \cap \mathcal{D}(C)$,
- [as before] $\sigma(u)(v) \in \mathcal{D}(T)$ if $v : \tau \in \mathcal{S}$ or $\tau \in \{C, C_0, 1\}$.
 - [changed] $\text{dom}(\sigma(u)) = \bigcup_{C \leq D} \text{attr}(C_0)$.
- Example:

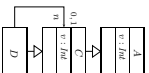


Note: the old setting still coincides with the special case $\triangleleft = \emptyset$.

Preliminaries: Expression Normalisation

Recall:

- we want to allow, e.g., "context $D \text{ inv } v < 0^*$,"
- we assume fully qualified names, e.g. $C::v$,
- Intuitively, v shall denote the "most special more general" $C::v$ according to \triangleleft .



OCL Syntax and Typing

- Recall (part of the) OCL syntax and typing:

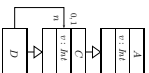
$$\begin{aligned} \text{expr} ::= & v(\text{expr}_1) && \tau_C \rightarrow \tau(v), && \text{if } v : \tau \in \mathcal{V} \\ & | r(\text{expr}_1) && \tau_C \rightarrow \tau_D, && \text{if } r : D_0 \text{!} \\ & | r(\text{expr}_1) && \tau_C \rightarrow \text{Set}(\tau_D), && \text{if } r : D_s \end{aligned}$$

The definition of the semantics remains (textually) the same.

Preliminaries: Expression Normalisation

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- Intuitively, v shall denote the "most special more general" $C::v$ according to \triangleleft .



To keep this out of typing rules, we assume that the following normalisation has been applied to all OCL expressions and all actions.

- Given expression v (or J) in context of class D , as determined by, e.g.
 - by the type of the navigation expression prefix, or
 - by the class, the state-machine where the action occurs belongs to,
 - similar for method bodies,
- normalise v to $(=$ replace by $C::v$,
- where C is the greatest class wrt. " \triangleleft " such that
- $C \preceq D$ and $C::v \in \text{def}(C)$.

More Interesting: Well-Typedness

- We want

$$\text{context } D \text{ inv } v < 0$$

to be well-typed.

Currently it isn't because

$$v(\text{expr}_1) : \tau_C \rightarrow \tau(v)$$

but $A \vdash \text{self} : \tau_D$.

(Because τ_D and τ_C are still different types, although $\text{dom}(\tau_D) \subset \text{dom}(\tau_C)$.)

- So, add a (first) new typing rule

$$\frac{A \vdash \text{expr}_1 : \tau_D}{A \vdash \text{expr}_1 : \tau_C} \text{ if } C \preceq D \quad (\text{th})$$

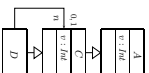
Which is correct in the sense that, if "expr" is of type τ_D , then we can use it everywhere, where a τ_C is allowed.

The system state is prepared for that.

Preliminaries: Expression Normalisation

Recall:

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- $C \preceq D$ and $C::v \in \text{def}(C)$.

If no (unique) such class exists, the model is considered not well-formed; the expression is ambiguous. Then: explicitly provide the qualified name.

Well-Typedness with Visibility Control

$$\frac{A, D \vdash \text{expr}_1 : \tau_C}{A, D \vdash C::v(\text{expr}_1) : \tau} \quad \xi = + \quad (\text{Pub})$$

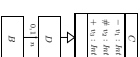
$$\frac{A, D \vdash \text{expr}_1 : \tau_C}{A, D \vdash C::v(\text{expr}_1) : \tau} \quad \xi = \#, \tau \preceq D \quad (\text{Prot})$$

$$\frac{A, D \vdash \text{expr}_1 : \tau_C}{A, D \vdash C::v(\text{expr}_1) : \tau} \quad \xi = -, C = D \quad (\text{Priv})$$

$$(C::v : \tau, \xi \in \{0, P\} \in \text{def}(C))$$

Example:

context / inv	$(v)_0 < 0$	$(v)_1 < 0$	$(v)_2 < 0$
C			
D			
B			

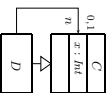


Satisfying OCL Constraints (Domain Inclusion)

- Let $\mathcal{M} = (\mathcal{U}, \mathcal{G}, \mathcal{D}, \mathcal{H}, \mathcal{J})$ be a UML model, and \mathcal{G} a structure.
- We (continue to) say $\mathcal{M} \models_{\text{expr}} \text{for context } C : \text{inv} : \text{expr}_0 \in \text{Inv}(\mathcal{M})$ iff

$$\forall \pi = (\sigma, \varepsilon), \varepsilon \in \llbracket \mathcal{M} \rrbracket \quad \forall t \in \mathbb{N} \quad \forall u \in \text{dom}(\sigma) \cap \mathcal{G}(C) : \\ \llbracket \text{expr}_0 \rrbracket(\sigma, \{\text{self} \mapsto u\}) = 1.$$
- \mathcal{M} is (still) consistent if and only if it satisfies all constraints in $\text{Inv}(\mathcal{M})$.

• **Example:**



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Transformers (Domain Inclusion)

- Transformers also remain **the same**, e.g. [VL 12, p. 18]

$$\text{update}(\text{expr}_1, v, \text{expr}_2) : (\sigma, \varepsilon) \mapsto (\sigma', \varepsilon)$$
 with

$$\sigma' = \sigma[u \mapsto \sigma(v)] \mapsto \llbracket \text{expr}_2 \rrbracket(\sigma)$$
 where $u = \llbracket \text{expr}_1 \rrbracket(\sigma)$.

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Semantics of Method Calls

- **Non late-binding:** clear, by normalisation.
- **Late-binding:** Construct a **method call transformer**, which is applied to all method calls.

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Inheritance and State Machines: Triggers

- **Warning:** triggers shall also be sensitive for inherited events, sub-class shall execute super-class' state-machine (unless overridden).

$(\sigma, \varepsilon) \xrightarrow[\text{inv}]{\text{consum, send}} (\sigma', \varepsilon')$ if

- $\exists u \in \text{dom}(\sigma) \cap \mathcal{G}(C) \exists \text{inv} \in \mathcal{H}(C) : \text{inv} \in \text{ready}(\sigma, u)$
- u is stable and in state machine state s , i.e. $\sigma(u)(\text{stable}) = 1$ and $\sigma(u)(s) = s$,
- a transition is enabled, i.e.

$$\exists (s, F, \text{expr}, \text{act}, s') \in \text{SM}(C) : F = E \wedge \llbracket \text{expr} \rrbracket(\sigma) = 1$$
 where $\delta = \sigma[u \mapsto \text{inv}](\sigma, \varepsilon \mapsto \text{inv})$.

 and

- (σ', ε') results from applying inv to (σ, ε) and removing inv from the state, i.e.

$$(\sigma', \varepsilon') = \text{inv}(\delta, \sigma \ominus u, \varepsilon)$$

 where δ depends:

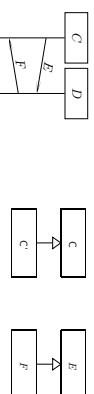
- If u becomes stable in s' , then $\delta = 1$. It does become stable if and only if there is no transition without trigger enabled for u in (σ', ε') .
- Otherwise $\delta = 0$.

• Consumption of inv and the side effects of the action are observed, i.e.

$$\text{cons} = (\{u, E, \sigma(u)\}) \cup \text{Send} = \text{Obs}_{\text{inv}}(\delta, \varepsilon \ominus \text{inv}).$$

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Domain Inclusion and Interactions



- Similar to satisfaction of OCL expressions above:
- An instance line stands for all instances of C' (exact or inheriting).
- Satisfaction of event observation has to take inheritance into account, too, so we have to fix, e.g.

$$\sigma, \text{cons}, \text{Send} \models_{\beta} F_{x, \beta}$$
 if and only if

$$\beta(x) \text{ sends an } F\text{-event to } \beta y \text{ where } E \preceq F.$$
- **Note:** C' -instance line also binds to C' -objects.

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Uplink Semantics

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- **Idea:**
- Continue with the existing definition of **structure**, i.e. disjoint domains for identities.
- Have an **implicit association** from the child to each parent part (similar to the implicit attribute for stability).



- Apply (a different) pre-processing to make appropriate use of that association, e.g. rewrite (C++)
- `x = 0;`
- in *D* to
- `uplinkC -> x = 0;`

- For each pair $C \triangleleft D$, extend *D* by a (fresh) association $uplink_C : C$ with $\mu = [1, 1]$; $\xi = +$ (Exercise: public necessary?)
- Given expression v (or f) in the **context** of class *D*,
- let *C* be the **smallest** class wrt. " \leq " such that
- $C \leq D$, and
- $C::x \in \text{attr}(D)$
- then there exists (by definition) $C \triangleleft C_1 \triangleleft \dots \triangleleft C_n \triangleleft D$,
- **normalise** v to (= replace by)

$$uplink_{C_n} \rightarrow \dots \rightarrow uplink_{C_1} \cdot C::x$$

- Again, if no (unique) smallest class exists the model is considered **not well-formed**: the expression is ambiguous.

- Definition of structure remains **unchanged**.
- Definition of system state remains **unchanged**.
- Typing and transformers remain **unchanged** — the preprocessing has put everything in shape.

- Let $\mathcal{M} = (\mathcal{K}, \mathcal{G}, \mathcal{P}, \mathcal{H}, \mathcal{J})$ be a UML model, and \mathcal{G} a structure.
 - We (**continue to**) say $\mathcal{M} \models expr$
- for
- context C inv: $expr_0 \in \text{Inv}(\mathcal{M})$
- $\stackrel{=expr}{\text{---}}$
- if and only if
- $\forall \tau = (a_i)_{i \in \mathbb{N}} \in \llbracket \mathcal{M} \rrbracket$
- $\forall i \in \mathbb{N}$
- $\forall u \in \text{dom}(a_i) \cap \mathcal{G}(C) :$
- $\llbracket expr \rrbracket[a_i, [a_i/f \mapsto u]] = 1,$
- \mathcal{M} is (still) consistent if and only if it satisfies all constraints in $\text{Inv}(\mathcal{M})$.

- What **has to change** is the **create transformer**: $create_C(C, expr, v)$
 - Assume, C 's inheritance relations are as follows.
- $$C_{1,1} \triangleleft \dots \triangleleft C_{1,n} \triangleleft C_i$$
- $$\dots$$
- $$C_{m,1} \triangleleft \dots \triangleleft C_{m,m} \triangleleft C$$
- Then, we have to
 - create one fresh object for each part, e.g.
- $$a_{1,1}, \dots, a_{1,n}, \dots, a_{m,1}, \dots, a_{m,m}$$
- set up the uplinks recursively, e.g.
- $$\sigma_{(1,1,2)}(uplink_{C_{1,1}}) = a_{1,1}$$
- And, if we had constructors, be careful with their order.

- Employ something similar to the "wastepac" trick (in a minute). But the result is typically far from concise. (Related to OCL's `IsKindOf()` function, and RTTI in C++)

Domain Inclusion vs. Uplink Semantics

```

• C c:
• D d:
• Identity upcast (C++):
  C* cp = kcd; // assign address of 'd' to pointer 'cp'
• Identity downcast (C++):
  D* dp = (D*)cp; // assign address of 'd' to pointer 'dp'
• Value upcast (C++):
  // copy attribute values of 'd' into 'c'; or
  // more precisely, the values of the C-part of 'd'
  *c = *d;

```

Cast-Transformers

```

• C c:
• D d:
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  *c = *d;

```

Casts in Domain Inclusion and Uplink Semantics

	Domain Inclusion	Uplink
C* cp = kcd	easy: immediately compatible (in underlying system state) because kcd yields an identity from $\mathcal{D}(D) \subset \mathcal{D}(C)$	easy: By pre-processing, C* cp = duplink(C);
D* dp = (D*)cp	easy: the value of cp is in $\mathcal{D}(D) \cap \mathcal{D}(C)$ because the pointed-to object is a D. Otherwise, error condition.	difficult: we need the identity of the D whose C-slice is denoted by cp. (See next slide.)
c = d;	hit difficult: set (for all $C \subseteq D$) $(C) \times \{ \cdot \} \rightarrow \Sigma \times \Sigma \rightarrow \Sigma_{\text{in}(C)}$ Note: $d^c = \text{rl}(C) \mapsto \text{rl}(d)$ is not type-compatible!	easy: By pre-processing, c = *(duplink(C));

Identity Downcast with Uplink Semantics

- **Recall** (C++): D d; C* cp = kcd; D* dp = (D*)cp;
- **Problem**, we need the identity of the D whose C-slice is denoted by cp.
- **One technical solution**:
- Give up disjointness of domains for one additional type comprising all identities, i.e. have

$$\text{all } e \in \mathcal{D}, \quad \mathcal{D}(\text{all}) = \bigcup_{C \in \mathcal{C}} \mathcal{D}(C)$$
- In each minimal class have associations "restrpc" pointing to most specialised slices, plus information of which type that slice is.
- Then downcast means, depending on the restrpc type (only finitely many possibilities), going down and then up as necessary, e.g.


```

        restrpc(restrpc-type) {
        case C :
        dp = cp -> restrpc -> uplinkC -> ... -> uplinkD -> uplinkD;
        ...
        }
      
```

Domain Inclusion vs. Uplink Semantics: Differences

- **Note**: The uplink semantics views inheritance as an abbreviation:
 - We only need to touch transformers (create) — and if we had constructors, we didn't even need that (we could encode the recursive construction of the upper slices by a transformation of the existing constructors.)
 - **So**:
 - Inheritance doesn't add expressive power.
 - And it also doesn't improve conciseness so dramatically.
- As long as we're "early binding", that is...

Domain Inclusion vs. Uplink Semantics: Motives

- **Exercise**
- What's the point of
 - having the tedious adjustments of the theory
 - if it can be approached technically?
 - having the tedious technical pre-processing
 - if it can be approached cleanly in the theory?

References

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