Software Design, Modelling and Analysis in UML

Lecture 02: Semantical Model

2013-10-23

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Last Lecture:

- Motivation: model-based development of things (houses, software) to cope with complexity, detect errors early
- Model-based (or -driven) Software Engineering
- UML Mode of the Lecture: Blueprint.

This Lecture:

- Educational Objectives: Capabilities for these tasks/questions:
 - Why is UML of the form it is?
 - Shall one feel bad if not using all diagrams during software development?
 - What is a signature, an object, a system state, etc.?
 What's the purpose of signature, object, etc. in the course?
 - How do Basic Object System Signatures relate to UML class diagrams?

Content:

- Brief history of UML
- Course map revisited
- Basic Object System Signature, Structure, and System State

Why (of all things) UML?

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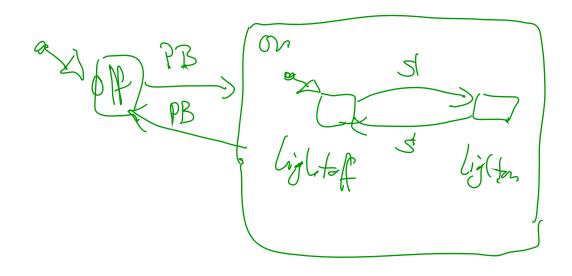
Why (of all things) UML?

- Note: being a modelling languages doesn't mean being graphical (or: being a visual formalism [Harel]).
- For instance, [Kastens and Büning, 2008] also name:
 - Sets, Relations, Functions
 - Terms and Algebras
 - Propositional and Predicate Logic
 - Graphs
 - XML Schema, Entity Relation Diagrams, UML Class Diagrams
 - Finite Automata, Petri Nets, UML State Machines
- Pro: visual formalisms are found appealing and easier to grasp.
 Yet they are not necessarily easier to write!
- **Beware**: you may meet people who dislike visual formalisms just for being graphical maybe because it is easier to "trick" people with a meaningless picture than with a meaningless formula.
 - More serious: it's maybe easier to misunderstand a picture than a formula.

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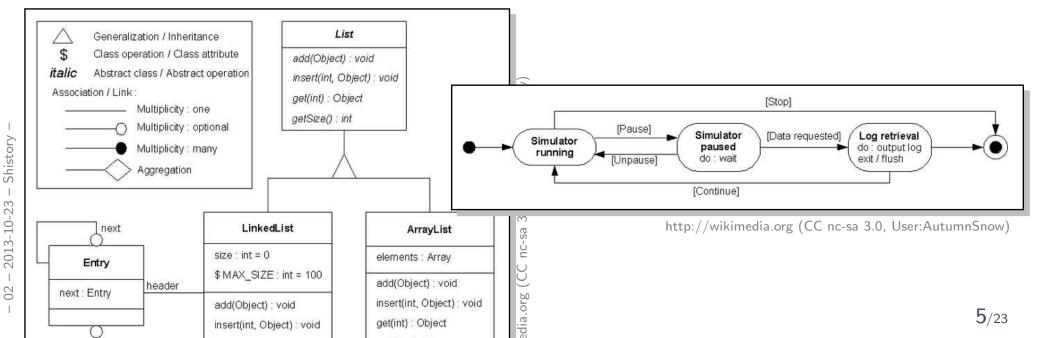
A Brief History of UML

- Boxes/lines and finite automata are used to visualise software for ages.
- 1970's, Software CrisisTM
 - Idea: learn from engineering disciplines to handle growing complexity. Languages: Flowcharts, Nassi-Shneiderman, Entity-Relation Diagrams
- Mid 1980's: Statecharts [Harel, 1987], StateMateTM [Harel et al., 1990]



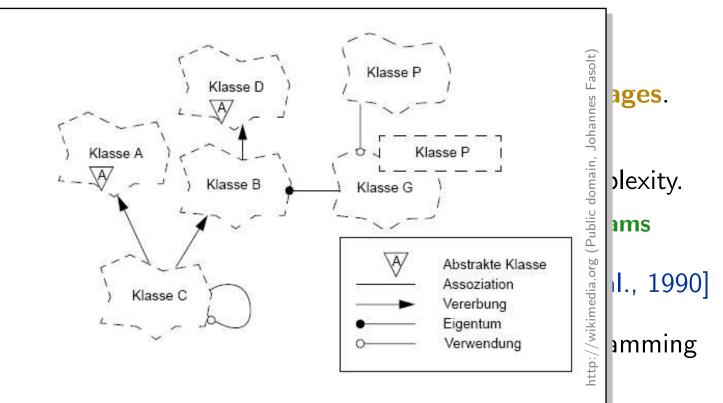
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- Early 1990's, advent of Object-Oriented-Analysis/Design/Programming
 - Inflation of notations and methods, most prominent:
 - Object-Modeling Technique (OMT) [Rumbaugh et al., 1990]



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 Languages:
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- Booch Method and Notation [Booch, 1993]

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 - Booch Method and Notation [Booch, 1993]
 - Object-Oriented Software Engineering (OOSE) [Jacobson et al., 1992]

Each "persuasion" selling books, tools, seminars...

- Late 1990's: joint effort UML 0.x, 1.x
 Standards published by Object Management Group (OMG), "international, open membership, not-for-profit computer industry consortium".
- Since 2005: UML 2.x

Figure A.5 - The taxonomy of structure and behavior diagram

[Dobing and Parsons, 2006]

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Common Expectations on UML

- Easily writeable, readable even by customers
- Powerful enough to bridge the gap between idea and implementation
- Means to tame complexity by separation of concerns ("views")
- Unambiguous
- Standardised, exchangeable between modelling tools
- UML standard says how to develop software
- Using UML leads to better software
- . . .

We will see...

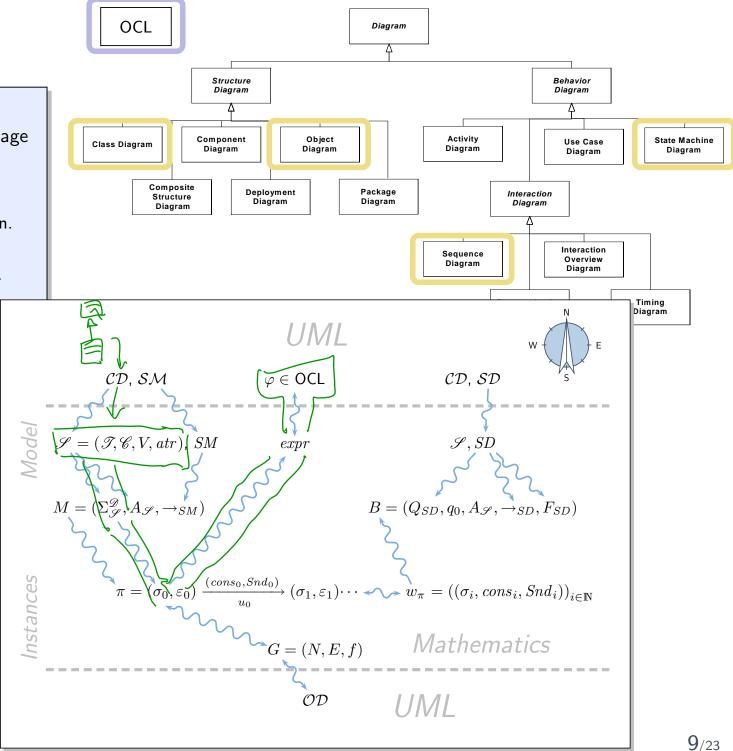
Seriously: After the course, you should have an own opinion on each of these claims. In how far/in what sense does it hold? Why? Why not? How can it be achieved? Which ones are really only hopes and expectations? . . . ?

Course Map Revisited

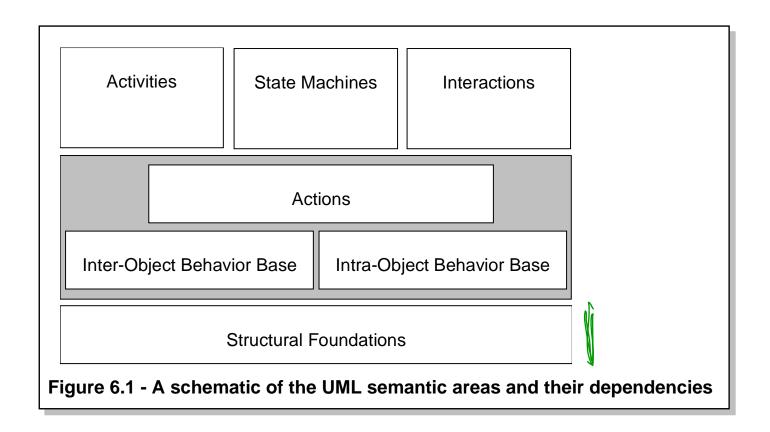
The Plan

Recall:

- Overall aim: a formal language for software blueprints.
- Approach:
 - (i) Common semantical domain.
 - (ii) UML fragments as syntax.
 - (iii) Abstract representation of diagrams.
- (iv) Informal semantics: UML standard
- (v) assign meaning to diagrar
- (vi) Define, e.g., consistency.



UML: Semantic Areas



[OMG, 2007b, 11]

Common Semantical Domain

Basic Object System Signature

Definition. A (Basic) Object System Signature is a quadruple

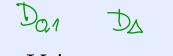
$$\mathscr{S} = (\mathscr{T}, \mathscr{C}, V, atr)$$

where

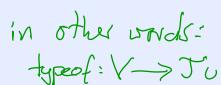
- \mathscr{T} is a set of (basic) types,
- \mathcal{C}
 is a finite set of classes,
- ullet V is a finite set of typed attributes/i.e., each $v\in V$ has type
 - $\tau \in \mathscr{T}$ or
 - $C_{0,1}$ or C_* , where $C \in \mathscr{C}$ (written $v:\tau$ or $v:C_{0,1}$ or $v:C_*$),
- $atr: \mathscr{C} \to 2^V$ maps each class to its set of attributes.

for each class DEC there are two different

types: ov:









01:

/ D <u>/</u>

total function powerset of V

Note: Inspired by OCL 2.0 standard [OMG, 2006], Annex A.

Basic Object System Signature Example

 $\mathscr{S} = (\mathscr{T}, \mathscr{C}, V, atr)$ where

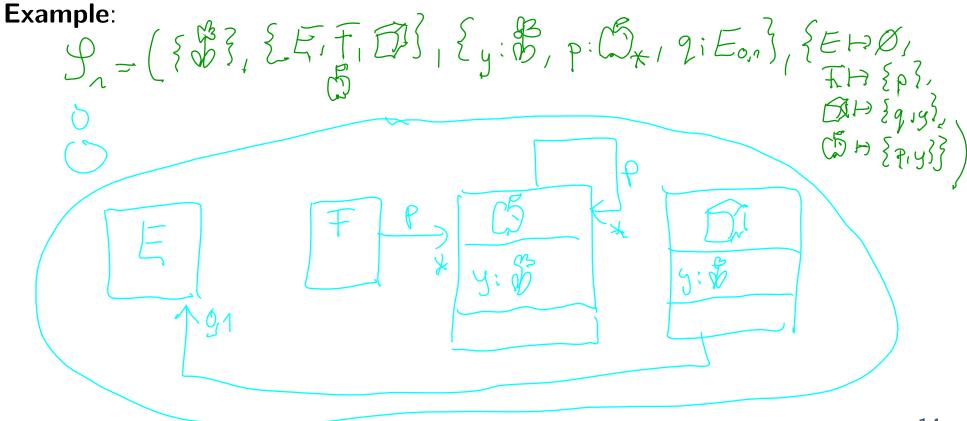
- (basic) types ${\mathscr T}$ and classes ${\mathscr C}$, (both finite),
- typed attributes V, τ from $\mathscr T$ or $C_{0,1}$ or C_* , $C\in\mathscr C$,
- $atr: \mathscr{C} \to 2^V$ mapping classes to attributes.

Example: basic types classes attributes that type int $\mathcal{S}_0 = (\{Int\}, \{C, D\}, \{x : Int, p : C_{0,1}, n : C_*\}, \{C \mapsto \{p, n\}, D \mapsto \{x\}\})$

Basic Object System Signature Another Example

 $\mathscr{S} = (\mathscr{T}, \mathscr{C}, V, atr)$ where

- (basic) types ${\mathscr T}$ and classes ${\mathscr C}$, (both finite),
- typed attributes V, τ from $\mathscr T$ or $C_{0,1}$ or C_* , $C\in\mathscr C$,
- $atr: \mathscr{C} \to 2^V$ mapping classes to attributes.



Basic Object System Structure

Definition. A Basic Object System Structure of

$$\mathscr{S} = (\mathscr{T}, \mathscr{C}, V, atr)$$

is a domain function 2 which assigns to each type a domain, i.e.

- $\tau \in \mathscr{T}$ is mapped to $\mathscr{D}(\tau)$,
- $C \in \mathscr{C}$ is mapped to an infinite set $\mathscr{D}(C)$ of (object) identities. Note: Object identities only have the "=" operation; object identities of different classes are disjoint, i.e. $\forall \, C, D \in \mathscr{C}: C \neq D \rightarrow \mathscr{D}(C) \cap \mathscr{D}(D) = \emptyset$.
- C_* and $C_{0,1}$ for $C \in \mathscr{C}$ are mapped to $2^{\mathscr{D}(C)}$.

We use $\mathscr{D}(\mathscr{C})$ to denote $\bigcup_{C\in\mathscr{C}}\mathscr{D}(C)$; analogously $\mathscr{D}(\mathscr{C}_*)$.

Note: We identify objects and object identities, because both uniquely determine each other (cf. OCL 2.0 standard).

Basic Object System Structure Example

Wanted: a structure for signature

$$\mathscr{S}_0 = (\{Int\}, \{C, D\}, \{x : Int, p : C_{0,1}, n : C_*\}, \{C \mapsto \{p, n\}, D \mapsto \{x\}\})$$

Recall: by definition, seek a \mathcal{D} which maps

- $\tau \in \mathscr{T}$ to some $\mathscr{D}(\tau)$,
- $c \in \mathscr{C}$ to **some** identities $\mathscr{D}(C)$ (infinite, disjoint for different classes),
- C_* and $C_{0,1}$ for $C \in \mathscr{C}$ to $\mathscr{D}(C_{0,1}) = \mathscr{D}(C_*) = 2^{\mathscr{D}(C)}$.

alternative

 $\mathcal{D}(Int) = \mathbb{Z}$ $\mathcal{D}(C) = \mathbb{N}^{+} \times \{C\} = \{16, 26, 36, 12\}$ $\mathcal{D}_{2}(C) = \{1, 3, 5, \dots\}$ $\mathscr{D}(Int) = /\!\!\!/$ $\mathcal{D}(D) = \mathbb{N}^{\frac{1}{2}} \times \{\mathbb{D}\} = \{1_{\mathbb{D}}, 2_{\mathbb{D}}, 3_{\mathbb{D}}, \dots\} \qquad \mathcal{D}(\mathbb{D}) = \{2, 4, 6, \dots\}$ $\mathscr{D}(C_{0,1}) = \mathscr{D}(C_*) = 2^{\mathcal{N}^{\dagger} \times \{c\}}$ $\mathscr{D}(D_{0,1}) = \mathscr{D}(D_*) = 2^{\mathcal{D}(D)}$

all object identifies partial function from partial function of domains

Definition. Let \mathscr{D} be a structure of $\mathscr{S} = (\mathscr{T}, \mathscr{K}, V, atr)$.

A system state of \mathscr{G}/wrt . \mathscr{D} is a **type-consistent** mapping $\sigma: \mathscr{D}(\mathscr{C}) \nrightarrow (V \nrightarrow (\mathscr{D}(\mathscr{T}) \cup \mathscr{D}(\mathscr{C}_*))).$

$$\sigma: \widetilde{\mathscr{D}(\mathscr{C})} \nrightarrow (V \nrightarrow (\mathscr{D}(\mathscr{T}) \cup \mathscr{D}(\mathscr{C}_*)))$$

That is, for each $u \in \mathcal{Q}(C)$, $C \in \mathcal{C}$, if $u \in \text{dom}(\sigma)$

- $\operatorname{dom}(\sigma(u)) = \operatorname{atr}(C)$
- $\bullet \ (\sigma(u)(v) \in \mathscr{D}(\tau) \text{ if } v : \tau, \tau \in \mathscr{T}$
- $\sigma(u)(v) \in \mathscr{D}(D_*)$ if $v: D_{0,1}$ or $v: D_*$ with $D \in \mathscr{C}$

We call $u \in \mathcal{D}(\mathscr{C})$ alive in σ if and only if $u \in \text{dom}(\sigma)$.

We use $\Sigma_{\mathscr{L}}^{\mathscr{D}}$ to denote the set of all system states of \mathscr{S} wrt. \mathscr{D} .

System State Example

Signature, Structure:

$$\mathscr{S}_0 = (\{Int\}, \{C, D\}, \{x : Int, p : C_{0,1}, n : C_*\}, \{C \mapsto \{p, n\}, D \mapsto \{x\}\})$$

$$\mathscr{D}(Int) = \mathbb{Z}, \quad \mathscr{D}(C) = \{1_C, 2_C, 3_C, ...\}, \quad \mathscr{D}(D) = \{1_D, 2_D, 3_D, ...\}$$

Wanted: $\sigma: \mathcal{D}(\mathscr{C}) \nrightarrow (V \nrightarrow (\mathcal{D}(\mathscr{T}) \cup \mathcal{D}(\mathscr{C}_*)))$ such that

- $dom(\sigma(u)) = atr(C)$,
- $\sigma(u)(v) \in \mathscr{D}(\tau)$ if $v: \tau, \tau \in \mathscr{T}$, $\sigma(u)(v) \in \mathscr{D}(C_*)$ if $v: D_*$ with $D \in \mathscr{C}$

or
$$= 0$$
 to supply function

one way to read out:

or $= \{1_{cl} + \sum_{l} \{p + \sum_{l} \{1_{cl}\}, n + \sum_{l} \{5_{cl}, 6_{cl}\}\}\}\}$
 $= 0$ bject 1_{cl} bas a p -link to 1_{cl} (i.e. to itself)

With D_2 :

 $= 0$ bject 1_{cl} refers to

System State Example

Signature, Structure:

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Wanted: $\sigma: \mathscr{D}(\mathscr{C}) \nrightarrow (V \nrightarrow (\mathscr{D}(\mathscr{T}) \cup \mathscr{D}(\mathscr{C}_*)))$ such that

- $dom(\sigma(u)) = atr(C)$,
- $\sigma(u)(v) \in \mathscr{D}(\tau)$ if $v: \tau, \tau \in \mathscr{T}$,
- $\sigma(u)(v) \in \mathcal{D}(C_*)$ if $v: D_*$ with $D \in \mathscr{C}$.
- Concrete, explicit:

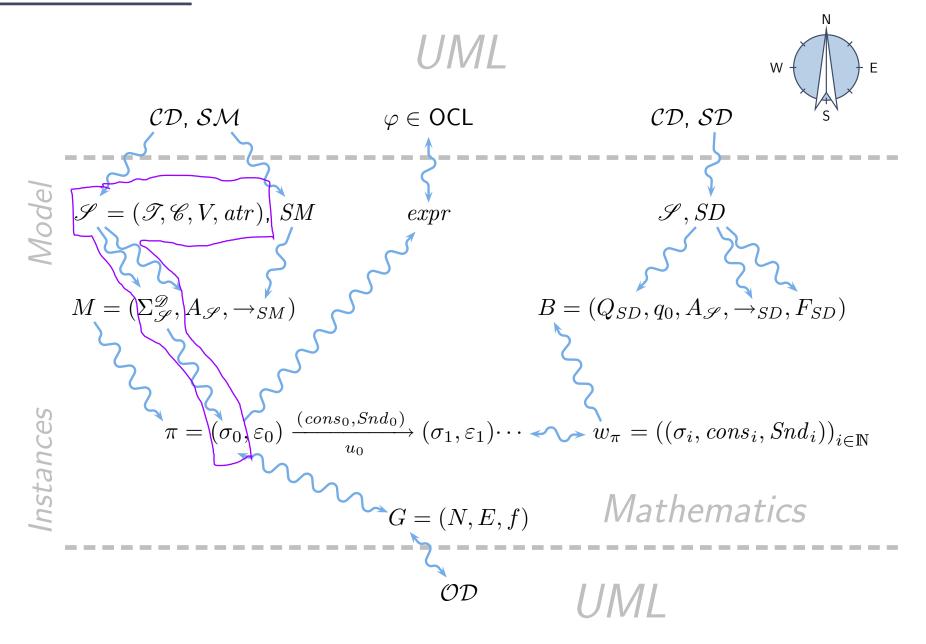
$$\sigma = \{ \downarrow C \mapsto \{p \mapsto \emptyset, n \mapsto \{5_C\}\}, 5_C \mapsto \{p \mapsto \emptyset, n \mapsto \emptyset\}, 1_D \mapsto \{x \mapsto 23\} \}.$$

Alternative: symbolic system state

$$\sigma = \{ \overrightarrow{c_1} \mapsto \{p \mapsto \emptyset, n \mapsto \{c_2\}\}, \overrightarrow{c_2} \mapsto \{p \mapsto \emptyset, n \mapsto \emptyset\}, d \mapsto \{x \mapsto 23\} \}$$
 assuming $\overrightarrow{c_1}, \overrightarrow{c_2} \in \mathscr{D}(C), d \in \mathscr{D}(D), c_1 \neq c_2.$

You Are Here.

Course Map



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