

Software Design, Modelling and Analysis in UML

Lecture 17: Hierarchical State Machines II

2014-01-20

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Contents & Goals

Last Lecture:

- State Machines and OCL
- Hierarchical State Machines Syntax
- Initial and Final State

This Lecture:

- **Educational Objectives:** Capabilities for following tasks/questions.
 - What does this State Machine mean? What happens if I inject this event?
 - Can you please model the following behaviour.
 - What does this **hierarchical** State Machine mean? What **may happen** if I inject this event?
 - What is: AND-State, OR-State, pseudo-state, entry/exit/do, final state, . . .
- **Content:**
 - Composite State Semantics
 - The Rest

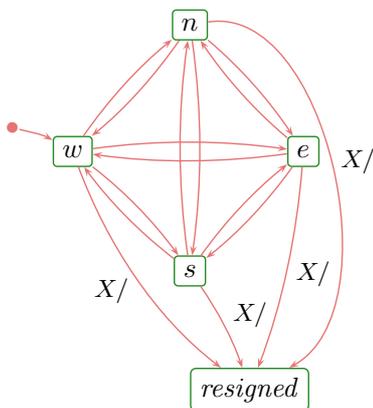
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Composite States

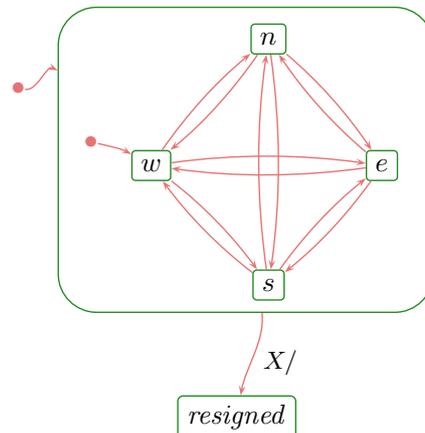
(formalisation follows [Damm et al., 2003])

Composite States

- In a sense, composite states are about **abbreviation**, **structuring**, and **avoiding redundancy**.
- Idea: in Tron, for the Player's Statemachine, instead of

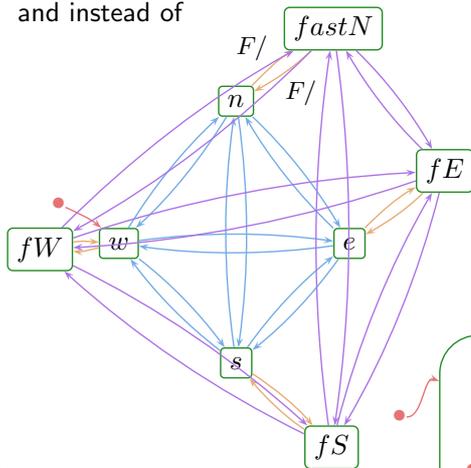


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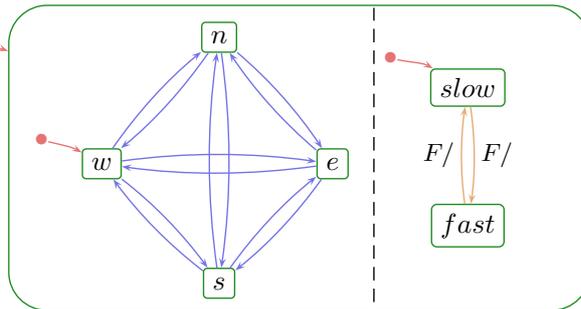


Composite States

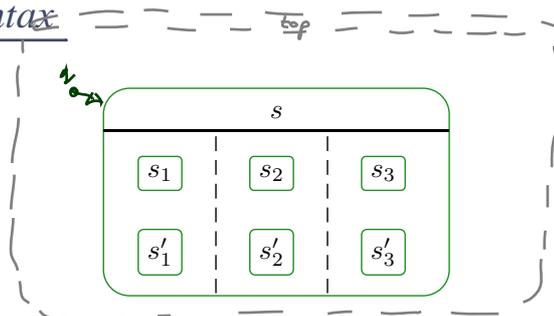
and instead of



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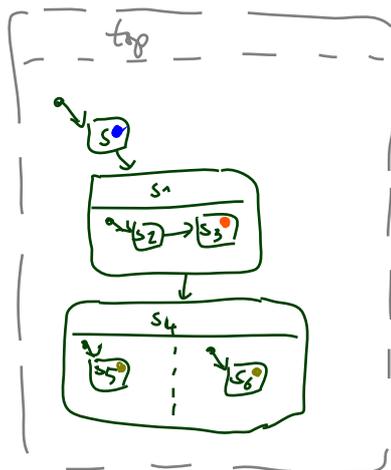
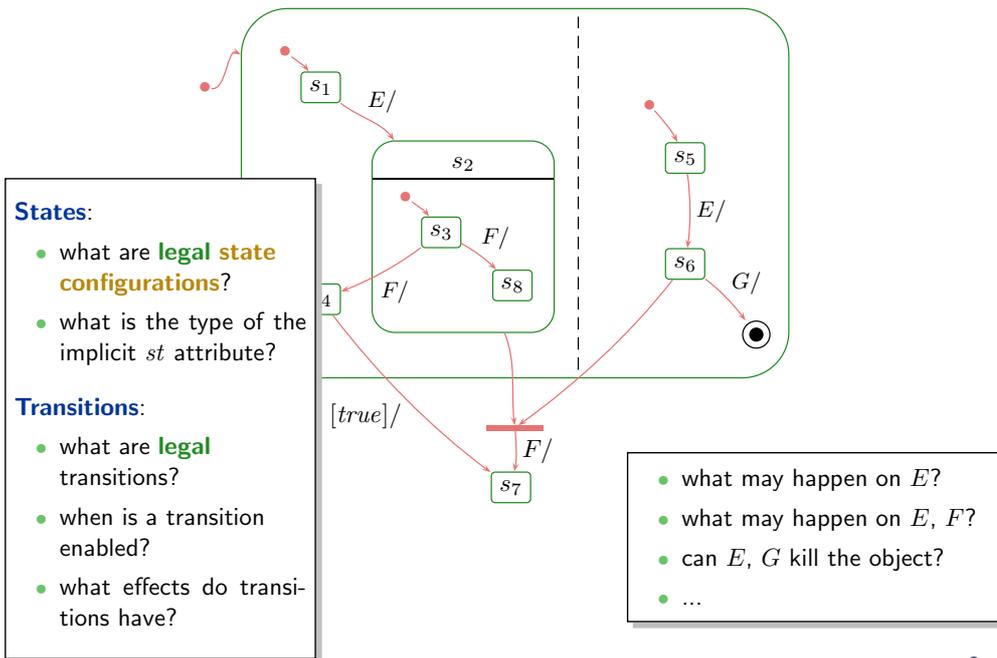
Recall: Syntax



translates to

$$\begin{aligned}
 & (q, \text{init}) \\
 & \underbrace{\{(top, st), (s, st), (s_1, st)(s'_1, st)(s_2, st)(s'_2, st)(s_3, st)(s'_3, st)\}}_{S, \text{kind}} \\
 & \underbrace{\{top \mapsto \{s\}, s \mapsto \{\{s_1, s'_1\}, \{s_2, s'_2\}, \{s_3, s'_3\}\}, s_1 \mapsto \emptyset, s'_1 \mapsto \emptyset, \dots\}}_{\text{region}} \\
 & \rightarrow, \psi, \text{annot}
 \end{aligned}$$

Composite States: Blessing or Curse?



OLD: $st: S \leftarrow$ set of states
 $st = s$

NEW: $st: 2^S \leftarrow$ sets of states

$st = \{s, top\}$

$st = \{s_3, s_1, top\}$

$st = \{ \{s_5, s_4, \dots\}, \{s_6, s_4, \dots\}, \{s_5, s_6, s_4, top\} \}$

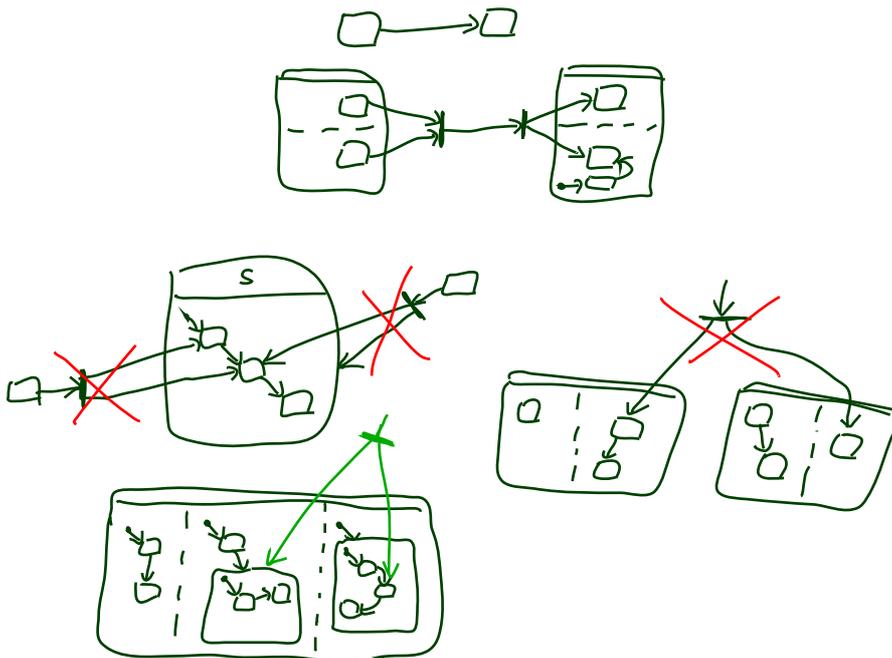
$st = \{s_2, s_6\}$ INCONSISTENT

equivalent information:
 $st = \{s_5, s_6\}$

State Configuration

- The type of st is from now on a **set of** states, i.e. $st : 2^S$
- A set $S_1 \subseteq S$ is called (**legal**) **state configurations** if and only if
 - $top \in S_1$, and
 - for each state $s \in S_1$, for each non-empty region $\emptyset \neq R \in region(s)$, exactly one (non pseudo-state) child of s (from R) is in S_1 , i.e.

$$|\{s_0 \in R \mid kind(s_0) \in \{st, fin\}\} \cap S_1| = 1.$$



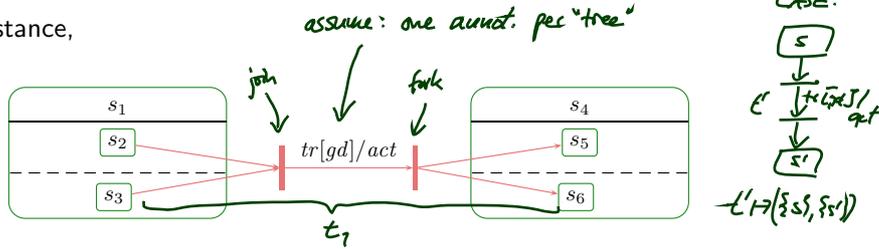
Syntax: Fork/Join

- For brevity, we always consider transitions with (possibly) multiple sources and targets, i.e.

$$\psi : (\rightarrow) \rightarrow (2^S \setminus \emptyset) \times (2^S \setminus \emptyset)$$

set of src states
set of target or desc. states

- For instance,



translates to

$$(S, kind, region, \underbrace{\{t_1\}}_{\rightarrow}, \underbrace{\{t_1 \mapsto (\{s_2, s_3\}, \{s_5, s_6\})\}}_{\psi}, \underbrace{\{t_1 \mapsto (tr, gd, act)\}}_{annot})$$

- Naming convention: $\psi(t) = (source(t), target(t))$.

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A Partial Order on States

The substate- (or **child-**) relation induces a **partial order on states**:

- $top \leq s$, for all $s \in S$,
- $s \leq s'$, for all $s' \in child(s)$,
- transitive, reflexive, antisymmetric,
- $s' \leq s$ and $s'' \leq s$ implies $s' \leq s''$ or $s'' \leq s'$.



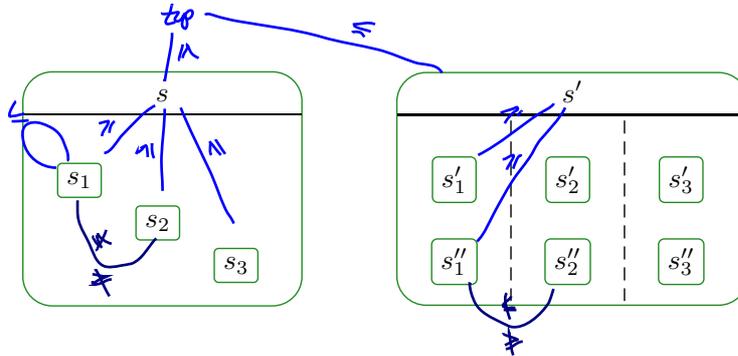
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$\forall s \bullet s \leq s$
write $s \geq s'$ iff $s' \leq s$



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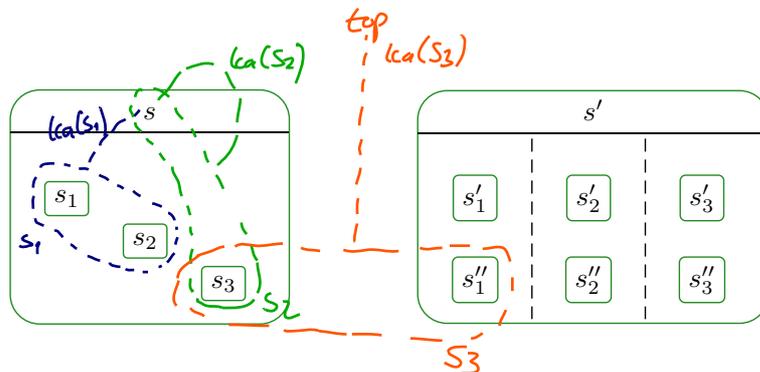
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Least Common Ancestor and Ting

- The **least common ancestor** is the function $lca : 2^S \setminus \{\emptyset\} \rightarrow S$ such that
 - The states in S_1 are (transitive) children of $lca(S_1)$, i.e.

$$lca(S_1) \leq s, \text{ for all } s \in S_1 \subseteq S,$$

- $lca(S_1)$ is minimal, i.e. if $\hat{s} \leq s$ for all $s \in S_1$, then $\hat{s} \leq lca(S_1)$
- **Note:** $lca(S_1)$ exists for all $S_1 \subseteq S$ (last candidate: top).



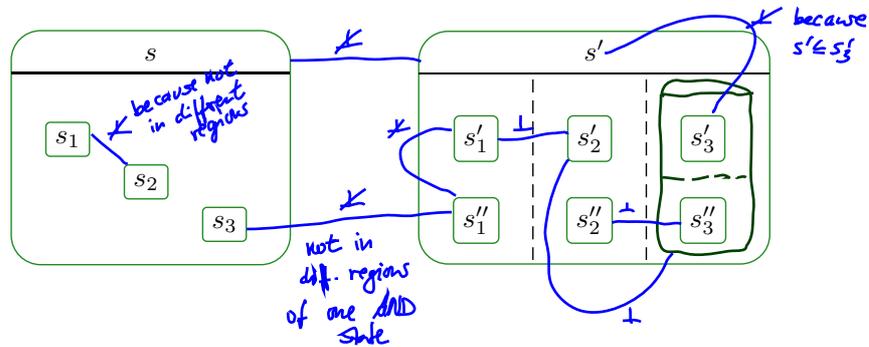
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Least Common Ancestor and Ting

- Two states $s_1, s_2 \in S$ are called **orthogonal**, denoted $s_1 \perp s_2$, if and only if
 - they are unordered, i.e. $s_1 \not\leq s_2$ and $s_2 \not\leq s_1$, and
 - they "live" in different regions of an AND-state, i.e.

$$\exists s, \text{region}(s) = \{S_1, \dots, S_n\} \exists 1 \leq i \neq j \leq n : s_1 \in \text{child}^*(S_i) \wedge s_2 \in \text{child}^*(S_j),$$

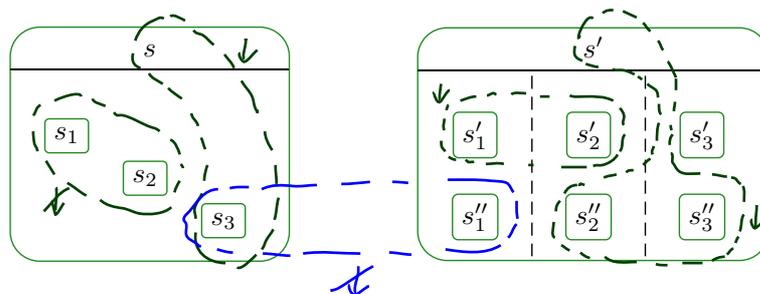


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Least Common Ancestor and Ting

- A set of states $S_1 \subseteq S$ is called **consistent**, denoted by $\downarrow S_1$, if and only if for each $s, s' \in S_1$,
 - $s \leq s'$, or
 - $s' \leq s$, or
 - $s \perp s'$.



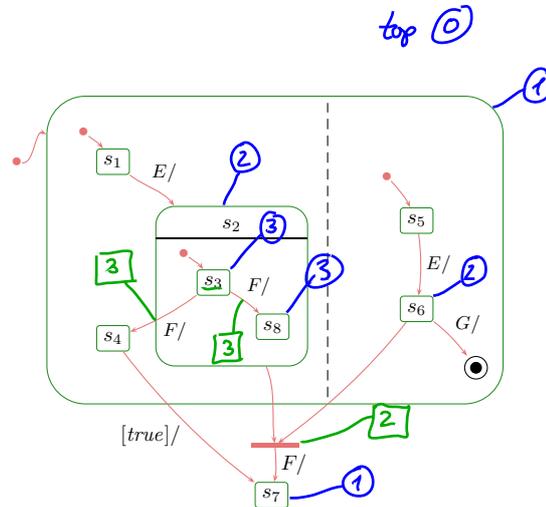
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The Depth of States

- $depth(top) = 0$,
- $depth(s') = depth(s) + 1$, for all $s' \in child(s)$

Example:



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Enabledness in Hierarchical State-Machines

- The **scope** ("set of possibly affected states") of a transition t is the **least common region** of

$$source(t) \cup target(t).$$

- Two transitions t_1, t_2 are called **consistent** if and only if their scopes are orthogonal (i.e. states in scopes pairwise orthogonal).
- The **priority** of transition t is the depth of its innermost source state, i.e.

$$prio(t) := \max\{depth(s) \mid s \in source(t)\}$$

- A set of transitions $T \subseteq \rightarrow$ is **enabled** in an object u if and only if
 - T is consistent,
 - T is maximal wrt. priority,
 - all transitions in T share the same trigger,
 - all guards are satisfied by $\sigma(u)$, and
 - for all $t \in T$, the source states are active, i.e.

$$source(t) \subseteq \sigma(u)(st) (\subseteq S).$$

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Transitions in Hierarchical State-Machines

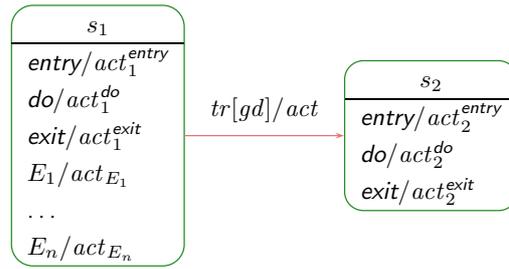
- Let T be a set of transitions enabled in u .
 - Then $(\sigma, \varepsilon) \xrightarrow{(cons, Snd)} (\sigma', \varepsilon')$ if
 - $\sigma'(u)(st)$ consists of the target states of t ,
i.e. for simple states the simple states themselves, for composite states the initial states,
 - σ' , ε' , $cons$, and Snd are the effect of firing each transition $t \in T$ **one by one, in any order**, i.e. for each $t \in T$,
 - the exit transformer of all affected states, highest depth first,
 - the transformer of t ,
 - the entry transformer of all affected states, lowest depth first.
- ↪ adjust (2.), (3.), (5.) accordingly.

Entry/Do/Exit Actions, Internal Transitions

Entry/Do/Exit Actions

- In general, with each state $s \in S$ there is associated
 - an **entry**, a **do**, and an **exit** action (default: skip)
 - a possibly empty set of trigger/action pairs called **internal transitions**,

(default: empty). $E_1, \dots, E_n \in \mathcal{E}$, 'entry', 'do', 'exit' are reserved names!



- Recall: each action's supposed to have a transformer. Here: $t_{act_1^{entry}}, t_{act_1^{exit}}, \dots$
- Taking the transition above then amounts to applying

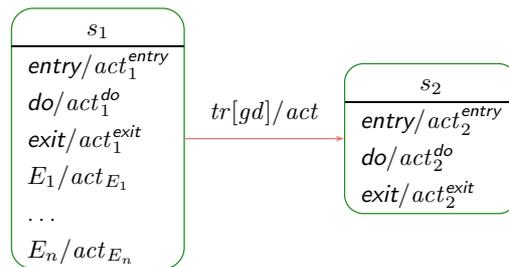
$$t_{act_{s_2}^{entry}} \circ t_{act} \circ t_{act_{s_1}^{exit}}$$

instead of only

$$t_{act}$$

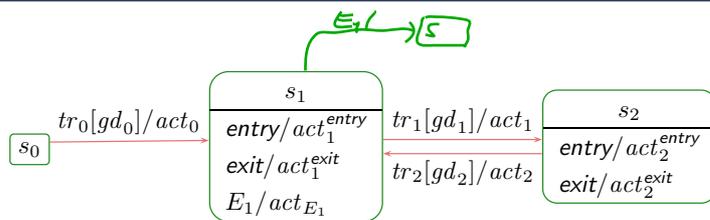
\rightsquigarrow adjust (2.), (3.) accordingly.

Internal Transitions

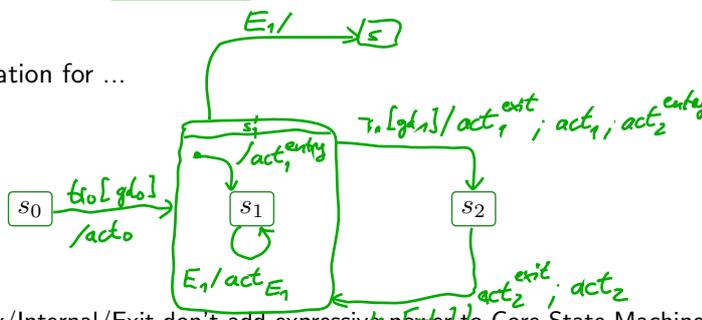


- For **internal transitions**, taking the one for E_1 , for instance, still amounts to taking **only** $t_{act_{E_1}}$.
- Intuition: The state is neither left nor entered, so: no exit, no entry.
 - \rightsquigarrow adjust (2.) accordingly.
- Note: internal transitions also start a run-to-completion step.
- Note: the standard seems not to clarify whether internal transitions have **priority** over regular transitions with the same trigger at the same state. Some code generators assume that internal transitions have priority!

Alternative View: Entry/Exit/Internal as Abbreviations

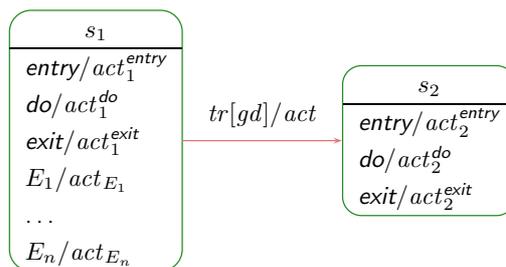


- ... as abbreviation for ...



- That is: Entry/Internal/Exit don't add expressive power to Core State Machines. If internal actions should have priority, s_1 can be embedded into an OR-state (see later).
- Abbreviation may avoid confusion in context of hierarchical states (see later).

Do Actions



- **Intuition:** after entering a state, start its do-action.
- If the do-action terminates,
 - then the state is considered **completed**,
- otherwise,
 - if the state is left before termination, the do-action is stopped.
- Recall the overall UML State Machine philosophy:
 - **"An object is either idle or doing a run-to-completion step."**
- Now, what is it exactly while the do action is executing...?

References

References

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