# Software Design, Modelling and Analysis in UML Lecture 02: Semantical Model

### 2014-10-23

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### Contents & Goals

### Last Lecture:

- Motivation: model-based development of things (houses, software) to cope with complexity, detect errors early
- Model-based (or -driven) Software Engineering
- UML Mode of the Lecture: Blueprint.

### This Lecture:

- Educational Objectives: Capabilities for these tasks/questions:
  - Why is UML of the form it is?
  - Shall one feel bad if not using all diagrams during software development?
  - What is a signature, an object, a system state, etc.?
     What's the purpose of signature, object, etc. in the course?
  - How do Basic Object System Signatures relate to UML class diagrams?

#### • Content:

- Brief history of UML
- Basic Object System Signature, Structure, and System State

Why (of all things) UML?

# Why (of all things) UML?

- Pre-Note: being a modelling languages doesn't mean being graphical (or: being a visual formalism [Harel]).
- [Kastens and Büning, 2008] consider as examples:
  - Sets, Relations, Functions
  - Terms and Algebras
  - Propositional and Predicate Logic
  - Graphs
  - XML Schema, Entity Relation Diagrams, UML Class Diagrams
  - Finite Automata, Petri Nets, UML State Machines
- **Pro**: visual formalisms are found appealing and easier to grasp. Yet they are not necessarily easier to write!
- **Beware**: you may meet people who dislike visual formalisms just for being graphical maybe because it is easier to "trick" people with a meaningless picture than with a meaningless formula.
  - More serious: it's maybe easier to misunderstand a picture than a formula.  $\frac{1}{4/23}$

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# A Brief History of UML

- Boxes/lines and finite automata are used to visualise software for ages.
- 1970's, Software Crisis<sup>TM</sup>

   Idea: learn from engineering disciplines to handle growing complexity.
   Languages: Flowcharts, Nassi-Shneiderman, Entity-Relation Diagrams
- Mid 1980's: Statecharts [Harel, 1987], StateMate<sup>TM</sup> [Harel et al., 1990]

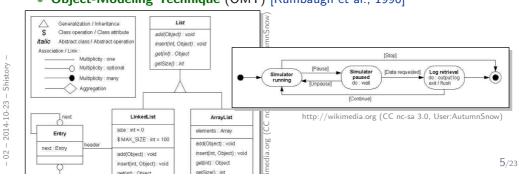


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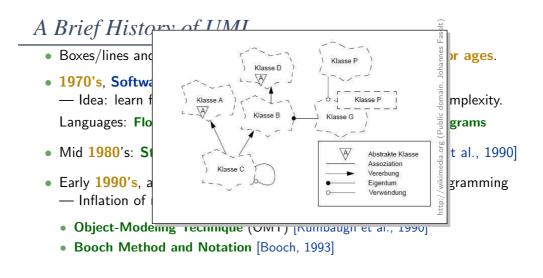
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- Early 1990's, advent of Object-Oriented-Analysis/Design/Programming
   Inflation of notations and methods, most prominent:



• Object-Modeling Technique (OMT) [Rumbaugh et al., 1990]



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## A Brief History of UML

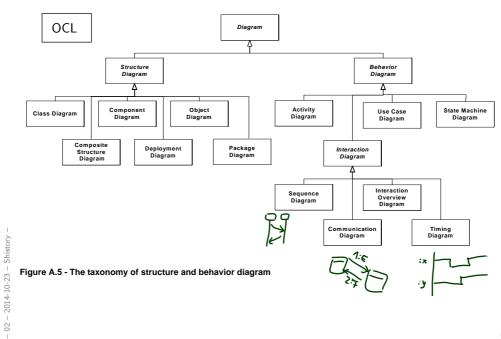
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   Inflation of notations and methods, most prominent:
  - Object-Modeling Technique (OMT) [Rumbaugh et al., 1990]
  - Booch Method and Notation [Booch, 1993]
  - Object-Oriented Software Engineering (OOSE) [Jacobson et al., 1992]

Each "persuasion" selling books, tools, seminars...

- Late 1990's: joint effort UML 0.x, 1.x
  - Standards published by **Object Management Group** (OMG), "*international, open membership, not-for-profit* **computer industry** *consortium*".

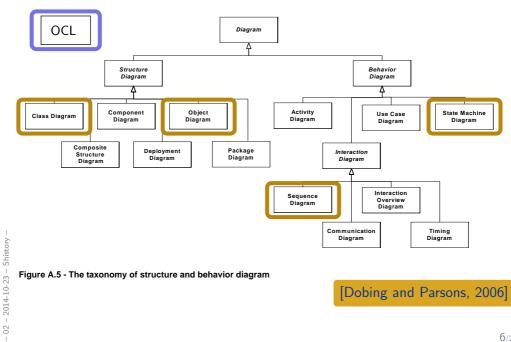
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## UML Overview [омд, 2007b, 684]



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# UML Overview [OMG, 2007b, 684]



## Common Expectations on UML

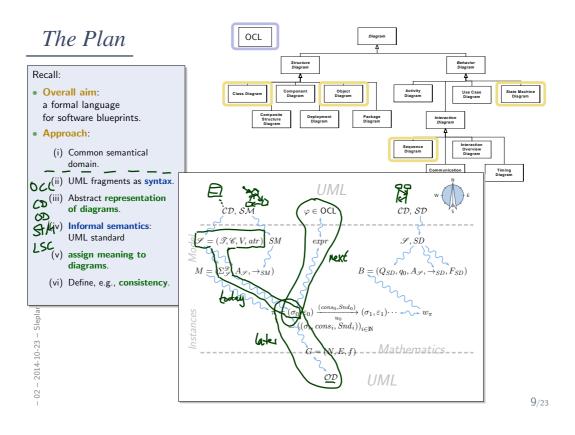
- Easily writeable, readable even by customers
- Powerful enough to bridge the gap between idea and implementation
- Means to tame complexity by separation of concerns ("views")
- Unambiguous
- Standardised, exchangeable between modelling tools
- UML standard says how to develop software
- Using UML leads to better software
- ...

# We will see...

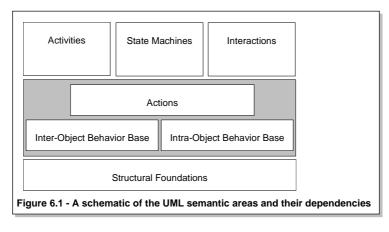
Seriously: After the course, you should have an own opinion on each of these claims. In how far/in what sense does it hold? Why? Why not? How can it be achieved? Which ones are really only hopes and expectations? ...?

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Course Map Revisited



UML: Semantic Areas

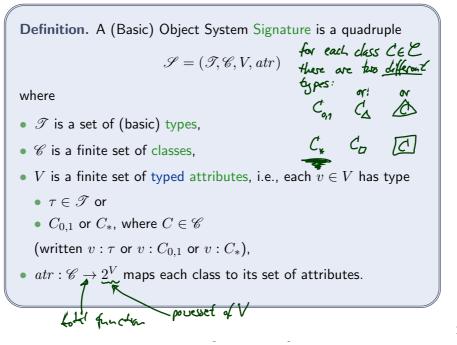


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Common Semantical Domain

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# Basic Object System Signature



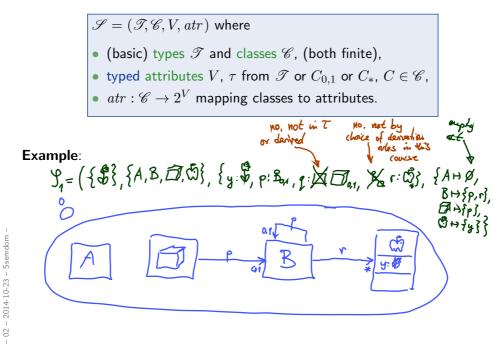
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## Basic Object System Signature Example

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 $\mathcal{S} = (\mathcal{T}, \mathcal{C}, V, atr) \text{ where}$ • (basic) types  $\mathcal{T}$  and classes  $\mathcal{C}$ , (both finite), • typed attributes  $V, \tau$  from  $\mathcal{T}$  or  $C_{0,1}$  or  $C_*, C \in \mathcal{C}$ , •  $atr : \mathcal{C} \to 2^V$  mapping classes to attributes. Example: types classes attributes  $\mathcal{S}_0 = (\{Int\}, \{C, D\}, \{x : Int, p : C_{0,1}, n : C_*\}, \{C \mapsto \{p, n\}, D \mapsto \{x\}\})$ attribute attribute attribute x has type n has type  $z \in [p, n]$  attribute  $z \in [p, n]$  attribute [p] attribute

# Basic Object System Signature Another Example



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**Definition.** A Basic Object System Structure of  $\mathscr{S} = (\mathscr{T}, \mathscr{C}, V, atr)$  is a domain function  $\mathscr{D}$  which assigns to each type a domain, i.e.

- $\tau \in \mathscr{T}$  is mapped to  $\mathscr{D}(\tau)$ ,
- $C \in \mathscr{C}$  is mapped to an infinite set  $\mathscr{D}(C)$  of (object) identities. Note: Object identities only have the "=" operation; object identities of different classes are disjoint, i.e.  $\forall C, D \in \mathscr{C} : C \neq D \rightarrow \mathscr{D}(C) \cap \mathscr{D}(D) = \emptyset$ .
- $C_*$  and  $C_{0,1}$  for  $C \in \mathscr{C}$  are mapped to  $2^{\mathscr{D}(C)}$ .

We use  $\mathscr{D}(\mathscr{C})$  to denote  $\bigcup_{C\in\mathscr{C}}\mathscr{D}(C);$  analogously  $\mathscr{D}(\mathscr{C}_*).$ 

**Note**: We identify objects and object identities, because both uniquely determine each other (cf. OCL 2.0 standard).

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## Basic Object System Structure Example

#### Wanted: a structure for signature

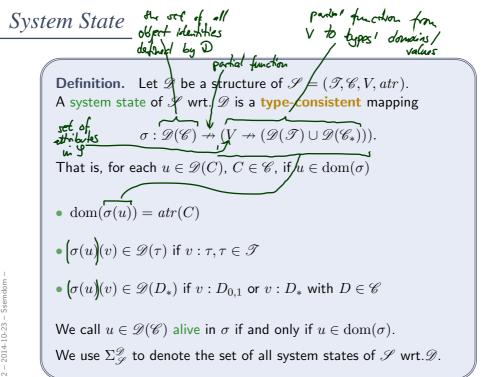
 $\mathscr{S}_0 = (\{Int\}, \{C, D\}, \{x : Int, p : C_{0,1}, n : C_*\}, \{C \mapsto \{p, n\}, D \mapsto \{x\}\})$ 

Recall: by definition, seek a  $\mathscr{D}$  which maps

- $\tau \in \mathscr{T}$  to some  $\mathscr{D}(\tau)$ ,
- $c\in \mathscr{C}$  to some identities  $\mathscr{D}(C)$  (infinite, disjoint for different classes),
- $C_*$  and  $C_{0,1}$  for  $C \in \mathscr{C}$  to  $\mathscr{D}(C_{0,1}) = \mathscr{D}(C_*) = 2^{\mathscr{D}(C)}$ .

 $\begin{aligned} \mathcal{D}(Int) &= \mathbb{Z} \\ \mathcal{D}(C) &= \mathbb{N}^{t} \times \{\mathcal{C}\} \stackrel{\sim}{=} \{1_{\mathcal{C}}, 2_{\mathcal{C}}, \cdots \} \quad 2_{\mathcal{C}} \\ \mathcal{D}(D) &= \mathbb{N}^{t} \times \{\mathcal{D}\} \stackrel{\sim}{=} \{1_{\mathcal{C}}, 2_{\mathcal{C}}, \cdots \} \quad 2_{\mathcal{C}} \\ \mathcal{D}(D) &= \mathbb{N}^{t} \times \{\mathcal{D}\} \stackrel{\sim}{=} \{1_{\mathcal{C}}, 2_{\mathcal{C}}, \cdots \} \quad 2_{\mathcal{C}} \\ \mathcal{D}(D) &= \mathbb{N}^{t} \times \{\mathcal{D}\} \stackrel{\sim}{=} \{1_{\mathcal{C}}, 2_{\mathcal{C}}, \cdots \} \quad 2_{\mathcal{C}} \\ \mathcal{D}(C_{0,1}) &= \mathcal{D}(C_{*}) &= 2^{\mathbb{D}(C)} \\ \mathcal{D}(D_{0,1}) &= \mathcal{D}(D_{*}) &= 2^{\mathbb{D}(C)} \quad \mathbf{e}_{\mathcal{C}} \quad \mathbf{e}_{\mathcal{D}} \quad \mathbf{e}_{\mathcal{D}} \\ \mathcal{D}(\mathcal{D}_{\mathcal{D}}) &= 2^{\mathbb{D}(C)} \\ \mathcal{D}(D_{0,1}) &= \mathcal{D}(D_{*}) &= 2^{\mathbb{D}(C)} \\ \mathbf{e}_{\mathcal{D}} \quad \mathbf{e}_{\mathcal{D}} \quad \mathbf{e}_{\mathcal{D}} \\ \mathcal{D}(\mathcal{D}_{\mathcal{D}}) &= 2^{\mathbb{D}(C)} \\ \mathcal{D}(\mathcal{D}) \\ \mathcal{D}(\mathcal{D}) &= 2^{\mathbb{D}(C)} \\ \mathcal{D}(\mathcal{D}) &= 2^{\mathbb{D}(C)} \\ \mathcal{D}(\mathcal{D}) \\ \mathcal{D}(\mathcal{D}) &= 2^{\mathbb{D}(C)} \\ \mathcal{D}(\mathcal{D}) \\ \mathcal{D}(\mathcal{D}) &= 2^{\mathbb{D}(C)} \\ \mathcal{D}(\mathcal{D}) \\ \mathcal{D}$ 

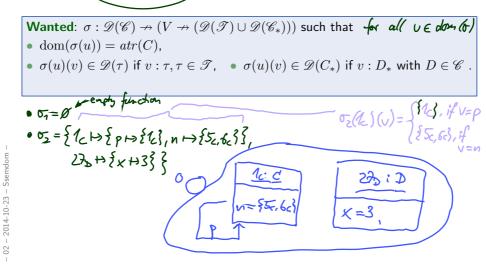
$$\begin{split} \mathcal{Y}_{q} &= \left( \left\{ \begin{array}{c} \left\{ \begin{array}{c} \left\{ \begin{array}{c} \left\{ \right\} \right\} \\ \left\{ A, B, \overrightarrow{D}, \overrightarrow{\Omega} \right\} \\ \left\{ y, \overrightarrow{\Psi} \right\} \\ p : B_{0,1}, q : \overrightarrow{D}_{0,1}, r : \left( \begin{array}{c} \left\{ A \mapsto \emptyset \right\} \\ B \mapsto \{p, r\} \\ \overrightarrow{D}_{1}, \beta \\ \end{array} \right\} \\ \left[ \begin{array}{c} \left\{ B \mapsto \{p, r\} \\ \overrightarrow{D}_{1}, \beta \\ \end{array} \right\} \\ \left[ \begin{array}{c} \left\{ A \mapsto \emptyset \\ \overrightarrow{D}_{1}, \alpha \\ \end{array} \right\} \\ \left[ \begin{array}{c} \left\{ A \mapsto \emptyset \\ \overrightarrow{D}_{1}, \alpha \\ \end{array} \right\} \\ \left[ \begin{array}{c} \left\{ A \mapsto \emptyset \\ \overrightarrow{D}_{1}, \alpha \\ \end{array} \right\} \\ \left[ \begin{array}{c} \left\{ A \mapsto \emptyset \\ \overrightarrow{D}_{1}, \alpha \\ 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### System State Example

### Signature, Structure:

$$\begin{aligned} \mathscr{S}_0 &= \left(\{Int\}, \{C, D\}, \{\underline{x} : Int, p : C_{0,1}, n : C_*\}, \{C \mapsto \{p, n\}, D \mapsto \{x\}\}\right) \\ &\underbrace{\mathscr{D}(Int) = \mathbb{Z}}_{}, \quad \mathscr{D}(C) \neq \{1_C, 2_C, 3_C, \ldots\}, \quad \mathscr{D}(D) = \{1_D, 2_D, 3_D, \ldots\} \end{aligned}$$



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System State Example

### Signature, Structure:

$$\begin{split} \mathscr{S}_{0} &= (\{Int\}, \{C, D\}, \{x: Int, p: C_{0,1}, n: C_{*}\}, \{C \mapsto \{p, n\}, D \mapsto \{x\}\}) \\ \mathscr{D}(Int) &= \mathbb{Z}, \quad \mathscr{D}(C) = \{1_{C}, 2_{C}, 3_{C}, \ldots\}, \quad \mathscr{D}(D) = \{1_{D}, 2_{D}, 3_{D}, \ldots\} \end{split}$$

$$\begin{split} & \textbf{Wanted: } \sigma: \mathscr{D}(\mathscr{C}) \nrightarrow (V \nrightarrow (\mathscr{D}(\mathscr{T}) \cup \mathscr{D}(\mathscr{C}_*))) \text{ such that} \\ & \text{ dom}(\sigma(u)) = atr(C), \\ & \sigma(u)(v) \in \mathscr{D}(\tau) \text{ if } v: \tau, \tau \in \mathscr{T}, \\ & \sigma(u)(v) \in \mathscr{D}(C_*) \text{ if } v: D_* \text{ with } D \in \mathscr{C} . \end{split}$$

• Concrete, explicit:

$$\sigma = \{1_C \mapsto \{p \mapsto \emptyset, n \mapsto \{5_C\}\}, 5_C \mapsto \{p \mapsto \emptyset, n \mapsto \emptyset\}, 1_D \mapsto \{x \mapsto 23\}\}$$

### • Alternative: symbolic system state

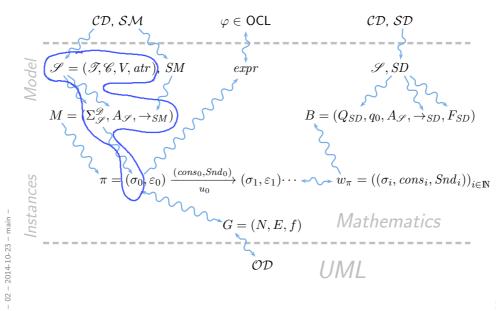
$$\sigma = \{c_1 \mapsto \{p \mapsto \emptyset, n \mapsto \{c_2\}\}, c_2 \mapsto \{p \mapsto \emptyset, n \mapsto \emptyset\}, d \mapsto \{x \mapsto 23\}\}$$
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You Are Here.

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# Course Map

# UML



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References

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