Software Design, Modelling and Analysis in UML

Lecture 21: Inheritance

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Motivations for Generalisation

- Re-use,
 Sharing,
 Avoiding Redundancy,
 Modularisation,
 Separation of Concerns,
 Abstraction,
- Extensibility,
- ightarrow See textbooks on object-oriented analysis, development, programming.

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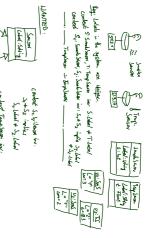
Contents & Goals

Last Lecture:

This Lecture:

- Live Sequence Charts Semantics
- Educational Objectives: Capabilities for following tasks/questions. What's the Liskov Substitution Principle?
- What's the effect of inheritance on LSCs, State Machines, System States? What is late/early binding?
 What is the subset, what the uplink semantics of inheritance?

- Inheritance in UML: concrete syntax
 Lislov Substitution Principle desired semantics
 Two approaches to obtain desired semantics





Abstract Syntax

Inheritance: Syntax

where F/mth are methods, analogously to attributes and V defined an object of G and an object of G. The second of G is a sum of G. is a generalisation relation such that $C \lhd^+ C$ for no $C \in \mathscr{C}$ ("acyclic") $\mathcal{S} = (\mathcal{S}, \mathcal{C}, V, atr, \mathcal{E}, F, mth, \triangleleft)$

Reflexive, Transitive Closure of Generalisation

Extend Typing Rules

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System States

Wanted: a formal representation of "if $C \leq D$ then D "is a' C", i.e.,

(i) D has the same attributes as C, and (ii) $\mathbf D$ objects (identities) can be used in any context where $\mathbf Q$ objects can be used.

We'll discuss two approaches to semantics:

Inheritance: System States

Domain-inclusion Semantics

(more theoretical) (more technical)

Uplink Semantics

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Well-Typedness with Inheritance

Recall: With extension for visibility we obtained

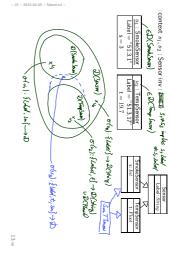
$$\begin{split} v(w) &: \tau_C \to \tau(v) & \langle v : \tau, \xi, \exp r_0, P_\theta \rangle \in \operatorname{atr}(C), \ w : \tau_C \\ v(\exp r_1(w)) &: \tau_{C_2} \to \tau(v) & \langle v : \tau, \xi, \exp r_0, P_\theta \rangle \in \operatorname{atr}(C_2), \\ \exp r_1(w) : \tau_{C_2}, \ w : \tau_{C_1}, \ \operatorname{and} \ C_1 = C_2 \ \operatorname{or} \ \xi = + \end{split}$$

 $v(expr_1(w)) : \tau_{C_2} \rightarrow \tau(v)$

 $\langle v:\tau,\xi,\exp r_0,R_e\rangle\in\operatorname{adr}(C),$ $w:\tau_{C_1},r_{C_2}\in C_1$ $w:\tau_{C_2},r_{C_2}\in C_1$ $\langle v:\tau,\xi,\exp r_0,R_e\rangle\in\operatorname{adr}(C_2),$ $\exp r_0(w):\tau_{C_2}, v:\tau_{C_2}, v:\tau_{C_2},$ $\exp r_1(w):\tau_{C_2}, w:\tau_{C_2},$ $\operatorname{and}(C_1=C_2)\circ\xi=+\operatorname{or}(C_2\preceq C_1\operatorname{and}\xi=\#)$ $\operatorname{add}(\operatorname{code}(-3i)\operatorname{adr})\circ\operatorname{adr}(C_2\preceq C_1\operatorname{and}\xi=\#)$ $\operatorname{add}(\operatorname{code}(-3i)\operatorname{adr})\circ\operatorname{adr}(\operatorname{code}(-3i)\operatorname{adr})\circ\operatorname{adr}(\operatorname{code}(-3i)\operatorname{adr})\circ\operatorname{adr}(\operatorname{code}(-3i)\operatorname{adr})\circ\operatorname{adr}(\operatorname{code}(-3i)\operatorname{adr})\circ\operatorname{adr}(\operatorname{code}(-3i)\operatorname{adr})\circ\operatorname{adr}(\operatorname{code}(-3i)\operatorname{adr})\circ\operatorname{adr}(\operatorname{code}(-3i)\operatorname{adr})\circ\operatorname{adr}(\operatorname{code}(-3i)\operatorname{adr})\circ\operatorname{adr}(\operatorname{code}(-3i)\operatorname{adr})\circ\operatorname{adr}(\operatorname{code}(-3i)\operatorname{adr})\circ\operatorname{adr}(\operatorname{code}(-3i)\operatorname{adr})\circ\operatorname{adr}(\operatorname{code}(-3i)\operatorname{adr})\circ\operatorname{adr}(\operatorname{code}(-3i)\operatorname{adr})\circ\operatorname{adr}(\operatorname{code}(-3i)\operatorname{adr})\circ\operatorname{adr}(\operatorname{code}(-3i)\operatorname{adr})\circ\operatorname{adr}(\operatorname{code}(-3i)\operatorname{adr})\circ\operatorname{adr}(\operatorname{code}(-3i)\operatorname{adr})\circ\operatorname{adr}(\operatorname{code}(-3i)\operatorname{adr})\circ\operatorname{adr}(\operatorname{code}(-3i)\operatorname{adr})\circ\operatorname{adr}(\operatorname{code}(-3i)\operatorname{adr})\circ\operatorname{adr}(\operatorname{code}(-3i)\operatorname{adr})\circ\operatorname{adr}(\operatorname{code}(-3i)\operatorname{adr})\circ\operatorname{adr}(\operatorname{code}(-3i)\operatorname{adr})\circ\operatorname{adr}(\operatorname{code}(-3i)\operatorname{adr})\circ\operatorname{adr}(\operatorname{code}(-3i)\operatorname{adr})\circ\operatorname{adr}(\operatorname{code}(-3i)\operatorname{adr})\circ\operatorname{adr}(\operatorname{code}(-3i)\operatorname{adr})\circ\operatorname{adr}(\operatorname{code}(-3i)\operatorname{adr})\circ\operatorname{adr}(\operatorname{code}(-3i)\operatorname{adr})\circ\operatorname{adr}(\operatorname{code}(-3i)\operatorname{adr})\circ\operatorname{adr}(\operatorname{code}(-3i)\operatorname{adr})\circ\operatorname{adr}(\operatorname{code}(-3i)\operatorname{adr})\circ\operatorname{adr}(\operatorname{code}(-3i)\operatorname{adr})\circ\operatorname{adr}(\operatorname{code}(-3i)\operatorname{adr})\circ\operatorname{adr}(\operatorname{code}(-3i)\operatorname{adr})\circ\operatorname{adr}(\operatorname{code}(-3i)\operatorname{adr})\circ\operatorname{adr}(\operatorname{code}(-3i)\operatorname{adr})\circ\operatorname{adr}(\operatorname{code}(-3i)\operatorname{adr})\circ\operatorname{adr}(\operatorname{code}(-3i)\operatorname{adr})\circ\operatorname{adr}(\operatorname{code}(-3i)\operatorname{adr})\circ\operatorname{adr}(\operatorname{code}(-3i)\operatorname{adr}(\operatorname{code}(-3i)\operatorname{adr})\circ\operatorname{adr}(\operatorname{code}(-3i)\operatorname{adr})\circ\operatorname{adr}(\operatorname{code}(-3i)\operatorname{adr})\circ\operatorname{adr}(\operatorname{code}(-3i)\operatorname{adr})\circ\operatorname{adr}(\operatorname{code}(-3i)\operatorname{adr}(-3i)\operatorname{adr}(\operatorname{code}(-3i)\operatorname{adr}(-3i)\operatorname{adr}(-3i)\circ\operatorname{ad$

Domain Inclusion Semantics

Domain Inclusion Semantics: Idea



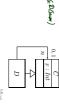
Satisfying OCL Constraints (Domain Inclusion)

- Let $\mathcal{M}=(\mathcal{CD},\mathcal{CD},\mathcal{SM},\mathcal{I})$ be a UML model, and $\mathcal D$ a structure.
- We (continue to) say $\mathcal{M} \models expr$ for context C inv : $expr_0 \in Inv(\mathcal{M})$ iff =expr

$$\begin{split} \forall \pi = (\sigma_i, \varepsilon_i)_{i \in \mathbb{N}} \in \llbracket \mathcal{M} \rrbracket \quad \forall i \in \mathbb{N} \quad \forall u \in \text{dom}(\sigma_i) \cap \mathscr{D}(C) : \\ I\llbracket expr_0 \rrbracket (\sigma_i, \{self \mapsto u\}) = 1. \end{split}$$

• $\mathcal M$ is (still) consistent if and only if it satisfies all constraints in $\mathit{Inv}(\mathcal M)$.

• Example: ©: [42.34] | 42.75 • O((Top-han) & O(han) $dom(r) \cap \mathcal{D}(Surper) = \{v_1, v_2\}$



Domain Inclusion Structure

Let $\mathscr{S}=(\mathscr{T},\mathscr{C},V,atr,\mathscr{E},F,mth,\lhd)$ be a signature.

Now a structure D

- [as before] maps types, classes, associations to domains,
- [for completeness] methods to transformers,
 [as before] indentities of instances of classes not (transitively) related by generalisation are disjoint,
- [changed] the indentities of a super-class comprise all identities of sub-classes, i.e.

 $\forall C \in \mathcal{C} : \mathcal{D}(C) \supseteq \bigcup_{C \triangleleft D} \mathcal{D}(D).$

Note: the old setting coincides with the special case $\triangleleft = \emptyset$.

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Domain Inclusion System States

Now: a system state of ${\mathcal S}$ wrt. ${\mathcal D}$ is a type-consistent mapping

$$\sigma: \mathscr{D}(\mathscr{C}) \to (V \to (\mathscr{D}(\mathscr{T}) \cup \mathscr{D}(\mathscr{C}_{0,1}) \cup \mathscr{D}(\mathscr{C}_*)))$$

that is, for all $u \in dom(\sigma) \cap \mathscr{D}(C)$,

- $\bullet \ \ [\text{as before}] \ \sigma(u)(v) \in \mathscr{D}(\tau) \ \text{if} \ v:\tau, \ \tau \in \mathscr{T} \ \text{or} \ \tau \in \{C_*,C_{0,1}\}.$
- [changed] $dom(\sigma(u)) = \bigcup_{C_0 \leq C} atr(C_0)$,



Note: the old setting still coincides with the special case $\triangleleft = \emptyset$.

Transformers (Domain Inclusion)

Inheritance and State Machines: Triggers Wanted: triggers shall also be sensitive for inherited events, sub-class shall execute super-class' state-machine (unless overridden).

Transformers also remain the same, e.g. [VL 12, p. 18]

 $update(expr_1, v, expr_2): (\sigma, \varepsilon) \mapsto (\sigma', \varepsilon)$

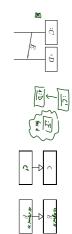
with where $u=I[\![expr_1]\!](\sigma).$ $\sigma' = \sigma[u \mapsto \sigma(u)[v \mapsto I[\![expr_2]\!](\sigma)]]$

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 If u becomes stable in s', then b = 1. It does become stable if and only
there is no transition without trigger enabled for u in (\sigma', \sigma').
 Otherwise b = 0. ullet (σ', ε') results from applying t_{act} to $(\sigma, arepsilon)$ and removing u_B from the ether, i.e * $\exists u \in \text{dom}(\sigma \cap \mathcal{G}(C)) \exists u_g \in \mathcal{G}(\mathcal{S}) : u_g \in ready(\varepsilon, u)$ * u is stable and in state machine state s, i.e. $\sigma(u)(stable) = 1$ and $\sigma(u)(st) =$ where $\tilde{\sigma} = \sigma[u.params_E \mapsto u_e]$. $(\sigma'',\varepsilon') = t_{act}(\bar{\sigma},\varepsilon \ominus u_E),$ $\sigma' = (\sigma''[u.st \mapsto s', u.stable \mapsto b, u.params_E \mapsto \emptyset])[g(\mathscr{C})\backslash \{u_E\}$ $\exists \, (s,F,expr,act,s') \in \rightarrow (\mathcal{SM}_C) : F = E \wedge I[expr](\tilde{\sigma}) = 1$ $(\sigma, \varepsilon) \xrightarrow[u]{\text{cons,Snd}} (\sigma', \varepsilon')$ if * H**

Domain Inclusion and Interactions



- Similar to satisfaction of OCL expressions above:
- \bullet An instance line stands for all instances of C (exact or inheriting).
- Satisfaction of event observation has to take inheritance into account, too, so we have to fix, e.g.

 σ , cons, $Snd \models_{\beta} E_{x,y}^!$

if and only if

 $\beta(x)$ sends an F-event to $\beta\!\!\!/_{\!\!\!\text{U}})$ where $E \preceq F$.

ullet C-instance line also binds to C'-objects.

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Uplink Semantics

Uplink Semantics: Idea

context $s_1, s_2:$ Sensor inv : v < 0

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Pre-Processing for the Uplink Semantics

Uplink Semantics

Continue with the existing definition of structure, i.e. disjoint domains for identities.

Have an implicit association from the child to each parent part (similar to the implicit attribute for stability).

x: Int D

- ullet For each pair $C \lhd D$, extend D by a (fresh) association
- $uplink_C: C \text{ with } \mu = [1,1], \ \xi = +$

(Exercise: public necessary?)

- Given expression v (or f) in the context of class D,
- ullet let C be the smallest class wrt. " \preceq " such that
- $C \preceq D$, and

• $C::v \in atr(D)$

• then there exists (by definition) $C \lhd C_1 \lhd \ldots \lhd C_n \lhd D$,

 \circ Apply (a different) pre-processing to make appropriate use of that association, e.g. rewrite (C++)

in D to

 $\mathtt{uplink}_C \mathbin{-\!\!\!\!\!\!>} \mathbf{x} = 0;$ $\mathbf{x} = 0;$

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• normalise v to (= replace by)

 $uplink_{C_n} -> \cdots -> uplink_{C_1}.C::v$

If no (unique) smallest class exists,
 the model is considered not well-formed; the expression is ambiguous.

Uplink Structure, System State, Typing

- Typing and transformers remain unchanged the preprocessing has put everything in shape.

Definition of structure remains unchanged.

Definition of system state remains unchanged.

Satisfying OCL Constraints (Uplink)

```
    We (continue to) say

                                                          \bullet Let \mathcal{M}=(\mathscr{CD},\mathscr{OD},\mathscr{SM},\mathscr{I}) be a UML model, and \mathscr{D} a structure.
```

 $\mathcal{M} \models expr$

 $\underbrace{\operatorname{context} \ C \ \operatorname{inv} : expr_0}_{= expr} \in \operatorname{Inv}(\mathcal{M})$

if and only if

 $\forall \pi = (\sigma_i)_{i \in \mathbb{N}} \in \llbracket \mathcal{M} \rrbracket$ $\forall i \in \mathbb{N}$ $\forall u \in \text{dom}(\sigma_i) \cap \mathcal{D}(C) :$ $I[[expr_0]](\sigma_i, \{self \mapsto u\}) = 1.$

 \bullet $\mathcal M$ is (still) consistent if and only if it satisfies all constraints in $\mathit{Inv}(\mathcal M)$.

Cast-Transformers

```
    Value upcast (C++):

    Identity downcast (C++):

                                                                                                                                                                                                                       Identity upcast (C++):
                       • *c = *d;

    D d;

    D* dp = (D*)cp;

    C* cp = &d;

// copy attribute values of 'd' into 'c', or, // more precise, the values of the C-part of 'd'
                                                                                                                                                                                        // assign address of 'd' to pointer 'cp'
                                                                                                       // assign address of 'd' to pointer 'dp'
```

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Casts in Domain Inclusion and Uplink Semantics

c = d;	D* dp = (D*)cp;	C* cp = &d
bit difficult: set (for all $C \leq D(\cdot, \cdot) : \tau_D \times \Sigma \to \Sigma _{dxt(C)}$ ($(u, \sigma) \mapsto \sigma(u) _{abr(C)} \times \Sigma \mapsto \sigma(u_D) _{abr(C)}$ Note: $\sigma' = \sigma(u_C \mapsto \sigma(u_D) _{abr(C)}$ not type-compatible!	easy: the value of cp is in $\mathcal{G}(D) \cap \mathcal{G}(C)$ because the pointed-to object is a D . Otherwise, error condition.	easy: immediately compatible (in underlying system state) because &d yields an identity from $\mathcal{D}(D) \subset \mathcal{D}(C)$.
easy: By pre-processing, $c = *(d.uplink_C);$	difficult: we need the identity of the <i>D</i> whose <i>C</i> -slice is denoted by <i>cp</i> . (See next slide.)	easy: By pre-processing, $C* cp = d.uplink_C$;

Transformers (Uplink)

```
    What has to change is the create transformer.
```

create(C, expr, v)

ullet Assume, C's inheritance relations are as follows.

 $C_{1,1} \triangleleft \ldots \triangleleft C_{1,n_1} \triangleleft C$,

 $C_{m,1} \triangleleft \ldots \triangleleft C_{m,n_m} \triangleleft C.$

Then, we have to

create one fresh object for each part, e.g.

 $u_{1,1},\ldots,u_{1,n_1},\ldots,u_{m,1},\ldots,u_{m,n_m},$

 set up the uplinks recursively, e.g. $\sigma(u_{1,2})(uplink_{C_{1,1}}) = u_{1,1}.$

And, if we had constructors, be careful with their order.

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Domain Inclusion vs. Uplink Semantics

Identity Downcast with Uplink Semantics

```
• Recall (C++): D d; C*cp = \&d; D*dp = (D*)cp;
```

- Problem: we need the identity of the D whose C-slice is denoted by cp.
- One technical solution:
- Give up disjointness of domains for one additional type comprising all identities, i.e. have

$$\mathtt{all} \in \mathscr{T}, \qquad \mathscr{D}(\mathtt{all}) = \bigcup_{C \in \mathscr{C}} \mathscr{D}(C)$$

- In each _minimal class have associations "mostagec" pointing to most appecialized sites; plus information of which type that site is:
 Then downcast means, depending on the mostagene type (only finitely many possibilities), going down and then up as necessary, e.g.

$$\begin{split} & \texttt{switch}(\texttt{mostspec_type}) \{ \\ & \texttt{case} \ C : \end{split}$$

 $\mathtt{dp} = \mathtt{cp} -\verb|>mostspec-> \mathtt{uplink}_{D_n} -> \ldots -> \mathtt{uplink}_{D_1} -> \mathtt{uplink}_D;$

Domain Inclusion vs. Uplink: Differences

- Note: The uplink semantics views inheritance as an abbreviation:
- We only need to touch transformers (create) and if we had constructors, we didn't even needed that (we could encode the recursive construction of the upper slices by a transformation of the existing constructors.)

- Inheritance doesn't add expressive power.
 And it also doesn't improve conciseness soo dramatically.

As long as we're "early binding", that is...

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Domain Inclusion vs. Uplink: Motivations

Exercise:

What's the point of

- having the tedious adjustments of the theory if it can be approached technically?
- having the tedious technical pre-processing if it can be approached cleanly in the theory?

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More Interesting: Behaviour

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Example: Behaviour of Kinds of Students

Desired Semantics of Specialisation: Subtyping

There is a classical description of what one expects from sub-types, which in the OO domain is closely related to inheritance:

The principle of type substitutability [Liskov, 1988, Liskov and Wing, 1994]. (Liskov Substitution Principle (LSP).)

"...shall be usable..." for UML

"If for each object o_1 of type S there is an object o_2 of type T such that for all programs P defined in terms of T, the behavior of P is unchanged when o_1 is substituted for o_2 then S is a subtype of T."























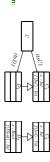


In other words: [Fischer and Wehrheim, 2000]

"An instance of the sub-type shall be usable whenever an instance of the supertype was expected, without a client being able to tell the difference."

So, what's "usable"? Who's a "client"? And what's a "difference"?

Easy: Static Typing for Attributes









assignment itsC1 := itsD1 being well-typed itsC1.x = 0, itsC1.f(0), itsC1! F being well-typed (and doing the right thing).

• x > 0 also well-typed for D_1

Simply define it as being well-typed,
 adjust system state definition to do the right thing.

Static Typing for Methods



Excursus: Late Binding of Behavioural Features

Notions (from category theory): D(Int)CD(Hont)

- invariance,
- covariance,

We could call, e.g. a method, sub-type preserving, if and only if it

- contravariance.
- This is a notion used by many programming languages and easily type-checked.

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 provides a more specialised type as output accepts more general types as input

(contravariant) (covariant).

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Late Binding in the Standard and in Prog. Lang.

In the standard, Section 11.3.10, "CallOperationAction":

Late Binding

What transformer applies in what situation? (Early (compile time) binding.)

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the type of the link determines which imply to trust at the trust at

"Semantic Variation Points

The mechanism for determining the method to be invoked as a result of a call operation is unspecified." [OMG, 2007b, 247]

- In C++,
- methods are by default "(early) compile time binding",
 can be declared to be "late binding" by keyword "virtual",
- the declaration applies to all inheriting classes.
- In Java,

(C::FO)

- methods are "late binding";
 there are patterns to imitate the effect of "early binding"

⊕ ⊕ ⊕

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Note: late binding typically applies only to methods, not to attributes. (But: getter/setter methods have been invented recently.) Exercise: What could be the rationale of the designers of C++?

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Back to the Main Track: "...tell the difference..." for UML

With Only Early Binding ...

- ...we're done (if we realise it correctly in the framework).
- Then
- if we're calling method f of an object u,

- * which is an instance of D with $C \preceq D$ via a Clink, via "A. K-mylono povind by C• then we (by definition) only sea and change the C-part. We cannot tell whether u is a C or an D instance.

So we immediately also have behavioural/dynamic subtyping

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Difficult: Dynamic Subtyping



C::f and D::f are type compatible, but D is not necessarily a sub-type of C.



• Examples: (C++)

int C::f(int) {
 return 0;

int D::f(int) {
 return 1;
}

VS.

}; 2); int C::f(int) {
 return (rand() % ٧S.

int D::f(int x) { return (x % 2);

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Ensuring Sub-Typing for State Machines

Instead, the state machine of a sub-class can only be obtained by applying actions from a restricted set to a copy of the original one.

Roughly (cf. User Guide, p. 760, for details),

But the state machine of a sub-class cannot be drawn from scratch.

In the CASE tool we consider, multiple classes in an inheritance hierarchy can have state machines.

References

Technically, the idea is that (by late binding) only the state machine of the most specialised classes are running.
 By knowledge of the famework, the (code for) state machines of super-classes is still accessible — but using it is hardly a good idea...

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They ensure, that the sub-class is a behavioural sub-type of the super class. (But method implementations can still destroy that property.)

 attach a transition to a different target (limited). add things into (hierarchical) states,

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Sub-Typing Principles Cont'd

In the standard, Section 7.3.36, "Operation"

"Semantic Variation Points

[...] When operations are referred in a specialization rules regarding invariance, covariance or communications of types and preconditions determine whether the specialized classifier is substitutable for its more signeral parent. Such rules <u>Constitute semantic variation points</u> with respect to redefinition of operations. *[ORG. 2013. 106]

So, better: call a method sub-type preserving, if and only if it

(ii) on the old values, has fewer behaviour (i) accepts more input values

(contravariant), (covariant).

Note: This (ii) is no longer a matter of simple type-checking!

And not necessarily the end of the story:

One could, e.g. want to consider execution time.

Or, like [Fischer and Wehrheim, 2000], relax to "fewer observable behaviour", thus admitting the sub-type to do more work on inputs.

Note: "testing" differences depends on the granularity of the semantics.

• Related: "has a weaker pre-condition," "has a stronger post-condition."

(contravariant), (covariant).45/48

[Fischer and Wehrheim, 2000] Fecher, C. and Wehrheim, H. (2000). Behavioural subpring relations for object-ordinated formalisms. In Ris, T., and editor, AMAST, number 1816 in Lecture Notes in Computer Science, Springer-Verlag, [Lisbov, 1988] Lisbov, B. (1989). Data abstraction and hierarchy. SIGPLAN Nat., 21(5):17–24. [Lislov and Wing, 1994] Lislov, B. H. and Wing, J. M. (1994). A behavioral notion of subtyping. ACM Transactions on Programming Languages and Systems (TOPLAS), 16(6):1811-1841.

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