

Software Design, Modelling and Analysis in UML

Lecture 18: Hierarchical State Machines II

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Contents & Goals

Last Lecture:

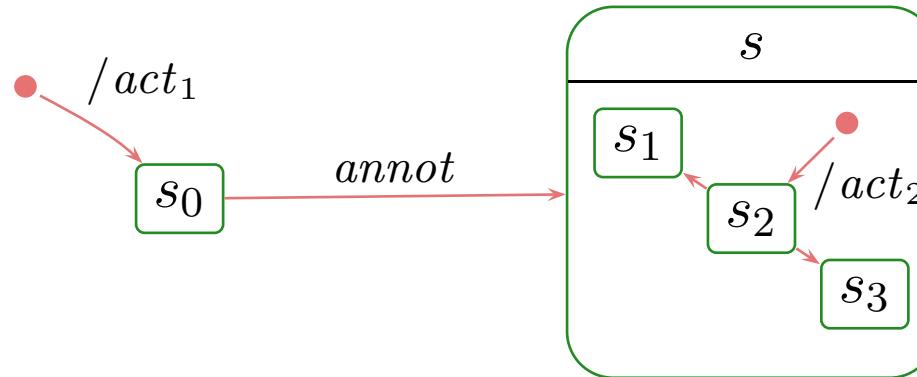
- Hierarchical State Machine Syntax
- Entry/Exit Actions

This Lecture:

- **Educational Objectives:** Capabilities for following tasks/questions.
 - What does this State Machine mean? What happens if I inject this event?
 - Can you please model the following behaviour.
 - What does this **hierarchical** State Machine mean? What **may happen** if I inject this event?
 - What is: AND-State, OR-State, pseudo-state, entry/exit/do, final state, ...
- **Content:**
 - Initial and Final State
 - Composite State Semantics
 - The Rest

Initial Pseudostates and Final States

Initial Pseudostate



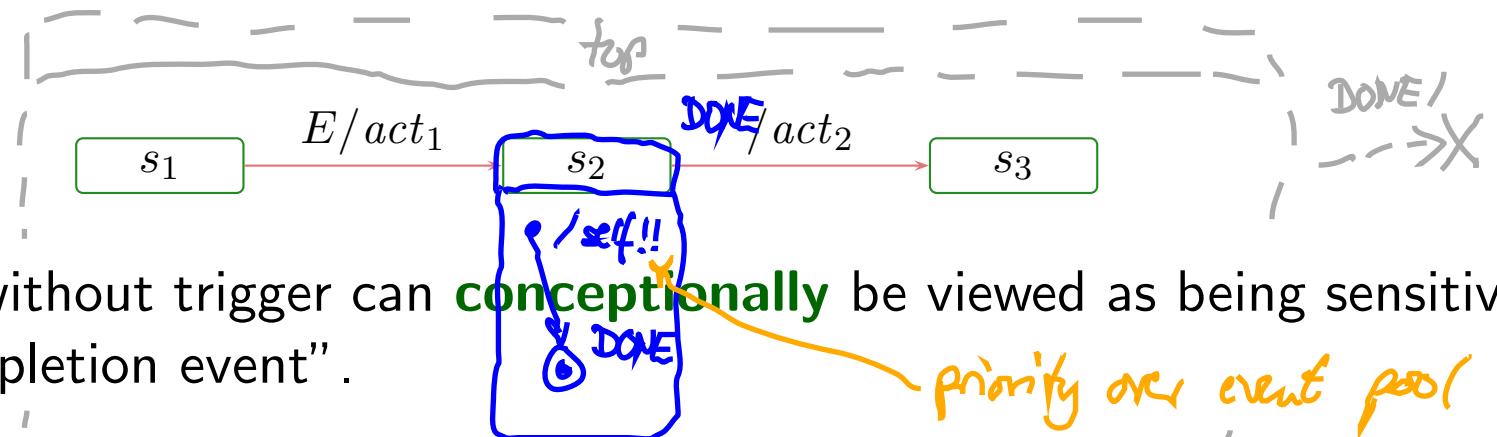
Principle:

- when entering a region **without** a specific destination state,
- then go to a state which is destination of an initiation transition,
- execute the action of the chosen initiation transitions **between** exit and entry actions.

Special case: the region of *top*.

- If class C has a state-machine, then “create- C transformer” is the concatenation of
 - the transformer of the “constructor” of C (here not introduced explicitly) and
 - a transformer corresponding to one initiation transition of the top region.

Towards Final States: Completion of States



- Transitions without trigger can **conceptionally** be viewed as being sensitive for the “completion event”. *priority over event pool*
- Dispatching (here: E) **can then alternatively** be **viewed** as
 - (i) fetch event (here: E) from the ether,
 - (ii) take an enabled transition (here: to s_2),
 - (iii) remove event from the ether,
 - (iv) after having finished entry and do action of current state (here: s_2) — the state is then called **completed** —,
 - (v) raise a **completion event** — with strict priority over events from ether!
 - (vi) if there is a transition enabled which is sensitive for the completion event,
 - then take it (here: (s_2, s_3)).
 - otherwise become stable.

Final States



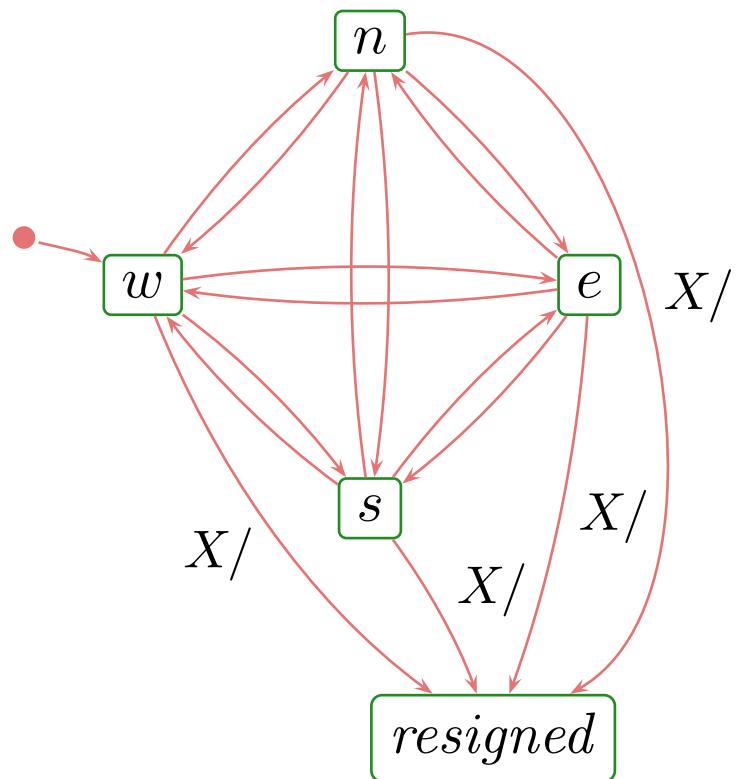
- If
 - a step of object u moves u into a final state (s, fin) , and
 - all sibling regions are in a final state,then (conventionally) a completion event for the current composite state s is raised.
- If there is a transition of a **parent state** (i.e., inverse of *child*) of s enabled which is sensitive for the completion event,
 - then take that transition,
 - otherwise kill u \rightsquigarrow adjust (2.) and (3.) in the semantics accordingly
- **One consequence:**
 u never “survives” reaching a state (s, fin) with $s \in \text{child}(\text{top})$.

Composite States

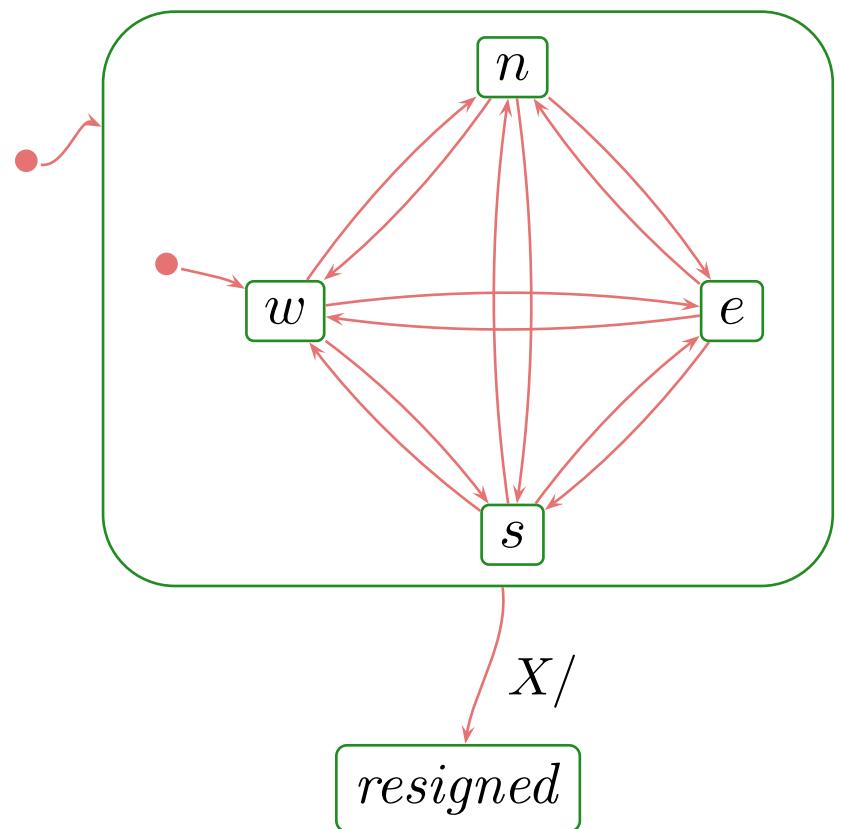
(formalisation follows [Damm et al., 2003])

Composite States

- In a sense, composite states are about **abbreviation, structuring**, and **avoiding redundancy**.
- Idea: in Tron, for the Player's Statemachine,
instead of

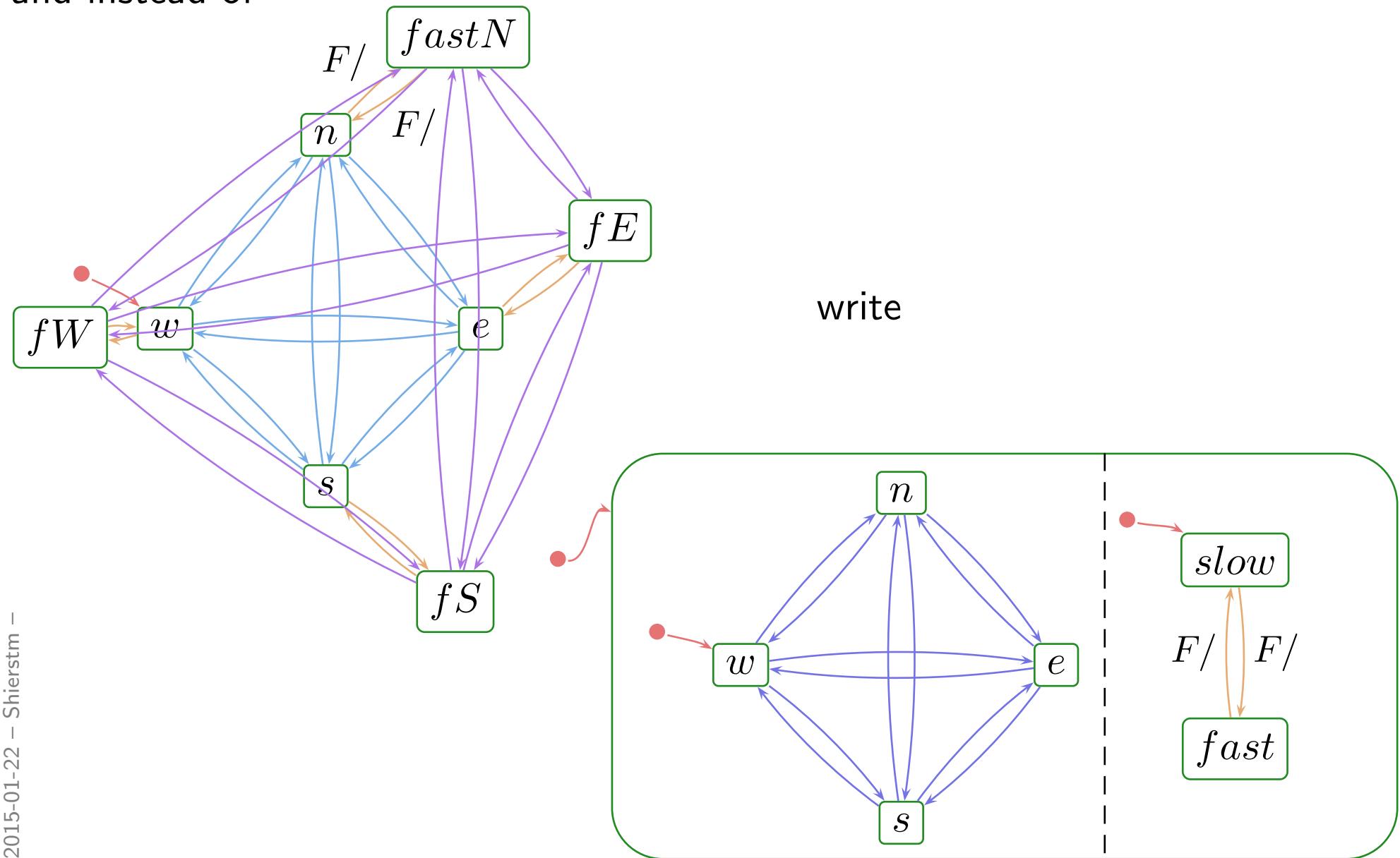


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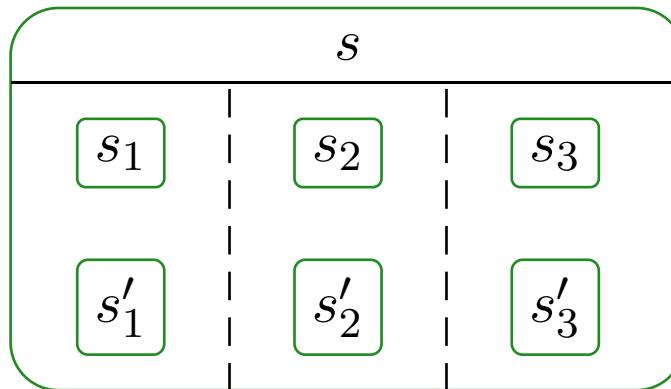


Composite States

and instead of



Recall: Syntax



translates to

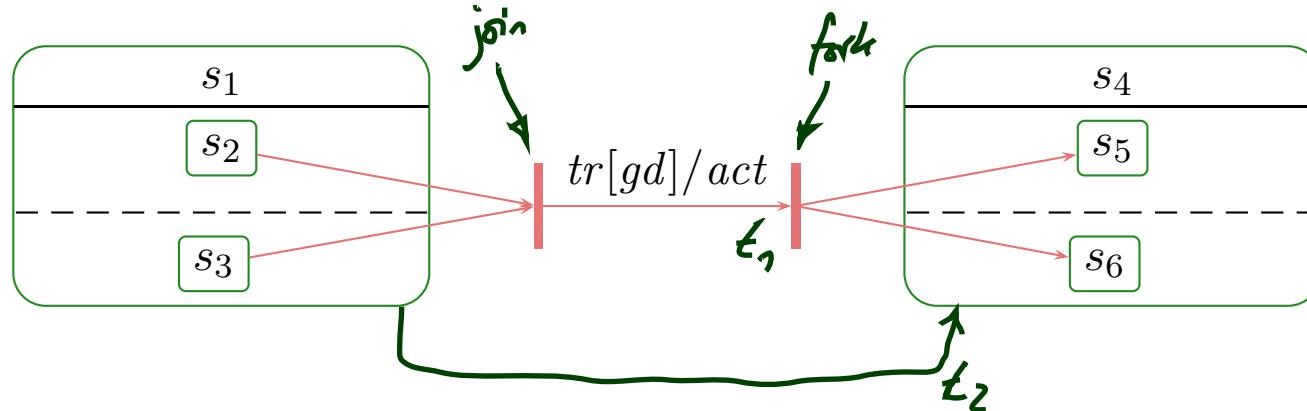
$$\underbrace{\{((top, st), (s, st), (s_1, st) \underbrace{(s'_1, st)(s_2, st)(s'_2, st)(s_3, st)(s'_3, st))\},}_{S, kind} \\ \underbrace{\{ top \mapsto \{ \{s\} \}, s \mapsto \{ \{s_1, s'_1\}, \{s_2, s'_2\}, \{s_3, s'_3\} \}, s_1 \mapsto \emptyset, s'_1 \mapsto \emptyset, \dots \},}_{region} \\ \rightarrow, \psi, annot)$$

Syntax: Fork/Join

- For brevity, we always consider transitions with (possibly) multiple sources and targets, i.e.

$$\psi : (\rightarrow) \rightarrow (2^S \setminus \emptyset) \times (2^S \setminus \emptyset)$$

- For instance,

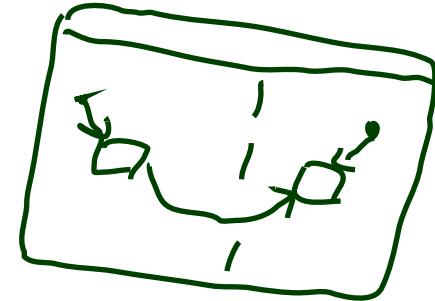
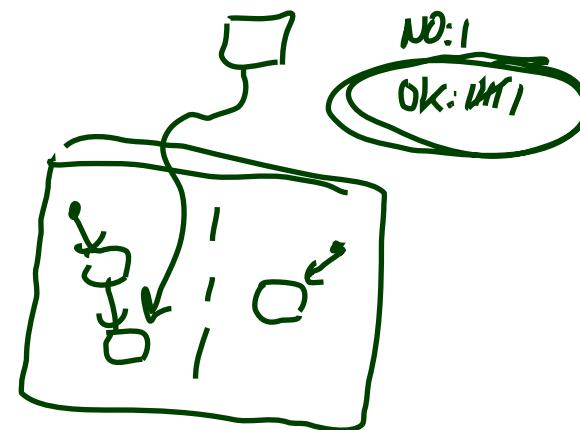
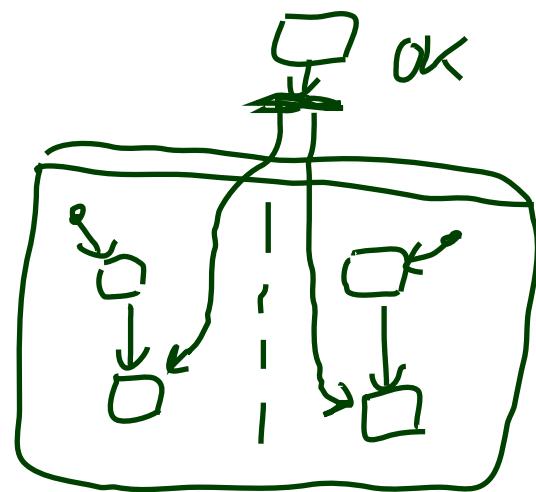
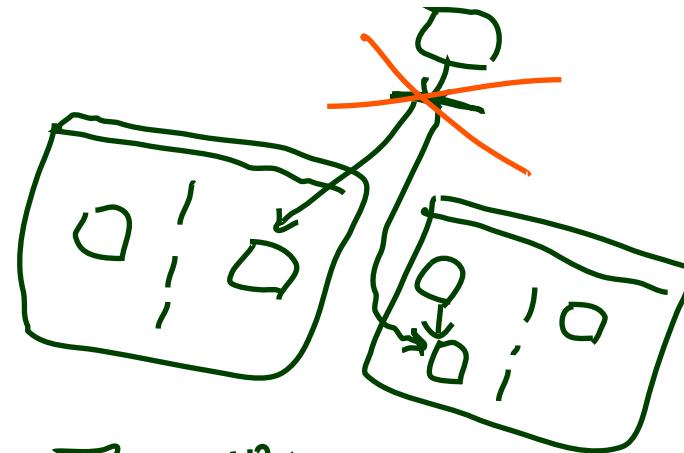
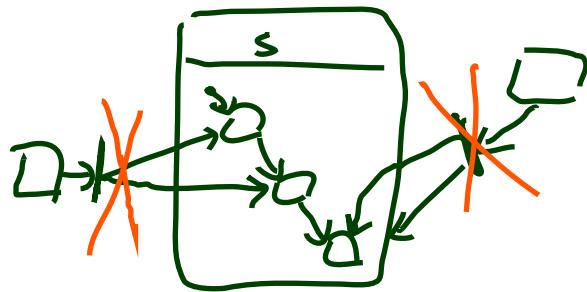
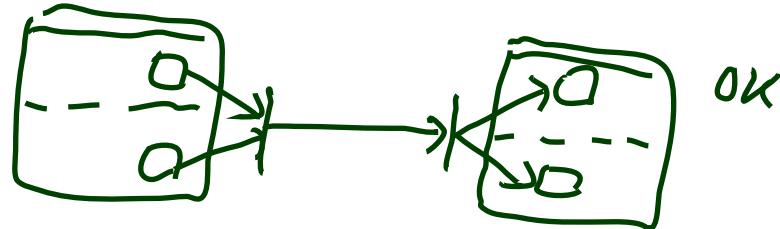


translates to

$$(S, kind, region, \underbrace{\{t_1\}}_{\rightarrow}, \underbrace{\{t_1 \mapsto (\{s_2, s_3\}, \{s_5, s_6\})\}}_{\psi}, \underbrace{\{t_1 \mapsto (tr, gd, act)\}}_{\text{annot}})$$

$t_2 \mapsto (\{s_1\}, \{s_4\})$

- Naming convention: $\psi(t) = (\text{source}(t), \text{target}(t))$.



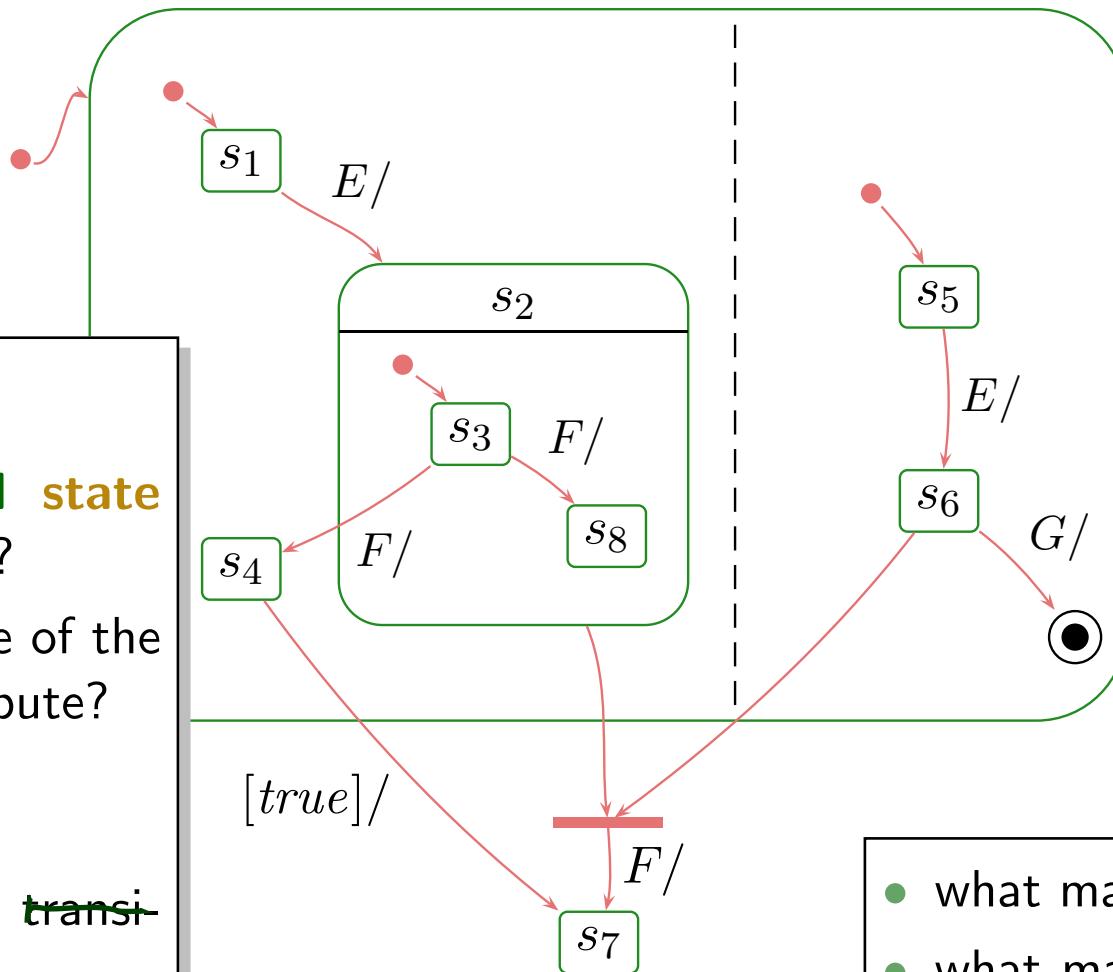
Composite States: Blessing or Curse?

States:

- what are **legal state configurations**?
- what is the type of the implicit *st* attribute?

Transitions:

- what are **legal transitions~~edges~~**?
- when is a transition enabled?
- what effects do transitions have?



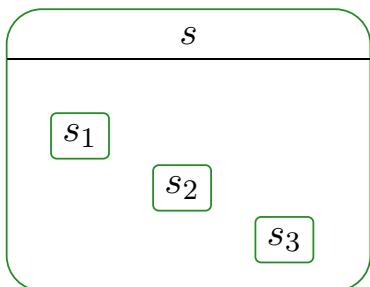
- what may happen on *E*?
- what may happen on *E, F*?
- can *E, G* kill the object?
- ...

State Configuration

- The type of st is from now on **a set of states**, i.e. $st : 2^S$
- A set $S_1 \subseteq S$ is called **(legal) state configurations** if and only if
 - $top \in S_1$, and
 - for each state $s \in S_1$, for each non-empty region $\emptyset \neq R \in region(s)$, exactly one (non pseudo-state) child of s (from R) is in S_1 , i.e.

$$|\{s_0 \in R \mid kind(s_0) \in \{st, fin\}\} \cap S_1| = 1.$$

- **Examples:**



$S = \{s_2\}$ \times (top missing)

$S = \{s_2, top\}$ \times (no child of top's region)

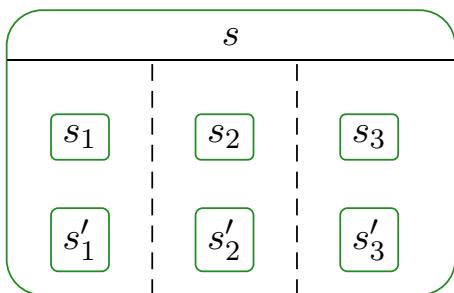
$S = \{top, s, s_2\}$ ✓

State Configuration

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- **Examples:**



$$S = \{top, s, s_1, s_2, s_3\} \quad \checkmark$$

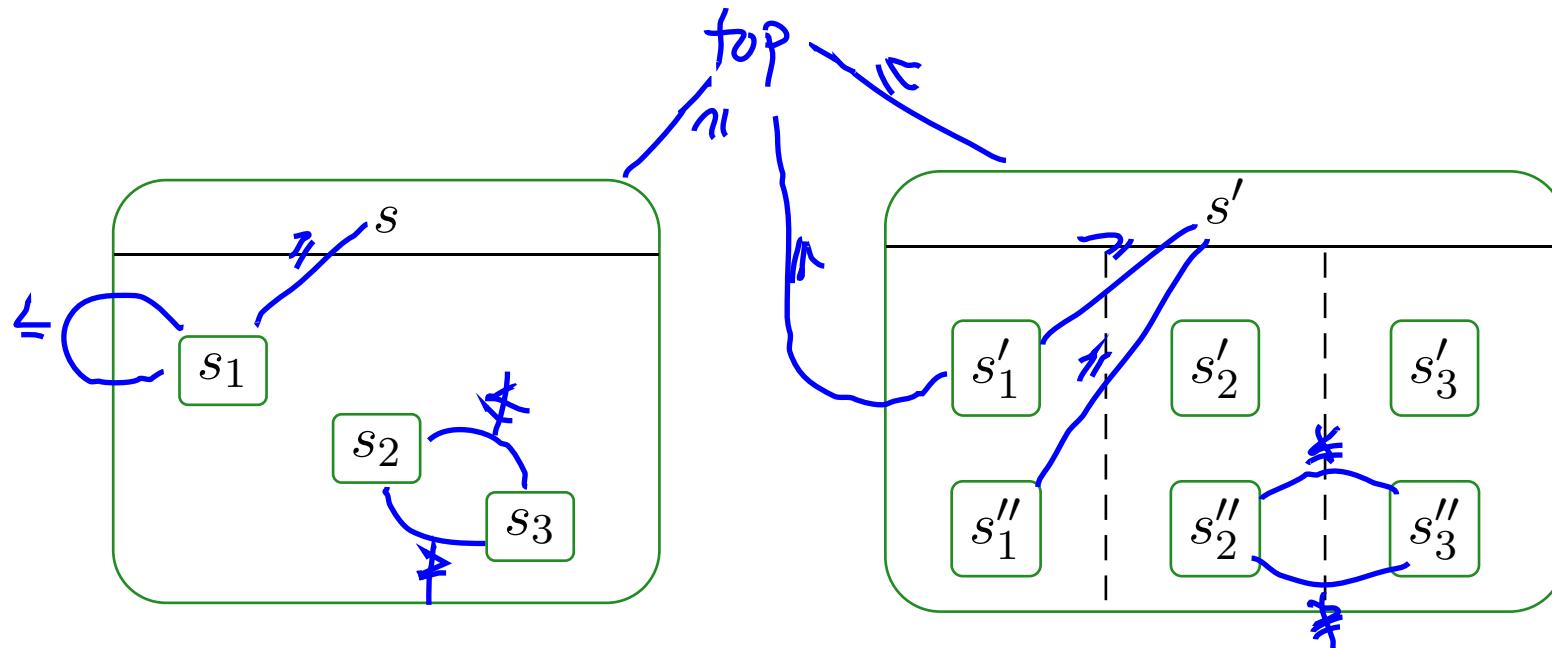
NOTE: S can be abbreviated as

$$\{s_1, s_2, s_3\}$$

A Partial Order on States

The substate- (or **child-**) relation **induces** a **partial order on states**:

- $\text{top} \leq s$, for all $s \in S$,
- $s \leq s'$, for all $s' \in \text{child}(s)$,
- transitive, reflexive, antisymmetric,
- $s' \leq s$ and $s'' \leq s$ implies $s' \leq s''$ or $s'' \leq s'$.

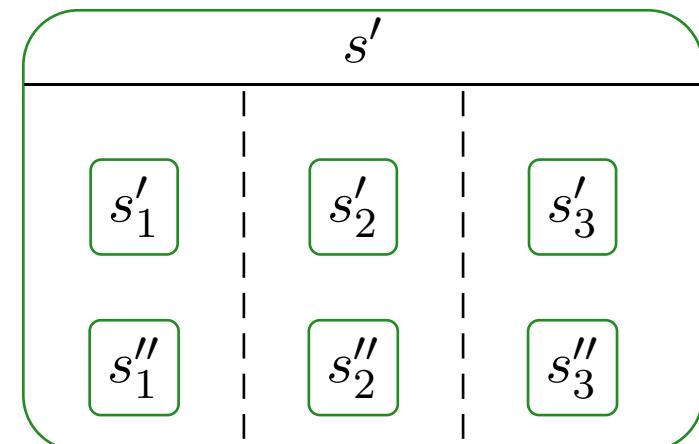
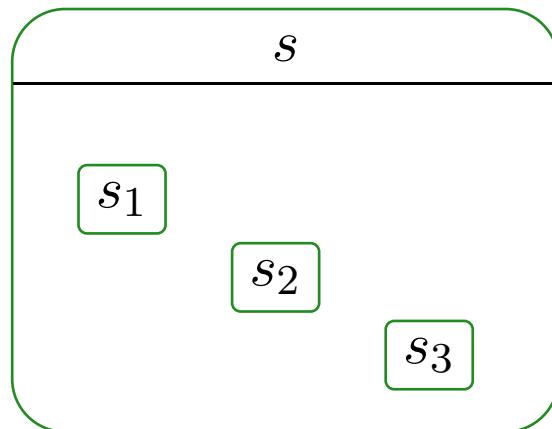


Least Common Ancestor and Ting

- The **least common ancestor** is the function $lca : 2^S \setminus \{\emptyset\} \rightarrow S$ such that
 - The states in S_1 are (transitive) children of $lca(S_1)$, i.e.

$$lca(S_1) \leq s, \text{ for all } s \in S_1 \subseteq S,$$

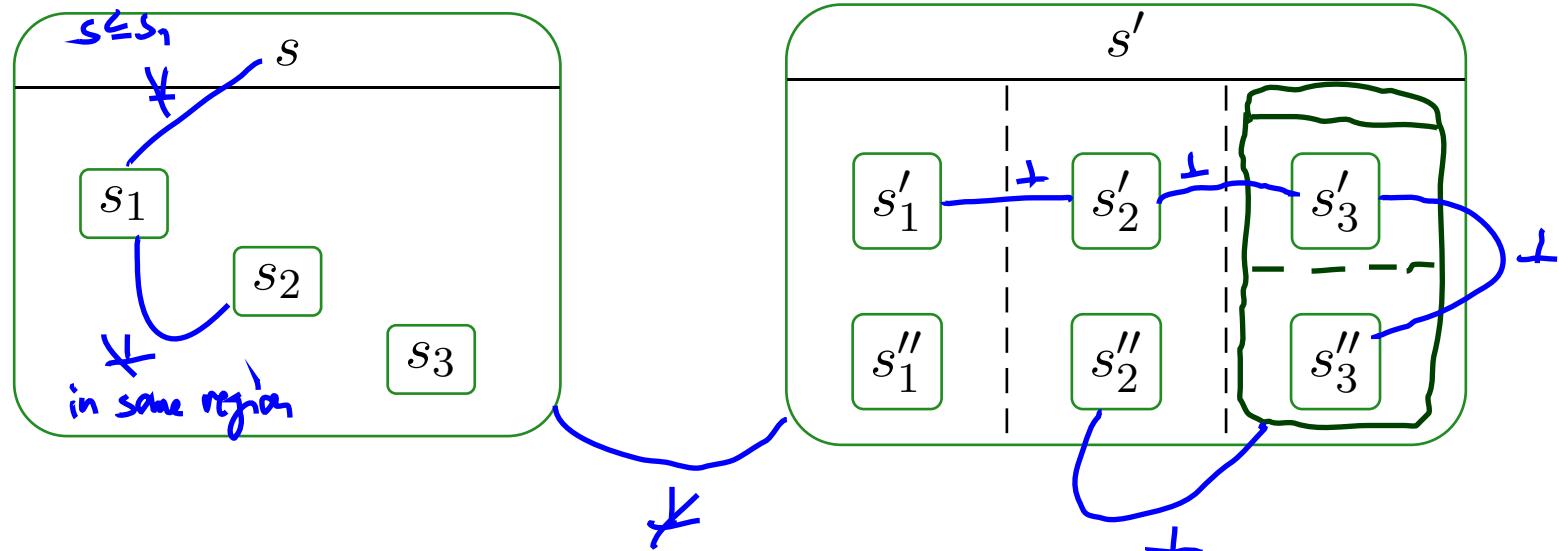
- $lca(S_1)$ is minimal, i.e. if $\hat{s} \leq s$ for all $s \in S_1$, then $\hat{s} \leq lca(S_1)$
- **Note:** $lca(S_1)$ exists for all $S_1 \subseteq S$ (last candidate: top).



Least Common Ancestor and Ting

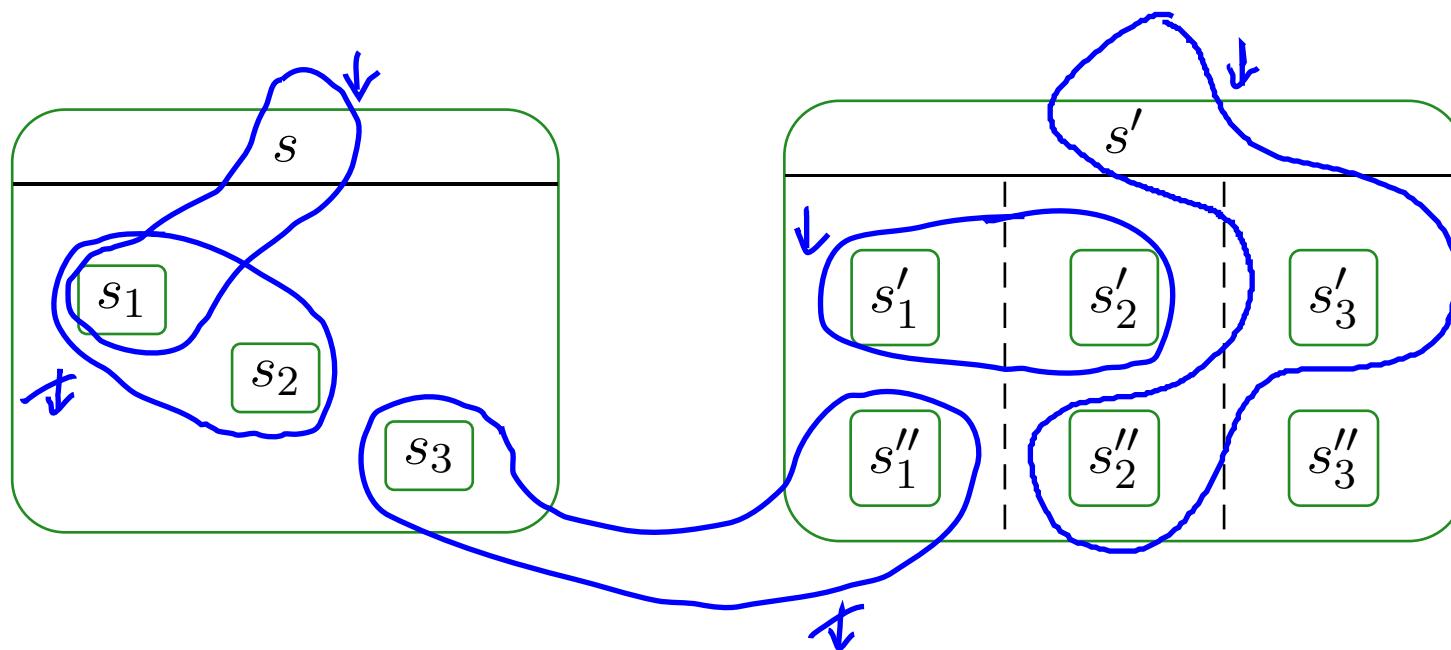
- Two states $s_1, s_2 \in S$ are called **orthogonal**, denoted $s_1 \perp s_2$, if and only if
 - they are unordered, i.e. $s_1 \not\leq s_2$ and $s_2 \not\leq s_1$, and
 - they “live” in different regions of an AND-state, i.e.

$$\exists s, \text{region}(s) = \{S_1, \dots, S_n\} \exists 1 \leq i \neq j \leq n : s_1 \in \text{child}^*(S_i) \wedge s_2 \in \text{child}^*(S_j),$$



Least Common Ancestor and Ting

- A set of states $S_1 \subseteq S$ is called **consistent**, denoted by $\downarrow S_1$, if and only if for each $s, s' \in S_1$,
 - $s \leq s'$, or
 - $s' \leq s$, or
 - $s \perp s'$.



Legal Transitions (Edges)

A hierarchical state-machine $(S, \text{kind}, \text{region}, \rightarrow, \psi, \text{annot})$ is called **well-formed** if and only if for all transitions $t \in \rightarrow$,

- (i) source and destination are consistent, i.e. $\downarrow \text{source}(t)$ and $\downarrow \text{target}(t)$,
- (ii) source (and destination) states are pairwise orthogonal, i.e.

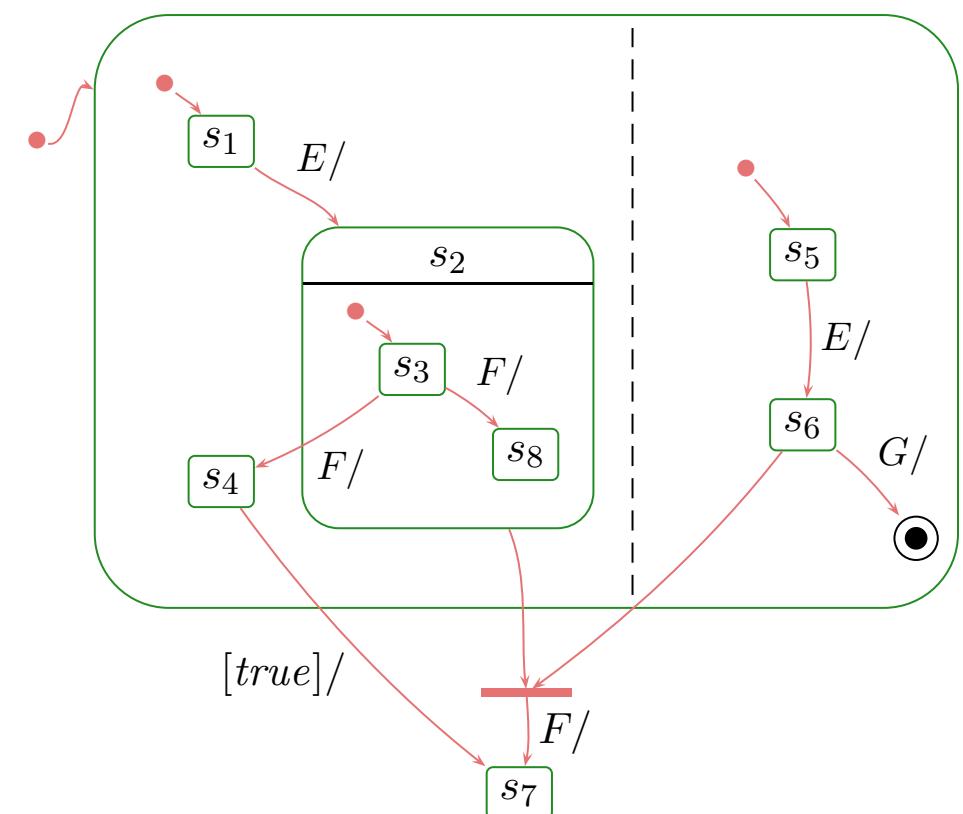
- forall $s \neq s' \in \text{source}(t)$ ($\in \text{target}(t)$), $s \perp s'$,

- (iii) the top state is neither source nor destination, i.e.

- $\text{top} \notin \text{source}(t) \cup \text{target}(t)$.

- Recall: final states are not sources of transitions.

Example:



References

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