

Software Design, Modelling and Analysis in UML

Lecture 03: Object Constraint Language

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Contents & Goals

($\{ \text{Im} \}, \{ \text{Co} \}, \{ \text{X} : \text{Int} \}, \{ \text{C} : \text{Ex} \}, \text{S} \vdash \sigma \}$)

Last Lecture:

- Basic Object System Signature \mathcal{S} and Structure \mathcal{D} , System State $\sigma \in \Sigma_{\mathcal{S}}^{\mathcal{D}}$

(Seems like they're related to class/object diagrams, officially we don't know yet...)

This Lecture:

- **Educational Objectives:** Capabilities for these tasks/questions:

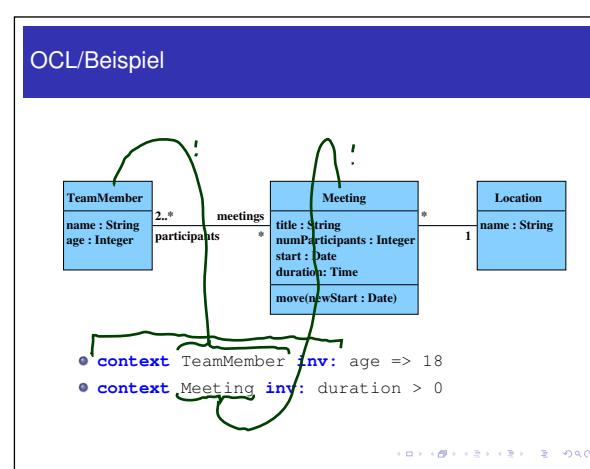
- Please explain this OCL constraint.
- Please formalise this constraint in OCL.
- Does this OCL constraint hold in this system state?
- Can you think of a system state satisfying this constraint?
- Please un-abbreviate all abbreviations in this OCL expression.
- In what sense is OCL a three-valued logic? For what purpose?
- How are $\mathcal{D}(C)$ and τ_C related?

- **Content:**

- OCL Syntax, OCL Semantics over system states

What is OCL? And What is It Good For?

- **OCL:** Object Constraint Logic.

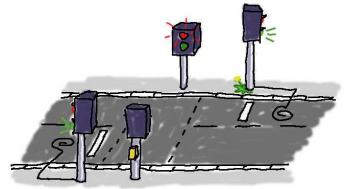


What's It Good For?

- **Most prominent:**

write down **requirements** supposed to be satisfied by all system states.

Often targeting all alive objects of a certain class.



context TLC inv:
 $\text{not}(\text{redP} \text{ and } \text{greenP})$

What's It Good For?

- **Most prominent:**

write down **requirements** supposed to be satisfied by all system states.

Often targeting all alive objects of a certain class.



context off
pre: (true)
post: (not redP
and not greenP)



• **Metamodeling:** the UML standard is a MOF-Model of UML.

OCL expressions define well-formedness of UML models (cf. Lecture ~ 21).

Plan.

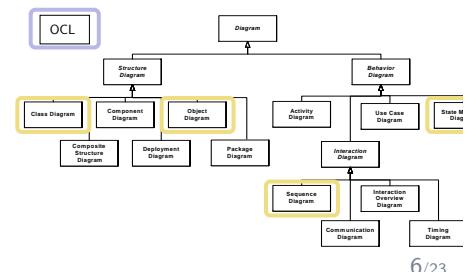
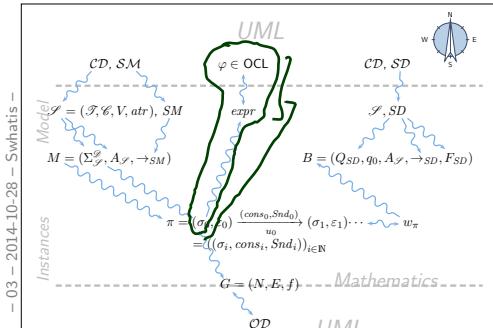
- **Today:**

- The set $OCLExpressions(\mathcal{S})$ of OCL expressions over \mathcal{S} .

- **Next time:**

- Given an OCL expression $expr$, a system state $\sigma \in \Sigma_{\mathcal{S}}^{\mathcal{D}}$, and a valuation of logical variables β , define the **interpretation function**

$$I[\![expr]\!](\sigma, \beta) \in \{ \text{true}, \text{false}, \perp \}.$$



(Core) OCL Syntax [OMG, 2006]

OCL Syntax 1/4: Expressions

expr ::=

- $w : \tau(w)$
- $| \ expr_1 =_{\tau} expr_2 : \tau \times \tau \rightarrow \text{Bool}$
- $| \ \text{oclIsUndefined}_{\tau}(expr_1) : \tau \rightarrow \text{Bool}$
- $| \ \{expr_1, \dots, expr_n\} : \tau \times \dots \times \tau \rightarrow \text{Set}(\tau)$
- $| \ \text{isEmpty}(expr_1) : \text{Set}(\tau) \rightarrow \text{Bool}$
- $| \ \text{size}(expr_1) : \text{Set}(\tau) \rightarrow \text{Int}$
- $| \ \text{allInstances}_C : \text{Set}(\tau_C)$
- $| \ v(expr_1) : \tau_C \rightarrow \tau(v)$
- $| \ r_1(expr_1) : \tau_C \rightarrow \tau_D$
- $| \ r_2(expr_1) : \tau_C \rightarrow \text{Set}(\tau_D)$

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Where, given $\mathcal{S} = (\mathcal{T}, \mathcal{C}, V, atr)$,

- $W \supseteq \{\text{self}_C \mid C \in \mathcal{C}\}$ is a set of typed logical variables,
 w has type $\tau(w)$, $\tau(\text{self}_C) = \tau_C$
- τ is any type from $\mathcal{T} \cup T_B \cup T_{\mathcal{C}}$
 $\cup \{\text{Set}(\tau_0) \mid \tau_0 \in T_B \cup T_{\mathcal{C}}\}$
- T_B is a set of basic types, in the following we use
 $T_B = \{\text{Bool}, \text{Int}, \text{String}\}$
- $T_{\mathcal{C}} = \{\tau_C \mid C \in \mathcal{C}\}$ is the set of object types,
- $\text{Set}(\tau_0)$ denotes the set-of- τ_0 type for $\tau_0 \in T_B \cup T_{\mathcal{C}}$ (sufficient because of "flattening" (cf. standard))
- $v : \tau(v) \in atr(C)$, $\tau(v) \in \mathcal{T}$,
- $r_1 : D_{0,1} \in atr(C)$,
- $r_2 : D_{*,*} \in atr(C)$,
- $C, D \in \mathcal{C}$.

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Expression Examples

expr ::=

| | |
|--|---|
| $w : \tau(w)$ | $ \ \text{size}(expr_1) : \text{Set}(\tau) \rightarrow \text{Int}$ |
| $ \ expr_1 =_{\tau} expr_2 : \tau \times \tau \rightarrow \text{Bool}$ | $ \ \text{allInstances}_C : \text{Set}(\tau_C)$ |
| $ \ \text{oclIsUndefined}_{\tau}(expr_1) : \tau \rightarrow \text{Bool}$ | $ \ v(expr_1) : \tau_C \rightarrow \tau(v)$ |
| $ \ \{expr_1, \dots, expr_n\} : \tau \times \dots \times \tau \rightarrow \text{Set}(\tau)$ | $ \ r_1(expr_1) : \tau_C \rightarrow \tau_D$ |
| $ \ \text{isEmpty}(expr_1) : \text{Set}(\tau) \rightarrow \text{Bool}$ | $ \ r_2(expr_1) : \tau_C \rightarrow \text{Set}(\tau_D)$ |

$$\mathcal{G} = (\{\text{Int}\}, \{\text{TeamMember}, \text{Meeting}\}, \{\text{age}, \text{hat}, \text{meeting} : \text{TM}_0, \text{partic} : \text{TM}_M\}, \\ (\text{short} : \text{TM}) \quad (\text{short M}) \quad \{\text{TM} \mapsto \{\text{age}, \text{meeting}\}, \text{M} \mapsto \{\text{partic}\}\})$$

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- $\text{self}_{\text{TM}} : \text{TM}$
- $\text{allInstances}_M : \text{Set}(\text{C}_M)$
- $\text{size}(\text{allInstances}_M) : \text{Set}(\text{C}_M) \rightarrow \text{Int}$
- $\text{age}(\text{self}_{\text{TM}}) : \text{C}_M \rightarrow \text{hat}$
- $\text{age}(\text{self}_M)$ NO, because $\text{age} \notin atr(M)$
- $\text{meeting}(\text{self}_{\text{TM}}) : \text{C}_M \rightarrow \text{C}_M$
- $\text{partic}(\text{self}_M) : \text{C}_M \rightarrow \text{Set}(\text{C}_M)$

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Notational Conventions for Expressions

- Each expression

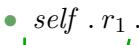
$$\omega(expr_1, expr_2, \dots, expr_n) : \tau_1 \times \dots \times \tau_n \rightarrow \tau$$

may alternatively be written ("abbreviated as")

- $expr_1 . \omega(expr_2, \dots, expr_n)$ if τ_1 is an **object type**, i.e. if $\tau_1 \in T_{\mathcal{C}}$.
- $expr_1 \rightarrow \omega(expr_2, \dots, expr_n)$ if τ_1 is a **collection type**
(here: only sets), i.e. if $\tau_1 = Set(\tau_0)$ for some $\tau_0 \in T_B \cup T_{\mathcal{C}}$.

$$\mathcal{C} = \{C, D\}, \text{ attr}(C) = \{v_1, r_2, r_3\}, \text{ attr}(D) = \{\omega\}$$

- **Examples:** ($self : \tau_C \in W; v, w : Int \in V; r_1 : D_{0,1}, r_2 : D_* \in V$)

- $self . v$ 
- $expr : \tau_C \omega$ 
- $self . r_1 . w$ 
- $self . r_2 \rightarrow \text{isEmpty}$ 

OCL Syntax 2/4: Constants & Arithmetics

For example:

| | |
|--------------------------------------|---|
| $expr ::= \dots$ | |
| true false | : Bool |
| $expr_1 \{and, or, implies\} expr_2$ | : Bool \times Bool \rightarrow Bool |
| not $expr_1$ | : Bool \rightarrow Bool |
| 0 -1 1 -2 2 ... | : Int |
| OclUndefined τ | : τ |
| $expr_1 \{+, -, \dots\} expr_2$ | : Int \times Int \rightarrow Int |
| $expr_1 \{<, \leq, \dots\} expr_2$ | : Int \times Int \rightarrow Bool |

Generalised notation:

$$expr ::= \omega(expr_1, \dots, expr_n) : \tau_1 \times \dots \times \tau_n \rightarrow \tau$$

with $\omega \in \{+, -, \dots\}$

eg. $+ (expr_1, expr_2)$
for
 $expr_1 + expr_2$

OCL Syntax 3/4: Iterate

$expr ::= \dots | expr_1 \rightarrow \text{iterate}(w_1 : \tau_1 ; w_2 : \tau_2 = expr_2 | expr_3)$

or, with a little renaming,

$expr ::= \dots | expr_1 \rightarrow \text{iterate}(iter : \tau_1; result : \tau_2 = expr_2 | expr_3)$

where

- $expr_1$ is of a **collection type** (here: a set $\text{Set}(\tau_0)$ for some τ_0),
- $iter \in W$ is called **iterator**, gets type τ_1
(if τ_1 is omitted, τ_0 is assumed as type of $iter$)
- $result \in W$ is called **result variable**, gets type τ_2 ,
- $expr_2$ in an expression of type τ_2 giving the **initial value** for $result$,
(‘OclUndefined’ if omitted)
- $expr_3$ is an expression of type τ_2
in which in particular $iter$ and $result$ may appear.

Iterate: Intuitive Semantics (Formally: later)

$expr ::= expr_1 \rightarrow \text{iterate}(iter : \tau_1;$
 $result : \tau_2 = expr_2 | expr_3)$

pseudocode

```

 $\text{Set}(\tau_0) hlp = \langle expr_1 \rangle;$ 
 $\tau_1 iter;$ 
 $\tau_2 result = \langle expr_2 \rangle;$ 
 $\text{while } (!hlp.empty()) \text{ do}$ 
     $iter = hlp.pop();$ 
     $result = \langle expr_3 \rangle;$ 
 $\text{od}$ 

```

*all instances T_h $\rightarrow \text{iterate}(\text{iter} : \tau_{T_h}; \text{result} : \text{Bool} = \text{true} |$
 $\text{result and iter.age} \geq 18)$*

Iterate: Intuitive Semantics (Formally: later)

$$\begin{aligned} \text{expr} ::= & \text{expr}_1 \rightarrow \text{iterate}(\text{iter} : \tau_1; \\ & \quad \text{result} : \tau_2 = \text{expr}_2 \mid \text{expr}_3) \end{aligned}$$

```

 $\text{Set}(\tau_0) \text{ hlp} = \langle \text{expr}_1 \rangle;$ 
 $\tau_1 \text{ iter};$ 
 $\tau_2 \text{ result} = \langle \text{expr}_2 \rangle;$ 
 $\text{while } (\text{!hlp.empty}()) \text{ do}$ 
 $\quad \text{iter} = \text{hlp.pop}();$ 
 $\quad \text{result} = \langle \text{expr}_3 \rangle;$ 
 $\text{od}$ 

```

Note: In our (simplified) setting, we always have $\text{expr}_1 : \text{Set}(\tau_1)$ and $\tau_0 = \tau_1$.

In the type hierarchy of full OCL with inheritance and `oclAny`,
they may be different and still type consistent.

Abbreviations on Top of Iterate

$$\begin{aligned} \text{expr} ::= & \text{expr}_1 \rightarrow \text{iterate}(w_1 : \tau_1; \\ & \quad w_2 : \tau_2 = \text{expr}_2 \mid \text{expr}_3) \end{aligned}$$

- $\text{expr}_1 \rightarrow \text{forAll}(w : \tau_1 \mid \text{expr}_3)$ is an abbreviation for $\text{expr}_1 \rightarrow \text{iterate}(w : \tau_1; w_1 : \text{Bool} = \text{true} \mid w_1 \text{ and } \text{expr}_3)$.
e.g.
all instances of
 $\rightarrow \text{forAll}(i / i.e.g.e}$
 > 18

(To ensure confusion, we may again omit all kinds of things, cf. [OMG, 2006]).

- Similar: $\text{expr}_1 \rightarrow \text{Exists}(w : \tau_1 \mid \text{expr}_3)$

OCL Syntax 4/4: Context

context ::= [context] $w_1 : \tau_1, \dots, w_n : \tau_n$ inv : expr

where $w \in W$ and $\tau_i \in T_{\mathcal{C}}$, $1 \leq i \leq n$, $n \geq 0$.

context [$w_1 : C_1, \dots, w_n : C_n$] inv : expr

is an **abbreviation** for

context TM, M inv:
 $\text{self}_M \rightarrow \text{partic}$
 $\rightarrow \text{contains}(\text{self}_M)$...
 implies
 $\text{self}_M \cdot \text{meeting}$
 $= \text{self}_n$
 ...
 $)$

allInstances_{C₁} -> forAll(w₁ : C₁ |
allInstances_{C_n} -> forAll(w_n : C_n |
expr
 $)$

context TM inv:
 $\text{age} \geq 18$
 \uparrow
allInstances_{TM}
 $\rightarrow \text{forAll}(\text{self}_M |$
 $\text{self}_M \cdot \text{age} \geq 18)$

Context: More Notational Conventions

- For

context self : τ_C inv : expr

we may alternatively write ("abbreviate as")

context τ_C inv : expr

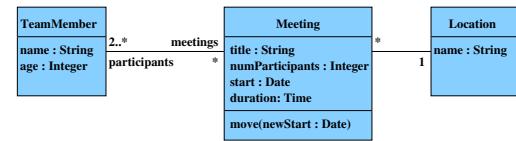
- Within the latter abbreviation, we may omit the "self" in *expr*, i.e. for

self.v and self.r

we may alternatively write ("abbreviate as")

v and r

Examples (from lecture)



- context TeamMember inv: age >= 18
- context Meeting inv: duration > 0

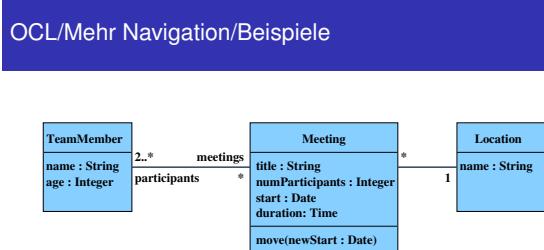
context self_{TM} : TeamMember inv: self_{TM}.age >= 18

all instances_{TM} → forAll (self_{TM}: TM | self_{TM}.age >= 18)

*all instances_{TM} → iterate (self_{TM}: TM; res : Boolean = true | res and self_{TM}.age >= 18)
} normalize*

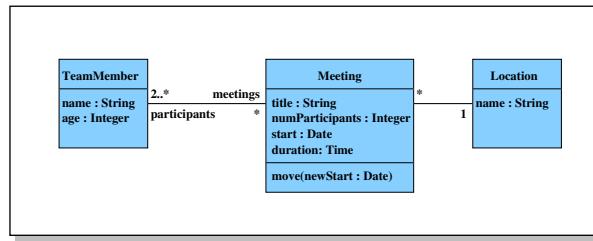
*all instances_{TM} → iterate (self_{TM}: TM; no : Boolean = true |
and (res, > (age (self_{TM}), 18)))*

Examples (from lecture “Softwaretechnik 2008”)



- context Meeting
 - inv: self.participants->size() = numParticipants
- context Location
 - inv: name="Lobby" implies meeting->isEmpty()

Example (from lecture “Softwaretechnik 2008”)



- context *Meeting* inv :

```
participants -> iterate(i : TeamMember; n : Int = 0 | n + i . age)  
/participants -> size() > 25
```

“Not Interesting”

Among others:

- Enumeration types
- Type hierarchy
- Complete list of arithmetical operators
- The two other collection types Bag and Sequence
- Casting
- Runtime type information
- Pre/post conditions
(maybe later, when we officially know what an operation is)
- ...

OCL Semantics: The Task

| | | | |
|--|---|--|------------------------------------|
| $expr ::=$ | | | |
| w | $: \tau(w)$ | $\mid \text{size}(expr_1)$ | $: Set(\tau) \rightarrow Int$ |
| $ \ expr_1 =_{\tau} expr_2$ | $: \tau \times \tau \rightarrow Bool$ | $\mid \text{allInstances}_{\mathcal{C}}$ | $: Set(\tau_C)$ |
| $ \ \text{occlsUndefined}_{\tau}(expr_1)$ | $: \tau \rightarrow Bool$ | $\mid v(expr_1)$ | $: \tau_C \rightarrow \tau(v)$ |
| $ \ \{expr_1, \dots, expr_n\}$ | $: \tau \times \dots \times \tau \rightarrow Set(\tau)$ | $\mid r_1(expr_1)$ | $: \tau_C \rightarrow \tau_D$ |
| $ \ \text{isEmpty}(expr_1)$ | $: Set(\tau) \rightarrow Bool$ | $\mid r_2(expr_1)$ | $: \tau_C \rightarrow Set(\tau_D)$ |

- Given an OCL expression $expr$, a system state $\sigma \in \Sigma_{\mathcal{G}}^{\mathcal{Q}}$, and a valuation of logical variables β , define

$$I[\![\cdot]\!](\cdot, \cdot) : OCLExpressions(\mathcal{S}) \times \Sigma_{\mathcal{S}}^{\mathcal{D}} \times (W \rightarrow I(\mathcal{T} \cup T_B \cup T_C)) \rightarrow I(Bool)$$

i.e.

$$\sigma = \{ \text{Im} \triangleright \{ \text{age} = 27, \text{height} = 5m \} \} \quad I[\![\text{expr}]\!](\sigma, \beta) \in \{\text{true}, \text{false}, \perp_{\text{Bool}}\}. \\ \vdash? \text{ self.age} > 18, \quad \beta : \text{self} \mapsto \text{Im}$$

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References

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