# Software Design, Modelling and Analysis in UML

Contents & Goals

Last Lectures:

## Lecture 8: Class Diagrams III

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• Class diagram:

C
v: Int
d:D.

Alternative prese Object diagram: Example system state: 
$$\begin{split} \sigma = \{1_C \mapsto \{v \mapsto 27, c \mapsto \{5_D, 7_D\}\}, \\ 5_D \mapsto \{d \mapsto \{1_C\}\}, 7_D \mapsto \{d \mapsto \{1_C\}\}\} \end{split}$$
$$\begin{split} \mathscr{S} &= (\{Int\}, \{C, D\}, \{v: Int, d: D_+, c: C_{0,1}\}, \\ \{C \mapsto \{v, d\}, D \mapsto \{c\}\}) \end{split}$$
v: Int c \* D Signature: extend again; represent association r with association ends a, b, and z (each with multiplicity, visibility, etc.) Object diagram: No... Example system state: Class diagram (with ternary association):  $\sigma = \{1_A \mapsto \{w \mapsto 13\}, 1_B \mapsto \emptyset, 1_Z \mapsto \emptyset\}$  $\lambda = \{\ r \mapsto \{(1_A,1_B,1_Z)\}\ \}$ 

 Educational Objectives: Capabilities for following tasks/questions. This Lecture: (v) Adjust interpretation I accordingly. (iv) Change syntax of OCL to refer to association ends. (iii) Define  $(\sigma,\lambda)$  system states with (ii) Extend signature accordingly. (i) Study association syntax. (Temporarily) extend signature, define mapping from diagram to signature.
 Study effect on OCL.
 Btw.: where do we put OCL constraints? Study concrete syntax for "associations". completed class diagrams... except for associations. Please explain this class diagram with associations.
 Which annotations of an association arrow are semantically relevant? What's the difference between "aggregation" and "composition"? What is "multiplicity"? How did we treat them semantically?
 What is "reading direction", "navigability", "ownership", ...? What's a role name? What's it good for? objects in σ (instances of classes), • links in λ (instances of associations). • Signature: extend again; represent association r with association ends a, b, and z (each with multiplicity, visibility, etc.) Class diagram (with ternary association): Example system state:  $\sigma = \{1_A \mapsto \{w \mapsto 13\}, 1_B \mapsto \emptyset, 1_Z \mapsto \emptyset\}$ w: Int \* z 1.5 0,1 B  $\lambda = \{\ r \mapsto \{(1_A,1_B,1_Z)\}\ \}$ 2/34

> • Class diagram:  $\frac{C}{v : Int}$   $\frac{d : D_*}{d : D_*}$ 
> $$\begin{split} \mathscr{S} &= (\{Int\}, \{C, D\}, \{v: Int, d: D_*, c: C_{0,1}\}, \\ &\{C \mapsto \{v, d\}, D \mapsto \{c\}\}) \end{split}$$
> v: Int c \* D Class diagram (with ternary association):
>  Association end ## ABOUR # 46 B contract 2 au : auguste > 3

$$\begin{split} \sigma &= \{1_C \mapsto \{v \mapsto 27, \mathbf{d} \mapsto \{5_D, 7_D\}\}, \\ 5_D \mapsto \{\mathbf{d} \mapsto \{1_C\}\}, 7_D \mapsto \{\mathbf{d} \mapsto \{1_C\}\}\} \end{split}$$
 $\frac{C}{v = 27} = \frac{d}{d} = \frac{D}{D}$ • Signature: extend again; represent association r represent association r and s (each with association ends a,b, and s (each with multiplicity, visibility, etc.)  $\frac{3}{2}$  + $\frac{1}{2}$  • Example system state:  $(\sigma,\lambda)$   $\frac{3}{2}$  + $\frac{1}{2}$   $\sigma = \{1_A \mapsto \{w \mapsto 13\}, 1_B \mapsto \emptyset, 1_Z \mapsto \emptyset\}$  $\begin{array}{c} \lambda = \left\{ \begin{array}{c} r \mapsto \left\{ \begin{pmatrix} 1_A, 1_B, 1_Z \end{pmatrix} \right\} \right\} \\ \begin{array}{c} r \colon \left[ \frac{\mathbf{d}}{\mathbf{d}_1}, \frac{\mathbf{d}}{\mathbf{d}_2}, \frac{\mathbf{d}}{\mathbf{d}_2} \right] \\ \frac{\mathbf{d}}{\mathbf{d}_1}, \frac{\mathbf{d}}{\mathbf{d}_1}, \frac{\mathbf{d}}{\mathbf{d}_2} \end{array} \right\} \\ \\ \begin{array}{c} \mathbf{d} \\ \mathbf{d}_1, \frac{\mathbf{d}}{\mathbf{d}_1}, \frac{\mathbf{d}}{\mathbf{d}_2} \end{array} \\ 3_{\ell} \end{array}$ 

Object diagram:

Example system state:

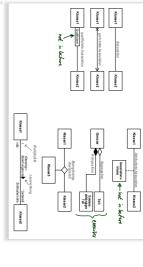
Associations: Syntax

(vi) ... go back to the special case of  $C_{0,1}$  and  $C_{\ast}$  attributes.

Object diagram: No...

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## UML Association Syntax Observed (2006)



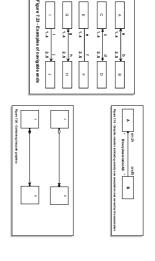
## More Association Syntax (OMG, 2011b, 61:43)

So, What Do We (Have to) Cover?

An association has

| Ramod | | | Ramod | Klassot grichtés

a reading direction, and
at least two ends. Each end has



• a multiplicity.
• a set of properties,
such as unique, ordered, etc.
• a qualifier, (wd in leader)
• a visibility,

a role name,

Wanted: places in the signature to represent the information from the picture.

Name 1 | Sandy | Name 2

a navigability,
an ownership,
and possibly a diamond. (دحرماها)

Manuari Manuar

Garces Agreement Tell

Composition Editor:

Edit

Kts seet Arthurster Association Ktssee2

# (Temporarily) Extend Signature: Associations

(Temporarily) Extend Signature: Associations

Only for the course of Lectures 08/09 we assume that each element in V is either a basic type attribute  $\langle v:T,\xi,exp_{T_0},P_c\rangle$  with  $T\in \mathscr{T}$  (as before), or an association of the form

 $r: \langle rele_1 : C_1, \mu_1, P_1, \xi_1, \nu_1, o_1 \rangle$ ,

association end

 $\langle role_n: C_n, \mu_n, P_n, \xi_n, \nu_n, o_n \rangle$   $\nwarrow$  the class solved this association and is localled

Only for the course of Lectures 08/09 we assume that each element in V is either a basic type attribute  $\langle v:T,\xi,\exp_{\Gamma_0},P_e\rangle$  with  $T\in\mathcal{S}$  (as before), or an association of the form

- $\langle r : \langle role_1 : C_1, \mu_1, P_1, \xi_1, \nu_1, o_1 \rangle,$
- $\langle role_n:C_n,\mu_n,P_n,\xi_n,\nu_n,o_n\rangle\rangle$
- $\begin{array}{ll} \bullet & n \geq 2 \text{ (at least two ends)}, \\ \bullet & r, \ mle_i \text{ are just names}, \\ \bullet & \text{the multiplicity } \mu_i \text{ is an expression of the form} \end{array}$
- P₁ is a set of properties (as before).
  ξ∈ {+, -, #, ~} (as before).
  ν₁∈ {x, -, >} is the navigability.
  ο₁∈ B is the ownership.  $\mu ::= N..M \mid N..* \mid \mu, \mu$ • N for N..N, • \* for 0..\* (use with care!) Multiplicity abbreviations:  $(N, M \in \mathbb{N})$

P<sub>i</sub> is a set of properties (as before),
\$ ∈ {+, -, #, ~} (as before),
\$\nu\_i ∈ {\times, -, >}\$ is the navigability,
\$\alpha\_i ∈ B\$ is the ownership.

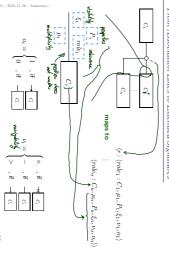
N for N..N.
for 0..\* (use with care!)

 $\bullet \ n \geq 2 \ (\text{at least two ends}), \\ \bullet \ r, \ mle_i \ \text{are just names}, \quad C_i \in \mathscr{C}, \ 1 \leq i \leq n, \\ \bullet \ \text{the multiplicity} \ \mu_i \ \text{is an expression of the form}$ 

 $\mu ::= N..M \mid N..* \mid \mu, \mu$ 

 $(N, M \in \mathbb{N})$ 

# From Association Lines to Extended Signatures



### Association Example

sture: 
$$\mathcal{S} = \{\{\mathcal{U}_i\}, \{\mathcal{C}_i \mathcal{D}\}, \{e_i \, l_i \mathcal{L}_i, \mathcal{S}_i \mathcal{C}_i \mathcal{D}_i, e_i \, l_i \mathcal{D}_i \mathcal{C}_i \mathcal{D}_i, \{e_i \, l_i \mathcal{L}_i, \mathcal{S}_i \mathcal{D}_i, e_i \, l_i \mathcal{D}_i \mathcal{D}_i, \mathcal{S}_i \mathcal{D}_i \mathcal{D$$

### Wait, If Omitting Things...

Temporarily (Lecture 8/9) Extended Signature

Definition. An (Extended) Object System Signature (with Associations) is a quadruple  $\mathscr{S}=(\mathscr{T},\mathscr{C},V,atr)$  where

ullet each element of V is

 $\label{eq:controller} \begin{array}{l} * \mbox{ either a basic type attribute } \langle v:T_1\xi, expr_0, P_v \rangle \mbox{ with } T \in \mathscr{T} \\ * \mbox{ or an association of the form} \\ \langle r: \mbox{ } \langle re: \mbox{ } \rangle, \\ \end{array}$ 

 $\langle role_n:C_n,\mu_n,P_n,\xi_n,\nu_n,o_n\rangle\rangle$ 

- ...is causing so much trouble (e.g. leading to misunderstanding), why does the standard say "In practice, it is often convenient..."?
- Is it a good idea to trade convenience for precision/unambiguity?

### It depends.

- Convenience as such is a legitimate goal.
- In UML-As-Sketch mode, precision "doesn't matter", so convenience (for writer) can even be a primary goal.
- In UML-As-Blueprint mode, precision is the primary goal.
   And misunderstandings are in most cases annoying.
- But: (even in UML-As-Blueprint mode)
- If all associations in your model have multiplicity \*, then it's probably a good idea not to write all these \*'s.

So: tell the reader about your convention and leave out the \*'s.

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only basic type attributes "belong" to a class (may appear in atr(C)).
 associations are not "owned" by a particular class (do not appear in any atr(C)).
 but "live on their own".

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•  $atr: \mathscr{C} \to 2^{\{v \in V \mid vT, T \in \mathscr{T}\}}$ •  $atr: \mathscr{C} \to 2^{\{v \in V \mid vT, T \in \mathscr{T}\}}$ maps each class to its set of basic type (!) attributes.

### What If Things Are Missing?

Most components of associations or association end may be omitted. For instance (OMG, 2011b, 17), Section 6.4.2, proposes the following rules:

Name: Use

if the name is missing.

Example:  $C \longrightarrow A.C.D$  D

Reading Direction: no default.

D

Role Name: use the class name at that end in lower-case letters

### What If Things Are Missing?

\* Multiplicity: 1 In my opinion, it's safer to assume 0.1 or \* (for 0.\*) In my opinion, it's safer to assume 0.1 or \* (for 0.\*) In the worst"). 

If there are no fixed, written, agreed conventions ("expect the worst").

Navigability and Ownership: not so easy. (OMG, 2011b, 43)

 Visibility: public Properties: Ø

"Various options may be chosen for showing navigation arrows on a diagram. In practice, it is often convenient to suppress some of the arrows and crosses and just show exceptional situations:

Show all arrows and x's. Navigation and its absence are made completely explicit.
 Suppress all arrows and x's. No inference can be drawn about navigation.
 This is similar to any situation in which information is suppressed from a view.

Suppress arrows for associations with navigability in both directions, and show arrows
only for associations with one-way navigability.
In this case, the two-way mayagibility cannot be distinguished from situations where
there is no navigation at all; however, the latter case occurs rarely in practice."

Associations: Semantics

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### Associations in General

### are "first-class citizens" next to objects, • do not belong (in general) to certain objects (in contrast to pointers, e.g.) The UML standard thinks of associations as **n-ary relations** which "live on their own" in a system state. (recall: we assume $P_1=P_n=\{\mathtt{unique}\}$ ). Only these parts are relevant for extended system states: Recall: We consider associations of the following form: That is, links (= association instances) $\langle r:\langle role_1:C_1,\mu_1,P_1,\xi_1,\nu_1,o_1\rangle,\ldots,\langle role_n:C_n,\mu_n,P_n,\xi_n,\nu_n,o_n\rangle\rangle$ $\langle r: \langle role_1: C_1, \neg, P_1, \neg, \neg, - \rangle, \dots, \langle role_n: C_n, \neg, P_n, \neg, \neg, - \rangle$

Links in System States

Association / Link Example

 $\langle r: \langle role_1: C_1, ..., P_1, ..., ..., \langle role_n: C_n, ..., P_n, ..., ... \rangle$ 

Only for the course of lectures  $8 \mathrel{/} 9$  we change the definition of system states

• a mapping  $\lambda$  which maps each association  $\langle r:\langle role_1:C_1\rangle,\ldots,\langle role_n:C_n\rangle\rangle\in V$  to a relation A system state of  $\mathscr S$  wrt.  $\mathscr D$  is a pair  $(\sigma,\lambda)$  consisting of a type-consistent mapping (as before) Definition. Let  $\mathscr D$  be a structure of the (extended) signature with associations  $\mathscr S=(\mathscr T,\mathscr E,V,atr).$ (i.e. a set of type-consistent n-tuples of identities).  $\sigma: \mathcal{D}(\mathcal{C}) \nrightarrow (atr(\mathcal{C}) \nrightarrow \mathcal{D}(\mathcal{T})),$  $\lambda(r) \subseteq \mathscr{D}(C_1) \times \cdots \times \mathscr{D}(C_n)$ 

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are (in general) not directed (in contrast to pointers).

Associations and OCL

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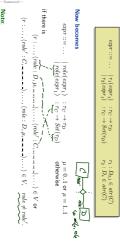
## OCL and Associations: Syntax

Recall: OCL syntax as introduced in Lecture 3, interesting part:

 $\begin{array}{ll} expr ::= \dots & |r_1(expr_1)| & :\tau_C \to \tau_D \\ |r_2(expr_1)| & :\tau_C \to Set(\tau_D) & r_2 : D_* \in atr(C) \end{array}$ 

OCL and Associations: Syntax

Recall: OCL syntax as introduced in Lecture 3, interesting part:

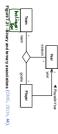


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Association name as such does not occur in OCL syntax, role names do.
 expr<sub>1</sub> has to denote an object of a class which "participates" in the association.

## OCL and Associations Syntax: Example





contest Player inv: team-> fill(t) t. herlicane)

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### References

Oesterich, B. (2006). Analyse und Design mit UML 2.1, 8. Auflage. Oldenbourg, 8. edition. OMG (2011a). Unified modeling language. Infrastructure, version 2.4.1. Technical Report formal / 2011-08-05.

OMG (2011b). Unified modeling language: Superstructure, version 2.4.1. Technical Report formal/2011-08-06.

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OCL and Associations: Semantics

Recall:  $\bullet \ I[r_1(c\sigma pr_1)][\sigma,\beta) \coloneqq \begin{cases} u & \text{, if } u_1 \in \text{dom}(\sigma) \text{ and } \sigma(u_1)(r_1) = \{u\} \\ \bot & \text{, otherwise} \end{cases}$  $I[r_2(\alpha pr_1)](\sigma,\beta) \coloneqq \begin{cases} \sigma(u_1)(r_2) & \text{. if } u_1 \in \text{dom}(\sigma) \\ \bot & \text{. otherwise} \end{cases}$  $\text{Assume } xpr_1:\tau_C \text{ for some } C\in \mathcal{C}. \text{ Set } u_1:=I[xpr_1](\sigma,\beta)\in \mathcal{D}(T_C).$ 

 $I[\![\mathit{role}(expr_1)]\!]((\sigma,\lambda),\beta)$ 

 $\langle r : \dots \langle rok : D, \mu, \dots, \dots \rangle \text{ for } i: C_{-----} \rangle \dots \rangle$ But it yields a set of n-tuples, of which some relate u and some instances of D.

• rok denotes the position of the D's in the tuples constituting the value of r. \* We cannot simply write  $\sigma(u)(vole)$ . Recall: rde is (for the moment) not an attribute of object u (not in atr(C)). \* What we have is  $\lambda(r)$  (with association name r, not with role name rolet).

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References

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