

## Software Design, Modelling and Analysis in UML

### Lecture 12: Core State Machines II

2015-12-15

Prof. Dr. Andreas Podelski, Dr. Bernd Westphal  
 Albert-Ludwigs-Universität Freiburg, Germany

#### Contents & Goals

##### Last Lecture:

- Basic causality model
- Ether-event pool
- System configuration

##### This Lecture:

- Educational Objectives: Capabilities for following tasks/questions.
  - What does this State Machine mean? What happens if I inject this event?
  - Can you please model the following behaviour?
  - What is Signal, Event, Ether, Transformer, Sep, RTC.
- Content:
  - System configuration cont'd
  - Transformers
  - Step, Run-to-Completion Step

#### System Configuration

##### System Configuration

**Definition:** Let  $\mathcal{S} = (\mathcal{P}_0, \mathcal{G}_0, V_0, \text{attr}_0, \mathcal{E})$  be a signature with signals,  $\mathcal{P}_0$  a structure of  $\mathcal{A}_0, E_0, \text{ready}, \oplus, \ominus, [-]$ , an ether over  $\mathcal{G}_0$  and  $\mathcal{G}_0$ .

Furthermore assume there is one core state machine  $M_C$  per class  $C \in \mathcal{C}$ .  
 A system configuration over  $\mathcal{A}_0, \mathcal{G}_0$  and  $E_0$  is a pair

$$(e, \varepsilon) \in \Sigma_{\mathcal{G}}^{\mathcal{P}_0} \times E_0$$

where

- $\mathcal{S} = (\mathcal{P}_0 \cup \{S_{uC} : C \in \mathcal{C}\}, \mathcal{G}_0, V_0, \text{attr}_0, \mathcal{E})$
- $V_0 \cup \{S_{uC} : C \in \mathcal{C}\} \cup \{S_{uC} : S_{uC} \rightarrow S_{uC}, S_{uC} \rightarrow \emptyset, S_{uC} \rightarrow S_{uC}\}$
- $\mathcal{E} = \{u \in \text{attr}_0 : u \rightarrow S_{uC}, u \rightarrow \text{ether}, u \rightarrow \text{transformer}, u \rightarrow \text{parameter}, u \rightarrow \text{ether}\}$  ( $C \in \mathcal{C}$ ,  $S_{uC}$ )
- $\mathcal{P}_0 = \mathcal{P}_0 \cup \{S_{uC} : u \rightarrow S_{uC}, u \rightarrow \text{ether}, u \rightarrow \text{transformer}, u \rightarrow \text{parameter}, u \rightarrow \text{ether}\}$  ( $C \in \mathcal{C}$ ,  $S_{uC}$ )

## Stability

Definition.

Let  $(\sigma, \varepsilon)$  be a system configuration over some  $\mathcal{S}_0, \mathcal{B}_0, \mathcal{E}h$ .  
We call an object  $u \in \text{dom}(\sigma) \cap \mathcal{D}(\mathcal{C}_0)$  **stable** in  $\sigma$  if and only if

$$\sigma(u).stable = \text{true}$$

And **unstable** otherwise.

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## Where are we?



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- The (simplified) syntax of transition annotations:  
 $anno ::= [ \langle event \rangle | "!" \langle guard \rangle "!" | "?" \langle action \rangle ]$
- **Clear:**  $\langle event \rangle$  is from  $\mathcal{E}$  of the corresponding signature.
- **But:** What are  $\langle guard \rangle$  and  $\langle action \rangle$ ?
- UML can be viewed as being **parameterized** in **expression language** (providing  $\langle guard \rangle$ ) and **action language** (providing  $\langle action \rangle$ ).
- **Examples:**
  - **Expression Language:**
  - **OCL:**
  - Java, C++, ... expressions
- **Action Language:**
- UML Action Semantics, “Executable UML”
- Java, C++, ... statements (plus some event send actions)

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## Recall

- The (simplified) syntax of transition annotations:  
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- **Examples:**
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## Needed: Semantics

In the following, we assume that we're given

- an **expression language**  $Expr$  for guards, and
- an **action language**  $Acl$  for actions,

and that we've **given**

• a semantics for boolean expressions in form of a partial function

$$I[\cdot] : \mathbb{B}(\cdot, \cdot) : Expr \times \Sigma_{\mathcal{E}}^{\mathcal{G}} \times \mathcal{D}(E) \xrightarrow{\perp} \mathbb{B}.$$

which evaluates expressions in a given system configuration. If  $I$  is not defined (for instance because of “dangling reference navigation or division-by-zero”), we want to go to a designated “error” system configuration.

- **Assuming**  $I$  to be partial is a way to treat “undefined” during runtime. If  $I$  is not defined (for instance because of “dangling reference navigation or division-by-zero”), we want to go to a designated “error” system configuration.
- **a transformer** for each action: for each  $act \in Acl$  we assume to have

$$t_{act} \subseteq \mathcal{D}(E) \times (\Sigma_{\mathcal{E}}^{\mathcal{G}} \times \mathcal{E}h) \times (\Sigma_{\mathcal{E}}^{\mathcal{G}} \times \mathcal{E}h)$$

## Transformer

- **Transformer**
- Definition
- Let  $\Sigma_{\mathcal{E}}^{\mathcal{G}}$  the set of system configurations over some  $\mathcal{S}_0, \mathcal{B}_0, \mathcal{E}h$ .  
We call a relation

$$t \subseteq \mathcal{D}(E) \times (\Sigma_{\mathcal{E}}^{\mathcal{G}} \times \mathcal{E}h) \times (\Sigma_{\mathcal{E}}^{\mathcal{G}} \times \mathcal{E}h)$$

a (system configuration) **transformer**.

### Example

- $t_{[i \mapsto j]}(\sigma, \varepsilon) \subseteq \Sigma_{\mathcal{E}}^{\mathcal{G}} \times \mathcal{E}h$  is
  - the set  $\{i\}$  of the system configurations
  - which **map** result from object  $u_i$
  - **executing** transformer  $t$ .
- $t_{\text{copy}}(u_2)(\sigma, \varepsilon) = \{(u, \varepsilon)\}$
- $t_{\text{create}}(u_2)(\sigma, \varepsilon)$ : add a previously non-alive object to  $\sigma$

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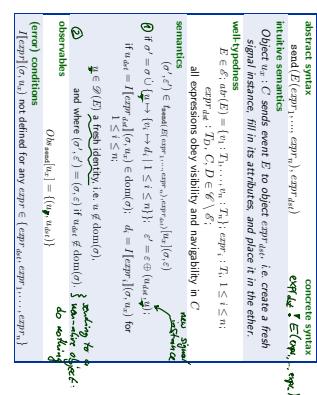
## Transformer

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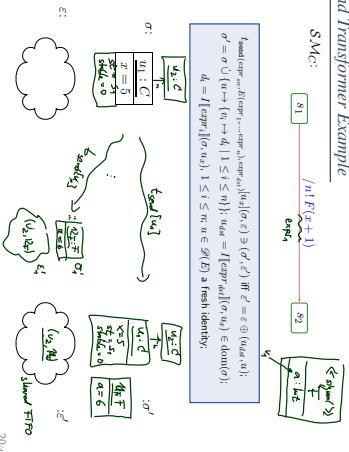
## Transformer: Send



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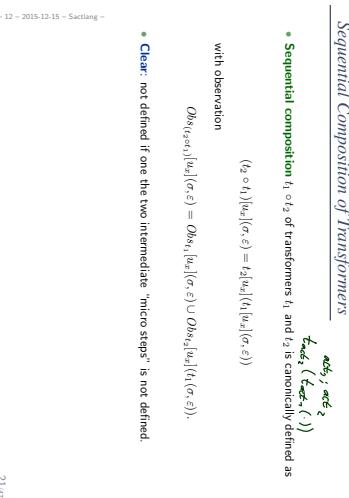
## Send Transformer Example



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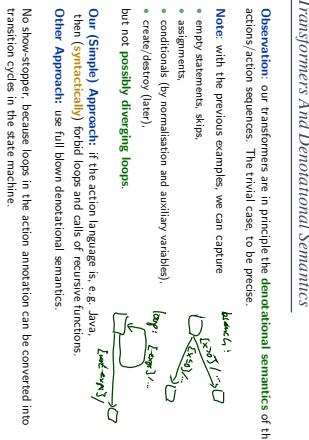
## Sequential Composition of Transformers



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