

Software Design, Modelling and Analysis in UML

Lecture 13: Core State Machines III

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Transition Relation, Computation

Definition: Let A be a set of labels and S a (not necessarily finite) set of states. We call

$$\rightarrow \subseteq S \times A \times S$$

a (labelled) **transition relation**.

Let $S_0 \subseteq S$ be a set of **initial states**. A (finite or infinite) sequence

$$s_0 \xrightarrow{a_0} s_1 \xrightarrow{a_1} s_2 \xrightarrow{a_2} \dots$$

with $s_i \in S_0, a_i \in A$ is called **computation** of the **labelled transition system** (S, A, \rightarrow, S_0) if and only if

- initiation:** $s_0 \in S_0$
- consistency:** $(s_i, a_i, s_{i+1}) \in \rightarrow$ for $i \in \mathbb{N}_0$.

Contents & Goals

Last Lecture:

- System configuration cont'd
- Action language and transformer

This Lecture:

- **Educational Objectives:** Capabilities for following tasks/questions.
 - What does this State Machine mean? What happens if I inject this event?
 - Can you please model the following behaviour.
 - What is: Signal, Event, Error, Transformer, Step, RTC.
- **Content:**
 - Step, Run-to-Completion Step

Active vs. Passive Classes/Objects

- **Note:** From now on, for simplicity, assume that all classes are **active**. We'll later briefly discuss the Rhapsody Framework which proposes a way how to integrate non-active objects.
- **Note:** The following RTC "algorithm" follows **Harel and Gery (1997)** (i.e. the one realised by the Rhapsody code generation) if the standard is ambiguous or leaves choices.

Transition Relation

Definition: Let $\mathcal{C}_0 = (C_0, \mathcal{M}_0, \mathcal{V}_0, \text{attr}_0, \mathcal{E})$ be a signature with signals (all classes in \mathcal{C}_0 **active**), \mathcal{M}_0 a structure of \mathcal{C}_0 , and $(\mathcal{E}, \text{env}_0, \text{sig}_0, \text{sig}_0^c)$ an ether over \mathcal{C}_0 and \mathcal{M}_0 . Assume there is one core state machine \mathcal{M}_0/C per class $C \in \mathcal{C}_0$.

We say, the state machines induce the following labelled transition relation on states $S := \mathcal{C}_0^* \times \mathcal{E} \times \mathcal{E} \times \mathcal{M}_0 \times \mathcal{M}_0$ with labels $A := \mathcal{C}_0 \times \mathcal{E} \times \mathcal{E} \times \mathcal{M}_0 \times \mathcal{M}_0$:

$$S \xrightarrow{(c, \sigma, \tau, \mu, \nu)} S'$$

if and only if

- an event with destination u is discarded,
- an event s dispatched to u , i.e. stable object processes an event, or
- run-to-completion processing by u continues, i.e. object u is not stable and continues to process an event,
- the environment interacts with object u .

if and only if

$$s \xrightarrow{(c, \sigma, \tau, \mu, \nu)} s'$$

if and only if

- an error condition occurs during consumption of env_0 , or
- $(s = \#$ and $\text{env}_0 \text{sig}_0 = \emptyset$).

From Core State Machines to LTS

(i) Discarding An Event

$$(a, \varepsilon) \xrightarrow{\text{cons, Snd}} (a', \varepsilon')$$

if

condition on (a, ε)

and
conditions on (a', ε')

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(i) Discarding An Event

$$(a, \varepsilon) \xrightarrow{\text{cons, Snd}} (a', \varepsilon')$$

if

$a \in \text{dom}(\sigma) \cap \mathcal{G}(C) \wedge \exists u \in \mathcal{G}(E) : u \in \text{read}(c, u)$

- u is stable and in state machine state s , i.e. $\sigma(u)(stable) = 1$ and $\sigma(u)(s) = s$,
- but there is no corresponding transition enabled (all transitions incident with current state of u either have other triggers or the guard is not satisfied)

$\forall (a', F, \text{cpr}, \text{act}, s') \Leftarrow (SMC) : F \neq E \vee \neg \text{enabl}[a, n] = 0$

and

- in the system configuration, stability may change, $u \in \text{read}(c, u)$
- where $b = 0$ if and only if there is a transition with trigger ε enabled for v in (a', ε') .
- the event $u \in \text{read}(c, u)$ is removed from the other, i.e.
- consumption of $u \in \text{read}(c, u)$ is observed, i.e.

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(ii) Dispatch

$$(a, \varepsilon) \xrightarrow{\text{cons, Snd}} (a', \varepsilon')$$

if

- $n \in \text{dom}(\sigma) \cap \mathcal{G}(C) \wedge \exists u \in \mathcal{G}(E) : u \in \text{read}(c, u)$
- u is stable and in state machine state s , i.e. $\sigma(u)(stable) = 1$ and $\sigma(u)(s) = s$
- a transition is enabled, i.e.

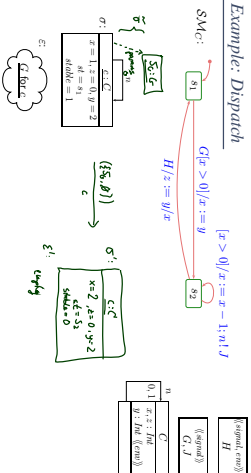
$$\exists (s', F, \text{cpr}, \text{act}, s') \Leftarrow (SMC) : F = E \wedge \text{enabl}[a, n] = 1$$

and

- (a', ε') results from applying read to (a, ε) and removing u from the other, i.e.
- $(a', \varepsilon') \in \text{enabl}[a', n']$
- read u
- cpr u
- act u
- Snd u
- where b depends (see (i))
- Consumption of $u \in \text{read}(c, u)$ and the side effects of the action are observed, i.e.

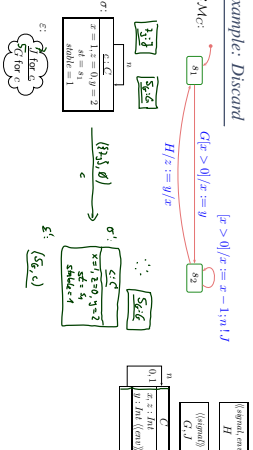
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Example: Dispatch



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Example: Discard



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(iii) Continue Run-to-Completion

$$(a, \varepsilon) \xrightarrow{\text{cons, Snd}} (a', \varepsilon')$$

if

- there is an unstable object u of a class \mathcal{C} , i.e.
- $u \in \text{dom}(\sigma) \cap \mathcal{G}(C) \wedge \sigma(u)(stable) = 0$
- there is a transition write u stg enabled from the current state $s = \sigma(u)(s)$, i.e.

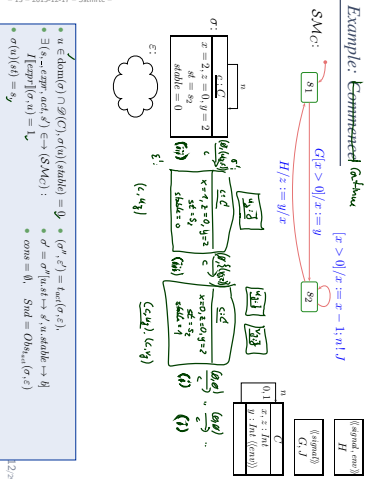
$$\exists (s', F, \text{cpr}, \text{act}, s') \Leftarrow (SMC) : \text{enabl}[a, n] = 1$$

and

- (a', ε') results from applying write to (a, ε) , i.e.
- $(a', \varepsilon') \in \text{enabl}[a', n']$
- where b depends as before.
- Only the side effects of the action are observed, i.e.

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Example: Commented Code



References

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References

- Haral, D. and Gery, E. (1997). Executable object modeling with statecharts. *IEEE Computer*, 30(7):31–42.
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- OMG (2011b). Unified modeling language: Superstructure, version 2.4.1. Technical Report formal/2011-08-08.

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